

1 **Influences of various magnetospheric and ionospheric current systems on**
2 **geomagnetically induced currents around the world.**

3 **J. S. de Villiers¹, M. Kosch^{1,2,3}, Y. Yamazaki², and S. Lotz¹**

4 ¹ SANSa Space Science, P.O. Box 32, Hermanus, 7200, South Africa.

5 ² Department of Physics, University of Lancaster, United Kingdom.

6 ³ Department of Physics, University of Western Cape, Bellville, South Africa.

7 Corresponding author: Michael Kosch (mkosch@sansa.org.za)

8 **Key Points:**

- 9 • Investigation of E-field influence on GIC from each source current by B-field inversion
- 10 • E-field of AEJ has more influence than EEJ and RC in their respective regions
- 11 • EEJ current strength is the weakest, while the RC is the strongest due to a larger flux of
- 12 charged particles flowing through it
- 13

14 **Abstract**

15 Ground-based observations of geomagnetic field (B-field) are usually a superposition of
16 signatures from different source current systems in the magnetosphere and ionosphere.
17 Fluctuating B-fields generate geoelectric fields (E-fields), which drive geomagnetically induced
18 currents (GIC) in technological conducting media at Earth's surface. We introduce a new Fourier
19 integral B-field model of east/west directed line current systems over a one-dimensional multi-
20 layered Earth in plane geometry. Derived layered-Earth profiles, given in the literature, are
21 needed to calculate the surface impedance, and therefore reflection coefficient in the integral.
22 The 2003 Halloween storm measurements were Fourier transformed for B-field spectrum
23 Levenberg-Marquardt least-squares inversion over latitude. The inversion modelled strength of
24 the equatorial (EEJ), auroral (AEJ) electrojets, and ring currents (RC) were compared to the
25 forward problem computed strength. It is found the optimized and direct results match each other
26 closely, and supplement previous established studies about these source currents. Using this
27 model, a data set of current system magnitudes may be used to develop empirical models linking
28 solar wind activity to magnetospheric current systems. In addition, the ground E-fields are also
29 calculated directly, which serves as a proxy for computing GIC in conductor-based networks.

30 **1 Introduction**

31 Geomagnetically induced currents (GIC) can occur in ground-based technical networks,
32 such as electric power transmission grids, oil and gas pipelines, telecommunication cables and
33 railway circuits. Solar events, such as geo-effective coronal mass ejections, create disturbances
34 within the Earth's magnetosphere, which can give rise to geomagnetic storms and substorms.
35 During geomagnetic storms, the compression of the magnetosphere by the solar wind, and the
36 interaction of the solar wind with the Earth's geomagnetic field (the B-field) enhance the

37 currents in both the magnetosphere and in the ionosphere [e.g. *Bothmer and Daglis, 2007*]. These
38 currents cause fluctuations in the B-field on the ground. Rapid changes in the B-field generate
39 geoelectric fields (E-fields) that drive GIC in the networks.

40 Ever since the discovery that the earth has a magnetic field [*Gilbert, 1600*] basic
41 electromagnetic theory suggests that a current system must be involved in driving this field. Its
42 fluctuations with periods shorter than a day have been connected to various current systems high
43 above the Earth's atmosphere. Each current system has its own geomagnetic signature, and a
44 number of standard geomagnetic indices have been developed to quantify each of these
45 signatures in the field. These individual systems have a unique influence on GIC, via the surface
46 E-field, in conductor networks in various parts of the world. GIC is known to have caused
47 damage and blackouts in power utility systems [e.g. *Kappenman, 2007; Gaunt and Coetzee,*
48 *2007*]. Where more than one system is influencing any one particular region, then a
49 superposition of individual signatures will result in a combined effect on GIC in this area
50 [*Anderson et al., 2006*].

51 1.1 Three Source Current Systems

52 Our world can be sub-divided into seven different regions according to the positions of
53 the separate electrojets. The region of the equatorial electrojet (EEJ) on the magnetic dip equator
54 is called the geomagnetic low-latitude region or Equatorial Region. The northern and southern
55 regions of the auroral electrojet (AEJ) with the ionospheric end of the field-aligned currents
56 (FAC) are called the geomagnetic high-latitude auroral regions. Both electrojets are about
57 100 km above the Earth's surface in the ionosphere, and by spherical geometric arguments their
58 influence only extends six to nine degrees away from their respective positions [*Anderson et al.,*
59 *2002, 2004, 2006*]. What is not covered by the electrojets is called the north and south Polar-Cap

60 Regions, enclosed by each AEJ; and the north and south mid-latitude regions of the Earth,
61 between the EEJ and either AEJ.

62 The Earth's ring current (RC) is partly responsible for shielding the lower latitudes of the
63 Earth from magnetospheric electric fields. It therefore has a large effect on the electrodynamic
64 of geomagnetic storms. The RC system is three to eight Earth radii distant in the equatorial plane
65 and circulates generally westwards. The particles of this region produce a magnetic field in
66 opposition to the Earth's magnetic field and so an observer on Earth would see a decrease in the
67 magnetic field in this area (as captured by the Dst index) [*Baumjohann and Treumann, 1996;*
68 *Kozyra and Liemohn, 2003*].

69 The term 'auroral electrojet' (or AEJ) is the name given to the large horizontal currents
70 that flow in the D and E regions of the auroral ionosphere confined to the high latitude regions
71 (65°N/S). The AEJ was first proposed to exist by *Alfven* [1939, 1940] and modelled by *Bostrom*
72 [1964]. During magnetically quiet periods, the electrojet is generally confined to the auroral oval.
73 However during disturbed periods, the electrojet increases in strength and expands to both higher
74 and lower latitudes. This expansion results from two factors, enhanced particle precipitation and
75 enhanced ionospheric electric fields.

76 Equatorial electrojet (EEJ) currents were first reported by *Egedal* [1947] to exist in the
77 equatorial ionosphere when the Huancayo geomagnetic observatory started operations in Peru.
78 The worldwide solar-driven wind results in the so-called Sq-current system in the E region of the
79 Earth's ionosphere (100– 130 km altitude). Resulting from this current is an electrostatic field
80 directed East-West (dawn-to-dusk) in the day side of the ionosphere. At the magnetic dip
81 equator, where the geomagnetic field is horizontal, this electric field results in an enhanced

82 eastward current within ± 3 degrees of the magnetic dip equator, known as the EEJ
83 [*Onwumechili*, 1998; *Casey*, 2005].

84 Recent research focusses on the topic of GICs in low-latitude or equatorial regions. The
85 impact of these currents at high latitudes has been extensively researched, but the magnetic
86 equator has been largely overlooked. In *Pulkkinen et al.* [2012] a series of 100-year extreme
87 E-field and GIC scenarios are explored by taking into account the key geophysical factors
88 associated with the geomagnetic induction process. *Ngwira et al.* [2013] report on the global
89 behavior of the horizontal B-field and the induced E-field fluctuations during severe/extreme
90 geomagnetic events. *Carter et al.* [2015] investigated the potential effects of interplanetary
91 shocks on the equatorial region and demonstrated that their magnetic signature is amplified by
92 the equatorial electrojet.

93 This paper will introduce a new geomagnetic inversion method of a line current model
94 that makes possible the computation of current strengths of the EEJ, the AEJ, and the RC and
95 determination of the separate ground E-fields that influence and drive GIC in conducting media
96 networks on the ground. We will use the input indices of EE (defined by *Uozumi et al.* [2008]),
97 AO (defined by *Davis and Sugiura* [1965]), and Dst (defined by *Sugiura* [1964] and *Gannon and*
98 *Love* [2011]) or SYM-H (defined by *Iyemori* [1990] and *Wanliss and Showalter* [2006]) for each
99 current system respectively. We will show the inversion results compares accurately to the direct
100 results of the forward problem. We base our geomagnetic inversion approach on the line
101 current's B- and E-field computations of *Boteler and Pirjola* [1998], *Pirjola and Viljanen*
102 [1998], *Pirjola* [1998], *Boteler et al.* [2000], *Pirjola and Boteler* [2002].

103 One motivation for using inversion techniques in this study is that the B-field
104 measurement is generally not available at the location of interest for calculation of the E-field. B-

105 field recordings are only made at established observatories and where additional magnetometers
106 were installed. When E-fields are directly computed from available B-field data, via ground
107 impedance from an appropriate conductivity profile, this can only be done at those locations. On-
108 site profiles may not even be available at such locations; thus, nearby profiles have to be found
109 and used instead. The inversion method allows one to compute the B-fields over a range of
110 latitudes along a chosen meridian in the vicinity of these stations. Once the current strength is
111 determined, as an output parameter, one can return to the model function in the forward problem
112 and use the parameter to calculate the E-fields anywhere other than just at B-field measurement
113 locations. Inversion provides an alternative way in which to estimate E-fields where it is not
114 possible by any other means [*De Villiers and Cilliers, 2014*].

115 **2 Background**

116 While *Cagnaird* [1953] was the seminal paper that opened the field of magneto-telluric
117 and GIC studies, *Wait* [1958, 1980] introduced the layered-Earth method for computing surface
118 impedances, reflection coefficients and related material properties of the ground underneath the
119 Earth. Originally introduced by *Wait and Spies* [1969], *Thomson and Weaver* [1975] applied the
120 complex image method to the induction of line currents in a layered Earth. The beginnings of a
121 theory of B-fields and E-fields of line current systems at a distance above the Earth's surface in
122 plane geometry has been researched by *Pirjola* [1982,1984,1985], *Viljanen* [1992] and later
123 *Pulkkinen* [2003a]. A comprehensive theory was presented by *Häkkinen and Pirjola* [1986] for
124 computing the B-fields and E-fields at the Earth's surface due to an electrojet or ring current in
125 the magnetosphere above a layered Earth.

126 We build on the above theory with a new approach presented by *De Villiers and Cilliers*
127 [2014] and *De Villiers et al.* [2016]. They introduced geomagnetic inversion to obtain

128 ionospheric current system parameters in the frequency ω and latitude x domain. In the former
129 reference, the setup was prepared for a given real-valued spectral current strength $J(\omega)$ at a
130 single frequency ω only, height h , and latitude position x_o . To test that the inversion techniques
131 work, simulated data were generated over x -space from the given parameter values and inserted
132 into the inversion setup to recover those parameters. In the latter reference, only the strength of
133 the current was determined with fixed distance parameters ($h \neq 0$, $x_o = 0$) by the same
134 inversion method from measured B-field data for two stations simultaneously (under and away
135 from the current system). The current strength was complex-valued this time and each complex
136 part became two independent model parameters, i.e. $J_r(\omega)$ and $J_i(\omega)$. The inversion was
137 repeated for the range of frequencies determined from a Fourier transform of the given
138 measurements.

139 The above methods were then adapted to this paper's approach described below. Source
140 currents can still be approximated with a line current system. Each current system is now
141 associated with only one appropriate geomagnetic index. The geomagnetic horizontal component
142 B_x is normally assigned to the index. No additional independent geomagnetic index is available
143 for the inversion. This makes the inversion underdetermined with two model parameters and
144 only a single Fourier transformed data point of the index, assumed to be located directly
145 underneath the source current. The procedure has to be adapted by generating at least one more
146 set of data from the same index and positioned away from the system. With two mutually
147 dependent data points at different locations sufficient for the inversion to be well-determined, a
148 perfect convergence results and the two parameters are determined exactly.

149 The Fourier integral of the B-field, extended for field observations above or below the
150 Earth's surface:

$$151 \quad \begin{bmatrix} B_x \\ B_z \end{bmatrix} (x, z, \omega) = \frac{\mu J(\omega)}{2\pi} \int_0^\infty \left\{ \begin{array}{l} [R(\nu, \omega) + 1] \cos(\nu x) \\ [R(\nu, \omega) - 1] \sin(\nu x) \end{array} \right\} e^{-\nu(z+h)} d\nu. \quad (1)$$

152 where $R(\nu, \omega)$ is the surface reflection coefficient and ν is the horizontal wavenumber. Only
 153 surface B-fields ($z = 0$ km) are evaluated and only the B_x component will be used as the input
 154 model function for the inversion process in this study. In general, the integrals involved have no
 155 analytical solutions and must be solved numerically.

156 **3 Methods and Procedures**

157 The source currents can be approximated by a line current physical system described in
 158 the previous section. Geomagnetic data is obtained in the form of indices for each current
 159 system: AO for the AEJ, EE for the EEJ, and Dst or SYM-H for the RC. The AO(= $\frac{1}{2}$ AU+ $\frac{1}{2}$ AL)
 160 index is preferred to the AE(=AU-AL) index since it represents the equivalent current for the
 161 auroral zone and not just the net effect of the eastward and westward electrojets. Then a
 162 geomagnetic least-square inversion is done by fitting the model function to the input index,
 163 determining the current strength as an output model parameter of the function, with the sum-of-
 164 squared-residuals as objective function. The current strength parameter can then be used to
 165 calculate the E-field on the Earth's surface directly underneath the current system. The E-field is
 166 responsible for driving GIC in conductor networks in a given region. Computation of GIC is
 167 outside the scope of this work, as it requires knowledge of grounded conductor network
 168 parameters.

169 We choose to analyze the Halloween Storm of the year 2003. This is a widely studied
 170 event with known GIC-related impact on networks at middle latitudes [e.g. *Love and Swidinsky,*
 171 *2015; Torta et al., 2012; Pulkkinen et al., 2012; Gaunt and Coetzee, 2007; Trivedi et al., 2007*].

172 Data of AO, Dst and SYM-H are already available on the Kyoto Space Weather Centre
173 website. However, the EE index, used as a measure of the zonal current intensity of the EEJ,
174 only started data records in the year 2010, and are thus unavailable for the storm in question. The
175 index represents horizontal magnetic perturbations at the magnetic equator corrected for the Dst
176 index. We derived the EE-index separately for the African and American sectors using magnetic
177 measurements from 26 October to 7 November 2003 at the INTERMAGNET stations [Kerridge,
178 2001] Addis Ababa (Ethiopia) and Huancayo (Peru) respectively (see Table 1 for the
179 coordinates). Dst minute data was taken from the United States Geological Survey (USGS)
180 website. Therefore $EE(t) = \Delta B_x(t) - Dst(t)$ where $\Delta B_x(t) = B_x(t) - \text{median}(B_x(t))$. The
181 median of B-field measurements was taken for the entire 13-day period.

182 Surface impedance and reflection coefficient data can be derived from conductivity
183 profiles of the ground. For the EEJ, the nearest available profile to Ethiopia is taken to be in
184 Nairobi, capital of Kenya, and was simplified from a more complete profile given in the
185 Appendix. The nearest available profile to Peru [Schwarz and Kruger, 1997: Fig.7a] is on strip A
186 across northern Chile at 21.5°S. We take the structure where this strip meets the Pacific coast, at
187 Tocopilla harbour. The profile is named after this harbour town, as it is not named in the given
188 reference (see Table 1 again for the coordinates). A deep-layer conductivity profile was also
189 derived from Swarm satellite geomagnetic measurements [Civet *et al.*, 2015], and appended to
190 the Nairobi and Tocopilla profiles from below. Table 2 lists the conductivities and thicknesses of
191 the profiles. The Quebec conductivity profile [Boteler and Pirjola, 1998] was used for the AEJ
192 E-field. The Swarm conductivity profile alone was sufficient to compute the RC E-field.

193 3.1 Forward Computation of Line Current Systems

194 From Eq.(1) the B-field north component is restated here for the forward problem
 195 [Häkkinen and Pirjola, 1986; Boteler et al. 2000].

$$196 \quad B_x(x, \omega) = B_{x,r}(x, \omega) + iB_{x,i}(x, \omega) = \frac{\mu}{2\pi} \int_0^\infty J(\nu, \omega) [R(\omega) + 1] e^{-\nu h} \cos(\nu x) d\nu \quad (2)$$

197 Note that, for purposes of this discussion, the current strength $J(\omega)$ was generalized for a
 198 latitude distributed current system and incorporated into the integral. This is easily computed
 199 provided the current strength $J(\nu, \omega)$, reflection coefficient $R(\omega, \nu)$ and fixed distance
 200 parameters (h, x) are known. However, if the $J(\nu, \omega)$ is unknown, then Eq.(2) must be
 201 determined from ground geomagnetic measurements instead. The current strength is still inside
 202 the integral, and cannot be separated from the integral while it still depends on the integration
 203 variable ν (i.e. it is integrated along with the rest of the integrand). Inversion alone will have to
 204 be applied to fit the right-hand-side of Eq.(2) model function to a Fourier transform of the left-
 205 hand-side of Eq.(2) geomagnetic measurements.

206 Line current systems make the forward problem easier, because then $J(\nu, \omega) \rightarrow J(\omega)$ and
 207 the current strength can be taken out of the integral. With $J(\omega)$ separated, we define a new
 208 function for the remaining integral:

$$209 \quad F_x(x, \omega) = F_{x,r}(x, \omega) + iF_{x,i}(x, \omega) = \frac{\mu}{2\pi} \int_0^\infty [R(\omega, \nu) + 1] e^{-\nu h} \cos(\nu x) d\nu \quad (3)$$

210 Eq.(2) then becomes $B_x(x, \omega) = J(\omega)F_x(x, \omega)$ and dividing through by Eq.(3) gives

$$211 \quad J(\omega) = J_r(\omega) + iJ_i(\omega) = \frac{B_x(x, \omega)}{F_x(x, \omega)} = \frac{F_x^*(x, \omega)B_x(x, \omega)}{|F_x(x, \omega)|^2} \quad (4)$$

212 allowing the current strength to be determined by forward calculation. All that remains then is to
 213 take the inverse Fourier transform of $J(\omega)$ to obtain time-series data $J(t)$ for the storm period.

214 3.2 Inverse Modelling of Line Current Systems

215 The $B_{x;n} = B_x(x_n, \omega)$ is the given data points at positions $x_n, n = 1, \dots, N$; and Eq.(2) is used as
216 the model function $B_x(x, \omega)$ for the adapted inversion problem [De Villiers et al., 2016]. The
217 inversion is a least-squares problem where the objective function is the sum-of-squared-
218 residuals, $SSR = \sum r_n^2$, where $r_n = B_x(x, \omega) - B_{x;n}$. Various optimization techniques are used
219 to minimize the SSR in order for Eq.(2) to be fitted to the given data. One technique robust
220 enough for this task is the Levenberg-Marquardt method [Press et al., 1992; Lourakis, 2005].
221 The model function is fitted to a set of input data points from the geomagnetic measurement
222 transform at different latitude positions along the meridian. To simplify calculations, the origin
223 of the x -space is always underneath the respective latitude position of each current system. On
224 this latitude space, the inversion is repeatedly run for each frequency of the resulting
225 measurement spectrum, each complex value fitted to the model function and the output model
226 parameters determined. For all given frequencies, therefore, a parameter spectrum of amplitudes
227 is set up.

228 As per definition, the model function must contain output model parameters which can be
229 adjusted by the inversion in order for the model function to best fit the given data. These
230 parameters are derived from two distinct elements of the physical setup: the thicknesses and
231 conductivities of layered-Earth profiles, and the current strength and distance positions (height
232 and latitude) of the line current system. When only the current strength is adjusted, the inversion
233 is a linear problem (the aim for this paper). When any of the other parameters are adjusted, with
234 or without the current strength, the inversion becomes non-linear.

235 **Figure 1** shows a diagram of the geomagnetic inversion over latitude space for only a
 236 single frequency representing either the real or complex part of the B-field measurement
 237 transform. Only one diagram is shown, the other diagram of the pair is similar. The plot consists
 238 of a bell-shaped inversion model function (solid curve) and three data points (circles). This setup
 239 will be used in all our line current inversion computations.

240 In the plot, the recorded index is to be associated with the central data point at the
 241 relevant current system position, i.e. $B_{index} = B_x(x = 0, \omega)$. This is also the maximum of the
 242 curve in **Fig.1**. However, the inversion cannot work with just one given data point (i.e. it is
 243 under-determined and ill-defined). It becomes necessary to strengthen the setup with at least two
 244 data points. For this to be done, first the forward calculation **Eq.(4)** is used to obtain the current
 245 strength: $J(\omega) = B_x(0, \omega)/F_x(0, \omega)$. Second the computed $J(\omega)$ is substituted into **Eq.(2)** for
 246 calculation of $B_x(x \neq 0, \omega)$. Then inversion can proceed.

247 Though not a requirement for inversion, the model function is also symmetric around
 248 $x = 0$ km. It is then possible to compute one data point at $x = x_s$ on one side of the current
 249 system. By symmetry, $B_x(-x_s, \omega) = B_x(+x_s, \omega)$ is computed for equal and opposite position
 250 $x = -x_s$ on the other side. This then defines two symmetric data points $B_x(\pm x_s, \omega)$ that anchor
 251 the central data point $B_x(0, \omega)$. We use these three input data points (thus $N = 3$) from only one
 252 measured geomagnetic data set (i.e. the index) to perform the inversion in this paper.

253 3.3 E-field Calculation

254 The E-field is important because it is regarded as the main driver for creating GIC in
 255 conductor networks on the surface of the Earth. There are two equally valid formulations:

256 1. The integral way is the calculation of the E-field from the given current system and the
 257 surface impedance via the surface reflection coefficient $R(\nu, \omega)$, without recourse to
 258 measured B-fields beforehand. The E-field Fourier integral [De Villiers et al., 2016] is

$$259 \quad E_y(x, \omega) = i\omega \frac{\mu_0 I(\omega)}{2\pi} \int_0^\infty [R(\nu, \omega) - 1] \nu^{-1} e^{-\nu h} \cos(\nu x) d\nu. \quad (5)$$

260 For $R(\nu, \omega) = \frac{i\omega\mu_0 - \nu Z(\omega)}{i\omega\mu_0 + \nu Z(\omega)}$, the field calculations give the same results in the integral
 261 method at the position ($x = 0$ km) of the current system, as those computed from the
 262 direct method. The surface impedance $Z(\omega)$ is embedded in the reflection coefficient,
 263 and computed from ground profiles.

264 2. The direct way is to calculate the ground E-field from the ground B-field by multiplying
 265 it by the surface impedance $Z(\omega)$, where the free space permeability constant is μ_0 :

$$266 \quad E_y(x, \omega) = -\frac{Z(\omega)}{\mu_0} B_x(x, \omega). \quad (6)$$

267 This equation is derived by substituting the expression of $R(\nu, \omega)$ into Eq.(5) and
 268 recovering the top vector component of Eq.(1) by separating $Z(\omega)/\mu_0$ from the resulting
 269 integral.

270 An E-field spectrum is set up by either method for latitudes $x \in [-x_s, 0, +x_s]$. Either way,
 271 the results will be the same and its spectrum is then inversely Fourier-transformed to the time-
 272 series E-field for the same period of the chosen storm.

273 4 Computations and Their Results

274 4.1 Placement of the Current Systems

275 E-field values are being calculated for three different heights: $h = 100$ km for the AEJ
276 and EEJ; $h = 3R_E$ and $h = 8R_E$ for the RC (Earth's radius: $R_E = 6371.2$ km). For $h = 100$ km,
277 the non-zero symmetric data points are selected to be 6 degrees latitude (or $x_s = 667$ km) away
278 on either side of the AEJ and EEJ. This latitude value is at or near the outer extent of their range-
279 of-influence, allowing the inversion setup to capture most of the magnetic signatures of the
280 electrojets.

281 The RC physical setup is more complicated, because of its placement in the upper
282 magnetosphere. Its B-field is super-imposed upon by the geomagnetic signatures from both
283 electrojets in the low and high latitudes. To escape the electrojets influence, one needs to enter
284 the middle latitudes. The mid-latitude region is exposed only to the influence of the RC (and
285 other upper magnetosphere current systems) during a geomagnetic storm. For this reason, the Dst
286 is computed from geomagnetic mid-latitude stations only (with the EEJ influence thus removed),
287 and then normalized to become an equatorial index [Sugiura, 1964]. In our approach then, the
288 index is positioned on the geomagnetic equator underneath the RC.

289 The index is used for the forward computation of its current strength at this central
290 location. For the inverse computation, a different pair of latitudes is computed to position the
291 symmetric data points on either side of the RC. Due to its height being so far from the Earth, the
292 range-of-influence of the RC nearly covers all geomagnetic latitudes of the Earth. In RC-Earth
293 spherical geometry, this latitude is calculated from a triangle with the RC-to-Earth's center
294 distance at the hypotenuse and the Earth's radius at the adjacent side. Thus for the upper height,

295 we have $\cos^{-1}[1R_E/(1+8)R_E] = 83.62^\circ$ (or $x_s = 9291$ km) north and south of the
 296 geomagnetic equator. With this setup, inversion can be applied to the RC as well.

297 It can be shown that since the same Dst (USGS) will be used for the RC at two different
 298 heights, then by Eq.(6) above, the corresponding E-field derived from the Dst (and its subsequent
 299 influence on GIC in the mid-latitudes) will also be independent of the RC height. When
 300 expressing the Dst by Fourier integral expressions instead, in the form $B_x(x, \omega) = J(\omega)F_x(x, \omega)$,
 301 then Eq.(3-4) applies. Only Eq.(3) [i.e. $F_x(x, \omega)$] contains the height parameter ($\propto e^{-\nu h}$ inside
 302 the integral). With the same Dst index used on the RC system, the current strength Eq.(4) [i.e.
 303 $J(\omega)$] must evaluate as an inverse of $F_x(x, \omega)$. For different given heights in $F_x(x, \omega)$, this
 304 scenario suggests a dependence $J(\omega) \propto e^{\nu h}$. However, this latter proportionality is not so simple,
 305 as the original exponential must still be evaluated over an integration range of wavenumber
 306 values ν in $F_x(x, \omega)$. Instead, the two given RC-heights is substituted in the exponential, the
 307 $F_x(x, \omega)$ integral is computed in each case and the corresponding current strength values are
 308 obtained. Taking the scaling factor then gives $\frac{J(\omega)|_{h=8R_E}}{J(\omega)|_{h=3R_E}} = \frac{F_x(x, \omega)|_{h=3R_E}}{F_x(x, \omega)|_{h=8R_E}} = 338$.

309 4.2 Input/Output Data and their Spectrums

310 [Figure 2](#) gives the one-minute sampled geomagnetic indices (SYM-H from Kyoto, Dst
 311 from USGS, the polar AO and equatorial EE for two stations) for the period from 26 October
 312 2003 to 7 November 2003. A major disturbance can be seen on a 3-day storm period (29-31
 313 October 2003), namely the geomagnetic Halloween Storm. Its sudden commencement (SC)
 314 starts at 06:14 on the first morning. We narrow the period to between 28 October and 1
 315 November 2003, and compute their Fourier transforms. A Brickwall low-pass filter [Owen,
 316 2007: pg.81] is applied on the Fourier transformed data. The amount of radiation energy allowed

317 to pass through [at the threshold cut-off frequency an eighth of Nyquist frequency (8.33 mHz)] is
318 given as a percentage of the total sum of the spectrum [Dst(USGS): 82%, AO: 64%, EE(AAE):
319 61%, EE(HUA): 66%].

320 When the inversion procedure is run, the geomagnetic model is fitted to the transformed
321 data of a given index at each frequency from 0 to 1.04 mHz of the spectrum incremented over
322 360 points (an eighth of 4 days times 1440 minutes per day), and the data shown is that at the
323 central position of the current system involved. [Figure 3](#) shows a comparison of the modelled
324 and measured data for all the indices in both the frequency and time domains. A cross-correlation
325 between the modelled and measured sets should approach autocorrelation of either set, if the two
326 sets are the same (i.e. a symmetric function around zero lag). This can be checked by
327 determining, not only the lag position of maximum cross-correlation, but the root-mean-square
328 (RMS) of the differences between symmetric pairs outward around that lag position. For all the
329 current systems concerned, both the lag and RMS values are found to be zero. The modelled
330 signatures are virtually on top of the measurements. This indicates that the model is correct and
331 complete resulting in a perfect fit to the measured data (with zero residuals in the SSR). This can
332 also be independently confirmed in the subsequent figures below.

333 [Figure 4](#) shows the current strengths of the three source current systems and its output
334 spectrums obtained from inversion of the three respective geomagnetic indices. While the
335 corresponding current strengths depend on the two different heights of the RC, this is indicated
336 on both vertical axes on either side of the plots in [Fig.4a](#). A sudden commencement (SC) of the
337 geomagnetic storm is visible in the RC current strength. The AEJ strength shows more rapid
338 fluctuations than the RC throughout the 4-day period. The EEJ strengths do not follow the storm
339 patterns seen in both AEJ and RC (i.e. deep negative values of the main phase), but are

340 nevertheless disturbed by rapid fluctuations of the storm. These fluctuations distort, but do not
341 destroy, the diurnal strength at both given stations. The HUA diurnal strength is stronger than
342 that of AAE. For each station, local midnight (UT-2.6 hours for AAE and UT+5 hours for HUA)
343 is indicated by vertical lines in the plots.

344 [Figure 5](#) shows the E-fields associated with each index that is computed for the three
345 source current systems. During the given 4-day period, all the E-fields show two distinct periods
346 of strong activity, and an intervening calm period. For the AEJ, the E-field appears more stable
347 than the corresponding fields of the other current systems due to a flat trend with small
348 fluctuations around 0 V/km in the quiet times. In the disturbed times, the AEJ E-field fluctuates
349 with the greatest range than the other current systems, ± 0.5 V/km. At AAE, the E-field of the
350 EEJ is around 10 times weaker than the AEJ E-field, ± 0.05 V/km. At HUA, the E-field of the
351 EEJ is stronger and shifted, $[-0.2, +0.3]$ V/km (half the range of the AEJ E-field). This is even
352 twice as strong as the RC E-field at $[-0.15, +0.1]$ V/km.

353 With the correct model, the E-fields can be determined through the conductivity profile.
354 Traditionally, in the frequency domain and on the surface, the E-field components are directly
355 related to the B-field components via the profile's impedance, see [Eq.\(6\)](#). However, the E-fields
356 can also be obtained via [Eq.\(5\)](#), involving a current density function and a reflection coefficient,
357 the latter of which contains the same surface impedance spectrum. Via $i\omega J(\omega) \leftrightarrow \partial J(t)/\partial t$, the
358 E-field is shown in the figures to be directly related to the rate-of-change of currents over time.
359 For rapid B-field changes, this shows up as large spikes that can generate GIC impulses down a
360 line segment of the conductor networks over a given area.

361 As a consequence of height independence of the Dst index and its E-field, only one transform
362 and its time series is shown in [Fig.3a](#) (Dst) and [Fig.5a](#) (Dst E-field). By contrast, [Fig.4a](#)

363 (currents) shows two transforms and its time series on either vertical axes of the plots,
364 corresponding to two different RC heights.

365 **5 Discussion**

366 The Spherical Elementary Current Systems (SECS) method was introduced by *Amm and*
367 *Viljanen*, [1999]. A matrix of such systems in the ionosphere is set up over a surface coordinate
368 grid of positions in any given region where a power network resides (e.g. *Pulkkinen et al.*,
369 [2003b] and *Wik et al.*, [2008]). A geomagnetic model function is fitted to known geomagnetic
370 measurements at selected observatories in this region, using any decomposition inversion
371 technique, with the currents as linear output parameters. *Vanhamäki et al.* [2003] developed a
372 one-dimensional version of SECS and found it to be 5-10% in error compared with the original
373 two-dimensional SECS in real situations. *Viljanen et al.* [2004] applied the method in GIC
374 studies in Finland using a plane-Earth layered model of conductivities, and found that a simple
375 plane-wave model is fairly accurate compared to GIC measurements. A Cartesian Elementary
376 Current Systems (CECS) version has also been developed [*Vanhamäki and Amm*, 2007]. This
377 interpolation method is best suited for determining all source current systems over a two-
378 dimensional (2D) ionospheric surface (without distinction between the AEJ, EEJ, and even the
379 Solar-quiet system) above and in parallel with the Earth at any instant in time.

380 Our inversion approach is more appropriate to the simpler setup of line currents systems
381 (applied in turn to RC, AEJ, and EEJ as physical systems) and generates current strength data at
382 a single location for a set of geomagnetic measurements over a given period. The advantage over
383 SECS is that this simplified inversion method provides only two linear output parameters $J_r(\omega)$
384 and $J_i(\omega)$ of the current strength [see [Eq.\(4\)](#)] of the line current system, while SECS requires

385 many current strength output parameters [the complex parts for two horizontal components,
386 $J_{x,y}(\omega)|_{(x_n,y_m)}$ at every coordinate grid point (x_n, y_m)].

387 5.1 Recent GIC research

388 *Pulkkinen et al.* [2012] specifically derive explicit E-field temporal profiles as a function
389 of ground conductivity structures and geomagnetic latitudes. They also demonstrate how extreme
390 E-field scenarios can be mapped into GIC. Generated statistics indicate 20 V/km and 5 V/km
391 100-year maximum 10-s E-field amplitudes at high-latitude locations with poorly conducting and
392 well-conducting ground structures, respectively. They show that there is an indication that E-
393 field magnitudes may experience a dramatic drop across a threshold latitude boundary at about
394 40–60 degrees of geomagnetic latitude. Below the boundary (equatorward) the E-field
395 magnitudes are about an order of magnitude smaller than those above the boundary (poleward).

396 *Ngwira et al.* [2013]'s work on the B-field behavior and the E-field fluctuations it
397 induces during severe geomagnetic events includes (1) an investigation of the latitude threshold
398 boundary, (2) the local time dependency of the maximum induced E-field, and (3) the influence
399 of the EEJ current on the occurrence of enhanced induced E-fields over ground stations located
400 near the dip equator. Using ground-based and the Defense Meteorological Satellite Program
401 measurements, they confirm that the latitude threshold boundary is associated with movements
402 of the auroral oval and the corresponding AEJ, which is the main driver of the largest
403 perturbations of the ground B-field at high latitudes. In addition, they show that the enhancement
404 of the EEJ is driven by the penetration of high-latitude E-fields and that the induced E-fields at
405 stations within the EEJ can be an order of magnitude larger than that at stations outside the EEJ.

406 Our results confirm the studies of *Pulkkinen et al.* [2012] and *Ngwira et al.* [2013]. The
407 E-field due to the AEJ is many times stronger than the RC, and its effects on GIC are taken more
408 seriously (as evidenced by the March 1989 Quebec power blackout event [*Beland and Small,*
409 2004]). The same is true of the southern high-latitude region; though in Antarctica no conducting
410 infrastructures exist over large areas. The southern AEJ also moves into the mid-latitudes during
411 major disturbances, as evidenced by significant GIC and the damage it caused in South Africa
412 [*Gaunt and Coetzee, 2007*] and New Zealand [*Marshall et al., 2012*].

413 In *Carter et al.* [2015], the local amplification of the EEJ magnetic signature is shown to
414 substantially increase the equatorial region's susceptibility to GICs in the presence of
415 interplanetary shocks. Importantly, this result applies to both geomagnetic storms and quiet
416 periods and thus represents a paradigm shift in our understanding of adverse space weather
417 impacts on technological infrastructure. In addition, it is shown that the amplification is larger at
418 Huancayo than that at Addis Ababa, and that this difference may be attributed to geological
419 differences on the two continents.

420 By comparison, our results show the EEJ is both weaker (at Addis Ababa) and stronger
421 (at Huancayo) than the background RC. An amplified E-field is superpositioned onto the E-field
422 of the RC at both stations for a combined effect on GIC in the magnetic dip equator region. GIC
423 effects in the low- and mid-latitude regions, however, are the lowest and affected by the RC
424 alone.

425 5.2 Behavior of the B-fields, E-fields and source currents

426 The B-field index of each current system exhibits different characteristic behaviours that
427 identify the different geomagnetic signatures. As such, the strength of the current systems also

428 behaves differently from each other, with similar characteristics to those of the B-field. By
429 contrast, the E-field exhibits behaviour that is different from that seen in the computed B-field
430 and current strength. In [Figure 5](#), the E-field appears to vary as the time rate-of-change of the B-
431 field and current strength in each system; while in [Figure 4](#), the current strengths vary as that of
432 the B-field indices ([Figure 3](#)).

433 For the RC ([Figure 3a](#)), and more rapidly the AEJ ([Figure 3b](#)), the B-field measurement
434 data shows an SC marking the initial phase of the geomagnetic storm. Not long after, the field
435 decreases substantially from its quiet-time variations around zero magnetic value, introducing the
436 main phase of the storm. After reaching a deep minimum, it gradually returns to the normal
437 quiet-time values in the recovery phase. In the EEJ ([Figure 3c](#)), this behaviour is absent and only
438 the rapid fluctuations are left to mark the presence of a storm, as distinct from the smooth
439 variations of the quiet times. Correspondingly, these different storm characteristics are also
440 strongly reflected in the current strength values among the current systems.

441 Corresponding to the B-fields, the E-fields show a characteristic amplitude modulation of
442 its oscillatory behaviour that can only be part of the main phase of the storm under all the
443 systems concerned. The E-field is the driver for GIC on the ground, and contains spikes that
444 translate into impulses of the GIC being sent down the conducting infrastructures and that could
445 potentially damage them. In the quiet times however ([Figure 5](#): around 04:00-18:00 on 30th,
446 before 06:00 on 29th, and after 14:00 on 31st October 2003), these oscillations are so small that
447 the E-fields may be considered to have vanished, with no concern for the infrastructures
448 involved.

449 5.3 E-fields on GIC

450 The horizontal vector E-fields drive GIC in any conductor network on the ground.
451 Computed from network circuitry parameters, the GIC would likely follow the changes of a
452 projected E-field along any one path of the network, with a good correlation. However, within
453 the scope of this study, only line currents in the east/west (or y-) direction are considered,
454 therefore only E_y can be computed that is parallel to it. No E-field north component was
455 involved, which therefore limits the GIC computation only in the east direction. Eq.1 of
456 *Pulkkinen et al.*, [2007] is adapted by removing the north E-field component term but keeping
457 the east E-field component term: $GIC(x, t) = bE_y(x, t)$. The GIC is now directly proportional to
458 the E-field east component, with b as proportionality coefficient. In the absence of available GIC
459 recordings, no b can be computed, thus a value must be chosen for it. This was determined in the
460 given reference to be of the order of tens of ampere-kilometers per volt. One typical value we
461 choose would be 50 A·km/V. The maximum E-field range seen in [Figure 5](#) is that of the AEJ.
462 Multiplying the E-field range with the coefficient gives $GIC \in [\pm 25]$ A. For the EEJ at AAE, the
463 GIC is smaller by 10 times. For the EEJ at HUA it is $GIC \in [-10, +15]$ A. For the RC we have
464 $GIC \in [-7.5, +5.0]$ A. This supports previous research that conductor networks in auroral regions
465 are at greatest risk of generating large GIC than networks in the rest of the world. For example,
466 *Danskin and Lotz* [2015] show that auroral regions are more prone to extreme events and
467 *Thomson et al.* [2011] also refer to the latitudinal dependence of extreme GIC. See *Ngwira*
468 [2013], *Pulkkinen et al.* [2012] (already cited) and the references within.

469 While calculations of *Barbosa et al.* [2015] and *Trivedi et al.* [2007] only produced 10 A
470 in GIC (for an E-field value: ~ 500 mV/km) in Brazil during the November 2004 geomagnetic
471 storm, *Barbosa et al.* [2015]'s model also estimated a value of 25 A (E-field: ~ 900 mV/km and

472 dB/dt: ~ 116 nT/min) in South Africa during the Halloween Storm of 2003. *Gaunt and Coetzee*
473 [2007] have already linked GIC as a likely cause to South African transformer damage at that
474 time. While GIC values are usually in the order of tens of Amperes, in Sweden *Wik et al.*, [2008]
475 reports (to our knowledge) the largest GIC ever recorded on a power transmission line: 300 A at
476 Simpevarp-2 power substation on 06 April 2000 (where a dB/dt value of around 500 nT/min.
477 was recorded at Brorfelde nearby). For this GIC-record, a possible estimate of an E-field could
478 be 4000 mV/km. But Sweden is in the auroral zone. In the mid-latitude region, *Watari et al.*
479 [2009] and *Watari* [2015] only reports a maximum GIC of 3.85 A (E-field value: ~ 40 mV/km;
480 dB/dt value: ~ 0.235 nT/s (or ~ 14 nT/min.)) at Memanbetsu magnetic station in Japan during a
481 moderate storm on 14-15 December 2006.

482 The GIC would likely also change in relative proportion to the time rate-of-change of the
483 B-fields and the currents (via the E-fields). When a sudden commencement occurs, marking the
484 start of a geomagnetic storm, the sudden change in the horizontal B-field would create spikes in
485 the perpendicular horizontal E-field that will send corresponding impulses of GIC through a
486 conductor path. Such impulses may cause damage or malfunction to any particular piece of
487 equipment or component parts of the conductor network [*Barbosa et al.*, 2015; *Zhang et al.*,
488 2015; *Liu et al.*, 2014; *Pulkkinen et al.*, 2012; *Thomson et al.*, 2005: Fig.3].

489 The optimal operation of equipment and related components are essential to the operation
490 of conducting infrastructure, therefore mitigation of GIC effects are critical. GIC can be
491 computed and therefore predicted, therefore comprehensive warning systems are being
492 developed to assist these utilities in taking pre-emptive measures to minimize or avoid any
493 damages and other consequences to the public.

494 **6 Summary**

495 In this paper, a simplified field inversion set-up is used in which ionospheric line currents
496 are computed from B-field observations on the ground. From these currents, we estimate the
497 induced E-fields at any location of interest, particularly those responsible for GIC in power grids.

498 One motivation for using this method is that B-field measurements are only made at
499 established observatories and additional installed locations. When only Eq.(6) is used, the E-
500 fields can only be computed at those locations from nearby conductivity profiles. By the
501 inversion method, B-fields can be computed over a section of the meridian close to these
502 stations. Once the current strength is determined, one can return to the forward problem Fourier
503 integral and use that parameter to calculate the E-fields anywhere, not possible by other means
504 [De Villiers and Cilliers, 2014]. Another motivation for computing ionospheric line currents by
505 this method lies in the B-field interaction with solar effects outside of the Earth's magnetosphere,
506 such as the solar wind. The line current strength can be used as an intermediary parameter for
507 modelling techniques that determine B-fields at selected locations from the solar wind
508 parameters. This simpler model provides an alternative method to estimate the currents in the
509 ionosphere, which may be more amenable to modelling from upstream inputs for investigating
510 storm characteristics all the way from the Sun to the Earth [De Villiers et al., 2016].

511 The dashed curves in Figures 3 to 5 are the B-field measurements and forward calculated
512 current strengths and E-fields. The solid curves are the inverted B-fields, modeled current
513 strengths and E-fields. A cross correlation between the dashed and solid curves show that it
514 equals an autocorrelation of either curve, indicating that they are identical. The results of the
515 optimization problem match perfectly with the results directly obtained. This confirms that the

516 geomagnetic model function of the line current system is correct. The dashed curves are exactly
517 over the solid curves.

518 This study has implications for current and future research. The process of computing the
519 current strengths and its E-fields provides outputs in three different directions of research. The
520 current density of Eq.(2) suggests that this work can be extended to distributions of currents, of
521 which the Solar-quiet (Sq-) current system is but one example. From scatter presentations, linear
522 correlations and regressions can be performed between measured B-field and modelled currents,
523 or between measured dB/dt and modelled E-field. From the inversion model, current strength
524 data sets may be created for use to develop empirical models linking solar wind activity to
525 magnetospheric current systems. The E-fields are the input data for computing and predicting
526 GIC in the various conductor-based networks on the ground at a given local region.

527

528 **Appendix**

529 The full profile given in *Omondi* (2013) and *Omondi et al.* (2014) has 21 layers and is
 530 reproduced here as comma-separated resistivities ρ_n (inverse conductivities $1/\sigma_n$) at
 531 corresponding depths d_n below Earth's surface (sum of successive thicknesses h_n), respectively:

$$d_n = \sum h_n = (3.2, 4, \underline{5}), (6.4, 8, 10, 12.6, 16, \underline{20}), (26, 32, 40, 50, 64, 70, \underline{80}), \underline{100}, (126, \underline{160}), (200, \underline{260}) \text{ km};$$

$$532 \rho_n = \frac{1}{\sigma_n} = \left\{ \begin{array}{l} ((\underline{78.26}, \underline{79.18}, 77.26), (66.25, 62.91, \underline{52.82}, 45.13, 38, 33.8), (30.74, 30.51, \\ (28.98, 33.32, 32.2, 25.9, \underline{29.74}), \underline{15.83}, (40.13, \underline{44.55}), (46.8, \underline{58.08}) \Omega \cdot \text{m}; \end{array} \right. \quad (\text{A1})$$

533 The profile was simplified by combining the selected number of adjacent layers in parentheses
 534 into one layer, and taking the underlined values of resistivities as its new values. We tried to
 535 retain the shape of the profile as best we could in our selections (See [Table 2](#)).

536

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541 promoting high standards of magnetic observatory practice (www.intermagnet.org).

542 The 1-minute Dst index were downloaded at the National Geomagnetism Program of the
543 U.S. Geological Survey (<http://geomag.usgs.gov>). The SYM-H and AO indices were
544 downloaded at the World Data Center, Kyoto University (<http://wdc.kugi.kyoto-u.ac.jp>).

545 The International Geomagnetic Reference Field (IGRF) model was used to obtain the
546 geomagnetic coordinates at the same Kyoto WDC. The Apex coordinates was obtained at the
547 Community Coordinated Modeling Center, Goddard Space Flight Center, National Admin. and
548 Space Agency (<http://ccmc.gsfc.nasa.gov/>).

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551 All numerical info is provided in the figures produced by solving the equations in the paper.

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554

555 **Table 1:** Locations of two stations and three conductivity structures on three continents.

556 **Table 2:** Parameters of 1D approximation to ground conductivity structure.

557 It is based on magneto-telluric measurements at two locations and a satellite.

558 **Figure 1:** A diagram of the least-squared residual inversion problem. A residual is the difference between the data
559 (circle) at a point and the model function (curve) value at that point. The “data of full index” (i.e. Dst) is at the origin
560 of latitude, the position of the current system. The data “derived from index along model function” is symmetrically
561 placed around the origin.

562 **Figure 2: (a)** Geomagnetic Dst-index measurements given by USGS and Kyoto for the RC. The Kyoto index is the
563 minute-sampled SYM-H data, not the Kyoto hourly Dst samples. **(b)** Geomagnetic AO-index derived by Kyoto from
564 northern polar stations for the AEJ current system. The Dst-index from USGS is also included for comparison. **(c)**
565 Geomagnetic EE-indices created by subtracting the Dst-index of the USGS from the (top) Addis Ababa [AAE] and
566 (bottom) Huancayo [HUA] geomagnetic measurements for the EEJ current system. The Dst-index from USGS is
567 also included for comparison.

568 **Figure 3: (a)** Modelled geomagnetic field directly under AEJ after the AE inversion. Solid curves are the model
569 results, dashed curves are measured data. Geomagnetic field directly under RC after the Dst inversion for height
570 three Earth radii above surface, and re-used again for height eight Earth radii. Only the USGS-Dst was used. Solid
571 curves are the model results, dashed curves are measured data. **(b)** Modelled geomagnetic field directly under AEJ
572 after the AO inversion. Solid curves are the model results, dashed curves are measured data. **(c)** Modelled
573 geomagnetic field directly under EEJ after the EE inversion for AAE (left) and HUA (right). AAE midnight is 2.6
574 hours ahead of UT, while HUA midnight is 5 hours behind UT. Solid curves are the model results, dashed curves are
575 measured data.

576 **Figure 4: (a)** RC current by geomagnetic Dst(USGS) inversion for three [black left axes] and eight [green right
577 axes] Earth radii height above surface. Solid curves are the model results, dashed curves are computed from the
578 measured data. **(b)** AEJ current by geomagnetic AO inversion. Solid curves are the model results, dashed curves are
579 measured data. **(c)** EEJ current by geomagnetic EE inversion from AAE (left) and HUA (right). AAE midnight is

580 2.6 hours ahead of UT, while HUA midnight is 5 hours behind UT. Solid curves are the model results, dashed
581 curves are measured data.

582 **Figure 5: (a)** Geoelectric field directly under RC after the Dst inversion independent of the height above the surface.
583 The USGS-Dst was used. Solid curves are the inverted results; dashed curves are the forward computed data from
584 Dst measurements. **(b)** Modelled geoelectric field directly under AEJ after the AO inversion. Solid curves are the
585 model results, dashed curves are measured data. **(c)** Modelled geoelectric field directly under EEJ after the EE
586 inversion for AAE (left) and HUA (right). AAE midnight is 2.6 hours ahead of UT, while HUA midnight is 5 hours
587 behind UT. Solid curves are the model results, dashed curves are measured data.

588

589 **Table 1:** Locations of two stations and three conductivity structures on three continents.

Placename	Coordinates [zero altitude assumed]		
	Geographic	Geomagnetic ^a (IGRF 2005)	Apex ^b (Year 2003.833)
Addis Ababa, Ethiopia	9.03N, 38.77E	5.26N, 111.70E	[0.5528N; 0.5532N], 111.61E
Huancayo, Peru	12.05S, 75.33W	1.74S, 3.45W	[0.5308N; 0.5312N], 3.51W
Quebec, Canada	53.75N, 71.98W	63.82N, 0.24W	[63.1673N; 63.1798N], 7.44E
Nairobi, Kenya.	1.27S, 36.80E	4.50S, 108.11E	[11.1327S; 11.1386S], 109.80E
Tocopilla, Chile.	22.10S, 70.20W	11.72S, 1.52E	[9.3586S; 9.3636S], 0.95E

590 ^a From <http://wdc.kugi.kyoto-u.ac.jp/igrf/gggm/index.html>.591 ^b From http://ccmc.gsfc.nasa.gov/coord_transform/index.php; Source (Richmond, 1995);
592 Apex format [MagApex-Latitude; QuasiDipole-Latitude], MA/QD-Longitude.

593

594 **Table 2:** Parameters of 1D approximation to ground conductivity structure.

595 It is based on magneto-telluric measurements at two locations and a satellite.

<i>Locations</i> →	<i>Nairobi [Modified]</i>		<i>Tocopilla</i>		<i>Swarm satellite</i>	
Layers ↓	Thickness	Conductivity	Thickness	Conductivity	Thickness	Conductivity
	(km)	(mS/m)	(km)	(mS/m)	(km)	(mS/m)
Layer 1	5	12.6	6	20.0	400	1.0
Layer 2	15	18.9	2	12.5	100	1.4
Layer 3	60	33.6	17	20.0	100	2.7
Layer 4	20	63.2	20	0.2	50	5.2
Layer 5	60	22.4	25	2.0	50	14.4
Layer 6	100	17.2	30	0.2	50	27.0
Layer 7					50	100
Layer 8					50	280
Layer 9					50	1050
Layer 10					350	2700
Layer 11					750 (∞)	3745

596 The structure for Quebec is given in (*Boteler and Pirjola, 1998*).

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