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# Pareto Optimal Regulatory Strategies for Coupled Ridesourcing and Taxi Markets with Impatient Passengers

## Abstract

This study develops a multi-objective bi-level programming model to identify the Pareto optimal combined regulatory strategy that simultaneously accounts for passengers, taxi drivers, ridesourcing vehicle (RSV) drivers, and the transportation network company (TNC). The upper level determines four regulatory controls, including the RSV fleet cap, taxi fare rate, government-guided RSV fare rate, and TNC wage rate floor, while the lower level obtains steady-state market performance, which is formulated as a fixed-point problem and approximated through iterative agent-based simulations. To solve the model, a multi-objective Bayesian optimization algorithm is developed. Based on the DiDi dataset collected from Hangzhou City in 2018, our experiments demonstrate that no regulatory strategy can simultaneously benefit all stakeholders. If the government considers maximizing vehicle utilization as a secondary criterion, then it should decrease the RSV fleet cap, impose higher fare rates, and allow the TNC to pay lower wages, compared with the benchmark scenario. Furthermore, it is recommended that the government should avoid regulations that primarily favor passengers or the TNC, as our results reveal that such policies could harm other stakeholders and reduce vehicle utilization by up to 11.6%. Finally, if passengers' impatience is overlooked, taxi drivers may lose 23.3% of potential profits.

## Keywords

Ridesourcing; Taxi; Impatient Passengers; Order cancellation; Multi-objective Bayesian optimization.

## 1 Introduction

Ridesourcing services have been growing rapidly in the last few years, driven by the emergence of transportation network companies (TNCs) that offer online platforms to connect passengers and drivers. By facilitating the interaction between passengers and drivers, ridesourcing platforms have reduced the information barrier caused by spatial bias between passengers and traditional taxi drivers. Hence, ridesourcing has been widely acknowledged for its potential to improve urban mobility (Rayle et al., 2016) and to attract a massive number of participants. For example, in China, the number of ride-hailing app users had reached 365 million by December 2020 (Li et al., 2023b). In 2022, Uber reported 131 million monthly active users, with nearly 5.4 million drivers completing 7.64 billion rides worldwide (Campbell, 2023).

However, the proliferation of RSV drivers has led to an oversupply in the ridesourcing market in many regions. This oversupply has contributed to a decline in the traditional taxi industry, prompting taxi drivers to join TNC platforms, which further exacerbates the supply issue. Moreover, the excessive

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1 number of RSVs enables TNCs to reduce wage rates, resulting in a decline in drivers' earnings.  
2 Consequently, many RSV and taxi drivers are compelled to work longer hours to meet their daily  
3 income targets, thereby creating a vicious cycle that undermines both market stability and  
4 transportation efficiency. Such a vicious cycle highlights the necessity of government regulation for  
5 coupled ridesourcing and taxi market (CRTM). The objective of this study is therefore to identify  
6 optimal regulatory strategies accommodating the interests of different stakeholders in CRTM.

7 The existing literature and practice have identified four main types of regulatory strategies, each  
8 aiming to improve welfare for specific stakeholders: i) Control the number of RSVs. In China, many  
9 city governments have capped the number of RSVs (Yu et al., 2020; Yang et al., 2021; Zhong et al.,  
10 2022). ii) Regulate taxi fares (Yu et al., 2020; Zhong et al., 2022). iii) Set RSV prices (Yang et al.,  
11 2021; Chen et al., 2024). TNCs in China are required to follow the government-guided fare rates when  
12 necessary. iv) Set the minimum wage paid by TNCs to drivers (Zha et al., 2018a; Ke et al., 2021;  
13 Vignon et al., 2023). In 2018, the New York City Council required that TNCs pay drivers a minimum  
14 wage (Shapiro, 2018).

15 Nevertheless, each strategy could potentially favor certain stakeholders and negatively impact  
16 other stakeholders. For example, limiting fleet size can increase the average profits of both RSV and  
17 taxi drivers, but it could lead to longer waiting times and potentially higher trip fares for passengers.  
18 In most existing ridesourcing studies, the overall impact of regulatory strategies on various  
19 stakeholders is typically modeled as a single objective, namely the social welfare (Yu et al., 2020; Tang  
20 et al., 2023; Mo et al., 2024). In contrast, this study aims to fill the gap to optimize regulatory strategies  
21 from a multi-objective Pareto optimal perspective. Meanwhile, to the best of our knowledge, no  
22 existing study has examined whether implementing a combination of these four regulatory strategies  
23 would be more effective than applying them individually, or, if so, how to optimize such strategies. It  
24 is important to fill this gap because fragmented regulation can skew the distribution of benefits in the  
25 market and may even result in substantial losses for certain stakeholders.

26 Essentially, regulatory strategies shape the market by influencing the behavior of drivers and  
27 passengers, such as drivers' work decisions and passengers' travel choices. [This underpins the rationale  
28 for developing a bi-level programming model, where the upper level determines regulatory strategies,  
29 while the behavioral dynamics or interactions between market supply and demand can be captured in  
30 the lower-level model, and a steady-state market performance can be obtained by solving it.](#) Notably,  
31 a distinct feature of the CRTM market is the impact of passenger impatience on overall performance.  
32 This impact can be observed in two main forms.

33 1) Passengers may cancel orders after sending online travel requests, not only due to incorrect  
34 entries or sudden changes in plans but also as a result of long waiting time or encountering vacant taxis  
35 (He et al., 2018). Cancellation behaviors caused by vacant taxis differ before and after order matching  
36 (Xu et al., 2022). Post-matching cancellations waste the limited supply and prevent other passengers  
37 from accessing potential travel opportunities (Wang et al., 2020), which is why passengers are usually  
38 charged a penalty in practice. In contrast, pre-matching cancellations reduce TNC profits but typically

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1 do not impose additional costs on passengers or harm market efficiency; in some cases, they may  
2 redirect demand toward taxi services, thereby supporting taxi drivers' earnings.

3 2) Passengers may update their requested hailing types between RSV and taxi services. For  
4 example, if an RSV passenger experiences prolonged waiting without a successful match, they may  
5 request taxi services due to impatience. This behavior is supported by certain ride-hailing apps, e.g.,  
6 DiDi, which allows passengers to append new service types within the same platform before matching.

7 The above impatient behaviours of passengers and their dynamic order matching with drivers are  
8 shaped by the short-term market environment, which, inherently, is the consequence of government  
9 regulatory strategies. Moreover, these behaviors could also endogenously impact market supply and  
10 demand in the long term, which in turn could lead to different behavioral patterns of passengers and  
11 drivers. To capture this feedback loop, we formulate a fixed-point problem to characterize the steady-  
12 state market performance under a given regulatory strategy. Then, we develop an agent-based  
13 simulation to depict the microscopic behaviors and capture their endogenous interactions. The steady-  
14 state market performance is approximated by averaging the results from iterative simulations. This  
15 simulation framework, mapping the complex nonlinear correlations of regulatory inputs to steady-state  
16 performance outputs, can be treated as a black-box function. Therefore, to efficiently solve for the  
17 optimal combined regulatory strategy within this black-box system, we utilize the multi-objective  
18 Bayesian optimization algorithm.

19 To sum up, this study aims to determine the optimal combinatorial configuration of four existing  
20 regulatory strategies on CRTM, considering the endogenous interaction between supply and demand  
21 with impatient passengers.

22 The main contributions of this study are summarized as follows:

23 (1) We formulate a bi-level multi-objective model for regulating CRTM. In contrast to prevailing  
24 single-objective studies that focus on designing one or two regulatory instruments, this study  
25 simultaneously optimises four prevalent regulatory strategies with the aim of maximising the benefits  
26 of passengers, taxi and RSV drivers, and the TNC.

27 (2) We develop a comprehensive agent-based simulation model that advances existing  
28 ridesourcing studies by capturing more realistic behavioural dynamics, including passengers' travel  
29 mode and hailing type choices, impatient passengers' abandonment and cancellation behaviors before  
30 and after order matching, and taxi drivers' work decisions between hybrid and street modes.

31 (3) We develop a solution methodology based on multi-objective Bayesian optimization. The  
32 objective functions are evaluated under the steady-state market performance, which is formulated as a  
33 fixed-point problem and approximated using iterative agent-based simulations. This framework can  
34 also be applied to other ridesourcing studies.

35 (4) We contribute several regulatory insights for the government from a Pareto optimal  
36 perspective. In brief, it recommends fewer RSVs, higher fare rates, and lower RSV wage rates, and the  
37 government should avoid prioritizing passengers or the TNC. Meanwhile, making passengers bear  
38 more costs appears to be an unavoidable sacrifice to improve overall market performance. Also, taxi

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1 drivers may lose potential profits while ignoring passengers' impatience.

2 The remainder of this paper is organized as follows. Section 2 reviews the relevant literature.  
3 Section 3 defines the problem statement and formulates the bi-level programming model. Section 4  
4 develops an agent-based simulation and outlines the solution framework. Section 5 conducts numerical  
5 experiments to validate the model, evaluate the impact of regulatory strategies, and identify Pareto  
6 optimal combined regulatory strategies. Finally, Section 6 concludes the main findings of this study  
7 and highlights directions for future research.

## 8 **2 Literature review**

9 This study is situated at the intersection of three key research streams: the regulation of ridesourcing  
10 services, modelling approaches for ride-hailing markets, and the optimization of black-box bi-level  
11 problems.

### 12 **2.1 Regulation for ridesourcing services**

13 In recent years, regulatory strategies for ridesourcing services have attracted growing attention (Zha et  
14 al., 2016; Zha et al., 2018a; Li et al., 2019). To enhance social welfare, typical regulatory strategies  
15 include limiting the number of vehicles, controlling the fare rates of ridesourcing and taxi services,  
16 and guaranteeing drivers' wage floors. Yu et al. (2020) showed that lowering taxi fare rates can improve  
17 overall social welfare. Yang et al. (2021) found that under fare rate regulation, TNCs would charge  
18 higher fares. Zhong et al. (2022) discovered that regulating the rates and number of taxis and RSVs  
19 can effectively increase social benefits. Vignon et al. (2023) showed that the government can maximize  
20 social surplus by regulating TNCs' per-trip commission (i.e., the difference of fare and driver earning  
21 per ride).

22 Other than improving the social welfare, alternative perspectives have been introduced to regulate  
23 the ridesourcing market. Qin et al. (2025) investigated whether the government could use a price-cap  
24 regulation and subsidy policy to encourage the ridesourcing platform to serve as a complement to  
25 public transit services. They found that the platform's profit decreased as the price-cap decreased and  
26 increased with the size of the subsidy, and under certain supply-demand ratios, both strategies could  
27 increase public transit ridership. Mo et al. (2024) studied how governments can regulate the  
28 ridesourcing market integrated with vehicle rental services through minimum driver wages and  
29 maximum vehicle rental fees. They found that when the government focused on only one policy  
30 without coordinating with the other, not all groups benefited; however, when the two policies are  
31 coordinated, higher total social welfare could be achieved.

32 It is worth noting that most of the preceding literature only considers a single objective. Few  
33 studies have investigated the impact of regulatory strategies from a multi-objective perspective. Ke et  
34 al. (2021) studied the effects of various regulatory strategies for the ridesourcing market from a Pareto-  
35 efficient perspective, considering traffic congestion and drivers' heterogeneity. In their study, the  
36 Pareto frontier is defined by the platform's profit and social welfare, where the social welfare is

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1 modeled as a linear sum of platform profit, passenger surplus, and other elements. However, their  
2 Pareto frontier does not fully capture the perspectives of all stakeholders, namely, passengers, taxi  
3 drivers, RSV drivers, and the TNC.

## 4 **2.2 Ridesourcing and taxi market modeling**

5 Early research on modeling the ridesourcing and taxi market primarily relied on steady-state market  
6 equilibrium analyses, employing economic models to characterize driver-passenger interactions and  
7 passengers' travel choices. (e.g., Yang et al., 2010; He and Shen, 2015; Wang et al., 2016; Zha et al.,  
8 2018b; Wang et al., 2020; Karamanis et al., 2021). Within this modeling approach, the existence of  
9 market equilibrium can be proved, and the effects of factors such as pricing and fleet size on the market  
10 have been examined. It is generally acknowledged that raising prices increases passengers' travel costs,  
11 thus leading to lower demand (Wang et al., 2016; Ke et al., 2020), while increasing fleet size makes  
12 the operation less efficient and less profitable for drivers (Liu et al., 2022a).

13 However, early studies overlooked a critical issue: not all ridesourcing requests can be completed,  
14 as a substantial proportion are canceled by passengers, which has a significant impact on the on-  
15 demand service platforms (Xu et al., 2021a). A primary reason that passengers cancel their requests is  
16 encountering vacant taxis. With the data collected by DiDi in Shanghai, Wang et al. (2020) illustrated  
17 the effect of vacant taxis on passengers' cancellations toward confirmed orders from a macro  
18 perspective. They calibrated a nonlinear aggregation model to characterize this effect. Furthermore,  
19 passengers' cancellations before and after order matching could be different (Ramezani and Valadkhani,  
20 2023). Jiao and Ramezani (2022) defined two types of cancellations in ridesourcing services: pre-  
21 matching abandonment, where passengers withdraw their request due to impatience before being  
22 matched; and post-matching cancellation, where passengers cancel confirmed orders due to  
23 dissatisfaction with the provided waiting time and trip fare. Many recent studies that consider  
24 passengers canceling ridesourcing services have taken into account different cancellations before and  
25 after order matching (Jiao and Ramezani, 2024; Wang et al., 2024; Jiao and Ramezani, 2025; Liu et  
26 al., 2025). In these studies, pre-order-matching cancellations are usually modeled as passengers  
27 abandoning their requests after reaching a maximum waiting time threshold, while post-order-  
28 matching cancellations are usually modeled based on the utility difference between ridesourcing and  
29 other travel services. For CRTM, passengers may encounter vacant taxis not only after order matching  
30 but also before, and they may also cancel their online orders before order matching (Xu et al., 2022).  
31 However, such pre-order-matching cancellations are different from abandonment because, although  
32 the TNC loses the same profit, the passenger's hailing demand is satisfied.

33 It should be noted that both RSVs and taxis can provide hailing services in CRTM, allowing  
34 passengers to choose between these two options. Existing CRTM studies generally assume that hailing  
35 demand is segmented into ridesourcing and taxi passengers (Wang et al., 2020; Xu et al., 2022).  
36 However, in real-world scenarios, passengers may simultaneously request both services. Furthermore,  
37 for impatient passengers, the sunk waiting cost may influence their decision-making behavior before

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1 matching (Liu et al., 2024b). However, to the best of our knowledge, no existing study has investigated  
2 passengers' dynamic updating of hailing types while awaiting a match.

3 In recent years, scholars have increasingly recognized the limitations of the traditional steady-  
4 state equilibrium-based modeling approach due to the complexity of the ridesourcing market. While  
5 previous studies have proven the existence of a market equilibrium state (Yang et al., 2010; Wang et  
6 al., 2016), such an equilibrium state is highly idealized and seldom observed in real-world markets,  
7 where supply and demand fluctuate continuously (Nie, 2017; Hamedmoghadam et al., 2019). When  
8 operational decisions in the market significantly change the state of the system, it takes a long time to  
9 restore the equilibrium state, which limits the applicability of economic models in practice (Nourinejad  
10 and Ramezani, 2020). Meanwhile, many traditional models assume that vehicles are parked when  
11 waiting for matching (Wang et al., 2020; Xu et al., 2022), making it challenging to describe the  
12 complex interaction between passengers and drivers in the real world and to accurately identify some  
13 key metrics, e.g., passengers' waiting time and vehicle utilization.

14 Consequently, researchers have increasingly turned to agent-based modeling to construct dynamic  
15 interactions between drivers and passengers (Wen et al., 2018; Beojone and Geroliminis, 2021; Cheong  
16 et al., 2023; Feng et al., 2023; Yao and Bekhor, 2024). In addition, agent-based modeling offers greater  
17 flexibility in representing taxi drivers' work mode choices, thereby facilitating the design of new  
18 operational mechanisms (Martinez et al., 2015). Therefore, this study develops an agent-based  
19 simulation model for the CRTM. Table 1 compares the modeling methods used in this study with those  
20 used in the literature. As summarized in the table, our model comprehensively accounts for passengers'  
21 pre-order matching abandonments and cancellations before and after order matching, and it also  
22 models the travel mode and hailing type choices of passengers, as well as the work mode choices of  
23 taxi drivers.

24

**Table 1**

Comparison with existing methods of the ridesourcing market modeling.

Literature	Passenger's behaviors				Driver's behaviors			System characteristics	
	Abandonment	Cancel before order matching	Cancel after order matching	Travel mode choice	Hailing type choice	Taxi work mode choice	Move while idling	Coupled RSV & taxi market	Dynamic supply and demand
<b>Aggregation model</b>									
Wang et al. (2016)							√	√	
He et al. (2018)			√	√		√	√	√	
Wang et al. (2020)			√		√			√	
Xu et al. (2022)		√	√		√			√	√
<b>Queue model</b>									
Banerjee et al. (2015)	√								
Sun et al. (2020)						√			
Feng et al. (2021)									√
Feng et al. (2022)	√								
<b>Simulation model</b>									
Agatz et al. (2011)							√		√
Nourinejad and Ramezani (2020)							√		√
Beojone and Geroliminis (2021)	√			√			√	√	√
Yao and Bekhor (2024)		√	√				√		√
<b>Our research</b>	√	√	√	√	√	√	√	√	√

Table 1 shows that there is still a gap in the literature regarding constructing a comprehensive simulation model of the CRTM that explicitly considers the actions of drivers and passengers during the hailing service.

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### 2.3 Bayesian optimization in solving black-box bi-level problems

In a general bi-level model for solving a transportation problem, the upper-level model determines the decisions of leaders, such as the government and operator, with the aim of maximizing or minimizing their objectives while considering the responses of the lower-level followers (Clegg et al., 2001; Santos et al., 2021), which be formulated either as analytical models that are solved by exact or approximate solutions (e.g., Ni et al., 2021; Xu et al., 2021b) or simulation models that can be treated as a black-box (Zhong et al., 2021; Huo et al., 2023a; Gong et al., 2025).

Bayesian optimization is a gradient-free optimization method that typically uses the Gaussian process regression as a probabilistic surrogate model to construct the analytical function for the black-box problem. The Gaussian process regression is more flexible than linear regression models because it does not assume a functional form for the mapping from input to output. As a result, it can capture complex and highly nonlinear relationships based on fewer sample points (Liu et al., 2022b). Other gradient-free methods, such as the genetic algorithm (Wei and Sun, 2018) and particle swarm optimization algorithms (Han et al., 2016), are also widely used in bi-level programming problems. In comparison, Bayesian optimization reduces the need for repeated evaluations of the lower-level model, resulting in greater computational efficiency and yielding higher-quality solutions (Olofsson et al., 2018).

Existing research has demonstrated the effectiveness of Bayesian optimization in solving black-box and bi-level problems (Zhong et al., 2021; Huo et al., 2023b). Yang et al. (2023) employed Bayesian optimization to jointly design the fleet size and charging facility configuration of an electric automated on-demand mobility system. Their results show that the method can find satisfactory solutions within a tight computational budget. Huo et al. (2023a) demonstrated that Bayesian optimization outperforms the simultaneous perturbation stochastic approximation method and the method proposed by Osorio (2019) in terms of solution efficiency and estimation accuracy when solving a bi-level OD estimation problem. Liu et al. (2024a) developed a multi-objective bi-level programming model to solve the joint optimal pricing problem of shared autonomous vehicles and road congestion pricing. They obtained an optimal solution that can simultaneously improve regional accessibility and transportation efficiency with the help of Bayesian optimization.

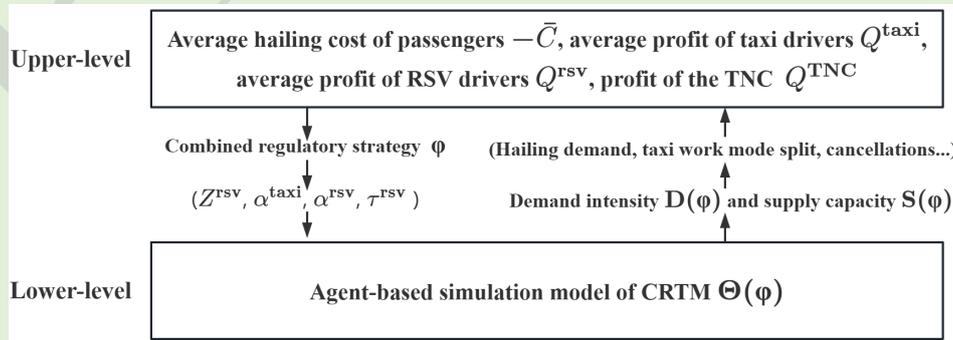
### 3 Problem statement

We consider a CRTM with a single TNC operating in a specific period and **urban area**, where both RSVs and taxis can provide hailing services. The fleet size of RSVs is fully controlled by the TNC, while the size of taxis is **fixed and** determined by the government. Taxis can serve roadside passengers through traditional cruising or accept assignments from the TNC to serve online orders (Wang et al., 2016; He et al., 2018). If a taxi is unwilling to accept online assignments during the study period, it is defined as a ‘street’ taxi, which only searches for roadside passengers by cruising; otherwise, if it is willing to accept online assignments, it is defined as a ‘hybrid’ taxi, which can also serve roadside passengers when idle. **Hybrid taxis receive full fare payments from passengers when operating in**

1 cruising mode, similar to traditional street-hailing taxis. When accepting online assignments from the  
 2 TNC, they earn a portion of the passenger payments as wages, like RSV drivers. Both taxi and RSV  
 3 drivers bear vehicle fuel and operation costs themselves. Passengers can choose between hailing  
 4 services and public transit to meet their travel needs. Passenger impatience manifests in three ways: 1)  
 5 abandonment of requests due to excessive waiting time before order matching, 2) cancellation of  
 6 unmatched or matched requests upon encountering vacant taxis either before or after the order  
 7 matching, and 3) updating their hailing type while waiting to be matched. The TNC generates income  
 8 by offering ridesourcing and online taxi services to passengers and incurs costs through wage payments  
 9 to RSV and hybrid taxi drivers.

10 In the online hailing process, passengers first send their travel requests along with their preferred  
 11 hailing type(s) to the TNC. Then, the TNC matches passengers with available hailing vehicles (i.e.,  
 12 RSVs and hybrid taxis) corresponding to their hailing requests. Once matched, the assigned vehicle  
 13 moves to pick up the passenger. If the passenger continues to wait till the vehicle arrives without  
 14 canceling, the driver collects the passenger and transports them to the requested destination.

15 In such a market, the government could intervene through four regulatory instruments: 1) capping  
 16 the number of RSVs,  $Z^{\text{RSV}}$ , 2) setting a regulated fare for taxi services,  $\alpha^{\text{taxi}}$ , 3) imposing a  
 17 government-guided RSV fare rate,  $\alpha^{\text{RSV}}$ , and 4) establishing a regulatory floor on the wage paid by the  
 18 TNC to RSV drivers,  $\tau^{\text{RSV}}$ . The combination of these four is termed a combined regulatory strategy  
 19  $\varphi = [Z^{\text{RSV}}, \alpha^{\text{taxi}}, \alpha^{\text{RSV}}, \tau^{\text{RSV}}]$ . In response to a combined regulatory strategy, the TNC determines the  
 20 number of operating RSVs and the wage rate for RSV drivers to maximize its profit while complying  
 21 with the government-guided RSV fare rate. Meanwhile, taxi drivers would make a work mode choice  
 22 between providing online and traditional services, and passengers may act to make various travel  
 23 decisions. As a result of the combined regulatory strategy and the responses from the CRTM, the  
 24 system results in different performance measurements, including the average hailing cost of passengers  
 25  $\bar{C}$ , the average profit of taxi drivers,  $Q^{\text{taxi}}$ , the average profit of RSV drivers,  $Q^{\text{RSV}}$ , and the profit of  
 26 the TNC,  $Q^{\text{TNC}}$ . The four indicators serve as proxies for the welfare (objectives) of passengers, taxi  
 27 drivers, RSV drivers, and the TNC, respectively.



28  
 29 **Fig. 1.** The framework of the multi-objective bi-level programming model

30 Under the preceding setting, this study aims to determine an optimal combined regulatory strategy  
 31 to cater to the interests of four stakeholders simultaneously and to identify the Pareto frontier to support

1 government decision-making. To this end, we adopt a bi-level programming approach. As illustrated  
 2 in Fig. 1, the upper level aims to find a combined regulatory strategy,  $\boldsymbol{\varphi}$ , that leads to a Pareto optimal  
 3 solution in four objectives, where  $\bar{C}$  is associated with a negative sign to reflect cost minimization.  
 4 The lower level is a simulation model that captures the supply-demand interaction and computes the  
 5 objective functions under the combined regulatory strategy  $\boldsymbol{\varphi}$  to obtain stabilized market performance.

6 The following multi-objective bi-level programming model is formulated.

$$7 \quad \max_{\boldsymbol{\varphi}} \mathbf{f}(\boldsymbol{\varphi}, \mathbf{D}(\boldsymbol{\varphi}), \mathbf{S}(\boldsymbol{\varphi})), \quad (1)$$

8 s.t.

$$9 \quad \boldsymbol{\varphi} \in \Omega, \quad (2)$$

$$10 \quad \mathbf{f}(\boldsymbol{\varphi}, \mathbf{D}(\boldsymbol{\varphi}), \mathbf{S}(\boldsymbol{\varphi})) = \{f^\omega(\boldsymbol{\varphi}, \mathbf{D}(\boldsymbol{\varphi}), \mathbf{S}(\boldsymbol{\varphi})), \omega = 1, 2, 3, 4\}, \quad (3)$$

$$11 \quad [\mathbf{D}(\boldsymbol{\varphi}), \mathbf{S}(\boldsymbol{\varphi})] = \Theta(\boldsymbol{\varphi}). \quad (4)$$

12  $\mathbf{f}(\cdot)$  denotes the vector of the four objective functions, where  $f^\omega$  is the  $\omega^{\text{th}}$  objective function.  
 13  $\Omega$  is the solution space of the regulatory strategies.  $\mathbf{D}(\boldsymbol{\varphi})$  and  $\mathbf{S}(\boldsymbol{\varphi})$  represent the stable demand level  
 14 and supply capacity under  $\boldsymbol{\varphi}$ .  $\Theta(\boldsymbol{\varphi})$  denotes the lower-level agent-based simulation model of CRTM,  
 15 reflecting the market performance under the combined regulatory strategy  $\boldsymbol{\varphi}$ . Eq. (3) states that  $\mathbf{f}(\cdot)$   
 16 consists of four objective functions, each of which is measured by the same  $\boldsymbol{\varphi}$  and corresponding  
 17 stable market supply and demand. Eq. (4) represents that the stable market supply and demand are  
 18 obtained from the lower-level model.

19 Solving the above bi-level model is challenging because the relationship between decision  
 20 variables and objective functions is complex and nearly black-box. The following Fig. 2 shows the  
 21 effects and interactions in the research problem and the composition of each objective function. **The**  
 22 **gradient-colored boxes in the left and right parts of Fig. 2 represent the decision variables and objective**  
 23 **functions, respectively. The white and gray boxes in the center represent endogenous and exogenous**  
 24 **variables, respectively. The blue arrow represents a positive effect between a pair of components, while**  
 25 **the red dashed arrow represents a negative effect. Decision variables and exogenous variables could**  
 26 **have positive or negative effects on different endogenous variables. Essentially, by influencing the**  
 27 **supply-demand pattern, decision variables can have a complex impact on objective functions. Note**  
 28 **that the endogenous/exogenous variables involved in this figure and the effects between variables are**  
 29 **not exhaustive, but they can reflect the basic mechanism of how the combined regulatory strategy**  
 30 **influences CRTM.**

31 To effectively model the sophisticated interactions, an agent-based simulation is developed to  
 32 characterize the complex influence process and identify the steady-state market performance of CRTM

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1 under different combined regulatory strategies. To solve the model, a solution methodology based on  
2 multi-objective Bayesian optimization is developed. In what follows, we first introduce the key  
3 [definitions](#), assumptions, and notations for the model, and we leave the notation for the multi-objective  
4 Bayesian optimization theory to be explained at usage in Section 4.4.

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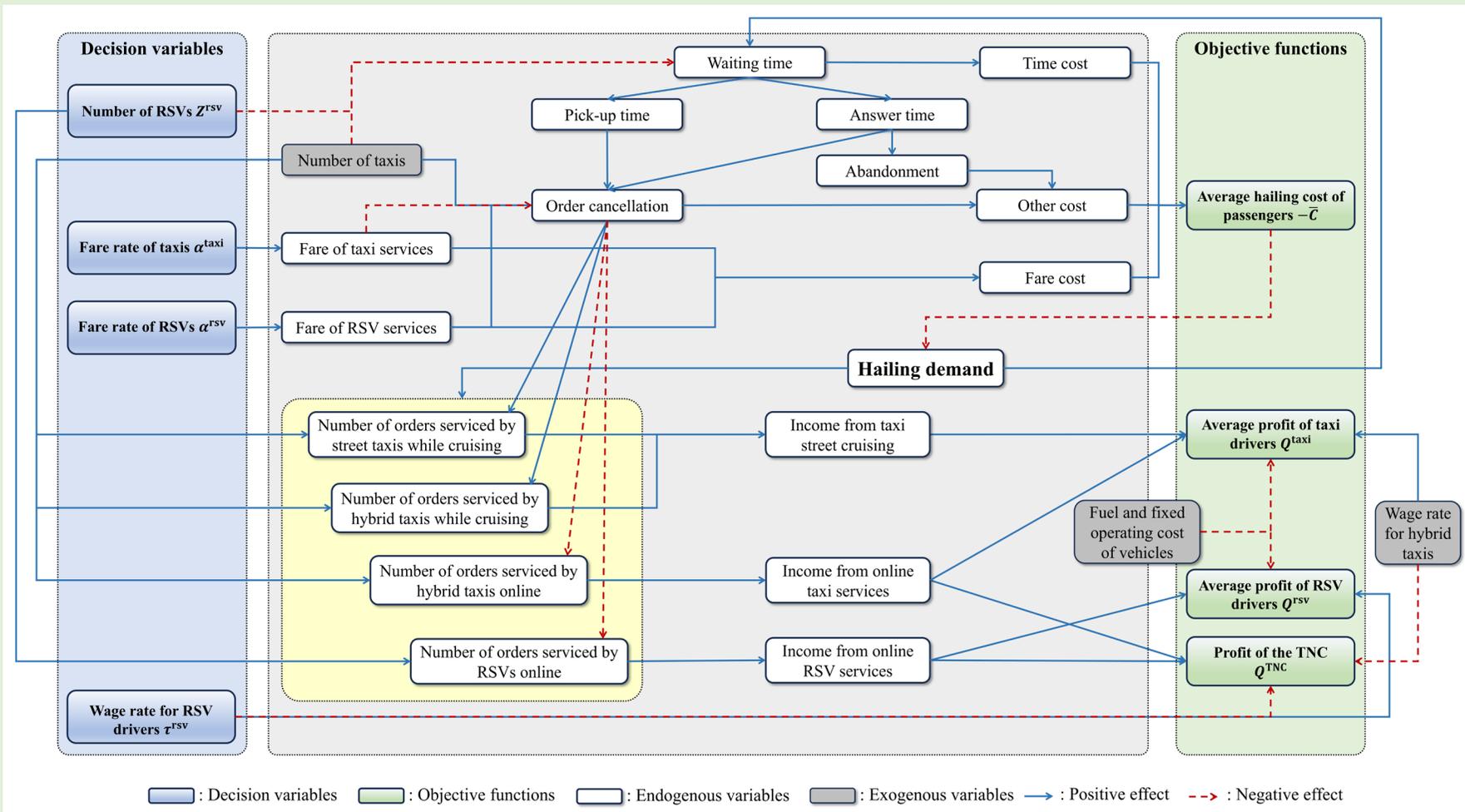


Fig. 2. The effects and interactions in the research problem

The following definitions clarify several “rates” with different meanings and units in this study.

**Definitions 1.** Fare rate (¥/km): the fare charged from passengers per kilometer for taking ridesourcing or taxi services.

**Definitions 2.** Wage rate (%): the percentage of fare income (charged from passengers) paid by the TNC to the assigned RSV or hybrid taxi driver for each completed online service.

**Definitions 3.** Demand rate (requests/min): the number of travel demands per minute.

The following assumptions clarify some basic supply-side settings in the model.

**Assumption 1.** Existing literature generally assumes that the number (or working hours) of drivers who provide hailing services is positively correlated with the expected profit (Nourinejad and Ramezani, 2020; Wang et al., 2020; Xu et al., 2022). However, in the real world, drivers are more likely to extend their working hours to reach their daily profit targets when their average profit declines, and they also tend to reduce break time after facing cancellations (Duong et al., 2023). Therefore, this study assumes that the number of taxis is exogenous and fixed during the study period. The same assumption has been adopted by Yu et al. (2020) and Zhong et al. (2022).

**Assumption 2.** Without loss of generality, it is assumed that there will always be some street taxis in the market that seek roadside passengers by cruising. In practice, experienced taxi drivers often take the opportunity to operate efficiently by declining online orders that require more idle miles and time in specific areas or periods, such as busy shopping areas or peak commuting hours.

**Assumption 3.** The wage rate for taxi drivers in our model is assumed to be exogenously given. This reflects the fact that taxi fare rates are regulated by the government rather than decided by the TNC, thereby requiring the TNC to pay hybrid taxi drivers a regulated and fixed wage rate.

**Assumption 4.** Once an order is matched, the assigned RSV or hybrid taxi driver is not allowed to cancel the order. This is a reasonable simplification since TNCs impose very strict rules and penalties on driver-side cancellation in practice. For example, DiDi drivers are only allowed to cancel under limited circumstances, but cannot cancel more than 3 times a day. If a driver cancels frequently, the TNC would reduce the driver’s future matching probability or impose temporary suspensions.

**Table 2**

Notations.

Symbol	Description
<i>Sets</i>	
$\Phi$	Set of a combined regulatory strategy
$\mathbf{f}$	Set of objective values
$G^{\text{RSV}}, G^{\text{h-taxi}}$	Set of passengers who are served by RSVs or hybrid taxis online, respectively
$G_{\text{cancel}}$	Set of passengers who cancel their orders before order matching

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$G_{cancel}^{rsv}, G_{cancel}^{h-taxi}$	Set of passengers who cancel RSV or hybrid taxi orders after order matching, respectively
$G_{abandon}$	Set of passengers who abandon their requests before order matching
$G_{street}^{h-taxi}, G^{s-taxi}$	Set of passengers who are served by hybrid taxis or street by traditional cruising, respectively
$\Phi^*$	Set of the Pareto optimal output solution

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### **Decision variables**

$Z^{rsv}$	Number of RSVs (veh)
$\alpha^{taxi}$	Fare rate of taxis (¥/km)
$\alpha^{rsv}$	Fare rate of RSVs (¥/km)
$\tau^{rsv}$	Wage rate paid by the TNC to RSV drivers (%)

---

### **Objective functions**

$\bar{C}$	Average hailing cost of passengers (¥)
$Q^{taxi}$	Average profit of taxi drivers (¥)
$Q^{rsv}$	Average profit of RSV drivers (¥)
$Q^{TNC}$	Profit of the TNC (¥)

---

### **Endogenous variables**

$\lambda, \lambda^{transit}$	Hailing demand rate and public transit demand rate (requests/min)
$U_i^s(t), s \in \{rsv, taxi\}$	Passenger $i$ 's mental accounting utility for hailing type $s$ after his/her order is initiated $t$ minutes (¥)
$\hat{u}_i$	Passenger $i$ 's valuation for unit travel distance (¥/km)
$u_i(t)$	Passenger $i$ 's mental account value for unit travel distance after his/her order is initiated $t$ minutes (¥/km)
$W_i^{answer}, W_i^{pick}$	Passenger $i$ 's order answer time and pick-up time, respectively (min)
$W_i^{b-vacant}, W_i^{a-vacant}$	Passenger $i$ 's waiting time to encounter a vacant taxi before and after order matching, respectively (min)
$C_i^1, C_i^2$	Utilities associated with keeping waiting and canceling an order upon passenger $i$ encountering a vacant taxi after order matching, respectively (¥)
$N(T, \lambda)$	The number of passengers who arrived and ended hailing service at the hailing demand rate $\lambda$ during a time interval $T$
$C_i$	Passenger $i$ 's generalized hailing cost (¥)
$\bar{L}$	The logsum of the disutility as perceived by a passenger choosing hailing services to meet travel demand (¥)
$\bar{C}^{rsv}, \bar{C}^{taxi}$	The average travel costs of passengers served by RSVs and taxis, respectively (¥)
$Z^{h-taxi}, Z^{s-taxi}$	Number of hybrid and street taxis, respectively (veh)
$Q^{h-taxi}, Q^{s-taxi}$	Average profits of hybrid and street taxi drivers, respectively (¥)
$\beta^{rsv}, \beta^{h-taxi}$	Time cost coefficient of RSVs and hybrid taxis, respectively (¥/min)

---

$\bar{L}(\phi, \lambda)$	The logsum disutility of hailing passengers under $\lambda$ and $\phi$ (¥)
$\lambda^*(\phi)$	The endogenously stable hailing demand rate under $\phi$ (requests/min)

---

**Parameters / Exogenous variables**

$T$	The duration of a single time interval (min)
$M$	The scale of the grid-type road network
$l_i$	Travel distance for passenger $i$ (km)
$\bar{l}$	Average travel distance of all passengers (km)
$R$	The maximum matching distance (km)
$\Lambda$	Total travel demand rate (requests/min)
$u_{\max}$	Passengers' highest hailing value rate (¥/km)
$\bar{C}^{\text{transit}}$	Average public transit cost (¥)
$\bar{W}^{\text{transit}}$	Average waiting time for public transit service (min)
$\alpha^{\text{transit}}$	Fare rate of public transit (¥/km)
$Z^{\text{taxi}}$	Number of taxis (veh)
$\tau^{\text{taxi}}$	Wage rate paid by the TNC to hybrid taxi drivers (%)
$W_{\max}$	Maximum patience time of passengers (min)
$\beta_{\text{time}}^{\text{pas}}$	Time cost coefficient of passengers (¥/min)
$\beta_{\text{sunk}}^{\text{pas}}$	Sunk time cost coefficient of passengers (¥/km·min)
$\hat{p}$	Penalty for canceling a matched order (¥)
$H$	The psychological cost of canceling a matched order (¥)
$v, v^{\text{transit}}$	The average speed of hailing vehicles and transit vehicles, respectively (km/min)
$\gamma$	Fuel cost per unit distance of hailing vehicles (¥/km)
$\hat{\gamma}^{\text{rsv}}, \hat{\gamma}^{\text{taxi}}$	Fixed operating cost of RSVs and taxis at each time interval, respectively (¥)
$\theta^{\text{pas}}, \theta^{\text{taxi}}$	Dispersion coefficients used in the Logit model
$\theta_0$	The logsum parameter
$\Omega$	Solution space of decision variables

---

1 Note: 1¥≈0.15US\$.

2 **4 Methodology**

3 **4.1 Agent-based simulation**

4 This study examines a CRTM with three main types of agents (i.e., passengers, RSVs, and taxis) in a  
5 grid-type road network (Fig. 3) following the prevailing studies (e.g., Feng et al., 2021; Besbes et al.,  
6 2022; Wang et al., 2024). The horizontal and vertical lines in the figure represent bidirectional roads  
7 for RSVs and taxis to travel. Our simulation model is inspired by Feng et al. (2021) and inherits a  
8 similar setting, in which the spatial heterogeneity of the road network is not considered, and the impact  
9 of private vehicles on traffic is reflected through average speed. The details of agents' states, behaviors,

properties, and KPIs are summarized in Appendix A.

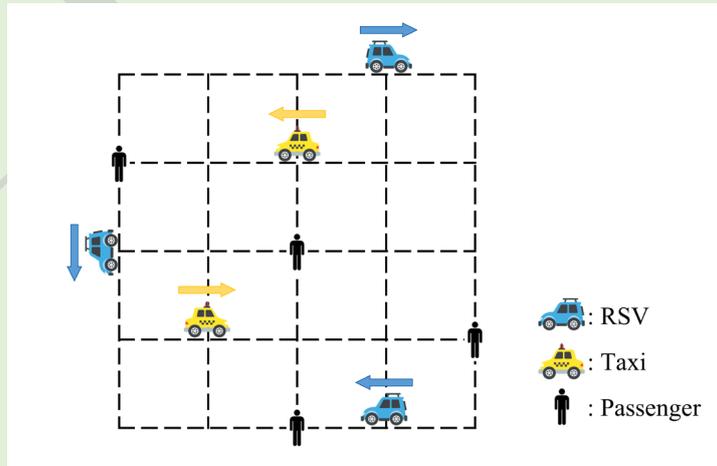
The simulation is time-based, and its runtime horizon consists of multiple time intervals, the length of each time interval is  $T$  minutes, and each minute indicates a time stamp. During each time interval, the CRTM's operational configuration is fixed, including the fleet sizes, fare rates, and wage rates paid by the TNC to drivers, and it is assumed that the travel demand remains unchanging. As for passengers, they enter the system following a Poisson process with a given total travel demand rate,  $\Lambda$ . Their origins and requested travel destinations are randomly generated at intersections of the horizontal and vertical lines. Denote passenger  $i$ 's initial location and destination are  $(x_i, y_i)$  and  $(x'_i, y'_i)$ , respectively. His/her travel distance can be expressed in terms of a Manhattan Distance as follows,

$$l_i = \|(x'_i - x_i, y'_i - y_i)\|_1. \quad (5)$$

Considering an  $M * M$  grid road network, the average travel distance of passengers is

$$\bar{l} = \frac{2(M^2 - 1)}{3M}. \quad (6)$$

For RSVs and taxis, their starting positions are randomly located in the road network, and their current travel directions are randomly set based on their locations. In the agent-based simulation, all vehicles remain in motion and do not park. When the time stamp updates, all vehicles move toward their current travel directions at a fixed travel speed  $v$ , after which they update their new travel directions based on their new locations and service states, i.e., idle, picking up, or in-service. Vehicles in picking-up and in-service states update their direction and trajectories according to the shortest path to the matched passengers and their requested destinations. Idle vehicles may choose any available direction except the one opposite to their current heading.

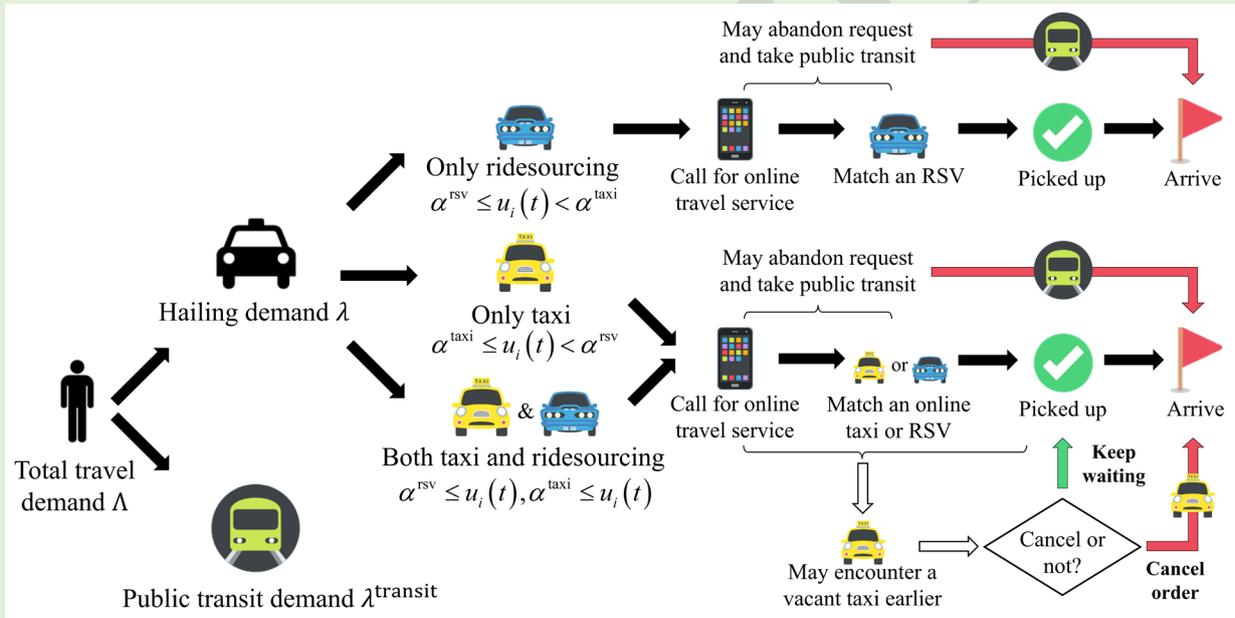


**Fig. 3.** Example of a grid-type road network

The TNC receives passengers' requests and matches them with RSVs and hybrid taxis. For the

1 matching strategy, we employ the well-known Nearest Neighbor (NN) scheduling algorithm  
 2 (Bertsimas and Van Ryzin, 1991). When a passenger arrives, if there are vehicles available in the  
 3 system, he/she will be matched with the closest one. If there is no available vehicle, he/she will wait  
 4 until there is an available one, and he/she is also the earliest arriving and closest passenger to the  
 5 vehicle among all waiting passengers. It is also important to note that any pair of matches must be  
 6 within the maximum matching distance  $R$  to avoid long waiting times for passengers and a ‘wild  
 7 goose chase’ for long pick-up distances of vehicles.

8 The activities and interactions of passengers, RSVs, and taxis are illustrated in Fig. 4. Once  
 9 passengers enter the system with an arrival rate of  $\Lambda$ , they first choose a travel mode between hailing  
 10 service and public transit. The latter, as an alternative to hailing services, has a lower fare rate  $\alpha^{\text{transit}}$ ,  
 11 slower travel speed  $v^{\text{transit}}$ , but longer average waiting time  $\bar{W}^{\text{transit}}$ . In this paper, we employ the Logit  
 12 model to approximate the split between the two travel modes (He et al., 2018; Li et al., 2022), with  
 13 details provided in Section 4.2. The resultant demand rates for hailing and public transit are given by  
 14  $\lambda$  and  $\lambda^{\text{transit}}$ , respectively, and  $\lambda + \lambda^{\text{transit}} = \Lambda$ .



16 **Fig. 4.** Passenger’s choice process of travel model and hailing type

17 For passengers selecting hailing services, their subsequent decision concerns which type of  
 18 hailing vehicles to request. Following Banerjee et al. (2015), Bai et al. (2019), and Yu et al. (2020),  
 19 this study proposes a method that selects the option(s) with the positive utility of hailing service. This  
 20 utility comprises the fare cost and the passenger’s valuation associated with his/her trip. Meanwhile,  
 21 we assume that the sunk cost due to wasted waiting time influences the hailing type decisions of  
 22 impatient passengers.

23 In line with Ülkü et al. (2020), we introduce the concept of mental accounting to characterize  
 24 passengers’ impatient behavior while waiting to be matched. According to Thaler (1980, 1985, 1990,

1999), people tend to record the time, money, or effort they have already invested in a virtual ‘mental account’ and do not immediately perceive these as a loss. When making decisions, to avoid a ‘deficit’ in the ‘mental account,’ people tend to ‘offset’ previous investments by increasing consumption, thereby demonstrating the sunk-cost effect. In this study, we consider that the sunk-cost effect on passengers caused by the elapsed waiting time would motivate them to request more hailing types before order matching. Meanwhile, it is assumed that this sunk-cost effect becomes more pronounced as the potential trip distance increases (Liu et al., 2024b).

To model such an impatient behavior, the mental accounting utility is adopted, which consists of the passenger’s valuation on the trip, the fare cost of the trip, and the sunk cost utility. Specifically, the valuation represents the monetary value of the requested trip to the passenger, which may vary depending on the purpose and distance of the trip. For passenger  $i$ , the mental accounting utility regarding hailing type  $s \in \{\text{rsv}, \text{taxi}\}$  at elapsed waiting time  $t$  can be formulated as

$$U_i^s(t) = \hat{u}_i \cdot l_i - \alpha^s \cdot l_i + \beta_{\text{sunk}}^{\text{pas}} \cdot l_i \cdot t, \quad (7)$$

where the first term on the right side of Eq. (7) represents the trip valuation, in which  $\hat{u}_i$  denotes passenger  $i$ ’s valuation for unit trip distance; the second term represents the fare cost, where  $\alpha^s$  denotes the fare rate of hailing type  $s$ ; the third term defines the sunk cost utility, and the coefficient  $\beta_{\text{sunk}}^{\text{pas}} \geq 0$  represents the effect of sunk waiting time on the passenger’s decision. In this study, we assume that passenger  $i$  is willing to request the corresponding hailing type  $s$  only if  $U_i^s(t) \geq 0$ .

Subsequently, define  $u_i(t) = \hat{u}_i + \beta_{\text{sunk}}^{\text{pas}} \cdot t$ , it denotes passenger  $i$ ’s mental account value for unit trip distance at  $t$ , then  $U_i^s(t) \geq 0$  can be reduced to  $u_i(t) \geq \alpha^s$  by canceling  $l_i$ . This means that if  $u_i(t)$  is higher than the fare rate of a particular hailing service,  $\alpha^{\text{rsv}}$  or  $\alpha^{\text{taxi}}$ , then passenger  $i$ ’s mental accounting utility is positive at  $t$  and would choose the corresponding hailing type  $s$ , i.e., RSV or taxi. In the simulation,  $\hat{u}_i$  is set to follow a uniform distribution  $U(\min\{\alpha^{\text{rsv}}, \alpha^{\text{taxi}}\}, u_{\text{max}})$  to distinguish the heterogeneity of passenger valuations across different travel purposes, where  $u_{\text{max}}$  denotes the highest valuation for unit trip distance. The range starts with  $\min\{\alpha^{\text{rsv}}, \alpha^{\text{taxi}}\}$  is aiming to ensure passengers who are willing to request hailing services would choose at least one hailing type in the beginning, i.e., ensuring  $u_i(0) \geq \min\{\alpha^{\text{rsv}}, \alpha^{\text{taxi}}\}$ . Accordingly, the passenger’s hailing type choice can be determined by the following Eq. (8).

$$\text{Hailing type at } t = \begin{cases} \text{only RSV,} & \text{if } \alpha^{\text{rsv}} \leq u_i(t) < \alpha^{\text{taxi}} \\ \text{only taxi,} & \text{if } \alpha^{\text{taxi}} \leq u_i(t) < \alpha^{\text{rsv}} \\ \text{both RSV and taxi,} & \text{if } \alpha^{\text{rsv}} \leq u_i(t) \text{ and } \alpha^{\text{taxi}} \leq u_i(t) \end{cases}. \quad (8)$$

For example, suppose passenger  $k$  has a 10-unit distance hailing request with  $\hat{u}_k = 2$  and  $\beta_{\text{sunk}}^{\text{pas}} = 0.2$ . The fare rates  $\alpha^{\text{rsv}} = 1$  and  $\alpha^{\text{taxi}} = 3$ . Initially,  $u_k(0) = 2$ , passenger  $k$  only requests RSV service since  $\alpha^{\text{rsv}} < u_k(0) < \alpha^{\text{taxi}}$ . After this, if the passenger has not been matched with any RSV until  $t = 5$ , then passenger  $k$  would request both RSV and taxi services because  $\alpha^{\text{rsv}} < \alpha^{\text{taxi}} = u_k(5) = 3$ .

Our proposed method is more general than existing studies (Wang et al., 2020; Yu et al., 2020; Xu et al., 2022) by adopting a linear function to characterize the effect of waiting time on passenger  $i$ 's hailing type decision via Eq. (7). That is to say, if one selected type of hailing vehicle is not available for a long time, the mental accounting utility of a passenger may be increased by the sunk time cost, leading him/her to request more hailing types. Ülkü et al. (2020) also suggest that people who spend a longer time waiting in line tend to consume more. In practice, a TNC, like DiDi, currently allows passengers to append the hailing types they prefer via its smartphone application.

Note that if a passenger requests both RSV and taxi services and there are available vehicles for both hailing types, then the TNC will match the passenger with the closest vehicle. If both types of closest vehicles are at the same distance from the passenger, then the less expensive one will be matched. Further, if the fares of both types of closest vehicles are the same, then the match is randomized.

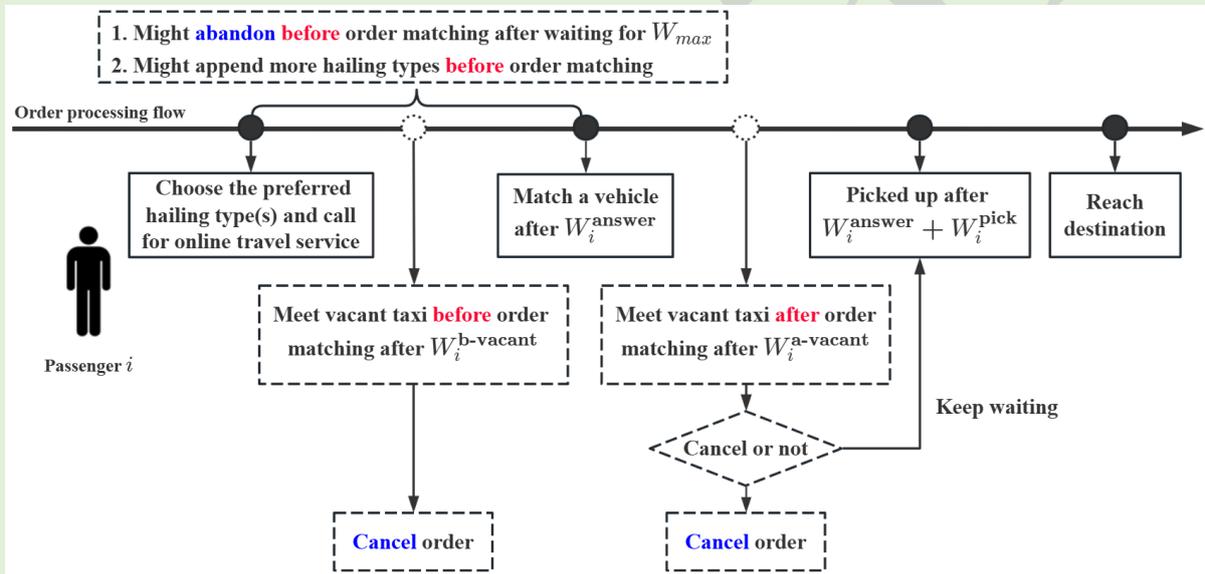


Fig. 5. Example of the hailing service process

The whole hailing service process is illustrated in Fig. 5. Initially, passenger  $i$  determines the preferred hailing type(s) with  $u_i(0)$  via Eq. (8), and sends an online travel request to the TNC. Note that the passenger might append more hailing types before order matching. Ideally, the TNC matches the request with a vehicle, either an RSV or a hybrid taxi. Then, the matched vehicle arrives at passenger  $i$ 's origin, the passenger boards the vehicle, travels to the destination, and the service ends. During such a process, the time difference between passenger  $i$  submitting the request and receiving the matched vehicle is the answer time,  $W_i^{\text{answer}}$ ; the elapsed time between passenger  $i$  matching to and boarding on the matched vehicle is the pick-up time,  $W_i^{\text{pick}}$ .

In the process, there are three main occasions when a passenger may cancel his/her request.

First, before an order is matched, a passenger abandons the request upon exhausting his/her patience. Specifically, if the answer time  $W_i^{\text{answer}}$  for the TNC to match passenger  $i$  with a vehicle

1 exceeds the passenger's maximum patience time  $W_{\max}$  (i.e.,  $W_i^{\text{answer}} > W_{\max}$ ), the request is abandoned  
 2 and he/she will take public transit to complete the trip. This reflects the natural decline in passenger  
 3 patience as waiting time increases.

4 Second, before an order is matched, a passenger cancels the request once he/she encounters a  
 5 cruising vacant taxi after waiting for  $W_i^{\text{b-vacant}}$  minutes while he/she is also opting for taxi service. This  
 6 decision is driven by two factors: first, taking the available taxi ensures an earlier arrival at the  
 7 destination; second, passengers tend to have lower patience before their ride is confirmed (Xu et al.,  
 8 2021a). Psychologically, uncertain waiting times feel longer than certain ones (Maister, 1984).

9 Third, after the order is matched, a passenger who is willing to accept taxi service may cancel the  
 10 order when he/she encounters a cruising vacant taxi. The decision depends on the utility difference  
 11 between completing the trip with the matched vehicle and opting for cruising taxis. The two utilities  
 12 are mathematically expressed in the following two equations, respectively.

$$13 \quad C_i^1 = \begin{cases} \beta_{\text{time}}^{\text{pas}} (W_i^{\text{answer}} + W_i^{\text{pick}} - W_i^{\text{a-vacant}}) + \alpha^{\text{rsv}} l_i, & \text{if matched with RSV} \\ \beta_{\text{time}}^{\text{pas}} (W_i^{\text{answer}} + W_i^{\text{pick}} - W_i^{\text{a-vacant}}) + \alpha^{\text{taxi}} l_i, & \text{if matched with hybrid taxi} \end{cases}, \quad (9)$$

$$14 \quad C_i^2 = \alpha^{\text{taxi}} l_i + \hat{p} + H. \quad (10)$$

15 In Eq. (9), the first part of the right side represents the remaining waiting time cost for the matched  
 16 vehicle, where  $\beta_{\text{time}}^{\text{pas}}$  is the passengers' time cost coefficient,  $W_i^{\text{a-vacant}}$  denotes the waiting time when  
 17 passenger  $i$  encounters a vacant taxi after order matching. The second part represents the fare cost.

18 In Eq. (10), the first part of the right side represents the fare cost of taking a vacant taxi,  $\hat{p}$  is the  
 19 penalty a passenger has to pay for canceling a matched order, and  $H$  is the corresponding  
 20 psychological cost (He and Shen, 2015; He et al., 2018; Wang et al., 2020; Li et al., 2023a).

21 It is worth noting that if a passenger encounters a vacant taxi before the matched vehicle arrives  
 22 and decides to continue waiting, he/she will consistently wait for the matched vehicle, even if other  
 23 vacant taxis appear before then. This behavior can be explained as follows. Suppose passenger  $i$  is  
 24 matched with an RSV and encounters a vacant taxi after order matching. If the passenger chooses to  
 25 continue waiting at this moment, it implies that  $C_i^1 \leq C_i^2$ . Let  $C_i^{1+} = \beta_{\text{time}}^{\text{pas}} (W_i^{\text{answer}} + W_i^{\text{pick}}) + \alpha^{\text{rsv}} l_i$ . Then,  
 26  $C_i^1 = C_i^{1+} - \beta_{\text{time}}^{\text{pas}} \cdot W_i^{\text{a-vacant}}$ . Let  $W_{i2}^{\text{a-vacant}}$  denote the time at which passenger  $i$  encounters another vacant  
 27 taxi after choosing to continue waiting for the first time, and let  $C_{i2}^1$  represent the utility of passenger  
 28  $i$  choosing to continue waiting for the second time after order matching. Thus, we have  
 29  $C_{i2}^1 = C_i^{1+} - \beta_{\text{time}}^{\text{pas}} \cdot W_{i2}^{\text{a-vacant}}$ . Since  $W_{i2}^{\text{a-vacant}} > W_i^{\text{a-vacant}}$ , it follows that  
 30  $C_{i2}^1 - \beta_{\text{time}}^{\text{pas}} \cdot W_{i,2}^{\text{a-vacant}} < C_i^{1+} - \beta_{\text{time}}^{\text{pas}} \cdot W_i^{\text{a-vacant}}$ . Therefore, we can obtain  $C_{i,2}^1 < C_i^1 \leq C_i^2$ , meaning that if  
 31 passenger  $i$  chooses to continue waiting for the first time, he/she will keep waiting until the matched  
 32 RSV arrives. The same reasoning applies to passengers matched with hybrid taxis.

## 33 4.2 Objective functions

1 This section formulates the four objective functions for passengers, taxi drivers, RSV drivers, and the  
 2 TNC, respectively. Each objective is modeled and evaluated within a single time interval.

3 **(1) Average hailing cost of passengers**

4 From the passengers' perspective, the objective is to minimize the average hailing cost. Mathematically,  
 5 this is expressed as:

$$6 \quad \bar{C} = \frac{1}{N(T, \lambda)} \sum_{i=1}^{N(T, \lambda)} C_i, \quad (11)$$

7 where  $N(T, \lambda)$  denotes the number of passengers who arrived and ended hailing service at the hailing  
 8 demand rate  $\lambda$  during a time interval  $T$ .  $C_i$  is the generalized hailing cost associated with passenger  
 9  $i$  and is calculated based on the selected hailing services. Mathematically, it is given by,

$$10 \quad C_i = \begin{cases} \beta_{\text{time}}^{\text{pas}} (W_i^{\text{answer}} + W_i^{\text{pick}} + l_i/v) + \alpha^{\text{taxi}} l_i, & i \in G^{\text{h-taxi}} \\ \beta_{\text{time}}^{\text{pas}} (W_i^{\text{answer}} + W_i^{\text{pick}} + l_i/v) + \alpha^{\text{rsv}} l_i, & i \in G^{\text{rsv}} \\ \beta_{\text{time}}^{\text{pas}} (W_i^{\text{b-vacant}} + l_i/v) + \alpha^{\text{taxi}} l_i, & i \in G_{\text{cancel}} \\ \beta_{\text{time}}^{\text{pas}} (W_i^{\text{a-vacant}} + l_i/v) + \alpha^{\text{taxi}} l_i + H + \hat{p}, & i \in G_{\text{cancel}}^{\text{h-taxi}} \cup G_{\text{cancel}}^{\text{rsv}} \\ \beta_{\text{time}}^{\text{pas}} (W_{\text{max}} + \bar{W}^{\text{transit}} + l_i/v^{\text{transit}}) + \alpha^{\text{transit}} l_i + \beta_{\text{time}}^{\text{pas}} (l_i/v^{\text{transit}} - l_i/v), & i \in G_{\text{abandon}} \end{cases}, \quad (12)$$

11 where  $G^{\text{h-taxi}}$  and  $G^{\text{rsv}}$  denote the sets of passengers served by hybrid taxi and RSV through online  
 12 matching, respectively;  $G_{\text{cancel}}$  denotes the set of passengers who canceled their requests before order  
 13 matching;  $G_{\text{cancel}}^{\text{h-taxi}}$  and  $G_{\text{cancel}}^{\text{rsv}}$  denote the sets of passengers who canceled hybrid taxi and RSV orders  
 14 after order matching, respectively;  $G_{\text{abandon}}$  denotes the set of passengers who abandoned their online  
 15 requests. For abandoned passengers, let  $\beta_{\text{time}}^{\text{pas}} (l_i/v^{\text{transit}} - l_i/v)$  denote an additional penalty item to  
 16 represent the loss of failing to get hailing services, which means the extra time cost of taking public  
 17 transit compared to hailing services.

18 For the split of travel demand, the hailing demand rate  $\lambda$  is calculated as below,

$$19 \quad \lambda = \Lambda \frac{\exp(-\theta^{\text{pas}} \bar{L})}{\exp(-\theta^{\text{pas}} \bar{L}) + \exp(-\theta^{\text{pas}} \bar{C}^{\text{transit}})}, \quad (13)$$

$$20 \quad \bar{C}^{\text{transit}} = \beta_{\text{time}}^{\text{pas}} (\bar{W}^{\text{transit}} + \bar{l}/v^{\text{transit}}) + \alpha^{\text{transit}} \bar{l} \quad (14)$$

$$21 \quad \bar{L} = \frac{1}{\theta_0} \ln \left\{ \exp(\theta_0 \bar{C}^{\text{rsv}}) + \exp(\theta_0 \bar{C}^{\text{taxi}}) \right\}, \quad (15)$$

22 where  $\theta^{\text{pas}}$  is the dispersion coefficient in the Logit model;  $\bar{C}^{\text{transit}}$  is the average travel cost associated

1 with public transit services;  $\bar{L}$  represents the logsum of the disutility as perceived by the passenger  
 2 who decides to take hailing services to fulfill the travel demand (Ben-Akiva and Lerman, 1985; He et  
 3 al., 2018), where  $\theta_0$  is the logsum parameter,  $\bar{C}^{\text{rsv}}$  and  $\bar{C}^{\text{taxi}}$  represent the average travel costs of  
 4 passengers who are served by RSVs and taxis, respectively, which can be calculated by the following  
 5 equations.

$$6 \quad \bar{C}^{\text{rsv}} = \frac{\sum_{i \in G^{\text{rsv}}} C_i}{|G^{\text{rsv}}|}, \quad (16)$$

$$7 \quad \bar{C}^{\text{taxi}} = \frac{\sum_{i \in G^{\text{h-taxi}} \cup G_{\text{cancel}}^{\text{h-taxi}} \cup G_{\text{cancel}}^{\text{rsv}}} C_i}{|G^{\text{h-taxi}} \cup G_{\text{cancel}}^{\text{h-taxi}} \cup G_{\text{cancel}}^{\text{rsv}}|}. \quad (17)$$

## 8 (2) Average profit of taxi drivers

9 For taxi drivers, their objective is to maximize the average profit, computed by,

$$10 \quad Q^{\text{taxi}} = \frac{\tau^{\text{taxi}} \left( \sum_{i \in G^{\text{h-taxi}}} \alpha^{\text{taxi}} l_i + \sum_{i \in G_{\text{cancel}}^{\text{h-taxi}}} \hat{p} \right) - \sum_{i \in G_{\text{cancel}}^{\text{h-taxi}}} \beta^{\text{h-taxi}} (W_i^{\text{a-vacant}} - W_i^{\text{answer}}) + \sum_{i \in G_{\text{street}}^{\text{h-taxi}}} \alpha^{\text{taxi}} l_i + \sum_{i \in G^{\text{s-taxi}}} \alpha^{\text{taxi}} l_i}{Z^{\text{taxi}}}, \quad (18)$$

$$- (vT\gamma + \hat{\gamma}^{\text{taxi}})$$

11 where  $Z^{\text{taxi}}$  is the number of total taxis;  $\tau^{\text{taxi}}$  is the wage rate paid by the TNC to hybrid taxi drivers;  
 12  $G_{\text{street}}^{\text{h-taxi}}$  denotes the set of passengers served by hybrid taxis on the street;  $G^{\text{s-taxi}}$  denotes the set of  
 13 passengers served by street taxis;  $\gamma$  is the fuel cost per unit distance of hailing vehicles;  $\hat{\gamma}^{\text{taxi}}$  is the  
 14 fixed operating cost of taxis (representing the cost of taxicab license fee, insurance, depreciation evenly  
 15 distributed over single time interval);  $\beta^{\text{h-taxi}}$  is the time cost coefficient of hybrid taxi drivers, which  
 16 represents the potential income per unit of time wasted by passengers' cancellation. Let  $Z^{\text{h-taxi}}$  and  
 17  $Z^{\text{s-taxi}}$  be the number of hybrid and street taxis in the system, respectively,  $Z^{\text{h-taxi}} + Z^{\text{s-taxi}} = Z^{\text{taxi}}$ . Then,  
 18  $\beta^{\text{h-taxi}}$  can be formulated as follows,

$$19 \quad \beta^{\text{h-taxi}} = \frac{\tau^{\text{taxi}} \left( \sum_{i \in G^{\text{h-taxi}}} \alpha^{\text{taxi}} l_i + |G_{\text{cancel}}^{\text{h-taxi}}| \cdot \hat{p} \right) + \sum_{i \in G_{\text{street}}^{\text{h-taxi}}} \alpha^{\text{taxi}} l_i}{Z^{\text{h-taxi}} \cdot T}. \quad (19)$$

20 Taxi drivers are assumed to update their work modes at the beginning of each time interval and  
 21 maintain them throughout the interval. We then employ a Logit model to approximate the work mode  
 22 split of taxi drivers (He and Shen, 2015; Wang et al., 2016):

$$23 \quad Z^{\text{h-taxi}} = Z^{\text{taxi}} \frac{\exp(\theta^{\text{taxi}} Q^{\text{h-taxi}})}{\exp(\theta^{\text{taxi}} Q^{\text{h-taxi}}) + \exp(\theta^{\text{taxi}} Q^{\text{s-taxi}})}, \quad (20)$$

$$Z^{s\text{-taxi}} = Z^{\text{taxi}} \frac{\exp(\theta^{\text{taxi}} Q^{s\text{-taxi}})}{\exp(\theta^{\text{taxi}} Q^{h\text{-taxi}}) + \exp(\theta^{\text{taxi}} Q^{s\text{-taxi}})}, \quad (21)$$

where  $\theta^{\text{taxi}}$  is the dispersion coefficient,  $Q^{h\text{-taxi}}$  and  $Q^{s\text{-taxi}}$  are the average profits of hybrid and street taxi drivers in a modeling time interval, respectively. They can be calculated by the following equations.

$$Q^{h\text{-taxi}} = \frac{\tau^{\text{taxi}} \left( \sum_{i \in G^{h\text{-taxi}}} \alpha^{\text{taxi}} l_i + |G_{\text{cancel}}^{h\text{-taxi}}| \cdot \hat{p} \right) - \sum_{i \in G_{\text{cancel}}^{h\text{-taxi}}} \beta^{\text{taxi}} (W_i^{\text{a-vacant}} - W_i^{\text{answer}}) + \sum_{i \in G_{\text{street}}^{h\text{-taxi}}} \alpha^{\text{taxi}} l_i}{Z^{h\text{-taxi}}} - (vT\gamma + \hat{\gamma}^{\text{taxi}}), \quad (22)$$

$$Q^{s\text{-taxi}} = \frac{\sum_{i \in G^{s\text{-taxi}}} \alpha^{\text{taxi}} l_i}{Z^{s\text{-taxi}}} - (vT\gamma + \hat{\gamma}^{\text{taxi}}). \quad (23)$$

### (3) Average profit of RSV drivers

The objective of RSV drivers is also to maximize the average profit within a modeling time interval. Mathematically, it is expressed by,

$$Q^{\text{RSV}} = \frac{\tau^{\text{RSV}} \left( \sum_{i \in G^{\text{RSV}}} \alpha^{\text{RSV}} l_i + |G_{\text{cancel}}^{\text{RSV}}| \cdot \hat{p} \right) - \sum_{i \in G_{\text{cancel}}^{\text{RSV}}} \beta^{\text{RSV}} (W_i^{\text{a-vacant}} - W_i^{\text{answer}})}{Z^{\text{RSV}}} - (vT\gamma + \hat{\gamma}^{\text{RSV}}), \quad (24)$$

where  $\hat{\gamma}^{\text{RSV}}$  is the fixed operating cost of RSVs (representing the cost of insurance and depreciation evenly distributed over one time interval);  $\beta^{\text{RSV}}$  is the time cost coefficient of the RSV drivers, which is given by

$$\beta^{\text{RSV}} = \frac{\tau^{\text{RSV}} \left( \sum_{i \in G^{\text{RSV}}} \alpha^{\text{RSV}} l_i + |G_{\text{cancel}}^{\text{RSV}}| \cdot \hat{p} \right)}{Z^{\text{RSV}} \cdot T}. \quad (25)$$

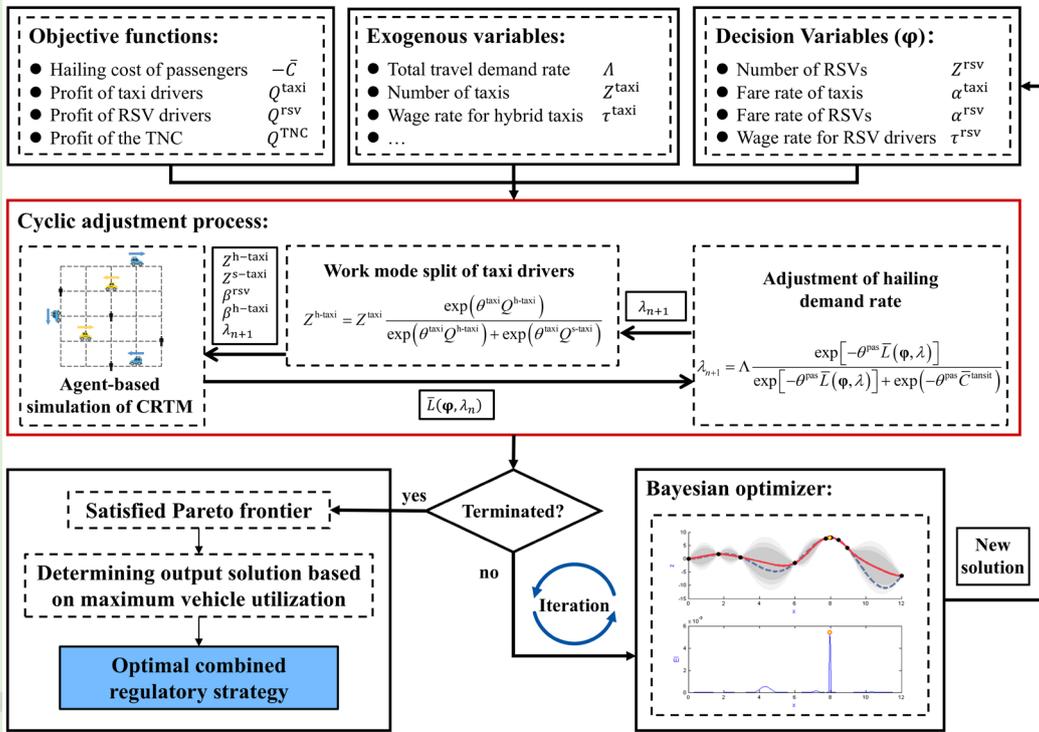
### (4) Profit of the TNC

The TNC generates income by charging passengers trip fares and collecting penalties when passengers cancel matched orders. Its cost arises from paying wages to RSV and hybrid taxi drivers. The objective of the TNC is to maximize its profit, which is:

$$Q^{\text{TNC}} = (1 - \tau^{\text{taxi}}) \left( \sum_{i \in G^{h\text{-taxi}}} \alpha^{\text{taxi}} l_i + |G_{\text{cancel}}^{h\text{-taxi}}| \cdot \hat{p} \right) + (1 - \tau^{\text{RSV}}) \left( \sum_{i \in G^{\text{RSV}}} \alpha^{\text{RSV}} l_i + |G_{\text{cancel}}^{\text{RSV}}| \cdot \hat{p} \right). \quad (26)$$

## 4.3 Solution Method

1 Solving the proposed bi-level model (Eq. (1)–(4)) is challenging. First, the proposed problem includes  
 2 multiple objectives and decision variables, leading to a high computational complexity. Second, the  
 3 lower-level problem involves complex interactions and behaviors of passengers and drivers, which are  
 4 difficult to analytically formulate, making it challenging to derive closed-form solutions or apply  
 5 tractable solution methods. Hence, we develop a solution approach based on the multi-objective  
 6 Bayesian optimization to solve this problem (Fig. 6). The merit of using Bayesian optimization to  
 7 address black-box bi-level optimization is avoiding frequent calls to the lower-level simulation via  
 8 constructing a surrogate model. The surrogate model approximates the lower-level model with an  
 9 analytical function based on a small amount of sample data. Then, new candidate solutions, which are  
 10 promising to achieve an improvement in the Pareto frontier, are generated based on the acquisition  
 11 function.



12  
 13 **Fig. 6.** A multi-objective Bayesian optimization based solution framework for optimizing the  
 14 combined regulatory strategy of CRTM

15 As discussed in Section 1, when optimizing the combined regulatory strategy, it is necessary to  
 16 evaluate the market performance with stable supply-demand patterns and obtain a stabilized hailing  
 17 demand rate  $\lambda^*(\boldsymbol{\varphi})$  and work mode split of taxi drivers under a given regulatory strategy  $\boldsymbol{\varphi}$ . Let  
 18  $\bar{L}(\boldsymbol{\varphi}, \lambda)$  denote the logsum disutility of hailing passengers under strategy  $\boldsymbol{\varphi}$  and demand rate  $\lambda$ . Here  
 19  $\bar{L}(\boldsymbol{\varphi}, \lambda)$  is a function of  $\lambda$ . Note that in Eq. (13),  $\lambda$  is also a function of  $\bar{L}$ . This results in a fixed-  
 20 point problem. Following existing studies that addressed similar fixed-point problems in transportation  
 21 simulation research (Flötteröd, 2017; Wen et al., 2018), we iteratively run the model to adjust hailing  
 22 demand rate until convergence, and then, output the corresponding objective values for further analysis  
 23 or optimization. The iterative adjustment process for determining the endogenously stable hailing

1 demand rate  $\lambda^*(\boldsymbol{\varphi})$  can be described as follows.

2 Define a sequence of real numbers  $\{\lambda_n\}$ , where  $\lambda_n \geq 0$  denotes the  $n^{\text{th}}$  adjusted hailing demand  
 3 rate at each iteration of the overall optimization process, we have:

$$4 \quad \lambda_{n+1} = \Lambda \frac{\exp[-\theta^{\text{pas}} \bar{L}(\boldsymbol{\varphi}, \lambda)]}{\exp[-\theta^{\text{pas}} \bar{L}(\boldsymbol{\varphi}, \lambda)] + \exp(-\theta^{\text{pas}} \bar{C}^{\text{transit}})}, \quad (27)$$

5 where the constants  $\Lambda > 0$ ,  $\theta^{\text{pas}} > 0$ ,  $\bar{C}^{\text{transit}} > 0$ .

6 As shown in the red box in Fig. 6, after each adjustment of the hailing demand rate, the first step  
 7 is to determine the work mode split of taxi drivers, which is influenced by decision variables and the  
 8 hailing demand rate. Then, the logsum disutility of hailing passengers calculated from the agent-based  
 9 simulation is fed back into Eq. (27) for the next adjustment. This iterative process terminates when the  
 10 adjusted hailing demand rate reaches the convergence condition. Then, the four corresponding  
 11 objective values are calculated and substituted into the Bayesian optimizer to acquire the next  
 12 candidate solution. Note that the hailing demand rate implies the average arriving number of  
 13 passengers who request hailing services per time stamp. In this study, we set the convergence condition  
 14 to be  $|\lambda_n - \lambda_{n-1}| < 1$  (request/min),  $n \geq 1$ , which means the iterative adjustment process stops when the  
 15 absolute difference between consecutive adjusted  $\lambda$  values does not exceed one passenger during each  
 16 iteration.

17 After several iterations of the overall multi-objective Bayesian optimization, we can obtain a  
 18 stabilized Pareto frontier with multiple non-dominated solution points. Then, the final Pareto optimal  
 19 output solution  $\boldsymbol{\varphi}^*$  is determined by a secondary criterion of maximizing total vehicle utilization.

## 20 4.4 Multi-objective Bayesian optimization

### 21 4.4.1 Surrogate model

22 The first step in the multi-objective Bayesian optimization is constructing a surrogate model based on  
 23 the sampled data. This paper employs the Gaussian process regression as the surrogate model to fit the  
 24 complex nonlinear relationship between the decision variables and the multi-objective functions  
 25 (Rasmussen, 2003; Frazier, 2018).

26 Consider a set of decision variables  $\mathbf{X}_m = (\mathbf{x}_1, \dots, \mathbf{x}_m)^\top = \begin{pmatrix} x_{1,1} & \cdots & x_{1,d} \\ \vdots & \ddots & \vdots \\ x_{m,1} & \cdots & x_{m,d} \end{pmatrix}$  with  $m$  samples in  $d$

27 dimensions ( $d = 4$  in this paper) and an associated set of objective function values

28  $\mathbf{f}_m^\omega = (f^\omega(\mathbf{x}_1), \dots, f^\omega(\mathbf{x}_m))^\top$ ,  $\omega = 1, 2, 3, 4$ . Note that  $x$  corresponds to a regulatory strategy and  $f$

29 corresponds to an objective function in this study. For example,  $x_{2,1}$  means the number of RSVs  $Z^{\text{RSV}}$

30 in the 2<sup>nd</sup> sample point,  $f^2(\mathbf{x}_1)$  indicates the average profit of taxi drivers under the 1<sup>st</sup> sample decision

1 variable vector  $\mathbf{x}_1 = (x_{1,1}, x_{1,2}, x_{1,3}, x_{1,4})$ .

2 Taking the  $\omega^{\text{th}}$  objective as an example, the Gaussian process assumes that for any given  $m$ ,  $\mathbf{f}_m^\omega$   
 3 follows an  $m$ -dimensional multivariate Gaussian distribution (Zhong et al., 2021; Huo et al., 2023a;  
 4 Huo et al., 2023b):

$$5 \quad \mathbf{f}_m^\omega \sim \mathcal{N}(\boldsymbol{\mu}_m^\omega, \mathbf{K}_m), \quad (28)$$

6 where  $\boldsymbol{\mu}_m^\omega = (E(f^\omega(\mathbf{x}_1)), \dots, E(f^\omega(\mathbf{x}_m)))^\top$ ,  $E(\cdot)$  denotes the expected value of the objective

7 function.  $\mathbf{K}_m = (\mathbf{k}_1, \dots, \mathbf{k}_m)^\top = \begin{pmatrix} k(\mathbf{x}_1, \mathbf{x}_1) & \cdots & k(\mathbf{x}_1, \mathbf{x}_m) \\ \vdots & \ddots & \vdots \\ k(\mathbf{x}_m, \mathbf{x}_1) & \cdots & k(\mathbf{x}_m, \mathbf{x}_m) \end{pmatrix}$ , where  $k(\cdot, \cdot)$  is the covariance kernel

8 function. In this study, the common Matérn 5/2 kernel is used as the covariance kernel function:

$$9 \quad k(\mathbf{x}, \mathbf{x}') = \left( 1 + \frac{\sqrt{5}\kappa}{\zeta} + \frac{5\kappa^2}{3\zeta^2} \right) \exp\left( -\frac{\sqrt{5}\kappa}{\zeta} \right), \quad (29)$$

10 where  $\kappa = |\mathbf{x} - \mathbf{x}'|$ ,  $\zeta$  is the hyperparameter that determines the Gaussian process curve, determined by  
 11 maximizing the log-marginal likelihood function as follows:

$$12 \quad \log p(\mathbf{f}_m^\omega | \mathbf{X}_m) = -\frac{1}{2} (\mathbf{f}_m^\omega)^\top \mathbf{K}_m^{-1} \mathbf{f}_m^\omega - \frac{1}{2} \log |\mathbf{K}_m| - \frac{m}{2} \log 2\pi. \quad (30)$$

13 Given a sampling point  $\mathbf{x}_{m+1}$ , the objective values predicted by the Gaussian process satisfy the  
 14 following distribution:

$$15 \quad f^\omega(\mathbf{x}_{m+1}) \sim \mathcal{N}(\boldsymbol{\mu}_{m+1}^\omega, \boldsymbol{\sigma}_{m+1}^\omega), \quad (31)$$

16 where  $\boldsymbol{\mu}_{m+1}^\omega = \mathbf{k}_{m+1}^\top \mathbf{K}_m^{-1} \mathbf{f}_m^\omega$  and  $\boldsymbol{\sigma}_{m+1}^\omega = k(\mathbf{x}_{m+1}, \mathbf{x}_{m+1}) - \mathbf{k}_{m+1}^\top \mathbf{K}_m^{-1} \mathbf{k}_{m+1}$ .

#### 17 4.4.2 Acquisition function

18 The second step of multi-objective Bayesian optimization is to acquire the next candidate solution in  
 19 the solution space based on the acquisition function that maximizes the improvement of the Pareto  
 20 frontier, which can also reduce calls to the lower-level model. This paper adopts hypervolume-based  
 21 probability of improvement (HVPoI) as the acquisition function to handle this multi-objective problem.  
 22 Hypervolume (HV) is widely used in multi-objective optimization (Beume et al., 2007), and HVPoI  
 23 can significantly reduce the overall computational complexity while retaining the advantages of using  
 24 HV (Couckuyt et al., 2014). The specific computational steps are as follows.

25 **Step 1.** Calculate the probability of improvement.

26 Given  $\mathbf{X}_m$ , the initial Pareto frontier  $\mathbb{P}$  can be expressed as:

$$\mathbb{P} = \{\mathbf{f}(\mathbf{x}_1^*), \dots, \mathbf{f}(\mathbf{x}_q^*)\}, \quad (32)$$

where  $q \leq m$  is the number of Pareto optimal (non-dominated) solutions, for  $i=1, \dots, q$ ,  $\mathbf{f}(\mathbf{x}_i^*) = (f^1(\mathbf{x}_i^*), \dots, f^4(\mathbf{x}_i^*))$ ,  $\mathbf{x}_i^* \in \mathbf{X}_m$ . The probability that a new sampled solution is in the non-dominated objective function space  $A$  is:

$$P(\mathbf{x}) = \int_{\mathbf{f}(\mathbf{x}) \in A} \prod_{\omega=1}^4 \phi^\omega [f^\omega(\mathbf{x})] df^\omega(\mathbf{x}), \quad (33)$$

where  $\phi^\omega(\mathbf{x})$  denotes the probability density function of  $f^\omega(\mathbf{x})$ , which can also be viewed as the probability that the new sampled solution improves the Pareto frontier  $\mathbb{P}$ . In this paper, we use the method of Couckuyt et al. (2014) to decompose the integration region  $A$  into  $b$  (hyper-)rectangular cells, then  $P(\mathbf{x})$  can be computed as follows:

$$P(\mathbf{x}) = \sum_{a=1}^b \pm \prod_{\omega=1}^4 (\Phi^\omega(U_a^\omega) - \Phi^\omega(L_a^\omega)), \quad (34)$$

where  $\Phi^\omega(\cdot)$  denotes the cumulative distribution function of  $f^\omega(\mathbf{x})$ ,  $U_a^\omega$  and  $L_a^\omega$  denote the upper and lower bounds of the  $\omega^{\text{th}}$  objective in the rectangular cell  $a$ , respectively. Since the method of Couckuyt et al. (2014) may have overlapping cells, the algorithm can use the  $\pm$  symbol to negate the overlapping contribution of some specific cells.

**Step 2.** Calculate the HV improvement caused by the objective value  $\mathbf{f}(\mathbf{x})$  of the sampled solution to the Pareto frontier  $\mathbb{P}$ .

HV denotes the volume of the region dominated by the Pareto frontier  $\mathbb{P}$ , which is bounded by the reference point  $\mathbf{f}_{\max}$  that is dominated by all the points of  $\mathbb{P}$ . Larger values of HV indicate a better Pareto frontier. The HV improvement of  $\mathbf{f}(\mathbf{x})$  on the Pareto frontier  $\mathbb{P}$  is defined as:

$$\mathbb{H}^{\text{imp}}(\mathbf{f}(\mathbf{x}), \mathbb{P}) = \mathbb{H}(\mathbb{P} \cup \{\mathbf{f}(\mathbf{x})\}) - \mathbb{H}(\mathbb{P}), \quad (35)$$

where  $\mathbb{H}(\cdot)$  denotes the HV indicator.  $\mathbb{H}^{\text{imp}}(\cdot)$  can be defined in terms of a non-negative scalar improvement function:

$$\mathbb{I}(\mathbf{f}(\mathbf{x}), \mathbb{P}) = \begin{cases} \mathbb{H}^{\text{imp}}(\mathbf{f}(\mathbf{x}), \mathbb{P}), & \text{if } \mathbf{f}(\mathbf{x}) \text{ is not dominated by } \mathbb{P} \\ 0, & \text{otherwise} \end{cases}. \quad (36)$$

**Step 3.** Create the HVPoI-based acquisition function.

To reduce the computational complexity, the HVPoI-based acquisition function can be expressed as:

$$P_{\text{HV}}(\mathbf{x}) = \mathbb{I}(\boldsymbol{\mu}(\mathbf{x}), \mathbb{P}) \cdot P(\mathbf{x}), \quad (37)$$

where  $\boldsymbol{\mu}(\mathbf{x}) = (\mu^1(\mathbf{x}), \dots, \mu^4(\mathbf{x}))$ .  $P_{\text{HV}}(\mathbf{x})$  can be calculated as follows:

$$P_{\text{HV}}(\mathbf{x}) = \left( \sum_{a=1}^b \pm \mathbb{V}(\boldsymbol{\mu}(\mathbf{x}), \mathbf{U}_a, \mathbf{L}_a) \right) \cdot P(\mathbf{x}), \quad (38)$$

$$\text{where } \mathbb{V}(\boldsymbol{\mu}(\mathbf{x}), \mathbf{U}_a, \mathbf{L}_a) = \begin{cases} \prod_{\omega=1}^4 (U_a^\omega - \max(L_a^\omega, \mu^\omega(\mathbf{x}))), & \text{if } U_a^\omega > \mu^\omega(\mathbf{x}) \text{ for } \omega=1,2,3,4, \\ 0, & \text{otherwise} \end{cases}, \mathbf{U}_a \text{ and}$$

$\mathbf{L}_a$  denote the sets of upper and lower bounds of the rectangular cell  $a$ , respectively.

## 5 Numerical experiments

In this section, we first validate the performance of the agent-based simulation model using real-world data. Then, the impact of each decision variable on different objective functions is investigated. After that, we present a case study to obtain the Pareto optimal combined regulatory strategy based on the proposed solution framework. Finally, we discuss the difference of optimizing regulatory strategies in a single-objective manner and examine the effects of ignoring passenger impatience.

The computations in this section were performed on a laptop equipped with an Intel Core Ultra 7 1.40 GHz CPU and 32 GB of RAM, and the simulation was coded based on Python. The details of the three main loops used in the following experiments are described in Appendix B.

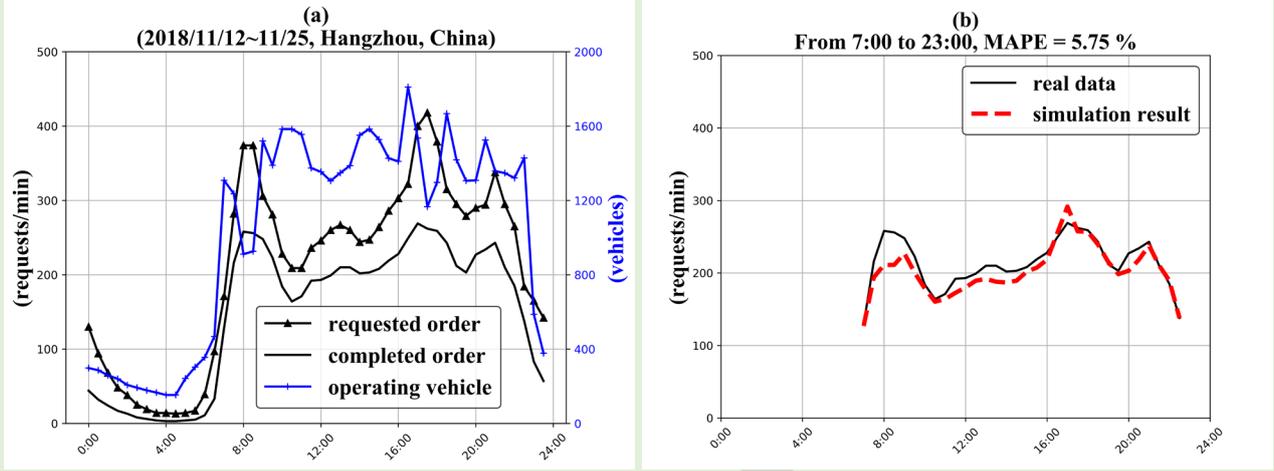
### 5.1 Model validation

To validate the agent-based simulation model, we use the open dataset provided by DiDi, one of the largest TNCs in China. The dataset contains the number of requested orders, completed orders, and operating vehicles in a specific area of Hangzhou City every half-hour for two weeks in November 2018 (Fig. 7(a)). However, since this dataset lacks trip information for each order, we select the number of orders completed between 7:00 to 23:00 to be the indicator for validating the performance of our simulation, as this period is considered to be the main operating hours of hailing services. The length  $T$  of each time interval is set to be 30 (min), each minute indicates one time stamp in the simulation. Meanwhile, the passengers in the model are considered to be homogeneous in the maximum waiting time  $W_{\max}$ , the time cost coefficient  $\beta_{\text{time}}^{\text{pas}}$ , the sunk time cost coefficient  $\beta_{\text{sunk}}^{\text{pas}}$ , and the psychological cost  $H$ .

The pricing and wage parameters in the model are set based on the market pricing in Hangzhou. In 2018, the flag-down fee for Hangzhou taxis was 11 (¥/3km), which was about 3.6 (¥/km), and the taxi kilometer fee was 2.5 (¥/km)<sup>1</sup>. For the ridesourcing services, the flag-down fee for DiDi Express

<sup>1</sup> [https://www.hangzhou.gov.cn/art/2019/10/30/art\\_1229063385\\_1721172.html](https://www.hangzhou.gov.cn/art/2019/10/30/art_1229063385_1721172.html)

1 was 8 (¥/2.5km), which was about 3.2 (¥/km), and the ridesourcing kilometer fee was about 1.7  
 2 (¥/km)<sup>2</sup>. The average commission rate charged by DiDi to drivers was 19%, and an average of 7% of  
 3 incentives were returned to drivers<sup>3</sup> in the 4th quarter of 2018. In the model, we approximate the fare  
 4 rate of taxis  $\alpha^{\text{taxi}} = 3.0$  (¥/km) and the fare rate of RSVs  $\alpha^{\text{RSV}} = 2.5$  (¥/km), and we round up to a 90%  
 5 wage rate  $\tau^{\text{RSV}}$  for RSV drivers.



6  
 7 **Fig. 7.** (a) Average number of requested orders, completed orders, and operating vehicles at different  
 8 day periods. (b) Comparison between the simulation results and the real data.

9 Due to privacy protection, geographic information is not provided in the DiDi dataset, so we  
 10 estimate the scale of the road network  $M$  based on the number of RSVs. The maximum number of  
 11 operating RSVs in the DiDi dataset between 7:00 to 23:00 is 1800, and the average number is 1400.  
 12 In November 2018, there were about 25500 registered RSVs in Hangzhou<sup>4</sup>. Meanwhile, the central  
 13 urban area of Hangzhou City is 1031 (km<sup>2</sup>)<sup>5</sup>. Then, based on the maximum number of RSVs in the  
 14 dataset, the area of the study region is estimated to be 72.7 (km<sup>2</sup>), which is proportionally computed  
 15 via  $1800 \times 1031 / 25500 \approx 72.7$ . Accordingly, we obtained the side length of the study region as 8.5 (km)  
 16 by taking the square root of 72.7. Let the length of each grid in the simulation be 0.5 (km), then a  
 17  $17 \times 17$  grid-type road network is employed to simulate the study region, i.e.,  $M = 17$ . Furthermore,  
 18 there were 11300 taxis in the central urban area of Hangzhou in 2018<sup>6</sup>. We proportionally compute the  
 19 number of taxis in the study region via  $1800 \times 11300 / 25500 \approx 814$ . Other parameter settings and  
 20 corresponding sources/references are provided in Appendix C. Moreover, we define a benchmark case  
 21  $\phi_0$  based on the above market scenario, in which  $Z^{\text{RSV}} = 1400$  (veh),  $\alpha^{\text{taxi}} = 3.0$  (¥/km),  $\alpha^{\text{RSV}} = 2.5$   
 22 (¥/km), and  $\tau^{\text{RSV}} = 90\%$ .

23 Based on the proceeding settings, we run the simulation using Algorithm B.2 and obtain the  
 24 number of completed orders between 7:00 to 23:00. For each run, the average number of requested

<sup>2</sup> <https://www.263th.com/shouqi/126708.html>

<sup>3</sup> [https://www.sohu.com/a/309891044\\_250147](https://www.sohu.com/a/309891044_250147)

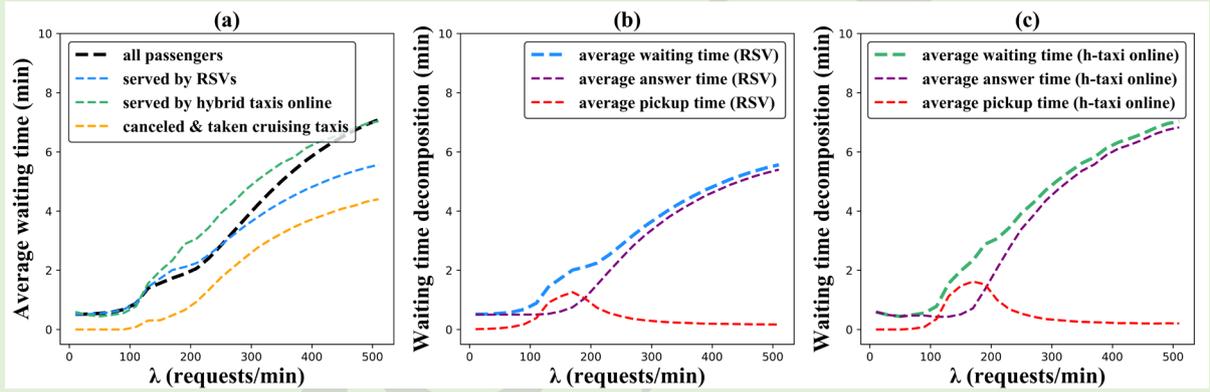
<sup>4</sup> [https://hznews.hangzhou.com.cn/chengshi/content/2018-08/30/content\\_7059606.htm](https://hznews.hangzhou.com.cn/chengshi/content/2018-08/30/content_7059606.htm)

<sup>5</sup> [http://ghzy.hangzhou.gov.cn/art/2020/1/9/art\\_1228962782\\_41563990.html](http://ghzy.hangzhou.gov.cn/art/2020/1/9/art_1228962782_41563990.html)

<sup>6</sup> <http://hangzhouds.org.cn/HangzhouBook/info.aspx?itemid=1197&page=1>

orders and operating vehicles in the DiDi dataset are respectively converted to the hailing demand rate  $\hat{\lambda}$  and the number of RSVs  $\hat{Z}^{\text{RSV}}$  as the input for Algorithm B.2. Refer to Wei et al. (2022), the Mean Absolute Percentage Error (MAPE) is adopted to evaluate the performance of the simulation. As illustrated in Fig. 7(b), the MAPE between the simulation result and real data is 5.75%, which shows a satisfactory performance. However, there is a significant difference during the morning peak period. A possible reason is that in 2018, most RSV drivers were part-time and had their own family commuting needs (Qi and Li, 2020), causing the number of operating RSVs from the DiDi dataset to be smaller in the morning peak than in the afternoon.

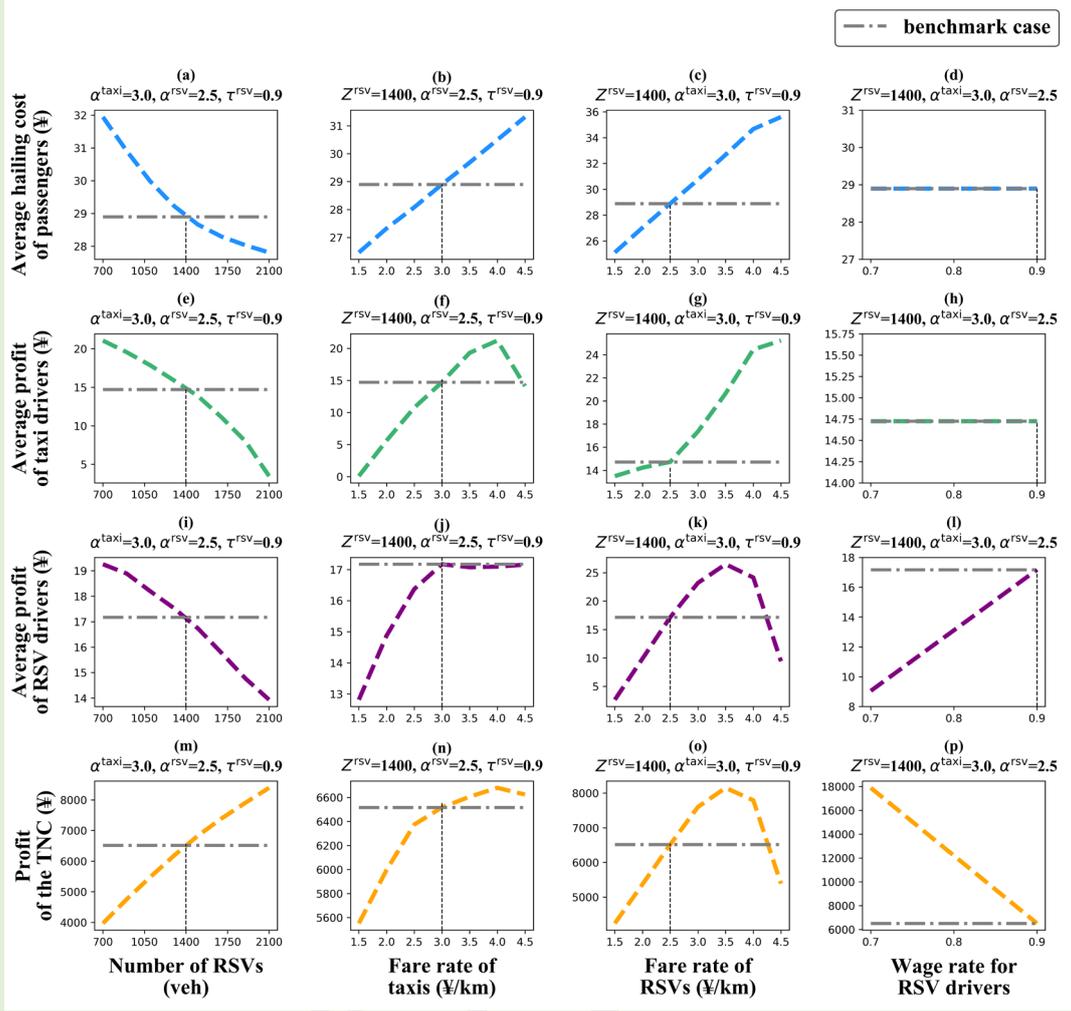
Furthermore, we also examine an important indicator that has received much attention in the literature, i.e., the average waiting time of passengers. Let the hailing demand rate  $\lambda$  varies between 0 and 500 (requests/min), we run Algorithm B.2 under the benchmark market case  $\Phi_0$ . Fig. 8(a) shows the average waiting times of all passengers and passengers served by RSVs, hybrid taxis online, and cruising taxis under different hailing demand rates. Note that passengers served by cruising taxis include both those served by street taxis and those served by hybrid taxis while cruising. As the hailing demand rate  $\lambda$  increases, all kinds of average waiting times show an overall increasing trend.



**Fig. 8.** (a) Average waiting times of passengers served by different carriers. (b) Waiting time decomposition of RSV passengers. (c) Waiting time decomposition of hybrid taxi passengers.

Notably, after decomposing the average waiting times of RSV and online taxi passengers into the answer time and the pick-up time (Fig. 7(b) and (c)), it is found that the average pick-up time shows a significant non-monotonicity. Since the speed of vehicles is set to be fixed, that implies the average distance between passengers and their matched vehicles is similarly non-monotonic. An explanation for this phenomenon is that as  $\lambda$  increases at first, the number of available vehicles in the system decreases, and the average distance between passengers and their matched vehicles gradually increases. When  $\lambda$  reaches a certain level, it becomes difficult to match newly arriving passengers to available vehicles directly, and the average answer time of passengers begins to increase. Further, as the passenger density in the network keeps increasing, the distance to the nearest passenger decreases when a vehicle becomes available, which leads to a non-monotonic pick-up time. The significant non-monotonicity in the average pick-up time is also reached by Castillo et al. (2017) and Feng et al. (2021), which further supports the validity of the model presented in this study.

## 1 5.2 Impact of regulatory strategies



2  
3 **Fig. 9.** Relationships between decision variables and objective functions.

4 Fig. 9 illustrates the impact of the number of RSVs  $Z^{\text{RSV}}$ , the fare rate of taxis  $\alpha^{\text{taxi}}$ ,  
5 RSVs  $\alpha^{\text{RSV}}$ , and the wage rate for RSV drivers  $\tau^{\text{RSV}}$  on the objective functions of different stakeholders.  
6 Each subfigure is examined by varying a single decision variable while keeping the others remain  
7 benchmark setting, and the results are computed using Algorithm B.3. From Fig. 9, it is evident that  
8 an increase or decrease in any of the decision variables does not benefit passengers, taxi drivers, RSV  
9 drivers, and the TNC simultaneously. Taking the regulation of the RSV number as an example, when  
10 the number of RSVs decreases, the average profits of both taxi and RSV drivers increase (Fig. 9(e)  
11 and (i)), but both passengers and the TNC experience negative effects (Fig. 9(a) and (m)). Conversely,  
12 an increase in the number of RSVs benefits both passengers and the TNC, but it results in a decrease  
13 in the average profits of both taxi and RSV drivers (Fig. 9(e) and (i)), which reflects the fact that  
14 unregulated growth in the number of RSVs leads to a loss of profit for both taxis and RSV drivers.

15 Notably, the average profit of taxi drivers does not increase monotonically with the fare rate of  
16 taxis (Fig. 9(f), which is the same for RSV drivers and RSV fare rate (Fig. 9 (k)). The reasons are

twofold. On the one hand, passengers can choose their hailing type with a lower fare rate. On the other hand, the hailing demand may shift to public transit due to higher hailing costs (Fig. 9(b) and (c)). Furthermore, an increase in lower taxi fare rates could make ridesourcing services more competitive and would increase profits for RSV drivers and the TNC. Nevertheless, RSV drivers and the TNC may also lose profits when taxi fare rate is overcharged (Fig. 9(j) and (n)), as hailing demand would be higher. Similarly, increasing the fare rate of RSVs can increase TNC's profit to an upper bound, but overpricing may lead to passenger losses, resulting in a decrease in TNC's profit (Fig. 9(o)). It should be noted that we did not model the labor supply of drivers, so the wage rate for RSV drivers only affects the profits of RSV drivers and the TNC.

Additionally, as the number of taxis and the wage rate for hybrid taxis may influence the market performance, we present a sensitivity analysis in Appendix D to examine the impact of these two key exogenous variables on different objectives.

### 5.3 Pareto optimal combined regulatory strategy

This section will validate the solution framework presented in Section 4.3 and analyze the optimal combined regulatory strategy. Based on the setting of the benchmark case  $\phi_0 = [1400, 3.0, 2.5, 90\%]$ , we further set the solution space  $\Omega$  as follows:

$$\Omega = \begin{cases} 700 \leq Z^{\text{RSV}} \leq 2100 \\ 1.5 \leq \alpha^{\text{taxi}} \leq 4.5 \\ 1.5 \leq \alpha^{\text{RSV}} \leq 4.5 \\ 0.7 \leq \tau^{\text{RSV}} < 1 \end{cases}, \quad (39)$$

where the upper and lower bounds of the domain for each decision variable are determined based on  $\pm 50\%$  expansion of the benchmark value. Specifically, the domain of the RSV fare rate is set to be the same as that for the taxi fare rate. Meanwhile, the Chinese government also requires that the wage rate for RSV drivers cannot be lower than 70%.

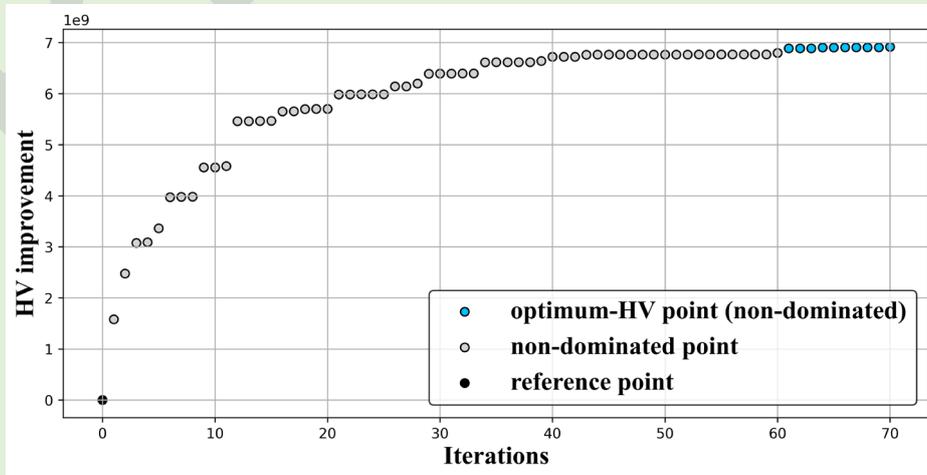
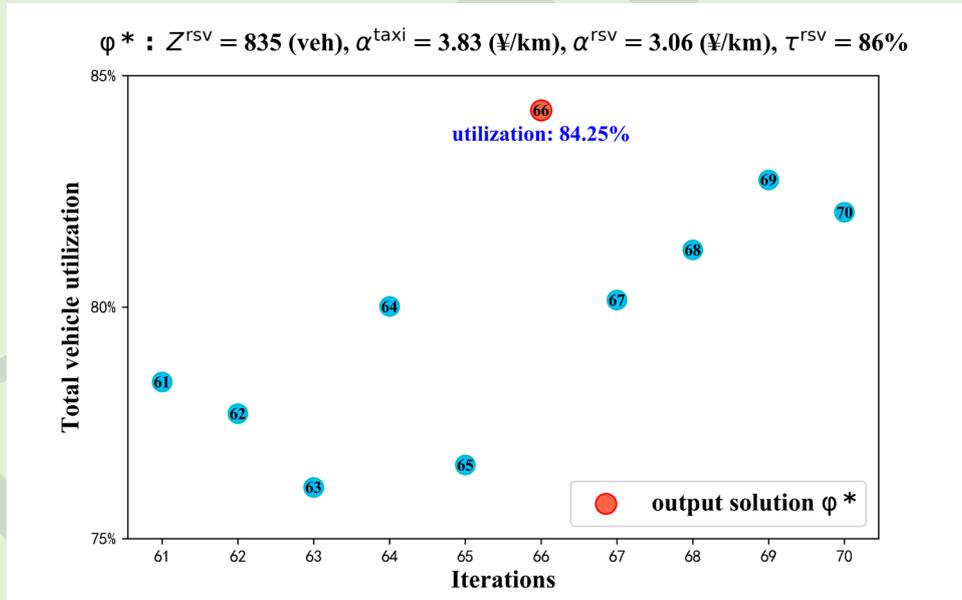


Fig. 10. Changes in the HV improvement over iterations.

1 Using 10 randomly selected points  $\{\phi^1, \dots, \phi^{10}\}$  from  $\Omega$  and their corresponding objective  
 2 values  $\{f(\phi^1), \dots, f(\phi^{10})\}$  as the initial samples of multi-objective Bayesian optimization, we obtained  
 3 the HV improvement of the Pareto frontier over 70 iterations in Fig. 10, where objective values are  
 4 computed using Algorithm B.3 during each iteration.

5 During each iteration of multi-objective Bayesian optimization, the acquisition function chooses  
 6 a new sampling solution within  $\Omega$ . In the first 21 iterations, the HV improvement value increases  
 7 rapidly from 0 to nearly  $6 \times 10^9$ . This increase accounts for more than 85% of the global improvement.  
 8 After the 60<sup>th</sup> iteration, updating the Pareto frontier no longer significantly increases the HV  
 9 improvement value, and the Pareto frontier tends to be stabilized. It should be noted that the points  
 10 acquired by the multi-objective Bayesian optimization within 70 iterations are all non-dominated.

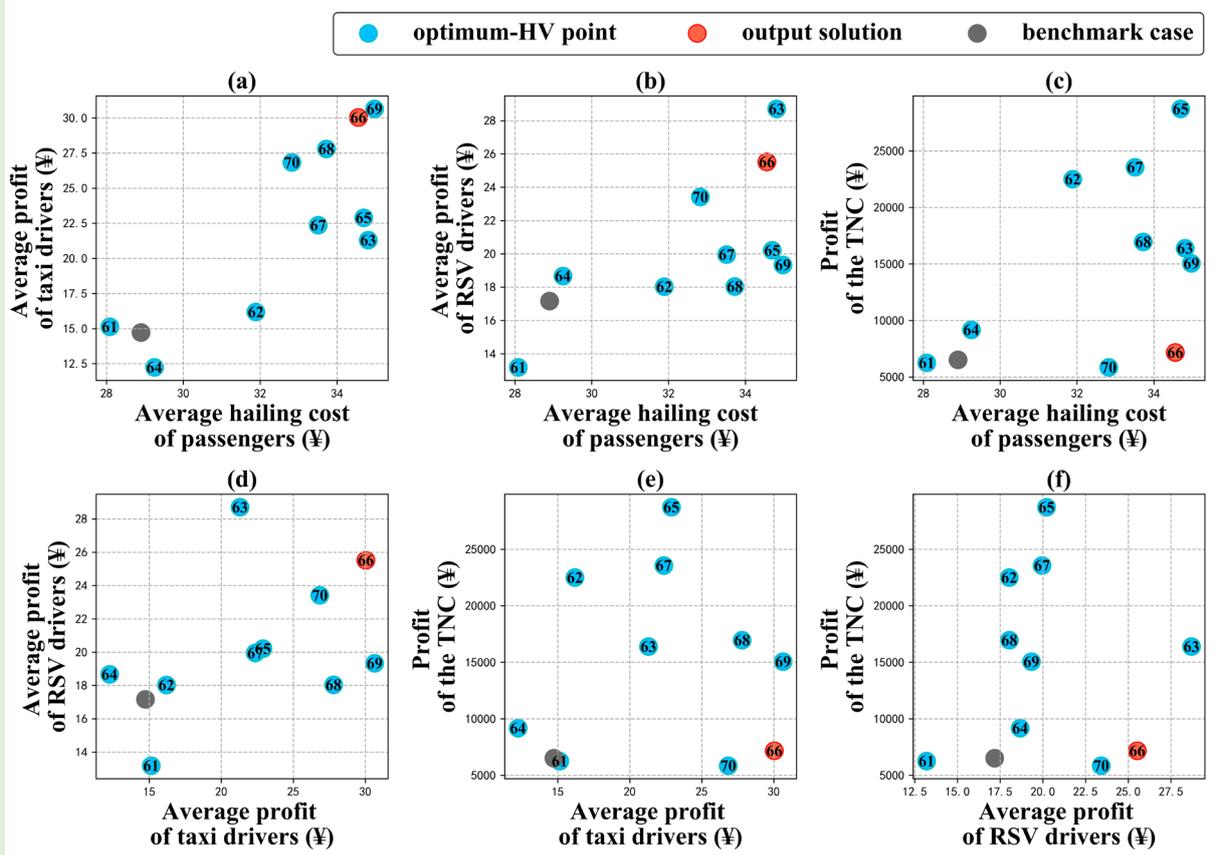
11 The final output solution is selected according to the principle of maximum total vehicle  
 12 utilization among the Pareto frontier, which is from the 66<sup>th</sup> iteration. Meanwhile, the last 10 solutions  
 13 with the highest HV improvement values on the Pareto frontier are marked in blue for further analysis  
 14 alongside the output solution. As illustrated in Fig. 11, the output solution  $\phi^*$  contains 835 RSVs, with  
 15 a taxi fare rate of 3.83 (¥/km), an RSV fare rate of 3.06 (¥/km), and a TNC wage rate for RSV drivers  
 16 of 86%. This solution results in a total vehicle utilization rate of 84.25%.



17  
 18 **Fig. 11.** Selection of the output solution based on maximizing total vehicle utilization.

19 Fig. 12 illustrates the distribution of objective values for these optimum-HV points and the  
 20 benchmark case. In the output solution, fewer RSVs and higher fare rates for both hailing types reduce  
 21 competition and increase incomes, making RSV and taxi drivers the most profitable stakeholders.  
 22 Although the TNC can pay RSV drivers a lower wage rate and charge passengers a higher fare rate,  
 23 the reduced number of RSVs only marginally increases its profit relative to the benchmark, while  
 24 passengers incur higher hailing costs. From the Pareto perspective, shifting more hailing costs to

1 passengers appears to be unavoidable for improving market performance. Among the 10 selected  
 2 optimum-HV points, only the 61<sup>st</sup> iteration resulted in a lower hailing cost than the benchmark case;  
 3 however, both RSV drivers and the TNC lose profits, and taxi drivers' profits do not have a significant  
 4 improvement. Note that in the Pareto frontier obtained from Fig. 10, the average passengers' hailing  
 5 cost is 32.5 (¥), which is 12.5% (via  $32.5/28.9 - 1$ ) more than the benchmark level.



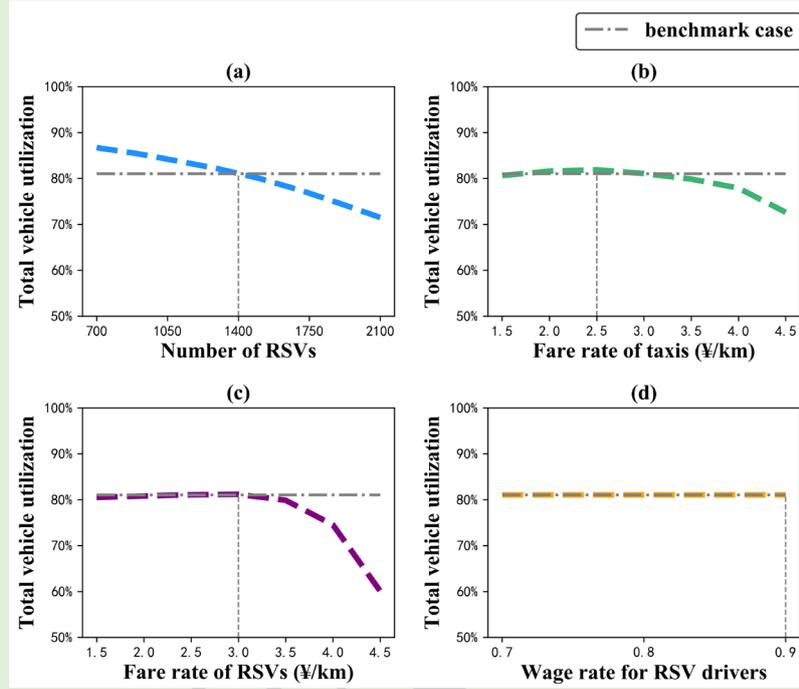
7 **Fig. 12.** The values of objective functions correspond to optimum-HV points, the output  
 8 solution, and the benchmark case.

9 **Table 3**

10 Performance comparison of different combined regulatory strategies.

Solution type	Decision variable				Objective function			Total vehicle utilization	
	$Z^{\text{RSV}}$	$\alpha^{\text{taxi}}$	$\alpha^{\text{RSV}}$	$\tau^{\text{RSV}}$	$-\bar{C}$	$Q^{\text{taxi}}$	$Q^{\text{RSV}}$		$Q^{\text{TNC}}$
Benchmark solution $\phi_0$	1400	3.0	2.5	0.9	-28.9	14.7	17.2	6516	81.05%
Random solution 1	1868	2.78	2.15	0.99	-26.3	6.67	13.2	1274	75.74%
Random solution 2	1207	2.01	1.58	0.84	-24.7	4.0	2.7	5681	84.01%
<b>Pareto optimal output solution <math>\phi^*</math></b>	<b>835</b>	<b>3.83</b>	<b>3.06</b>	<b>0.86</b>	<b>-34.6</b>	<b>30.0</b>	<b>25.5</b>	<b>7172</b>	<b>84.25%</b>

1 We select the benchmark solution and two randomly selected solutions to compare with the output  
 2 solution (Table 3). We can see that the Pareto optimal output solution demonstrates significant  
 3 advantages over the benchmark and random solutions, delivering enhanced welfare for taxi drivers,  
 4 RSV drivers, and the TNC, alongside increased total vehicle utilization, while passengers are required  
 5 to bear more hailing costs. Although the output solution cannot dominate all the objectives, the profits  
 6 of taxi drivers, RSV drivers, and the TNC improved by 104.1%, 48.3%, and 10.1% compared to the  
 7 benchmark, respectively, with 19.7% of the cost increase for passengers.



8  
 9 **Fig. 13.** Impact of four regulatory strategies on total vehicle utilization.

10 To figure out the relationship between the output solution and the total vehicle utilization, Fig. 13  
 11 illustrates the impact of the number of RSVs, the fare rates of taxis and RSVs, and the wage rate for  
 12 RSV drivers on total vehicle utilization. Each subfigure is examined using Algorithm B.3 by varying  
 13 a single decision variable while keeping the others fixed at the benchmark setting. It's clear that the  
 14 number of RSVs results in an overall negative impact on total vehicle utilization, and higher fare rates  
 15 would decrease utilization, while the impact of the RSV wage rate is found to be insignificant.  
 16 Accordingly, if the output solution is selected at the Pareto frontier based on the principle of maximum  
 17 total vehicle utilization, it's very likely to result in solutions with fewer RSVs and less expensive fare  
 18 rates. However, a lower number of RSVs will negatively impact passengers and the TNC, while lower  
 19 taxi and RSV fare rates will negatively impact the profits of taxi drivers, RSV drivers, and the TNC  
 20 (Fig. 9 (f), (g), (j), (k), (n), (o)).

21 Besides, the government can select the appropriate solution on the Pareto frontier according to  
 22 the market situation. Table 4 displays the benchmark case and four solutions in the set of non-  
 23 dominated points that are most favorable to passengers, taxi drivers, RSV drivers, and the TNC,  
 24 respectively. Obviously, every stakeholder could benefit compared to the benchmark case under

1 corresponding favorable regulation. If the government favors passengers, more RSVs and lower fare  
2 rates are needed. If the government favors taxi drivers, fewer RSVs and higher taxi fare rates are  
3 required. If the government favors RSV drivers, higher RSV fares and wage rates are needed. If the  
4 government favors the TNC, it requires more RSVs, higher fare rates, and pays RSV drivers the lowest  
5 wage rate. However, when the government prioritizes the passengers' welfare, both taxi and RSV  
6 drivers will lose profits, and the TNC's profit and the vehicle utilization are slightly lower than the  
7 benchmark level. Meanwhile, under a TNC-favored strategy, passengers bear higher hailing costs, yet  
8 neither taxi nor RSV drivers achieve significant profit gains, and the transportation system becomes  
9 inefficient, with total vehicle utilization approximately 10% lower than the benchmark (81.05% vs.  
10 71.68%). Thus, prioritizing passenger welfare may not lead to driver-friendly regulation, whereas  
11 prioritizing the TNC's profit could be the worst option for government regulation, as it not only harms  
12 passengers but also substantially reduces total vehicle utilization.

13 **Table 4**

14 Pareto optimal results for different favorable stakeholders.

Beneficiary	Decision variable				Objective function				Total vehicle utilization
	$Z^{\text{rsv}}$	$\alpha^{\text{taxi}}$	$\alpha^{\text{rsv}}$	$\tau^{\text{rsv}}$	$-\bar{C}$	$Q^{\text{taxi}}$	$Q^{\text{rsv}}$	$Q^{\text{TNC}}$	
None ( $\varphi_0$ )	1400	3.0	2.5	0.9	-28.9	14.7	17.2	6516	81.05%
Passenger	1609	2.79	2.19	0.86	<b>-26.9</b>	10.1	10.7	6259	80.02%
Taxi	813	4.01	3.10	0.80	-35.3	<b>31.9</b>	22.9	9720	83.60%
RSV	1295	3.89	3.67	0.95	-35.0	26.8	<b>37.2</b>	4924	80.93%
TNC	1921	3.66	3.89	0.70	-34.7	15.4	17.7	<b>31492</b>	71.68%

## 15 5.4 Discussions

### 16 5.4.1 Optimizing the combined regulatory strategy from a single-objective perspective

17 In comparison to the prevailing literature that examined the regulation of the ridesourcing market based  
18 on a single objective, i.e., social welfare, this section establishes a single-objective function of social  
19 welfare and analyzes the corresponding optimal combined regulatory strategy. The social welfare of  
20 CRTM in a modeling time interval  $T$  is formulated as:

$$21 \quad SW(\varphi) = -w^{\text{pas}} \sum_{i=1}^{N(T, \lambda^*(\varphi))} C_i + w^{\text{taxi}} Q^{\text{taxi}} Z^{\text{taxi}} + w^{\text{rsv}} Q^{\text{rsv}} Z^{\text{rsv}} + w^{\text{TNC}} Q^{\text{TNC}}, \quad (40)$$

22 where  $SW(\varphi)$  is a function of  $\varphi$ , note that its value could be negative since we use the average hailing  
23 cost to represent the welfare of passengers;  $w^s$  is the weight assigned to each stakeholder,  
24  $s \in \{\text{pas, taxi, rsv, TNC}\}$ ,  $\sum w^s = 1$ .

25 Based on the solution framework presented in Section 4.3, we calculate  $SW(\varphi)$  using Algorithm  
26 B.3 in each iteration. The Expected Improvement (Jones et al., 1998; Mockus, 1998) is adopted as the  
27 acquisition function for single-objective Bayesian optimization. Table 5 shows the optimization results

1 under different government regulatory strategies with a certain prioritization, where we set  $w^s=0.7$  to  
2 indicate a favored weight for a group  $s \in \{\text{pas}, \text{taxi}, \text{rsv}, \text{TNC}\}$ .

3 **Table 5**

4 Optimal results (using social welfare) for different government regulatory focuses.

Beneficiary and weight $\mathbf{w}$	Decision variable				Objective function					Total vehicle utilization
	$Z^{\text{rsv}}$	$\alpha^{\text{taxi}}$	$\alpha^{\text{rsv}}$	$\tau^{\text{rsv}}$	$SW(\boldsymbol{\varphi})$	$-\bar{C}$	$Q^{\text{taxi}}$	$Q^{\text{rsv}}$	$Q^{\text{TNC}}$	
Benchmark $\boldsymbol{\varphi}_0$	1400	3.0	2.5	0.9	/	-28.9	14.7	17.2	6516	81.05%
Evenhanded [0.25] * 4	820	4.5	4.5	0.75	-28658	-39.9	43.2	36.4	16574	84.97%
Passenger [0.7, 0.1, 0.1, 0.1]	1424	4.5	1.5	1.0	-95528	<b>-26.7</b>	4.8	5.0	769	69.50%
Taxi [0.1, 0.7, 0.1, 0.1]	700	4.5	4.5	0.7	10135	-40.1	<b>44.4</b>	33.1	17329	85.93%
RSV [0.1, 0.1, 0.7, 0.1]	2100	4.5	4.42	1.0	43245	-38.0	5.1	<b>45.6</b>	719	67.11%
TNC [0.1, 0.1, 0.1, 0.7]	2100	4.5	4.5	0.7	10600	-38.2	13.2	25.0	<b>41283</b>	67.65%

5 Note  $\mathbf{w} = [w^{\text{pas}}, w^{\text{taxi}}, w^{\text{rsv}}, w^{\text{TNC}}]$ .

6 First, the results obtained by single-objective optimization have some similarities with those  
7 obtained by multi-objective optimization. If the government doesn't focus on a specific stakeholder  
8 (i.e., the Evenhanded solution in Table 5 and the Pareto output solution  $\boldsymbol{\varphi}^*$  in Table 3), both solutions  
9 have fewer RSVs, higher fare rates, and lower RSV wage rates, as well as high vehicle utilizations.  
10 Meanwhile, the passenger-favored regulations may lead to a harmful market for both drivers and the  
11 TNC ( $Q^{\text{taxi}} = 4.8$  and  $Q^{\text{rsv}} = 5.0$  in Table 5), which is the same in multi-objective optimization.  
12 Moreover, both the TNC-favored regulations could not significantly improve drivers' profits and could  
13 lead to higher hailing costs for passengers (-34.7 in Table 4 and -38.2 in Table 5).

14 In this study, if the government prefers to regulate CRTM by maximizing social welfare, the RSV-  
15 favored solution is the best choice, which has the maximum  $SW(\boldsymbol{\varphi})$  and a 165% (via  $45.6/17.2 - 1$ )  
16 improvement in the average profit of RSV drivers compared to the benchmark case. However, this  
17 regulation is impractical, as the profits of both taxi drivers and the TNC are very low, and the total  
18 vehicle utilization is 13.9% (via  $81.05\% - 67.11\%$ ) lower than the benchmark level.

19 Additionally, since most solutions obtained in Table 5 are bound by the solution space  $\Omega$ , an  
20 ensuing auxiliary experiment is to examine the single-objective optimization results under a larger  
21 solution space  $\Omega'$ , which is specified in Eq. (41). In this experiment, the objective weight  $w^s$  of each  
22 favored group  $s$  is also set to be 0.7. From the results presented in Table 6, it can be found that the  
23 optimal fare rates of RSV and taxi services increase except for the passenger-favored solution, since  
24 lower fare rates and more RSVs help reduce passengers' time and fare costs. Besides, the results show  
25 worse vehicle utilizations except for the taxi-favored solution, which is reasonable because this  
26 solution would lead to a minimum RSV cap to enhance the competitiveness of taxis. Based on Fig.  
27 13(a), fewer RSVs generate higher vehicle utilization. Moreover, all the solutions are impractical

1 because some drivers would suffer losses from working. Specifically, taxi drivers would lose 18 ¥ in  
 2 30 minutes under the Evenhanded solution in Table 6. This could suggest that when regulating CRTM  
 3 by a single objective of maximizing social welfare, the taxi industry may be removed from the market  
 4 without special attention. Yu et al. (2020) also found that if the government did not place more weight  
 5 on taxi drivers, it would be hard for them to survive in the market.

$$\Omega' = \begin{cases} 100 \leq Z^{\text{RSV}} \leq 3000 \\ 0.1 \leq \alpha^{\text{taxi}} \leq 10.0 \\ 0.1 \leq \alpha^{\text{RSV}} \leq 10.0 \\ 0.1 \leq \tau^{\text{RSV}} < 1 \end{cases} \quad (41)$$

7 **Table 6**

8 Optimal results of single-objective optimization with the larger solution space  $\Omega'$ .

Beneficiary	Decision variable				Objective function					Total vehicle utilization
	$Z^{\text{RSV}}$	$\alpha^{\text{taxi}}$	$\alpha^{\text{RSV}}$	$\tau^{\text{RSV}}$	$SW(\varphi)$	$-\bar{C}$	$Q^{\text{taxi}}$	$Q^{\text{RSV}}$	$Q^{\text{TNC}}$	
Evenhanded	1216	9.2	8.9	0.54	-23404	-64	-18	57	78543	55.21%
Passenger	2430	4.6	0.1	0.1	-67207	<b>-14</b>	-18	-19	3231	59.77%
Taxi	100	9.0	9.5	0.84	49433	-58	<b>120</b>	-17	3042	80.30%
RSV	2221	9.2	8.7	1.0	107821	-61	-22	<b>98</b>	10.9	54.91%
TNC	3000	10	6.8	0.1	104313	-50	-22	-11	<b>197625</b>	49.36%

#### 9 5.4.2 Implications of overlooking passenger patience

10 Passengers' impatient behavior is a key factor influencing market performance and, consequently, the  
 11 design of government regulation in the CRTM. In this subsection, we consider a hypothetical market  
 12 with patient passengers, those who neither abandon nor cancel orders, and whose hailing-type choices  
 13 are unaffected by sunk costs. With the same solution framework presented in Section 4.3, we obtain  
 14 Pareto optimal solutions in Table 7 and compare the results considering passenger patience.

15 In such a patient market, passengers would not abandon requests due to long waiting times or  
 16 cancel RSV orders upon encountering a vacant taxi. Compared with the impatient market, the  
 17 government could set a lower RSV fleet cap to reduce drivers' competition and impose a higher  
 18 government-guided RSV fare rate to benefit RSV drivers and the TNC. However, because taxis cannot  
 19 'steal' passengers already matched with RSVs, their profitability declines. To maintain taxi drivers'  
 20 profits, the government would need to lower taxi fares to attract more hailing passengers. Furthermore,  
 21 in the last row of Table 7, we show the values of four objective functions when implementing the  
 22 patient regulatory strategies in the impatient market. It is found that only minor changes appear in the  
 23 vehicle utilization and the welfare of passengers, RSV drivers, and the TNC, while taxi drivers lose  
 24 23.3% of profits (via  $1 - 23.1/30.0$ ). We conclude that regulating the CRTM without accounting for  
 25 passenger impatience may lead to underestimating taxi driver profitability and setting fares too low,  
 26 thereby causing drivers to forgo potential profits.

1 **Table 7**

2 Pareto optimal solutions of impatient and patient passengers.

Market type	Decision variable				Objective function				Total vehicle utilization
	$Z^{RSV}$	$\alpha^{taxi}$	$\alpha^{RSV}$	$\tau^{RSV}$	$-\bar{C}$	$Q^{taxi}$	$Q^{RSV}$	$Q^{TNC}$	
Impatient	835	3.83	3.06	0.86	-34.6	30.0	25.5	7172	84.25%
Patient	795	2.94	3.63	0.85	-33.8	21.2	31.0	7532	85.16%
Implement patient regulation in the impatient market					-34.4	23.1	28.7	7290	85.15%

3 **6 Conclusion**

4 Ridesourcing has improved travel services and efficiency for passengers, but the large influx of RSV  
5 drivers and the irrational operation of TNCs in recent years have posed great challenges to the  
6 government's regulatory work. This paper presents a multi-objective bi-level programming model to  
7 help policymakers find a Pareto optimal combined regulatory strategy for CRTM, including RSV fleet  
8 cap, taxi and RSV fare rate control, and TNC wage rate floor. The upper-level problem is to determine  
9 the combination of regulatory strategies with the objectives of minimizing the average hailing cost of  
10 passengers and maximizing the average profit of taxi drivers, the average profit of RSV drivers, and  
11 the profit of the TNC. The lower level aims to reflect the steady-state market performance under  
12 different regulations, where an agent-based simulation is developed to examine the impact of different  
13 regulatory strategies. The simulation model not only captures the travel mode choice and hailing type  
14 choice behaviors of passengers but also the work mode choice of taxi drivers between online matching  
15 and street cruising. Moreover, the abandonment and different cancellation behaviors of impatient  
16 passengers before and after order matching are considered. To solve the bi-level model, we developed  
17 a solution framework based on multi-objective Bayesian optimization, which can capture the complex  
18 nonlinear relationships in CRTM and substantially decrease calls to the lower-level simulation. During  
19 each iteration, the lower-level problem is solved as a fixed-point problem via iterating the agent-based  
20 simulation to obtain stabilized hailing demand and market supply. After validating the simulation  
21 model with a real-world dataset, experiments are conducted to illustrate the impact of the different  
22 regulatory strategies and explore the Pareto optimal solution for the government.

23 The main findings of this study can be summarized as follows:

- 24 (1) If the government regulates CRTM without considering the impatience of passengers, it may  
25 underestimate the profitability of taxi drivers and implement a lower taxi fare rate, causing  
26 taxi drivers to lose potential profits.
- 27 (2) No single strategy can simultaneously benefit passengers, taxi drivers, RSV drivers, and the  
28 TNC; excessively high fare rates instead reduce the profitability of both drivers and the TNC.
- 29 (3) When selecting a solution from the Pareto frontier coupled using a secondary criterion of  
30 maximizing total vehicle utilization, the government should set a lower RSV fleet cap than  
31 in the benchmark case, impose higher taxi and government-guided RSV fare rates, and allow  
32 the TNC to pay RSV drivers lower wage rates.

- 
- 1 (4) Increasing passenger hailing costs appears to be an unavoidable trade-off for improving  
2 overall market performance. This increase could reach up to 12.5%.
  - 3 (5) If the government prioritizes passengers in its regulation, both RSV and taxi drivers would  
4 lose profits. Under a TNC-favored regulation, passengers would face higher costs, while total  
5 vehicle utilization may become inefficient.
  - 6 (6) If the government prefers to regulate CRTM in a single-objective manner by maximizing  
7 social welfare, it should lower the RSV fleet cap and increase hailing fare rates. While the  
8 RSV-favored regulation generates the highest social welfare, it is impractical to implement  
9 due to poor overall market performance.

10 Furthermore, this paper identifies several promising directions for future research, which can be  
11 categorized into two main areas. First, regarding the agent-based simulation of hailing services, future  
12 research could explore the impact of allowing drivers to cancel assignments when the pick-up location  
13 is far from their current position. Such cancellations might influence drivers' satisfaction, passengers'  
14 waiting time, and overall market efficiency (Zhang et al., 2023; Xu et al., 2024). Incorporating a more  
15 dynamic decision-making process for drivers in the model could yield deeper insights into the interplay  
16 between driver behaviors and market dynamics. Second, concerning CRTM regulation, the bi-level  
17 model and solution framework developed in this study demonstrate the capability to handle  
18 optimization problems with high-dimensional objective functions and decision variables. This  
19 flexibility provides opportunities to explore more complex government regulatory strategies and  
20 stakeholder interactions. For instance, while this paper focuses on a single TNC, future research could  
21 investigate market dynamics involving multiple competing TNCs and the corresponding regulatory  
22 challenges for governments (Guo et al., 2019; Siddiq and Taylor, 2022). Similarly, addressing the  
23 regulation of passengers who frequently cancel orders or those who simultaneously request services  
24 from multiple platforms warrants further investigation. [If the time-resolved traffic data is available, it  
25 is also promising to investigate a time-dependent fleet cap over an extended modeling horizon.](#)

## Appendix A. The agent-based simulation framework

The following table lists the agents' states, behaviors, properties, and KPIs in the agent-based simulation framework. The states, behaviors, properties, and KPIs mentioned in our framework are not exhaustive but represent the focus of attention in this study.

**Table A.1**

Agent types, states, behaviors, properties, and KPIs

Types	States	Behaviors	Properties	KPIs
<b>Passenger</b>	<ul style="list-style-type: none"> <li>● Waiting to be matched</li> <li>● Abandoned</li> <li>● Canceled before order matching</li> <li>● Matched</li> <li>● Canceled after order matching</li> <li>● Served by an RSV</li> <li>● Served by a hybrid taxi</li> <li>● Served by a cruising taxi</li> <li>● Served by public transit</li> <li>● Left the system (completed hailing/transit trip)</li> </ul>	<ul style="list-style-type: none"> <li>● Travel mode choice (public transit or hailing service)</li> <li>● Hailing type choice (RSV or taxi)</li> <li>● Abandon request</li> <li>● Cancel order (before or after order matching)</li> </ul>	<ul style="list-style-type: none"> <li>● ID</li> <li>● Arrival time</li> <li>● Origin and destination</li> <li>● Maximum waiting time</li> <li>● Time cost coefficient</li> <li>● Sunk cost coefficient</li> <li>● Psychological cost</li> </ul>	<ul style="list-style-type: none"> <li>● Waiting time</li> <li>● Answer time</li> <li>● Pick-up time</li> <li>● Hailing cost</li> </ul>
<b>RSV</b>	<ul style="list-style-type: none"> <li>● Idle</li> <li>● Picking up</li> <li>● In-service</li> </ul>	<ul style="list-style-type: none"> <li>● Driving direction choice</li> </ul>	<ul style="list-style-type: none"> <li>● ID</li> <li>● Current location</li> <li>● Target location</li> <li>● Current travel direction</li> <li>● Time to become available</li> <li>● Time cost coefficient</li> <li>● Fuel cost coefficient</li> <li>● Fixed operating cost</li> </ul>	<ul style="list-style-type: none"> <li>● Idling distance</li> <li>● Pick-up distance</li> <li>● Service distance</li> <li>● Wasted distance</li> <li>● Service volume</li> <li>● Operating profit</li> <li>● Vehicle utilization</li> </ul>
<b>Taxi</b>	<ul style="list-style-type: none"> <li>● Idle</li> <li>● Picking up</li> <li>● In-service</li> </ul>	<ul style="list-style-type: none"> <li>● Driving direction choice</li> <li>● Work mode choice</li> </ul>	<ul style="list-style-type: none"> <li>● ID</li> <li>● Current location</li> <li>● Target location</li> <li>● Current travel direction</li> <li>● Time to become available</li> <li>● Time cost coefficient</li> <li>● Fuel cost coefficient</li> <li>● Fixed operating cost</li> </ul>	<ul style="list-style-type: none"> <li>● Idling distance</li> <li>● Pick-up distance</li> <li>● Service distance</li> <li>● Wasted distance</li> <li>● Online service volume</li> <li>● Cruising service volume</li> <li>● Operating profit</li> <li>● Vehicle utilization</li> </ul>

Note: Vehicle utilization is the ratio of service distance to total distance driven.

---

## Appendix B. Main loops of the simulation

Algorithm B.1 represents the basic agent-based simulation process of CRTM, which simulates the interactions and behaviors of drivers and passengers in the market and would be called multiple times by Algorithm B.2 and B.3. Algorithm B.2 is used in Section 5.1, its task is to stabilize drivers' work mode choices and their time cost coefficients under a given hailing demand rate and output corresponding market performance metrics. Algorithm B.3 represents the lower-level model of the research problem, which outputs market performance metrics with a stabilized supply-demand pattern under a given combined regulatory strategy. It is used in Sections 5.2-5.4.

---

**Algorithm B.1:** Basic simulation loop of CRTM within one time interval  $T$ .

---

**Input:** Combined regulatory strategy  $\phi$ , hailing demand  $\lambda$ , average profit of hybrid taxis  $Q^{\text{h-taxi}}$  and street taxis  $Q^{\text{s-taxi}}$ , time cost coefficients of RSVs  $\beta^{\text{rsv}}$  and hybrid taxis  $\beta^{\text{h-taxi}}$

**Output:** Market performance metrics

```
1 Set warm-up time  $T_0 = 10\% \times T$ , time stamp  $ts = 1$ 
2 Generate passengers, RSVs, taxis, and initialize simulation settings
3 while time stamp  $ts \leq T + T_0$  do
4     Update vehicles' locations and travel directions
5     if number of unmatched passengers  $> 0$  & number of available hailing vehicles  $> 0$  then
6         Match passengers with their preferred hailing vehicles based on the NN algorithm
7     end if
8     for passenger  $i$  who has arrived at  $t_i$  but hasn't been picked up do
9         if passenger  $i$  hasn't been matched then
10             if  $ts - t_i > W_{\max}$  then
11                 Passenger  $i$  abandons the online request before order matching
12             else if  $ts - t_i \leq W_{\max}$  &  $u_i(ts - t_i) \geq \max\{\alpha^{\text{taxi}}, \alpha^{\text{rsv}}\}$  then
13                 Passenger  $i$  requests for both hailing types
14             end if
15             if the number of available hailing vehicles  $> 0$  then
16                 Passenger  $i$  is matched
17             else if no available hailing vehicles & encountering a vacant taxi then
18                 Passenger  $i$  cancels before order matching
19             else
20                 Passenger  $i$  is waiting to be matched
21             end if
22         else if passenger  $i$  has been matched but hasn't been picked up then
23             if  $W_i^{\text{pick}} \leq ts - t_i$  then
24                 Passenger  $i$  is picked up and served by an RSV or a hybrid taxi
25             else if  $W_i^{\text{pick}} > ts - t_i$  & encountering a vacant taxi then
26                 if  $C_i^1 \leq C_i^2$  then
27                     Passenger  $i$  will keep waiting for the matched vehicle
28                 else
29                     Passenger  $i$  cancels after order matching
30             end if
```

---

---

```

31         else
32             Passenger  $i$  is waiting to be picked up
33         end if
34     end if
35 end for
36 if  $ts > T_0$  then
37     Count and calculate market performance metrics
38 end if
39 end

```

---

**Algorithm B.2:** Simulation loop for stabilizing drivers' work mode split and time cost coefficients.

---

**Input:** Combined regulatory strategy  $\phi$ , hailing demand  $\lambda$

**Output:** Average market performance metrics

```

1 Initialize  $Q^{h-taxi}$ ,  $Q^{s-taxi}$ ,  $\beta^{rsv}$ ,  $\beta^{h-taxi}$ 
2 Set  $n = 1$ ,  $Z_0^{h-taxi} = 0$ ,  $Z_1^{h-taxi} = e^{\theta^{taxi} Q^{h-taxi}} / (e^{\theta^{taxi} Q^{h-taxi}} + e^{\theta^{taxi} Q^{s-taxi}})$ 
3 while  $|Z_n^{h-taxi} - Z_{n-1}^{h-taxi}| < 1$  (veh) do
4      $Z^{s-taxi} \leftarrow Z^{taxi} - Z_n^{h-taxi}$ 
5     Run OneSim( $\phi, \lambda, [Q^{h-taxi}, Q^{s-taxi}, \beta^{rsv}, \beta^{h-taxi}]$ ) of Algorithm B.1 for 100 times and
        calculate the average market performance metrics
6     Update  $Q^{h-taxi}$ ,  $Q^{s-taxi}$ ,  $\beta^{rsv}$ ,  $\beta^{h-taxi}$ 
7      $Z_{n+1}^{h-taxi} \leftarrow e^{\theta^{taxi} Q^{h-taxi}} / (e^{\theta^{taxi} Q^{h-taxi}} + e^{\theta^{taxi} Q^{s-taxi}})$ 
8      $n \leftarrow n + 1$ 
9 end

```

---

**Algorithm B.3:** Simulation loop for stabilizing supply-demand pattern.

---

**Input:** Combined regulatory strategy  $\phi$

**Output:** Average market performance metrics

```

1 Initialize  $\bar{L}$ 
2 Define a sequence of real numbers  $\{\lambda_n\}$ 
3 Set  $n = 1$ ,  $\lambda_0 = 0$ ,  $\lambda_1 = \Lambda e^{-\theta^{pas} \bar{L}} / (e^{-\theta^{pas} \bar{L}} + e^{-\theta^{pas} \bar{C}^{transit}})$ 
4 while  $|\lambda_n - \lambda_{n+1}| < 1$  (request/min) do
5      $\lambda^{transit} \leftarrow \Lambda - \lambda_n$ 
6     Run DriverStableSim( $\phi, \lambda_n$ ) of Algorithm B.2 and calculate the average market
        performance metrics
7     Calculate  $\bar{C}^{rsv}$  and  $\bar{C}^{taxi}$ 
8      $\bar{L}(\phi, \lambda_n) \leftarrow \ln(e^{\theta_0 \bar{C}^{rsv}} + e^{\theta_0 \bar{C}^{taxi}}) / \theta_0$ 
9      $\lambda_{n+1} \leftarrow \Lambda e^{-\theta^{pas} \bar{L}(\phi, \lambda_n)} / (e^{-\theta^{pas} \bar{L}(\phi, \lambda_n)} + e^{-\theta^{pas} \bar{C}^{transit}})$ 
10     $n \leftarrow n + 1$ 
11 end

```

---

## Appendix C. Parameter settings

Table C.1

Parameter settings and corresponding sources/references.

Symbol	Value/Range	Unit	Source/Reference
<i>Benchmark case <math>\Phi_0</math></i>			
$Z^{\text{rsv}}$	1400	(veh)	Average number of RSVs in the DiDi dataset between 7:00 to 23:00
$\alpha^{\text{taxi}}$	3.0	(¥/km)	Market price in Hangzhou, 2018
$\alpha^{\text{rsv}}$	2.5	(¥/km)	Market price in Hangzhou, 2018
$\tau^{\text{rsv}}$	90	(%)	Market price in Hangzhou, 2018
<i>Parameters / Exogenous variables</i>			
$T$	30	(min)	Specified in this study
$M$	17	/	Estimated in Section 5.1
$l_i$	Between[1,32]	(km)	Calculated based on Eq. (5)
$\bar{l}$	$\approx 11.3$	(km)	Calculated based on Eq. (6)
$R$	5	(km)	Haliem et al. (2021); Manchella et al. (2021)
$\Lambda$	500	(requests/min)	Wang et al. (2020)
$u_{\max}$	5	(¥/km)	Specified in this study
$\bar{C}^{\text{transit}}$	$\approx 28.6$	(¥)	Calculated based on Eq. (14)
$\bar{W}^{\text{transit}}$	10	(min)	Beojone and Geroliminis (2021)
$\alpha^{\text{transit}}$	0.5	(¥/km)	Parameter setting of this paper
$Z^{\text{taxi}}$	814	(veh)	Estimated in Section 5.1
$\tau^{\text{taxi}}$	0.95	(%)	Specified in this study
$W_{\max}$	10	(min)	Beojone and Geroliminis (2021)
$\beta_{\text{time}}^{\text{pas}}$	1	(¥/min)	Wang et al. (2016); Li et al. (2022)
$\beta_{\text{sunk}}^{\text{pas}}$	0.1	(¥/km·min)	Specified in this study
$\hat{p}$	2	(¥)	Wang et al. (2020)
$H$	2	(¥)	Wang et al. (2020)
$v_{,}$	0.5	(km/min)	BaiduMaps (2019)
$v^{\text{transit}}$	$0.87 \times v = 0.435$	(km/min)	Kieu et al. (2015)
$\gamma$	0.5	(¥/km)	Xu et al. (2022)
$\hat{\gamma}^{\text{rsv}}, \hat{\gamma}^{\text{taxi}}$	10,15	(¥/30min)	Li et al. (2022)
$\theta^{\text{pas}}, \theta^{\text{taxi}}$	0.02,0.02	/	Wang et al. (2016)
$\theta_0$	2	/	He et al. (2018)

## Appendix D. Sensitivity analysis of the number and wage rate of taxis

Based on the basic assumptions in this study, the number of taxis  $Z^{\text{taxi}}$  and the wage rate for hybrid taxi drivers  $\tau^{\text{taxi}}$  are exogenously given. However, these two exogenous variables might influence the system's performance. In Fig. D1, we examine the impact of the two factors on each objective function, where the results are computed under the benchmark case  $\phi_0$  using Algorithm B.3. In brief, the results obtained are similar to those for RSV number and RSV wage rate (Fig. 9), where the impact of hybrid taxi wage rate on passengers and RSVs is both insignificant, and passengers and the TNC would benefit from more taxis, but drivers would not.

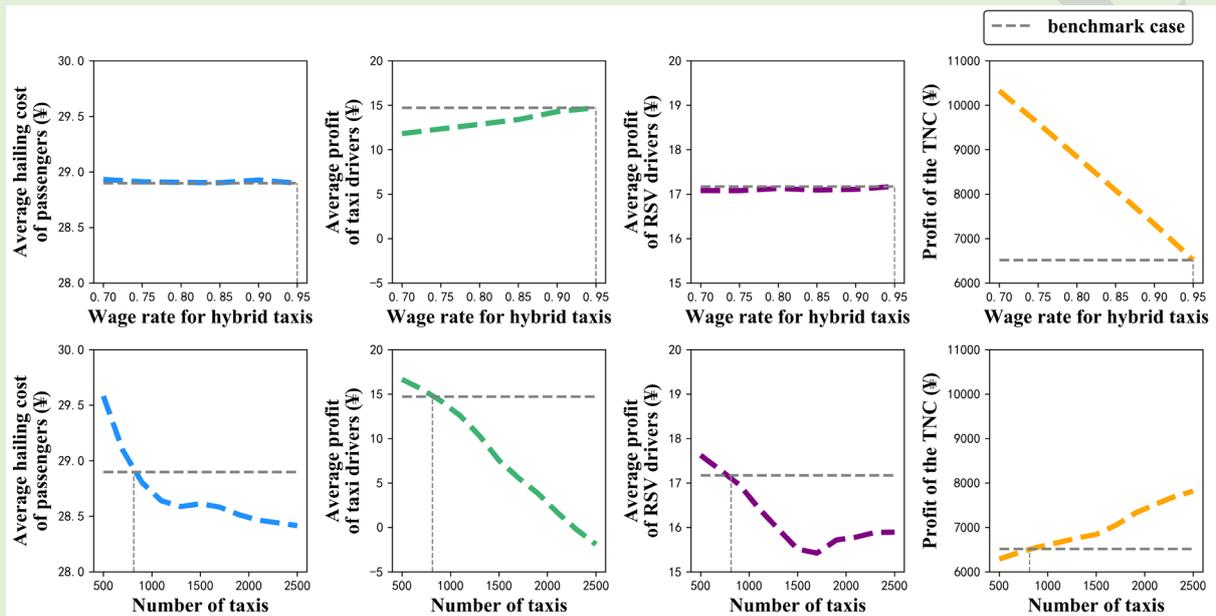


Fig. D1. Impact of taxi number and hybrid taxi wage rate on different objective functions.

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