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# Secure Source-Relay Link Based Threshold DF Relaying Scheme

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## Abstract

In this work, a dual-hop cooperative system, in which there are a Source-Destination ( $S$ - $D$ ) pair, a relay node ( $R$ ) and an eavesdropper ( $E$ ), which attempts to eavesdrop the confidential message sent by  $S$  and forwarded by  $R$ , is considered. In order to enhance the system performance and save the system resource, we propose an  $S - R$  link based threshold decode-and-forward (DF) relaying scheme for  $R$  to decide whether to aid  $S$ - $D$  pair's information transmission or not, other than the traditional DF relaying scheme. The secrecy outage performance of the considered system is investigated and the closed-form analytical expression for secrecy outage probability is derived and verified via Monte-Carlo simulations.

*Keywords:*

Decode-and-forward, dual-hop, Rayleigh fading, secrecy outage.

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## 1. Introduction

Due to the openness of wireless medium, the probability that the delivered information suffers eavesdropping will increase, when there is an eavesdropper trying to overhead the information transmission between the source and the destination. Then, the amount of secrecy information capacity of the data transmission between the source and the destination will degrade, resulting in poor physical layer security. [1] firstly described the wiretap channel, in which two legitimate terminals want to have secure communication with an eavesdropper appears in the channel.

Recently, plenty of works have been presented to study the security at the physical layer [2-8]. The author of [2] examined the security issue in the 5G network by considering the randomness of the communication terminals with disruptive technologies. [3] proposed a secure multiple-input multiple-output (MIMO) system consisting of a base station, an information-decoding user, and an energy-harvesting user, while considering simultaneous wireless information and power transfer (SWIPT). The authors of [4] and [5] investigated the secrecy performance of visible light communication system, while considering the randomness of the locations of the terminals. [6] presented a new key management mechanism which combines trusted-server scheme and key pre-distribution scheme to satisfy the security network architecture. The author of [7] also studied the secrecy outage performance for an underlay cognitive radio unit system over Nakagami- $m$  fading channel. [8] studied a MIMO cognitive wiretap system, which adapts generalized selection combining over Nakagami- $m$  channels in place of a multiple-antenna eavesdropper. Moreover, [9] investigated the secrecy capacity for classic Wyner's model over

$\alpha$ - $\mu$  fading channels.

Therefore, one can clearly see that physical layer security issue is quite important and urgent for wireless relay communication systems, as more information leakage might happen over the extended links [10]. In other words, the additional communication links from the source to relays can improve the system's coverage and throughput [11-12], however eavesdropping can also take place over these relaying links. Therefore, the security of the wireless cooperative/relay systems attracts more and more researchers' interests [13-24]. Several cooperation strategies were considered in [13] to derive the optimal rate-equivocation region for four-terminal relay-eavesdropper channel. A best decode-and-forward (DF) relay was selected by adopting selection combining (SC) technique to communicate with a destination [14]. In order to improve the security against eavesdroppers, an opportunistic selection scheme of two relay nodes was proposed in [15]. Partial relay selection schemes were proposed for cooperative systems with multi-relays in [16]. Hybrid decode-amplify-forward relay with three different selection schemes was introduced to enhance the secrecy performance of the considered wireless system in [17]. In [18], the outage and symbol error performance has been studied for a dual-hop conditional DF relay system. The influence of SWIPT at the relay on the outage of A dual-hop DF system was investigated in [19]. In [20], the authors studied the physical layer secrecy performance of multi-hop DF relay network was investigated in the presence of multiple passive eavesdroppers over Nakagami- $m$  fading channels. For time-division multiple-access based DF cooperative protocols, the authors of [21] analyzed achievable secrecy rates with total and individual relay power constraints and

design relay beamforming weights to improve the secrecy rate. [22] presented and analyzed a jamming power allocation method that can effectively achieve the secrecy rate in cooperative network. An exponential-type integral representation for the logarithmic function was utilized to derive an approximate expression for the ergodic secrecy rates of cooperative DF relay networks only in terms of the moment generating function of signal-to-noise ratio (SNR) [23]. In order to provide security at the physical layer, [24] designed a cooperative protocol relying on both cooperative relaying and jamming.

However, to the best of our knowledge, the secrecy performance has not been well studied for cooperative systems, as most of the existing works focus on traditional relay schemes, e.g., amplify-to-forward and DF schemes. In this work, a dual-hop cooperative system, in which there are a Source-Destination ( $S$ - $D$ ) pair, a relay node ( $R$ ) and an eavesdropper ( $E$ ), which attempts to eavesdrop the confidential message sent by  $S$  and forwarded by  $R$ , is considered.  $R$  tries to coordinate the processes of information decoding from the received signal, by recoding and forwarding the received messages to  $D$ . Further,  $R$  adopts threshold DF relaying scheme to decide whether to aid  $S$ - $D$  pair's information transmission or not, aiming to enhancing the system performance and save the system resource. The main contributions of this work are listed as follows:

- 1) In this work, we propose  $S$ - $R$  link based threshold DF scheme, which can improve the secrecy outage performance and system resource consumption when the quality of  $S$ - $R$  link is not good;
- 2) The secrecy outage performance of  $S$ - $R$  link based threshold DF scheme is studied and the closed-form expression for secrecy outage probability has

been derived.

The rest of the paper is structured as follows. In Section 2, the system model is introduced. The secrecy outage performance is studied for threshold DF scheme by deriving the closed-form analytical expressions for the secrecy outage probability of the considered system, in Section 3. Monte-Carlo simulations are conducted to verify the proposed analytical models in Section 4. Finally, Section 5 concludes the paper.

## 2. System model

In this section, a cooperation group including a  $S$ - $D$  pair,  $R$  and  $E$ , which attempts to eavesdrop the confidential message sent by  $S$  and forwarded by  $R$ , is considered. All links experience independent and identically Rayleigh fading. An  $S$ - $R$  link based threshold relay scheme is considered in this work in order to enhance the system performance and save the system resource. Namely,  $R$  will decide to forward the decoded information bits according to the transmission over  $S$ - $R$  link: if it is not successful,  $R$  will not take any action and keep silence; otherwise,  $R$  will forward its decoded information to  $D$ <sup>1</sup>. Therefore, one can clearly see that, compare to the traditional DF relay

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<sup>1</sup>Once  $R$  can successfully decode the received signal from  $S$ , it will forward the received signal to  $D$ . Under this case, there will be two copies of the transmitted signal at both  $D$  and  $E$ . However, for practical scenarios, the main channels (including  $S - R$  and  $R - D$  links) should outperform the eavesdropping channels (including  $S - E$  and  $R - E$  links); otherwise, the secrecy capacity will be zero and the information delivery will be meaningless. So even under this case, the secrecy performance of the system will be improved as the improvement at  $D$  benefited from diversity receiving schemes (like maximal ratio combining and SC) outperforms the one at  $E$ .

scheme, under the considered threshold DF relay scheme system source can be saved while the information transmission over  $S$ - $R$  link is not successful. Moreover, it is also assumed that each terminal has a single antenna and operates in half-duplex mode.

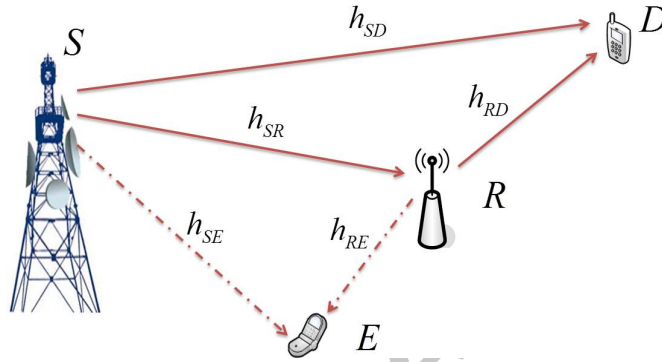


Figure 1: Secure cooperative system model

Then, we can divide the information transmission process into the following two phases:

1)  $S$  broadcasts the information to  $R$  and  $D$ ;

2) Under threshold DF relay scheme,  $R$  adopts its instantaneous SNR of the received signal over  $S$ - $R$  link as an indication of the reliability of the relaying transmission. If the SNR is larger than a predefined threshold ( $\gamma_0$ ), the probability of an error at  $R$  is small. Hence  $R$  will forward the signal after decoding. Otherwise,  $R$  remains silent.

### 3. Secrecy outage analysis

If  $R$  forwards the message, there will be two copies of the transmitted signals at both of  $D$  and  $E$ . In this work we assume SC scheme is adopted

at both of  $D$  and  $E$  to process the received two copies of the signals.

In Phase 2, the received signals at  $R$ ,  $D$  and  $E$  are given by

$$y_R = \sqrt{P_S} h_{SR} s + n_R \quad (1-a)$$

$$y_{D1} = \sqrt{P_S} h_{SD} s + n_D \quad (1-b)$$

$$y_{E1} = \sqrt{P_S} h_{SE} s + n_E \quad (1-c)$$

respectively, where  $P_i$  ( $i \in \{S, R, D\}$ ) is the transmit power at node  $i$ ,  $h_{ij}$  ( $i, j \in \{S, D, R, E\}$ ) is the link channel gain between node  $i$  and  $j$ ,  $s$  denotes the transmitted symbols from  $S$ ,  $n_i$  ( $i \in \{D, R, E\}$ ) denotes the independent complex Gaussian noise at  $R$ ,  $D$  and  $E$ . In this work, to simplify the analysis, we assume that  $n_R$ ,  $n_D$  and  $n_E$  are with zero means and a same variances,  $N_0$ .

Therefore, the SNR of the received signal at  $R$ ,  $D$  and  $E$  can be written as

$$\gamma_R = \frac{P_S |h_{SR}|^2}{N_0} \quad (2-a)$$

$$\gamma_{D1} = \frac{P_S |h_{SD}|^2}{N_0} \quad (2-b)$$

$$\gamma_{E1} = \frac{P_S |h_{SE}|^2}{N_0} \quad (2-c)$$

respectively.

The probability density function (PDF) of  $|h_{SR}|^2$ ,  $|h_{SD}|^2$  and  $|h_{SE}|^2$  can be given as

$$f_{|h_{SR}|^2}(x) = \frac{1}{h_{SR}} \exp\left(-\frac{x}{h_{SR}}\right) \quad (3-a)$$

$$f_{|h_{SD}|^2}(x) = \frac{1}{h_{SD}} \exp\left(-\frac{x}{h_{SD}}\right) \quad (3-b)$$



$$f_{|h_{SE}|^2}(x) = \frac{1}{h_{SE}} \exp\left(-\frac{x}{h_{SE}}\right) \quad (3 - c)$$

respectively, where  $h_{SR}$ ,  $h_{SD}$  and  $h_{SE}$  are the expectation of channel power gain  $|h_{SR}|^2$ ,  $|h_{SD}|^2$  and  $|h_{SE}|^2$ , respectively.

Further, we can obtain  $\gamma_R \sim \text{Exp}(\lambda_{SR})$ ,  $\gamma_{D1} \sim \text{Exp}(\lambda_{SD})$  and  $\gamma_{E1} \sim \text{Exp}(\lambda_{SE})$ , respectively, where  $\lambda_{SR} = \frac{N_0}{h_{SR}P_S}$ ,  $\lambda_{SD} = \frac{N_0}{h_{SD}P_S}$  and  $\lambda_{SE} = \frac{N_0}{h_{SE}P_S}$ , respectively.

In the second phase, if  $R$  decides to forward the detected symbol,  $s_R$ , to  $D$  after regenerating, the received signal at  $D$  and  $E$  is

$$y_{D2} = \sqrt{P_R} h_{RD} s_R + n_D \quad (4 - a)$$

$$y_{E2} = \sqrt{P_R} h_{RE} s_R + n_E \quad (4 - b)$$

respectively.

Therefore, the SNR of the received signal at  $D$  and  $E$  can be written as

$$\gamma_{D2} = \frac{P_R |h_{RD}|^2}{N_0} \quad (5 - a)$$

$$\gamma_{E2} = \frac{P_R |h_{RE}|^2}{N_0}, \quad (5 - b)$$

respectively.

The PDF of  $|h_{RD}|^2$  and  $|h_{RE}|^2$  can be written as  $f_{|h_{RD}|^2}(x) = \frac{1}{h_{RD}} \exp\left(-\frac{x}{h_{RD}}\right)$  and  $f_{|h_{RE}|^2}(x) = \frac{1}{h_{RE}} \exp\left(-\frac{x}{h_{RE}}\right)$ , respectively, where  $h_{RD}$  and  $h_{RE}$  is the expectation of channel power gain  $|h_{RD}|^2$  and  $|h_{RE}|^2$ , respectively. Then, we can also obtain  $\gamma_{D2} \sim \text{Exp}(\lambda_{RD})$  and  $\gamma_{E2} \sim \text{Exp}(\lambda_{RE})$ , respectively.

Then, when SC scheme is adopted, we can have

$$\gamma_D = \begin{cases} \gamma_{D1} & \text{if } \gamma_{SR} \leq \gamma_0 \\ \max\{\gamma_{D1}, \gamma_{D2D}\} & \text{else} \end{cases} \quad (6 - a)$$

$$\gamma_E = \begin{cases} \gamma_{E1} & \text{if } \gamma_{SR} \leq \gamma_0 \\ \max\{\gamma_{E1}, \gamma_{E2}\} & \text{else} \end{cases}, \quad (6-b)$$

respectively, where  $\gamma_{D2D} = \min\{\gamma_{SR}, \gamma_{D2}\}$  is the end-to-end SNR of  $S-R-D$  link under DF scheme, the cumulative distribution function (CDF) of which can be written as  $F_{\gamma_{D2D}}(x) = 1 - \exp(-(\lambda_{SR} + \lambda_{RD})x)$ .

Therefore, the instantaneous secrecy capacity of the considered system can be written as

$$C_s = \begin{cases} \log_2(1 + \gamma_D) - \log_2(1 + \gamma_E) & \text{if } \gamma_E \leq \gamma_D \\ 0 & \text{else} \end{cases} \quad (7-a)$$

If  $\gamma_{SR} \leq \gamma_0$ , we can have

$$C_s = \begin{cases} \log_2(1 + \gamma_{D1}) - \log_2(1 + \gamma_{E1}) & \text{if } \gamma_{D1} \geq \gamma_{E1} \\ 0 & \text{else} \end{cases} \quad (7-b)$$

If  $\gamma_{SR} \geq \gamma_0$ , it deduces

$$C_s = \begin{cases} \log_2(1 + \max\{\gamma_{D1}, \gamma_{D2D}\}) - \log_2(1 + \max\{\gamma_{E1}, \gamma_{E2}\}) & \text{if } \gamma_D \geq \gamma_E \\ 0 & \text{else} \end{cases} \quad (7-c)$$

where  $\gamma_D = \max\{\gamma_{D1}, \gamma_{D2D}\}$  and  $\gamma_E = \max\{\gamma_{E1}, \gamma_{E2}\}$ .

Therefore, the secrecy outage probability for the considered system using threshold can be expressed as

$$\begin{aligned} \Pr_{\text{out}}(C_{\text{th}}) &= \Pr\{\gamma_{SR} > \gamma_0\} \Pr\{C_s \leq C_{\text{th}} | \gamma_{SR} > \gamma_0\} \\ &\quad + \Pr\{\gamma_{SR} \leq \gamma_0\} \Pr\{C_s \leq C_{\text{th}} | \gamma_{SR} \leq \gamma_0\} \end{aligned} \quad (8)$$

In the following, we derive the terms in (8), respectively.

The probability that the SNR of the  $S$ - $R$  link  $\gamma_0$  is below the threshold can be given as

$$\Pr \{ \gamma_{SR} \leq \gamma_0 \} = \int_0^{\gamma_0} \lambda_{SR} \exp(-\lambda_{SR}x) dx = 1 - \exp(-\lambda_{SR}\gamma_0) \quad (9)$$

Then, it is easy to obtain

$$\Pr \{ \gamma_{SR} > \gamma_0 \} = 1 - \Pr \{ \gamma_{SR} \leq \gamma_0 \} = \exp(-\lambda_{SR}\gamma_0) \quad (10)$$

When  $\gamma_{SR} \leq \gamma_0$ , the probability that the instantaneous secrecy capacity  $C_s$  drops below  $C_{th}$  can be presented as

$$\begin{aligned} \Pr \{ C_s \leq C_{th} | \gamma_{SR} \leq \gamma_0 \} &= \Pr \{ C_s \leq C_{th} \} \\ &= \Pr \{ \log_2(1 + \gamma_{D1}) - \log_2(1 + \gamma_{E1}) \leq C_{th} \} \\ &= \Pr \left\{ \log_2 \left( \frac{1 + \gamma_{D1}}{1 + \gamma_{E1}} \right) \leq C_{th} \right\} \\ &= \Pr \left\{ \frac{1 + \gamma_{D1}}{1 + \gamma_{E1}} \leq 2^{C_{th}} \right\} \\ &= \Pr \{ \gamma_{D1} \leq \lambda \gamma_{E1} + \lambda - 1 \} \\ &= \int_0^{\infty} \lambda_{SE} \exp(-\lambda_{SE}\gamma_{E1}) \int_0^{\lambda\gamma_{E1} + \lambda - 1} \lambda_{SD} \exp(-\lambda_{SD}\gamma_{D1}) d\gamma_{D1} d\gamma_{E1} \\ &= \int_0^{\infty} \lambda_{SE} \exp(-\lambda_{SE}\gamma_{E1}) [1 - \exp(-\lambda_{SD}(\lambda\gamma_{E1} + \lambda - 1))] d\gamma_{E1} \\ &= 1 - \int_0^{\infty} \lambda_{SE} \exp(-(\lambda_{SE} + \lambda_{SD}\lambda)\gamma_{E1} - \lambda_{SD}(\lambda - 1)) d\gamma_{E1} \\ &= 1 - \frac{\lambda_{SE} \exp(-\lambda_{SD}(\lambda - 1))}{\lambda_{SE} + \lambda_{SD}\lambda} \end{aligned} \quad (11)$$

where  $\lambda = 2^{C_{th}}$ .

When  $\gamma_{SR} > \gamma_0$ , the probability that the instantaneous secrecy capacity

$C_s$  drops below  $C_{th}$  can be presented as

$$\begin{aligned}
\Pr \{C_s \leq C_{th}\} &= \Pr \{\log_2(1 + \gamma_D) - \log_2(1 + \gamma_E) \leq C_{th}\} \\
&= \Pr \{\gamma_D \leq \lambda\gamma_E + \lambda - 1\} \\
&= \int_0^\infty f_{\gamma_E}(\gamma_E) \int_0^{\lambda\gamma_E + \lambda - 1} f_{\gamma_D}(\gamma_D) d\gamma_D d\gamma_E \\
&= \int_0^\infty f_{\gamma_E}(\gamma_E) F_{\gamma_D}(\lambda\gamma_E + \lambda - 1) d\gamma_E
\end{aligned} \tag{12}$$

where  $f_{\gamma_D}(x)$  and  $f_{\gamma_E}(x)$  are the PDF of  $\gamma_D$  and  $\gamma_E$ , respectively,  $F_{\gamma_D}(x)$  denotes the CDF of  $\gamma_D$ .

As  $\gamma_D = \max\{\gamma_{D1}, \gamma_{D2D}\}$  and  $\gamma_E = \max\{\gamma_{E1}, \gamma_{E2}\}$ ,  $f_{\gamma_E}(x)$  and  $F_{\gamma_D}(x)$  can be presented as

$$\begin{aligned}
f_{\gamma_E}(x) &= \lambda_{SE} \exp(-\lambda_{SE}x) [1 - \exp(-\lambda_{RE}x)] \\
&\quad + \lambda_{RE} \exp(-\lambda_{RE}x) [1 - \exp(-\lambda_{SE}x)]
\end{aligned} \tag{13-a}$$

$$F_{\gamma_D}(x) = [1 - \exp(-\lambda_{SD}x)] [1 - \exp(-(\lambda_{SR} + \lambda_{RD})x)] \tag{13-b}$$

Substituting Eq. (13) into (12), we can obtain

$$\begin{aligned}
\Pr \{C_s \leq C_{th}\} &= \int_0^\infty \lambda_{SE} \exp(-\lambda_{SE}\gamma_E) [1 - \exp(-\lambda_{RE}\gamma_E)] \\
&\quad \times [1 - \exp(-\lambda_{SD}(\lambda\gamma_E + \lambda - 1))] \\
&\quad \times [1 - \exp(-(\lambda_{SR} + \lambda_{RD})(\lambda\gamma_E + \lambda - 1))] d\gamma_E \\
&\quad + \int_0^\infty \lambda_{RE} \exp(-\lambda_{RE}\gamma_E) [1 - \exp(-\lambda_{SE}\gamma_E)] \\
&\quad \times [1 - \exp(-\lambda_{SD}(\lambda\gamma_E + \lambda - 1))] \\
&\quad \times [1 - \exp(-(\lambda_{SR} + \lambda_{RD})(\lambda\gamma_E + \lambda - 1))] d\gamma_E
\end{aligned} \tag{14}$$

In order to facilitate the following analysis, we will consider a new integral

$$I = \int_0^\infty \exp(-ax) [1 - \exp(-bx)] [1 - \exp(-cx - e)] [1 - \exp(-dx - f)] dx \text{ (where}$$

$a, b, c, d, e$  and  $f$  are constant, and  $a > 0, b > 0, c > 0$  and  $d > 0$ ), which can be calculated as

$$\begin{aligned}
I &= \int_0^{\infty} \exp(-ax) dx - \int_0^{\infty} \exp(-(a+b)x) dx \\
&\quad - \int_0^{\infty} \exp(-(a+c)x - e) dx - \int_0^{\infty} \exp(-(a+d)x - f) dx \\
&\quad + \int_0^{\infty} \exp(-(a+b+c)x - e) dx + \int_0^{\infty} \exp(-(a+b+d)x - f) dx \\
&\quad + \int_0^{\infty} \exp(-(a+c+d)x - e - f) dx \\
&\quad - \int_0^{\infty} \exp(-(a+b+c+d)x - e - f) dx \\
&= \frac{1}{a} - \frac{1}{a+b} - \frac{1}{a+c} \exp(-e) - \frac{1}{a+d} \exp(-f) \\
&\quad + \frac{1}{a+b+c} \exp(-e) + \frac{1}{a+b+d} \exp(-f) \\
&\quad + \frac{1}{a+c+d} \exp(-e - f) - \frac{1}{a+b+c+d} \exp(-e - f)
\end{aligned} \tag{15}$$

By using Eq. (15) into (14), we obtain

$$\begin{aligned}
\Pr \{C_s \leq C_{th}\} &= 1 - \left( \frac{\lambda_{SE}}{\lambda_{SE} + \lambda_{SD}\lambda} + \frac{\lambda_{RE}}{\lambda_{RE} + \lambda_{SD}\lambda} \right) \exp(\lambda_{SD}(1 - \lambda)) \\
&\quad - \left( \frac{\lambda_{SE}}{\lambda_{SE} + (\lambda_{SR} + \lambda_{RD})\lambda} + \frac{\lambda_{RE}}{\lambda_{RE} + (\lambda_{SR} + \lambda_{RD})\lambda} \right) \exp((\lambda_{SR} + \lambda_{RD})(1 - \lambda)) \\
&\quad + \frac{\lambda_{SE} + \lambda_{RE}}{\lambda_{SE} + \lambda_{RE} + \lambda_{SD}\lambda} \exp(\lambda_{SD}(1 - \lambda)) \\
&\quad + \frac{\lambda_{SE} + \lambda_{RE}}{\lambda_{SE} + \lambda_{RE} + (\lambda_{SR} + \lambda_{RD})\lambda} \exp((\lambda_{SR} + \lambda_{RD})(1 - \lambda)) \\
&\quad + \left( \frac{\lambda_{SE}}{\lambda_{SE} + \lambda_{SD}\lambda + (\lambda_{SR} + \lambda_{RD})\lambda} + \frac{\lambda_{RE}}{\lambda_{RE} + \lambda_{SD}\lambda + (\lambda_{SR} + \lambda_{RD})\lambda} \right) \\
&\quad \times \exp((\lambda_{SD} + \lambda_{SR} + \lambda_{RD})(1 - \lambda)) \\
&\quad - \frac{\lambda_{SE} + \lambda_{RE}}{\lambda_{SE} + \lambda_{RE} + \lambda_{SD}\lambda + (\lambda_{SR} + \lambda_{RD})\lambda} \exp((\lambda_{SD} + \lambda_{SR} + \lambda_{RD})(1 - \lambda))
\end{aligned} \tag{16}$$

Therefore, the SOP for the threshold DF scheme can be obtained by substituting Eqs. (9), (10), (11) and (16) into (8).

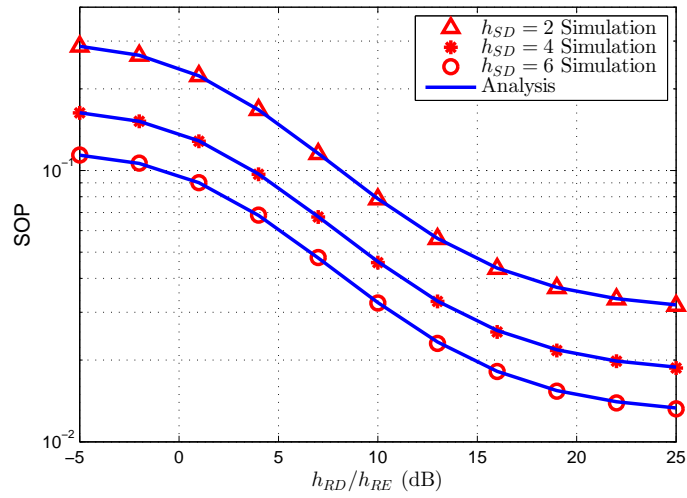
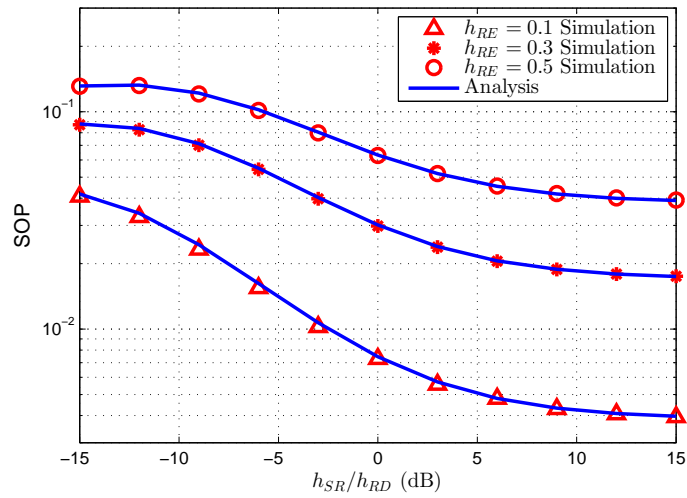
#### 4. Numerical and simulation results

In order to confirm our proposed model, in this section we compare Monte-Carlo simulation and analytical results corresponding to the secrecy outage over independent Rayleigh fading channels. During each simulation,  $S$  sends  $10^6$  bits to  $D$ .

Figure 2 presents the result of the SOP versus  $(h_{RD}/h_{RE})$ . Unless otherwise explicitly specified, the parameters are set as  $P_s = 5$  dB,  $P_r = 5$  dB,  $N_0 = 1$  dB,  $C_{th} = 3$  dB,  $\gamma_0 = 0.05$ . It is obvious that SOP can be improved while  $(h_{RD}/h_{RE})$  increases, because a larger  $(h_{RD}/h_{RE})$  means a better  $R$ - $D$  link with high security. Further, it can also be seen that simulation results match very well with analytical ones. In Figure 2 simulation and analytical results are presented for  $h_{SD} = 2, 4, 6$ . It could be observed that the SOP for a higher  $h_{SD}$  outperforms that of a smaller  $h_{SD}$  as a higher  $h_{SD}$  represents a better  $S$ - $D$  link.

Figure 3 presents the results of the SOP versus  $(h_{SR}/h_{RD})$ . Unless otherwise explicitly specified, the parameters are set as  $P_s = 5$  dB,  $P_r = 5$  dB,  $N_0 = 1$  dB,  $C_{th} = 3$  dB,  $\gamma_0 = 0.05$ . It is obvious that SOP can be improved while  $(h_{SR}/h_{RD})$  increases, because a larger  $(h_{SR}/h_{RD})$  represents a better  $S$ - $R$  link. Further, one can also be seen that simulation results match very well with analytical ones. In Figure 3, we can also see that simulation and analytical results of SOP are given while  $h_{RE} = 0.1, 0.3$  and  $0.5$ . It could be observed that the SOP for a higher  $h_{RE}$  outperforms that of a smaller  $h_{RE}$  as a smaller  $h_{RE}$  represents a worse  $R$ - $E$  link.

Figure 4 and 5 present the results of the SOP versus  $P_s$ . We find that SOP can be improved with the increasing of  $P_s$ , as larger  $P_s$  indicates that

Figure 2: SOP versus  $(h_{RD}/h_{RE})$  for different  $h_{SD}$ Figure 3: SOP versus  $(h_{SR}/h_{RD})$  for different  $h_{RE}$

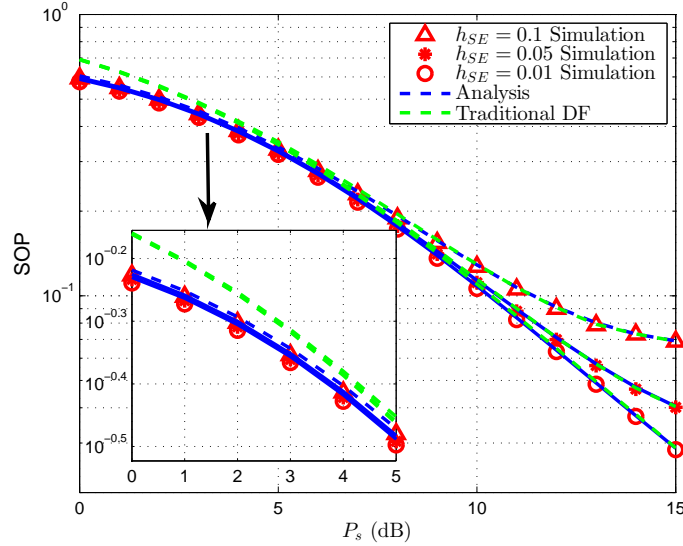


Figure 4: SOP versus  $P_s$  for different  $h_{SE}$

a larger success probability of the transmission over  $S$ - $R$  and  $S$ - $D$  links. In Figure 4, we compare simulation and analytical results while  $h_{SE} = 0.1, 0.05$  and  $0.01$  with  $P_r = 10$  dB,  $N_0 = 0.5$  dB,  $C_{th} = 1$ ,  $\gamma_0 = 0.5$ . It is observed that SOP can be improved with the decreasing of  $h_{SE}$  in the high  $P_s$  region, while no more improvement can be found in the low  $P_s$  region. Because, when  $P_s$  is low, the probability that  $\gamma_{SR} \leq \gamma_0$  will increase, as suggested by Eq. (11).

In Figure 5, we present the simulation and analytical results of SOP while  $h_{RD} = 2, 4$  and  $6$  with  $P_r = 10$  dB,  $N_0 = 1$  dB,  $C_{th} = 1.5$ ,  $\gamma_0 = 1$ . It is observed that SOP can be enhanced with the increase of  $h_{RD}$  in the high  $P_s$  region. One can also clearly observe that there exists a fluctuation and the SOP for different  $h_{RD}$  will approach to a constant. Because when  $P_s$  is high, the SNR of  $S$ - $D$  link will be improved, which indicates that the data



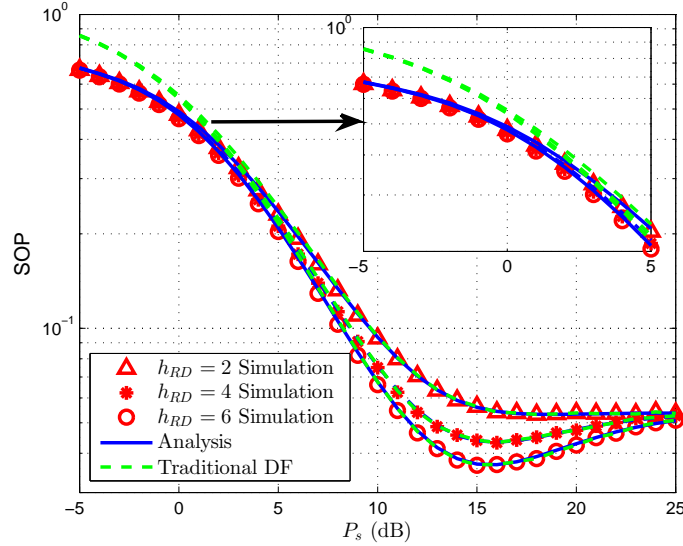


Figure 5: SOP versus  $P_s$  for different  $h_{RD}$

transmission over  $S$ - $R$  link will succeed. Then  $R$  will aid the information delivery between  $S$  and  $D$ , finally resulting in the diversity gain at  $D$ . So under this case the proposed threshold DF scheme will be degraded to the traditional DF scheme, and the secrecy outage performance of the target system will tend to a constant in high  $h_{RD}$ .

Moreover, as observed in Figs. 4 and 5, the proposed threshold DF scheme outperforms the traditional DF scheme in low  $P_s$  region. It can be explained by the following fact: Under the proposed threshold DF scheme,  $R$  will not forward the information for  $S$  and  $D$ , as  $R$  finds the  $S$ - $R$  transmission does not satisfy the requirement of quality. Then, in low  $P_s$  region only  $S$ - $D$  transmission happens and  $E$  only can overhear the data transmission for one time, leading to the improved secrecy outage performance. The performance of the proposed threshold DF scheme approaches to the one of the traditional

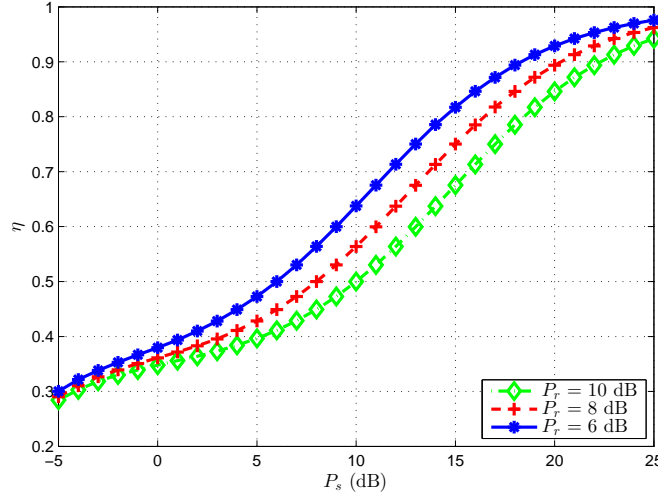


Figure 6:  $\eta$  versus  $P_s$  for different  $P_r$

DF scheme in high  $P_s$  region. Because  $R$  will play as the relay for  $S$ - $D$  transmission to forward the information over  $R$ - $D$  link, which inevitably increases the eavesdropping probability of the data transmission.

In the following, we define the total consumption power of the considered system with the proposed threshold DF relaying scheme as  $P_{SUM}$  and the total consumption power of the considered system with traditional DF system as  $P_{SUM}^{DF}$ , respectively. In Figure 6, we define a new performance index  $\eta = \frac{P_{SUM}}{P_{SUM}^{DF}}$  to illustrate the proposed threshold DF system can significantly save the consumed power. We can see from Figure 6 that  $\eta \leq 1$ , which means that the proposed threshold DF scheme can significantly save more consumed power than the traditional DF scheme, especially in low  $P_s$  region. Because when  $S$ - $R$  link is poor,  $R$  will keep silent and save the transmit power consumed over the relay link from  $R$  to  $D$ .

## 5. Conclusions

In this work, we have investigated the secrecy outage performance of a dual-hop DF cooperative network. We derived the closed-form analytical expressions for SOP while considering the proposed  $S - R$  link based threshold DF relay scheme, which is verified via Monte-Carlo simulations. By observing these numerical results, we can conclude that lower transmit power at the source can obtain lower secrecy outage probability. However, when the transmit power at the source increases, the data forwarding offered by threshold DF relay from the relay to the destination will inevitably increase the probability of the data transmission being eavesdropped, and then SOP will degrade and approaches to a constant, as the traditional DF scheme.

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