

STAR-RIS Assisted MISO-NOMA Networks: A Simultaneous Signal Enhancement and Interference Mitigation Design

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Abstract—Simultaneous transmitting and reflecting (STAR) reconfigurable intelligent surface (RIS) technique has recently received considerable attention due to its omnidirectional radiation capability. In this paper, motivated by the interference-mitigation-based (IMB) and signal-enhancement-based (SEB) designs, we introduce an innovative STAR-RIS assisted simultaneous-signal-enhancement-and-interference-mitigation (SSEIM) design in non-orthogonal multiple access (NOMA) multiple-input single-output cellular communication networks. Our objective is to maximize the system spectral efficiency (SE) by jointly optimizing the reflection and transmission phase shifts at the STAR-RIS, the precoding matrix of BSs, and the power allocation factors of NOMA users. We propose a low-complexity simultaneous enhancement and mitigation algorithm. Furthermore, by exploiting the manifold optimization technique, we introduce the Riemannian conjugate gradient algorithm to solve the non-convex subproblems with unit modulus constraint. Our analysis reveals that the proposed SSEIM design exceeds the traditional RIS-aided SEB and IMB designs.

Index Terms—Active beamforming, STAR-RIS, NOMA, SSEIM, manifold optimization.

I. INTRODUCTION

Reconfigurable intelligent surfaces (RISs) are emerging as a pivotal technology in the advancement of 6G networks. By

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manipulating electromagnetic waves via a controllable array of passive elements, RISs offer transformative benefits, such as easy deployment, environment-friendly, low cost, enhanced coverage, high energy efficiency (EE) and superior spectral efficiency (SE) [1]–[4]. In addition, RISs have extensive application prospects for vehicular, robotic, visible light communications, and near-field communications [5]–[7]. Despite the promising capabilities of RISs, traditional designs have been limited to signal reflection, thereby restricting the service coverage to 180 degrees. The advent of simultaneous transmitting and reflecting RIS (STAR-RIS) technology addresses the limitation, enabling full 360-degree coverage and opening new avenues for wireless communication enhancements [8]–[10]. Specifically, the signal model based on dual-sided STAR-RIS, as presented in [11], improves signal transmission and coverage by reflecting signals in two opposite directions simultaneously. The advanced dual-sided STAR-RIS significantly extends coverage and addresses modern communication challenges effectively [12]–[14].

Recently, the research on RIS/STAR-RIS enhanced networks is mainly divided into two categories: interference-mitigation-based (IMB) [15], [16] and signal-enhancement-based (SEB) designs [17], [18]. In [17], an RIS-assisted multiple-input multiple-output (MIMO) network was proposed, where the desired signal can be adjusted by managing the reflection coefficients of RIS elements. In the millimeter wave assisted mobile scenario, STAR-RIS can enhance the received signal of both roadside units and in-vehicle users [18]. Unfortunately, the interferences will be increased with the support of SEB design, which significantly limits the network performance in the high signal-to-noise-ratio (SNR) scenarios. In contrast, an uplink heterogeneous network joint integrating non-orthogonal multiple access (NOMA) and AirFL framework was proposed, where STAR-RIS is utilized to eliminate co-channel interferences [19]. With the rapid expansion of base stations (BSs), an RIS-NOMA-enhanced IMB design was proposed in [20], which mitigates both inter-cluster and inter-cell interferences. However, the IMB design fails to enhance the desired signal, which constrains the communication performance in low-SNR scenarios. To improve the performance in both high-SNR and low-SNR regimes, a novel concept of simultaneous-signal-enhancement-and-cancellation-based (SSECB) was proposed in [21], which is capable of enhancing and mitigating the desired signals and the interference signals simultaneously.

Leveraging STAR-RIS arrays, the SSECB design of the NOMA coordinated multi-point transmission networks can be accomplished. However, only the simplest single-input single-output scenario is considered in [21]. In actual multi-antenna scenarios, the beamforming at the BSs and the correlation of channels need to be considered [22]–[24]. In a double-RIS-aided MISO network, the spatial correlation of RISs can improve the achievable rate, whereas there is a negative impact on the transmit correlation at BSs [22]. Moreover, STAR-RIS inherently has a complex parameter space. Numerous parameters are mixed up with each other, which makes it difficult to solve optimization problems. The currently available algorithms are of high complexity, which demand a large amount of computing and time resources [25], [26].

The integration of NOMA and STAR-RISs can provide synergistic advantages, such as supporting massive connectivity, enhancing SE, and facilitating flexible resource allocation by intelligently controlling the channel state information (CSI) of users [27]–[30]. However, traditional RIS can only reflect signals, resulting in similar channel conditions for users in the reflected space, which limits the full advantages of NOMA. Therefore, the application prospect of STAR-RIS-NOMA networks has been explored [31]–[35]. In [31], a STAR-RIS assisted NOMA downlink (DL) architecture was proposed, where the effective channel capacity was improved. Then, the data rate of STAR-RIS-NOMA assisted communication system in the case of statistical CSI is analyzed in [32]. The joint optimization of passive beamforming at STAR-RIS, the decoding order and the active beamforming at BS was proposed in [35], maximizing the achievable sum data rate.

A. Motivations and Contributions

Existing research predominantly focuses on RIS-assisted SEB design or RIS-assisted IMB design [16]–[19]. In practical applications, the signal enhancement design will also enhance the interferences, while the interference mitigation design will not enhance any desired signals. Therefore, it is urgent to find a scheme for enhancing and mitigating the desired signals and the interference signals simultaneously, which poses two critical challenges: i) Traditional RIS cannot deliver full-space communication services to massive users, integrating STAR-RIS with NOMA techniques into cellular networks is essential. ii) Compared to traditional RIS, STAR-RIS necessitates optimization within a more complex parameter space, demanding enhanced computational capabilities and algorithmic support. Moreover, An increase in the number of parameters may compromise system stability and reliability, making existing research approaches complex and challenging to implement in practice. To tackle these issues while offering valuable engineering insights, we present an innovative low-complexity simultaneous-signal-enhancement-and-interference-mitigation (SSEIM) design tailored for dual-sided STAR-RISs assisted MISO-NOMA cellular networks. The primary contributions are concluded as follows:

- An innovative SSEIM design for a dual-sided STAR-RISs assisted multiuser MISO-NOMA downlink cellular network is proposed. With STAR-RIS deployed at the

junction of two cells, the SSEIM design can enhance and mitigate the desired signals and the interference signals simultaneously. The reflected signal is used to enhance the desired signals, while the transmitted signal is used to mitigate interference signals, which are defined as SEB-sector and IMB-sector, respectively.

- We develop an optimization problem aimed at maximizing SE and present a systematic approach by partitioning it into three sub-problems. First, for the SEB-sector, we utilize the maximum ratio transmission (MRT) precoding matrix to optimize the reflection phase shifts of STAR-RIS and the active beamformer at BSs jointly. Next, for the IMB-sector, we optimize the transmission phase shifts of STAR-RIS to mitigate both inter-cell and intra-cell interferences. Finally, we optimize the NOMA power allocation factors based on the target data rates.
- We propose a low-complexity simultaneous enhancement and mitigation (LSEM) algorithm. By exploiting the complex circle manifold optimization technique, the unit modulus constraints can be effectively addressed by the Riemannian conjugate gradient (RCG) algorithm. Additionally, we consider the effects of spatial correlation and determine the minimum required number of STAR-RIS elements for the IMB-sector.
- Our numerical results demonstrate that: 1) Compared to the RIS-aided SEB and IMB designs, the EE and SE of our proposed STAR-RIS assisted SSEIM design are significantly improved; 2) Compared with the zero forcing (ZF) precoding and identity precoding matrices, the proposed SSEIM design has superior performance in the case of MRT precoding matrix; 3) There is an optimal range of the reflection power coefficient, which indicates that a tradeoff exists between SEB-sector and IMB-sector.

B. Organization and Notations

In Section II, we present a dual-sided STAR-RIS aided multiuser MISO-NOMA DL cellular communication network model, and the corresponding optimization problem is formulated. We propose a LSEM algorithm to solve the optimization problem. Specifically, the RCG algorithm is utilized to solve both SEB-sector and IMB-sector subproblems in Section III and Section IV. Numerical results are given in Section V to demonstrate the effectiveness of the proposed STAR-RIS assisted SSEIM design. Finally, Section VI provides the conclusion and outlines potential future applications.

Notations: \mathbf{H}^* , \mathbf{H}^H and \mathbf{H}^T denote the conjugate, conjugate transpose and transpose of the matrix \mathbf{H} , respectively. \circ and \otimes represent the Hadamard product and the Kronecker product, respectively. $\text{diag}[\cdot]$ symbolizes a diagonal matrix. $|\bullet|$ and $\|\bullet\|_2$ denote the absolute value and the Frobenius norm, respectively. \mathcal{C}^L is the space of $L \times 1$ complex vector.

II. SYSTEM MODEL AND PROBLEM FORMULATION

A. System Model

We consider a dual-sided STAR-RIS assisted multiuser MISO-NOMA downlink cellular communication network, as depicted in Fig. 1. The network comprises a STAR-RIS, two

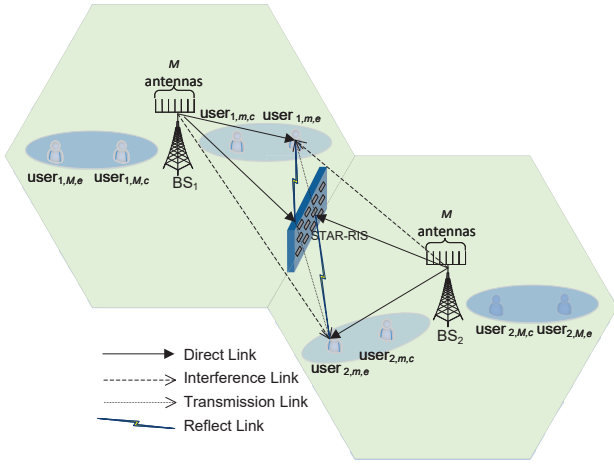


Fig. 1: STAR-RIS assisted cellular MISO-NOMA downlink network.

cells, two base stations (BSs), and M clusters in each cell. The BS situated at the center of the cell is equipped with M transmitting antennas (TAs) that are arranged in a uniform linear array (ULA). Each cluster contains two users, namely the cell-center user (CCU) and cell-edge user (CEU) based on the distance from BS to user. Each user has a single receiving antenna. All users can receive the direct link signals, the signals reflected by STAR-RIS, the signals transmitted by STAR-RIS, and the channel noise¹.

A dual-sided uniform planar array (UPA) STAR-RIS is deployed at the junction of two cells with $L = L_H \times L_V$ passive STAR-RIS elements. Utilizing energy splitting (ES) protocol, the STAR-RIS elements can transmit and reflect signals simultaneously [10]. After the signal from the BS 1 reaches the STAR-RIS, the dual-sided STAR-RIS reflects it to the users in cell 1 and transmit it to the users in cell 2. Based on the insights of [9] and [33], we also consider the ES factor for the transmitted and reflected signals to be uniform across all STAR-RIS elements, while the phase shift of each STAR-RIS element can be adjusted independently. Since the signals from BS do not carry the information of the users in adjacent cells, the signals transmitted by STAR-RIS are all used to mitigate the interferences. In order to implement the proposed SSEIM design, the signals reflected by STAR-RIS are used to amplify the desired signals, thus improving the overall communication quality.

B. Channel Model

In this paper, both line-of-sight (LoS) and non-LoS (NLoS) components are considered in the BS-user links. We model the channels from the BS located in cell $i \in \{1, 2\}$ to the m -th cluster of cell i as spatially correlated Rician fading channels

$$\mathbf{w}_{i,i,m,c} = \sqrt{\frac{\mathcal{K}_1}{\mathcal{K}_1 + 1}} \mathbf{w}_{i,i,m,c}^{\text{LoS}} + \sqrt{\frac{1}{\mathcal{K}_1 + 1}} \mathbf{w}_{i,i,m,c}^{\text{NLoS}} \mathbf{R}_d^{1/2}, \quad (1)$$

¹The direct link signal from BS to users within the same cell is inter-cluster interference and the desired signal, whereas the direct link signal from BS to users in the adjacent cell results in inter-cell interference.

where $\mathbf{w}_{i,i,m,c}^{\text{LoS}}$ and $\mathbf{w}_{i,i,m,c}^{\text{NLoS}}$ are the LoS and NLoS components with $(1 \times M)$ elements. \mathcal{K} is the Rician factor, representing the power ratio between LoS and NLoS components. \mathbf{R}_d denotes the BS transmit correlation matrix with $(M \times M)$ elements. By utilizing the exponential model, the ULA spatial correlation matrix is represented as follows [22]–[24]

$$R_d(x, y) = \begin{cases} (r_d e^{j'\vartheta})^{y-x}, & \text{if } x \leq y, \\ ((r_d e^{j'\vartheta})^*)^{x-y}, & \text{otherwise,} \end{cases} \quad (2)$$

where $R_d(x, y)$ denotes the element in the y -th column and x -th row of matrix \mathbf{R}_d . The correlation coefficient is set to $r_d \in [0, 1]$, the corresponding vertical or horizontal angle of departure (AoD) is denoted by ϑ , the imaginary unit is represented by $j' = \sqrt{-1}$.

Since many obstacles are located between users and the BS in the adjacent cell, the channel from the BS located in cell i to the CCU in cluster m of cell j ($j \in \{1, 2\}, j \neq i$) is expressed as

$$\mathbf{w}_{i,j,m,c} = [w_1^{i,j,m,c} \quad \dots \quad w_M^{i,j,m,c}], \quad (3)$$

where $\mathbf{w}_{i,j,m,c}$ is a $(1 \times M)$ vector, which follows Rayleigh distribution. $f(x) = e^{-x}$ is the probability density function.

The dual-sided STAR-RIS UPA can reflect and transmit signals from the BS in cell 1 and the BS in cell 2. Similar to (1), we define the spatial correlation channel matrix from BS i to STAR-RIS as

$$\mathbf{F}_i = \sqrt{\frac{\mathcal{K}_2}{\mathcal{K}_2 + 1}} \mathbf{F}_i^{\text{LoS}} + \sqrt{\frac{1}{\mathcal{K}_2 + 1}} \mathbf{R}_R^{1/2} \mathbf{F}_i^{\text{NLoS}} \mathbf{R}_d^{1/2}, \quad (4)$$

where \mathbf{F}_i is a $(L \times M)$ matrix, which follows the Rician distribution. $\mathbf{F}_i^{\text{LoS}}$ stands for the LoS component, while $\mathbf{F}_i^{\text{NLoS}}$ stands for the NLoS component. \mathbf{R}_R is a $(L \times L)$ receiving correlation matrix of STAR-RIS. It can be approximated exploiting the Kronecker model as

$$\mathbf{R}_R \approx \mathbf{R}_{R,H} \otimes \mathbf{R}_{R,V}, \quad (5)$$

where $\mathbf{R}_{R,V} \in \mathcal{C}^{\sqrt{L} \times \sqrt{L}}$ and $\mathbf{R}_{R,H} \in \mathcal{C}^{\sqrt{L} \times \sqrt{L}}$ are the vertical ULA and horizontal ULA correlation matrices, respectively.

In the proposed networks, the channel from the STAR-RISs to the CCU in cluster m of cell i can be modeled as

$$\mathbf{g}_{i,m,c} = \sqrt{\frac{\mathcal{K}_3}{\mathcal{K}_3 + 1}} \mathbf{g}_{i,m,c}^{\text{LoS}} + \sqrt{\frac{1}{\mathcal{K}_3 + 1}} \mathbf{g}_{i,m,c}^{\text{NLoS}} \mathbf{R}_{R,i,m,c}^{1/2}, \quad (6)$$

where $\mathbf{g}_{i,m,c}$ is a $(1 \times L)$ vector, which follows Rician distribution. $\mathbf{g}_{i,m,c}^{\text{LoS}}$ stands for the LoS component, while $\mathbf{g}_{i,m,c}^{\text{NLoS}}$ stands for the NLoS component. $\mathbf{R}_{R,u}$ is the spatial correlation matrix between the users and the STAR-RIS. Similar to (5), it can be represented as the Kronecker product of the vertical and horizontal correlation matrix.

We then pay attention to the impact of the path loss, and the large-scale fading from BS i to CCU in cluster m of cell j ($i \neq j$) is represented as

$$\varepsilon_{i,j,m,c} = d_{i,j,m,c}^{-\alpha_1}, \quad (7)$$

where α_1 is the path loss exponent for the BS-user link in different cell, $d_{i,j,m,c}$ is the distance between BS i and CCU

of cluster m located in the adjacent cell.

With the distance $d_{i,i,m,c}$ between BS i and CCU of cluster m within the same cell, the path loss exponent α_2 , the large-scale fading of BS-user link can be calculated by

$$\varepsilon_{i,i,m,c} = d_{i,i,m,c}^{-\alpha_2}. \quad (8)$$

The STAR-RIS is deployed at the border of two cells, we consider the large-scale fading of BS-RIS-user links as LoS links. The large-scale fading from BS i to the CCU in cluster m of cell j through STAR-RIS is represented to be

$$\varepsilon_{i,R,j,m,c} = d_{i,R}^{-\alpha_3} d_{R,j,m,c}^{-\alpha_4}, \quad (9)$$

where the distance from the STAR-RIS to CCU in cluster m of cell j and from the BS i to the STAR-RIS are given by $d_{R,j,m,c}$ and $d_{i,R}$, respectively. The path loss exponents of the RIS-user and BS-RIS links can be defined as α_3 and α_4 , respectively.

C. Signal Model

The information bearing vector transmitted by BS i can be denoted by

$$\mathbf{s}_i = \begin{bmatrix} \alpha_c s_{i,1,c} + \alpha_e s_{i,1,e} \\ \vdots \\ \alpha_c s_{i,m,c} + \alpha_e s_{i,m,e} \\ \vdots \\ \alpha_c s_{i,M,c} + \alpha_e s_{i,M,e} \end{bmatrix}, \quad (10)$$

where \mathbf{s}_i contains M elements. α_c and α_e are the power allocation factors of CCU and CEU with $\alpha_c^2 + \alpha_e^2 = 1$, respectively. The transmitted symbol for CCU and CEU of the m -th cluster in BS i is denoted by $s_{i,m,c}$ and $s_{i,m,e}$, respectively.

Due to the symmetry of dual-sided STAR-RIS [11], the reflection coefficients are identical for both leftward and rightward reflections, and the transmission coefficients from the left are equivalent to those from the right. The reflection and transmission coefficients are independent, which are defined as follows:

$$\begin{aligned} \Phi_R &\triangleq \text{diag}[\beta_{R,1}\phi_{R,1}, \dots, \beta_{R,L}\phi_{R,L}], \\ \Phi_T &\triangleq \text{diag}[\beta_{T,1}\phi_{T,1}, \dots, \beta_{T,L}\phi_{T,L}], \end{aligned} \quad (11)$$

where $\beta_{R,l} \in (0, 1]$ and $\beta_{T,l} \in (0, 1]$ are the reflected and transmitted amplitude coefficients of the l -th STAR-RIS element, respectively. $\phi_{R,l} = \exp(j'\theta_{R,l})$ and $\phi_{T,l} = \exp(j'\theta_{T,l})$ are the corresponding phase shifts, satisfying $\theta_{R,l} \in [0, 2\pi)$, $\theta_{T,l} \in [0, 2\pi)$.

Independent adjustment of the transmission and reflection phase shifts are possible for each passive STAR-RIS element [10], [33], [36], while due to energy conservation law, the total power of reflection and transmission coefficients is constrained to

$$\beta_{R,l}^2 + \beta_{T,l}^2 \leq 1, \forall l = 1, \dots, L, \quad (12)$$

where we set $\beta_{R,l}^2 + \beta_{T,l}^2 = 1$ for simplicity.

Similar to [11], the amplitude coefficients are assumed to be identical, i.e., $\beta_{R,l} = \beta_R, \beta_{T,l} = \beta_T, \forall l = 1, \dots, L$. Then, the STAR-RIS coefficient matrix is further simplified to

$$\begin{aligned} \Phi_R &= \beta_R \text{diag} [e^{j'\theta_{R,1}}, \dots, e^{j'\theta_{R,L}}], \\ \Phi_T &= \beta_T \text{diag} [e^{j'\theta_{T,1}}, \dots, e^{j'\theta_{T,L}}]. \end{aligned} \quad (13)$$

We define the transmit power and the precoding matrix of the i -th BS as p_i and \mathbf{P}_i , respectively. Hence, the received signal of users in cluster m of cell 1 is represented as

$$\begin{aligned} y_{1,m,k} &= \sqrt{\varepsilon_{1,1,m,k}} \mathbf{w}_{1,1,m,k} \mathbf{P}_1 \sqrt{p_1} \mathbf{s}_1 \\ &+ \sqrt{\varepsilon_{1,R,1,m,k}} \mathbf{g}_{1,m,k} \Phi_R \mathbf{F}_1 \mathbf{P}_1 \sqrt{p_1} \mathbf{s}_1 \\ &+ \sqrt{\varepsilon_{2,1,m,k}} \mathbf{w}_{2,1,m,k} \mathbf{P}_2 \sqrt{p_2} \mathbf{s}_2 \\ &+ \sqrt{\varepsilon_{2,R,1,m,k}} \mathbf{g}_{1,m,k} \Phi_T \mathbf{F}_2 \mathbf{P}_2 \sqrt{p_2} \mathbf{s}_2 + N_0^{1,m,k}, \end{aligned} \quad (14)$$

where $k \in \{c, e\}$, N_0 is the additive white Gaussian noise (AWGN), which has variance σ^2 and mean 0.

D. Analysis of Desired Signal and Interference

Based on the dual-sided STAR-RIS assisted SSEIM design, we enhance the desired signals by superimposing them with the STAR-RIS-reflected signals. Consequently, we can represent the effective channel gains of the CCU and CEU in cluster m of cell i as

$$\begin{aligned} |h_{i,m,c}^2| &= \left| \left(\sqrt{\varepsilon_{i,i,m,c}} \mathbf{w}_{i,i,m,c} + \sqrt{\varepsilon_{i,R,i,m,c}} \mathbf{g}_{i,m,c} \Phi_R \mathbf{F}_i \right) \mathbf{P}_i \bar{\mathbf{1}}_m \right|^2, \\ |h_{i,m,e}^2| &= \left| \left(\sqrt{\varepsilon_{i,i,m,e}} \mathbf{w}_{i,i,m,e} + \sqrt{\varepsilon_{i,R,i,m,e}} \mathbf{g}_{i,m,e} \Phi_R \mathbf{F}_i \right) \mathbf{P}_i \bar{\mathbf{1}}_m \right|^2, \end{aligned} \quad (15)$$

where $\bar{\mathbf{1}}_m = [0 \dots 0 \ 1 \ 0 \dots 0]^T$ represents an $(M \times 1)$ vector, the m -th row of $\bar{\mathbf{1}}_m$ is 1.

Generally speaking, the effective inter-cell interference of the CCU and CEU in cluster m of cell i can be expressed as

$$\begin{aligned} D_{i,m,c} &= \sqrt{\varepsilon_{j,i,m,c}} \mathbf{w}_{j,i,m,c} \mathbf{P}_j \mathbf{1}_M, \\ D_{i,m,e} &= \sqrt{\varepsilon_{j,i,m,e}} \mathbf{w}_{j,i,m,e} \mathbf{P}_j \mathbf{1}_M, \end{aligned} \quad (16)$$

where $\mathbf{1}_M$ represents an all one vector with $(M \times 1)$ elements.

The inter-cluster interference of the CCU and CEU in cluster m of cell i can be expressed as

$$\begin{aligned} B_{i,m,c} &= \sqrt{\varepsilon_{i,i,m,c}} \mathbf{w}_{i,i,m,c} \mathbf{P}_i \bar{\mathbf{0}}_m, \\ B_{i,m,e} &= \sqrt{\varepsilon_{i,i,m,e}} \mathbf{w}_{i,i,m,e} \mathbf{P}_i \bar{\mathbf{0}}_m, \end{aligned} \quad (17)$$

where $\bar{\mathbf{0}}_m = [1 \dots 1 \ 0 \ 1 \dots 1]^T$ represents an $(M \times 1)$ vector containing a zero element in the m -th row.

The BS-RIS-user reflection links for SEB cause additional interference. The CCU and CEU in cluster m of cell i receives interference reflected by STAR-RIS, which can be given by

$$\begin{aligned} Q_{i,m,c} &= \sqrt{\varepsilon_{i,R,i,m,c}} \mathbf{g}_{i,m,c} \Phi_R \mathbf{F}_i \mathbf{P}_i \bar{\mathbf{0}}_m, \\ Q_{i,m,e} &= \sqrt{\varepsilon_{i,R,i,m,e}} \mathbf{g}_{i,m,e} \Phi_R \mathbf{F}_i \mathbf{P}_i \bar{\mathbf{0}}_m. \end{aligned} \quad (18)$$

Then, we can express all interferences of CCU and CEU in cluster m of cell i as

$$\begin{aligned} I_{i,m,c} &= D_{i,m,c} + B_{i,m,c} + Q_{i,m,c}, \\ I_{i,m,e} &= D_{i,m,e} + B_{i,m,e} + Q_{i,m,e}. \end{aligned} \quad (19)$$

In the STAR-RIS assisted multiuser MISO-NOMA cellular network, we define the equivalent interferences of CCU and CEU in cluster m of cell i as $\hat{I}_{i,m,c}$ and $\hat{I}_{i,m,e}$. We mitigate the interferences by superimposing them with the STAR-RIS-transmitted signals. Consequently, $\hat{I}_{i,m,c}$ and $\hat{I}_{i,m,e}$ can be represented as

$$\begin{aligned}\hat{I}_{1,m,c} &= |I_{1,m,c} + \sqrt{\varepsilon_{2,R,1,m,c}} \mathbf{g}_{1,m,c} \Phi_T \mathbf{F}_2 \mathbf{P}_2 \mathbf{1}_m|^2, \\ \hat{I}_{1,m,e} &= |I_{1,m,e} + \sqrt{\varepsilon_{2,R,1,m,e}} \mathbf{g}_{1,m,e} \Phi_T \mathbf{F}_2 \mathbf{P}_2 \mathbf{1}_m|^2, \\ \hat{I}_{2,m,c} &= |I_{2,m,c} + \sqrt{\varepsilon_{1,R,2,m,c}} \mathbf{g}_{2,m,c} \Phi_T \mathbf{F}_1 \mathbf{P}_1 \mathbf{1}_m|^2, \\ \hat{I}_{2,m,e} &= |I_{2,m,e} + \sqrt{\varepsilon_{1,R,2,m,e}} \mathbf{g}_{2,m,e} \Phi_T \mathbf{F}_1 \mathbf{P}_1 \mathbf{1}_m|^2.\end{aligned}\quad (20)$$

Lemma 1. *We assume that the small-scale fading environments of BS-STAR-RIS and STAR-RIS-user links are strong enough, i.e., $\mathcal{K}_2 = \mathcal{K}_3 \sim \infty$. Hence, to mitigate the interferences of the dual-sided STAR-RIS assisted cellular MISO-NOMA network, the following conditions must be satisfied:*

$$L \geq \max \{ \Omega_{1,m,c}, \Omega_{1,m,e}, \Omega_{2,m,c}, \Omega_{2,m,e} \}. \quad (21)$$

$$\begin{aligned}\beta_R &< \frac{M \sqrt{d_{1,R}^{-\alpha_3}}}{M \sqrt{d_{1,R}^{-\alpha_3}} + (M-1) \sqrt{d_{2,R}^{-\alpha_3}}}, \\ \beta_R &< \frac{M \sqrt{d_{2,R}^{-\alpha_3}}}{M \sqrt{d_{2,R}^{-\alpha_3}} + (M-1) \sqrt{d_{1,R}^{-\alpha_3}}}.\end{aligned}\quad (22)$$

where

$$\begin{aligned}\Omega_{1,m,k} &= \frac{(M-1) \sqrt{d_{1,1,m,k}^{-\alpha_2}} + M \sqrt{d_{2,1,m,k}^{-\alpha_1}}}{\left[(1-M) \beta_R \sqrt{d_{1,R}^{-\alpha_3}} + M \beta_T \sqrt{d_{2,R}^{-\alpha_3}} \right] \sqrt{d_{R,1,m,k}^{-\alpha_4}}}, \\ \Omega_{2,m,k} &= \frac{(M-1) \sqrt{d_{2,2,m,k}^{-\alpha_2}} + M \sqrt{d_{1,2,m,k}^{-\alpha_1}}}{\left[(1-M) \beta_R \sqrt{d_{2,R}^{-\alpha_3}} + M \beta_T \sqrt{d_{1,R}^{-\alpha_3}} \right] \sqrt{d_{R,2,m,k}^{-\alpha_4}}}.\end{aligned}\quad (23)$$

Proof: To eliminate inter-cluster interference, it is necessary to satisfy

$$\begin{aligned}(M-1) \sqrt{d_{1,1,m,k}^{-\alpha_2}} &\leq \beta_T L M \sqrt{d_{2,R}^{-\alpha_3} d_{R,1,m,k}^{-\alpha_4}}, \\ (M-1) \sqrt{d_{2,2,m,k}^{-\alpha_2}} &\leq \beta_T L M \sqrt{d_{1,R}^{-\alpha_3} d_{R,2,m,k}^{-\alpha_4}}.\end{aligned}\quad (24)$$

Similarly, to eliminate the inter-cell interference, it is necessary to satisfy

$$\begin{aligned}M \sqrt{d_{2,1,m,k}^{-\alpha_1}} &\leq \beta_T L M \sqrt{d_{2,R}^{-\alpha_3} d_{R,1,m,k}^{-\alpha_4}}, \\ M \sqrt{d_{1,2,m,k}^{-\alpha_1}} &\leq \beta_T L M \sqrt{d_{1,R}^{-\alpha_3} d_{R,2,m,k}^{-\alpha_4}}.\end{aligned}\quad (25)$$

To eliminate the interference caused by SEB-sector, the following conditions need to be met

$$\begin{aligned}\beta_R L (M-1) \sqrt{d_{1,R}^{-\alpha_3} d_{R,1,m,k}^{-\alpha_4}} &\leq \beta_T L M \sqrt{d_{2,R}^{-\alpha_3} d_{R,1,m,k}^{-\alpha_4}}, \\ \beta_R L (M-1) \sqrt{d_{2,R}^{-\alpha_3} d_{R,2,m,k}^{-\alpha_4}} &\leq \beta_T L M \sqrt{d_{1,R}^{-\alpha_3} d_{R,2,m,k}^{-\alpha_4}}.\end{aligned}\quad (26)$$

Combining (24), (25) and (26), the required number of

STAR-RIS elements for interference mitigation needs to satisfy

$$\begin{aligned}(M-1) \sqrt{d_{1,1,m,k}^{-\alpha_2}} + M \sqrt{d_{2,1,m,k}^{-\alpha_1}} &+ \\ \beta_R L (M-1) \sqrt{d_{1,R}^{-\alpha_3} d_{R,1,m,k}^{-\alpha_4}} &\leq \beta_T L M \sqrt{d_{2,R}^{-\alpha_3} d_{R,1,m,k}^{-\alpha_4}}, \\ (M-1) \sqrt{d_{2,2,m,k}^{-\alpha_2}} + M \sqrt{d_{1,2,m,k}^{-\alpha_1}} &+ \\ \beta_R L (M-1) \sqrt{d_{2,R}^{-\alpha_3} d_{R,2,m,k}^{-\alpha_4}} &\leq \beta_T L M \sqrt{d_{1,R}^{-\alpha_3} d_{R,2,m,k}^{-\alpha_4}}.\end{aligned}\quad (27)$$

After some algebraic operations, Eq. (27) can be rewritten as

$$\begin{aligned}L &\geq \frac{(M-1) \sqrt{d_{1,1,m,k}^{-\alpha_2}} + M \sqrt{d_{2,1,m,k}^{-\alpha_1}}}{\left[(1-M) \beta_R \sqrt{d_{1,R}^{-\alpha_3}} + M \beta_T \sqrt{d_{2,R}^{-\alpha_3}} \right] \sqrt{d_{R,1,m,k}^{-\alpha_4}}}, \\ L &\geq \frac{(M-1) \sqrt{d_{2,2,m,k}^{-\alpha_2}} + M \sqrt{d_{1,2,m,k}^{-\alpha_1}}}{\left[(1-M) \beta_R \sqrt{d_{2,R}^{-\alpha_3}} + M \beta_T \sqrt{d_{1,R}^{-\alpha_3}} \right] \sqrt{d_{R,2,m,k}^{-\alpha_4}}},\end{aligned}\quad (28)$$

where

$$\begin{aligned}(1-M) \beta_R \sqrt{d_{1,R}^{-\alpha_3}} + M \beta_T \sqrt{d_{2,R}^{-\alpha_3}} &> 0, \\ (1-M) \beta_R \sqrt{d_{2,R}^{-\alpha_3}} + M \beta_T \sqrt{d_{1,R}^{-\alpha_3}} &> 0.\end{aligned}\quad (29)$$

After some algebraic manipulations, the results in (21) and (22) can be deduced, completing the proof of **Lemma 1**. ■

E. Problem Formulation

Based on the expression of the effective channel gains in (15) and the equivalent interferences in (20), we can express the SINR of CCU and CEU in cluster m of cell i as

$$\begin{aligned}SINR_{i,m,c} &= \frac{|h_{i,m,c}|^2 p_i \alpha_c^2}{\hat{I}_{i,m,c} p_i + N_0^{i,m,c}}, \\ SINR_{i,m,e} &= \frac{|h_{i,m,e}|^2 p_i \alpha_e^2}{|h_{i,m,e}|^2 p_i \alpha_c^2 + \hat{I}_{i,m,e} p_i + N_0^{i,m,e}}.\end{aligned}\quad (30)$$

By jointly optimizing the power allocation factors of NOMA users, the precoding matrix of BSs, as well as the reflection and transmission phase shifts at the STAR-RIS, we can formulate the spectral efficiency maximization problem as

$$\begin{aligned}\max_{\Phi_R, \Phi_T, \mathbf{P}_1, \mathbf{P}_2, \alpha_c, \alpha_e} & \sum_{i=1}^2 \sum_{m=1}^M (\hat{R}_{i,m,c} + \hat{R}_{i,m,e}) \\ \text{s.t.} & C1: \theta_{R,l} \in [0, 2\pi), \forall l = 1, 2, \dots, L, \\ & C2: \theta_{T,l} \in [0, 2\pi), \forall l = 1, 2, \dots, L, \\ & C3: \beta_R^2 + \beta_T^2 = 1, \\ & C4: \alpha_c^2 + \alpha_e^2 = 1, \\ & C5: \hat{R}_{i,m,c} \geq R_{i,m,c}^*, \hat{R}_{i,m,e} \geq R_{i,m,e}^*, \\ & C6: \|\mathbf{P}_1\|_2^2 \leq 1, \|\mathbf{P}_2\|_2^2 \leq 1.\end{aligned}\quad (31)$$

where $\hat{R}_{i,m,c} = \log_2(1 + SINR_{i,m,c})$ and $\hat{R}_{i,m,e} = \log_2(1 + SINR_{i,m,e})$ represent the achievable rates of CCU and CEU, respectively. $R_{i,m,c}^*$ and $R_{i,m,e}^*$ are the target data rates of CCU and CEU, respectively. C1, C2 and C3 are the constraint

conditions of the dual-sided STAR-RIS array, $C4$ is the constraint condition of the power allocation factors, $C5$ is the constraint condition of the achievable rate, $C6$ is the constraint condition of the precoding matrix.

Based on the proposed SSEIM design, we aim at maximizing the desired signals and minimizing the interference signals. We can decompose the optimization problem in (31) into three subproblems: the SEB-sector, the IMB-sector and the power allocation sector. Since the SEB-sector can cause additional interference, it should be designed first. We first focus on maximizing the effective channel power gain by jointly optimizing the reflection phase shifts of each STAR-RIS element and the precoding matrix of BSs as follows:

$$\begin{aligned} \max_{\Phi_R, \mathbf{P}_1, \mathbf{P}_2} \quad & \sum_{i=1}^2 \sum_{m=1}^M (|h_{i,m,c}^2| + |h_{i,m,e}^2|) \\ \text{s.t.} \quad & C1, C6. \end{aligned} \quad (32)$$

Next, the equivalent interference can be minimized by optimizing the transmission phase shifts of each STAR-RIS elements as follows:

$$\begin{aligned} \min_{\Phi_T} \quad & \sum_{i=1}^2 \sum_{m=1}^M (\hat{I}_{i,m,c} + \hat{I}_{i,m,e}) \\ \text{s.t.} \quad & C2. \end{aligned} \quad (33)$$

Finally, to guarantee users' fairness, the optimization of power allocation factors for NOMA users is conducted based on the target data rate and CSI. We develop the optimization problem as:

$$\begin{aligned} \max_{\alpha_c, \alpha_e} \quad & \sum_{i=1}^2 \sum_{m=1}^M (\hat{R}_{i,m,c} + \hat{R}_{i,m,e}) \\ \text{s.t.} \quad & C4, C5. \end{aligned} \quad (34)$$

III. SIGNAL ENHANCEMENT DESIGN

In this section, we first pay attention to the SEB-sector. Similar to equation (30), we can express the SNR of CCU and CEU in cluster m of cell i as

$$\begin{aligned} SNR_{i,m,c} &= \frac{|h_{i,m,c}^2| p_i \alpha_c^2}{N_0^{i,m,c}} \\ SNR_{i,m,e} &= \frac{|h_{i,m,e}^2| p_i \alpha_e^2}{|h_{i,m,e}^2| p_i \alpha_c^2 + N_0^{i,m,e}}. \end{aligned} \quad (35)$$

By utilizing the high SNR approximation in [37], the SNR of CEU in the m -th cluster is further expressed as

$$SNR_{i,m,e} \approx \frac{\alpha_e^2}{\alpha_c^2}, \quad (36)$$

which is a constant. It shows that the effective channel power gain of CCU plays a major role in the SEB-sector. Therefore, the optimization problem (32) can be transformed into

$$\begin{aligned} \max_{\Phi_R, \mathbf{P}_1, \mathbf{P}_2} \quad & \sum_{m=1}^M (|h_{1,m,c}^2| + |h_{2,m,c}^2|) \\ \text{s.t.} \quad & C1, C6. \end{aligned} \quad (37)$$

To enhance the effective channel power gain, the MRT technique is employed to jointly optimize the precoding matrix \mathbf{P}_i and the phase shifts of dual-sided STAR-RIS [38], [39]. As defined by equation (15) for $|h_{i,m,c}^2|$, the MRT beamforming vector of the m -th cluster of BS i is a $(M \times 1)$ vector, which is specified as follows:

$$\hat{\mathbf{p}}_{i,m}^H = \frac{(\sqrt{\varepsilon_{i,i,m,c}} \mathbf{w}_{i,i,m,c} + \sqrt{\varepsilon_{i,R,i,m,c}} \mathbf{g}_{i,m,c} \Phi_R \mathbf{F}_i)}{\|\sqrt{\varepsilon_{i,i,m,c}} \mathbf{w}_{i,i,m,c} + \sqrt{\varepsilon_{i,R,i,m,c}} \mathbf{g}_{i,m,c} \Phi_R \mathbf{F}_i\|_2}. \quad (38)$$

We define an $(L \times 1)$ effective STAR-RIS reflection vector $\Psi_R = [\phi_{R,1}, \dots, \phi_{R,L}]^H = [e^{j\theta_{R,1}}, \dots, e^{j\theta_{R,L}}]^H$. Concurrently, the effective channel power gains of the CCU can be reformulated as

$$\begin{aligned} |h_{1,m,c}^2| &= |(\sqrt{\varepsilon_{1,1,m,c}} \mathbf{w}_{1,1,m,c} + \Psi_R^H \tilde{\mathbf{a}}_{1,m}) \hat{\mathbf{p}}_{1,m}|^2, \\ |h_{2,m,c}^2| &= |(\sqrt{\varepsilon_{2,2,m,c}} \mathbf{w}_{2,2,m,c} + \Psi_R^H \tilde{\mathbf{a}}_{2,m}) \hat{\mathbf{p}}_{2,m}|^2, \end{aligned} \quad (39)$$

where $\tilde{\mathbf{a}}_{i,m} = \beta_R \sqrt{\varepsilon_{i,R,i,m,c}} \text{diag}(\mathbf{g}_{i,m,c}) \mathbf{F}_i$, $\hat{\mathbf{p}}_{i,m}$ in (38) can be further transformed into

$$\hat{\mathbf{p}}_{i,m}^H = \frac{\sqrt{\varepsilon_{i,i,m,c}} \mathbf{w}_{i,i,m,c} + \Psi_R^H \tilde{\mathbf{a}}_{i,m}}{\|\sqrt{\varepsilon_{i,i,m,c}} \mathbf{w}_{i,i,m,c} + \Psi_R^H \tilde{\mathbf{a}}_{i,m}\|_2}. \quad (40)$$

The objective function $f(\Psi_R)$ is given by

$$f(\Psi_R) = - \sum_{i=1}^2 \sum_{m=1}^M \Lambda_{i,m} \Lambda_{i,m}^H, \quad (41)$$

where $\Lambda_{i,m} = \sqrt{\varepsilon_{i,i,m,c}} \mathbf{w}_{i,i,m,c} + \Psi_R^H \tilde{\mathbf{a}}_{i,m}$.

The constraint condition $\theta_{R,l} \in [0, 2\pi)$ can be expressed in terms of the modulus of a complex exponential, where $|\phi_{R,l}| = |e^{j\theta_{R,l}}| = 1$. The formulation states that the magnitude of the complex number, represented as the exponential of a purely imaginary number $j\theta_{R,l}$, is equal to one. We can reframe the problem presented in (37) accordingly:

$$\begin{aligned} \min_{\Psi_R} \quad & f(\Psi_R) \\ \text{s.t.} \quad & C7: |\phi_{R,l}| = 1, \forall l = 1, \dots, L. \end{aligned} \quad (42)$$

We can see that the objective function $f(\Psi_R)$ is continuous and differentiable, the constraint condition is intrinsically non-convex. The optimization variables $\Psi_R(\phi) = [\phi_{R,1}, \dots, \phi_{R,L}]^H$ are on an L -dimensional Riemannian submanifold \mathcal{M}_{cc}^L , which can be defined by

$$\mathcal{M}_{cc}^L = \{\Psi_R \in \mathcal{C}^L \mid \phi_{R,1}^* \phi_{R,1} = \phi_{R,l}^* \phi_{R,l} = \phi_{R,L}^* \phi_{R,L} = 1\}, \quad (43)$$

where \mathcal{C}^L is a L -dimensional complex space [40].

We introduce the proposed RCG algorithm to solve the above optimization problem, which can effectively deal with non-convex optimization problems [15], [40]–[42]. The following are three basic steps of the proposed RCG algorithm:

1) *Calculate Riemannian Gradient*: Riemannian gradient is the fastest growing direction (tangent vector) of the objective function, which can be calculated by the orthogonal projection of the Euclidean gradient $\nabla f(\Psi_R)$ as follows:

$$\text{grad} f = \nabla f(\Psi_R) - \text{Re}\{\nabla f(\Psi_R) \circ \Psi_R^*\} \circ \Psi_R, \quad (44)$$

where $f(\Psi_R)$ is the Euclidean gradient, which is calculated

as

$$\begin{aligned} \nabla f(\Psi_R) = & \\ & - \sum_{m=1}^M 2 \left[\tilde{\mathbf{a}}_{1,m} \tilde{\mathbf{a}}_{1,m}^H \Psi_R + \tilde{\mathbf{a}}_{1,m} (\sqrt{\varepsilon_{1,1,m,c}} \mathbf{w}_{1,1,m,c})^H \right] \\ & - \sum_{m=1}^M 2 \left[\tilde{\mathbf{a}}_{2,m} \tilde{\mathbf{a}}_{2,m}^H \Psi_R + \tilde{\mathbf{a}}_{2,m} (\sqrt{\varepsilon_{2,2,m,c}} \mathbf{w}_{2,2,m,c})^H \right]. \end{aligned} \quad (45)$$

2) *Search Direction*: For the conjugate gradient (CG) method on manifolds, the tangent vector conjugate to $\text{grad}f$ is our search direction, which is formulated as

$$d = -\text{grad}f + \tau \Xi(\bar{d}), \quad (46)$$

where τ is the conjugate gradient update parameter, which changes with the number of iterations k . \bar{d} denotes the previous search direction, and the vector transport function $\Xi(\bullet)$ can be given by

$$\Xi(d) = d - \text{Re}\{d \circ \Psi_R^*\} \circ \Psi_R. \quad (47)$$

3) *Retraction*: In order to determine the next point on the complex circle manifold, we project the tangent vector back to the manifold itself, which is called retraction, and it can be represented as

$$(\Psi_R)_k \leftarrow \frac{(\Psi_R + \nu d)_k}{|(\Psi_R + \nu d)_k|}, \quad (48)$$

where ν is the Armijo step size.

We initialize $\Psi_{R,0}$ by using a heuristic method [41]. By relaxing the constraint condition $C7$ to $\|\Psi_R\|_2^2 = L$, the optimal solution of problem (42) can be written as

$$\hat{\Psi}_R^H = \frac{\sqrt{L} \sum_{i=1}^2 \sum_{m=1}^M \left(-\sqrt{\varepsilon_{i,i,m,c}} \mathbf{w}_{i,i,m,c} (\tilde{\mathbf{a}}_{i,m})^+ \right)}{2M}, \quad (49)$$

where $(\tilde{\mathbf{a}}_{i,m})^+$ is the pseudo-inverse matrix of $\tilde{\mathbf{a}}_{i,m}$.

By utilizing the proposed RCG algorithm, an optimal solution of Ψ_R for maximizing the effective channel power gain can be obtained. We can formulate the MRT precoding matrix according to (40), which can be rewritten as $\mathbf{P}_i = (\hat{\mathbf{p}}_{i,1}, \dots, \hat{\mathbf{p}}_{i,M})$. Thus, the solution of optimization problems (42) and (32) is obtained. The detailed process of RCG algorithm is shown in **Algorithm 1**, where the initial point $\Psi_{R,0}$ is given by $\hat{\Psi}_R / |\hat{\Psi}_R|$.

IV. INTERFERENCE MITIGATION DESIGN

A. Interference mitigation

We then optimize the transmission phase shifts of STAR-RIS elements to mitigate the interferences. In the proposed SSEIM design, the $(L \times 1)$ effective STAR-RIS transmission vector can be defined by

$$\Psi_T(\phi) = [\phi_{T,1}, \dots, \phi_{T,L}]^H = [e^{j\theta_{T,1}}, \dots, e^{j\theta_{T,L}}]^H. \quad (50)$$

Then, the interferences in (20) can be rewritten as

$$\begin{aligned} \hat{I}_{i,m,c} &= |I_{i,m,c} + \Psi_T^H \mathbf{V}_{i,m,c}|^2, \\ \hat{I}_{i,m,e} &= |I_{i,m,e} + \Psi_T^H \mathbf{V}_{i,m,e}|^2, \end{aligned} \quad (51)$$

Algorithm 1 The proposed RCG algorithm

Require: $L, M, \sqrt{\varepsilon_{1,1,m,c}} \mathbf{w}_{1,1,m,c}, \sqrt{\varepsilon_{2,2,m,c}} \mathbf{w}_{2,2,m,c}, \tilde{\mathbf{a}}_{1,m}, \tilde{\mathbf{a}}_{2,m}$

- 1: Initialize $k = 0, \Psi_{R,0} \in \mathcal{M}_{cc}^L, d_0 = \text{grad}f(\Psi_{R,0})$.
 - 2: **while** not converged **do**
 - 3: Choose Armijo step size ν_k .
 - 4: Calculate $\Psi_{R,k}$ according to (48): $\Psi_{R,k+1} = \frac{\Psi_{R,k} + \nu_k d_k}{|\Psi_{R,k} + \nu_k d_k|}$.
 - 5: Based on (44) and (45), compute the Riemannian gradient: $g_{k+1} = \text{grad}f(\Psi_{R,k+1})$.
 - 6: Determine vector transports $\Xi(g_k)$ and $\Xi(d_k)$ of gradient g_k and conjugate direction d_k according to (47).
 - 7: Compute conjugate gradient update parameters τ : $\tau = \frac{g_{k+1}^H g_{k+1}}{\bar{g}_k^H \bar{g}_k}$.
 - 8: Calculate the search direction d_{k+1} by (46).
 - 9: Update $k \leftarrow k + 1$.
 - 10: **end while**
 - 11: **return** $\Psi_R = \Psi_{R,k+1}$
-

where

$$\begin{aligned} \mathbf{V}_{i,m,c} &= \beta_T \sqrt{\varepsilon_{j,R,i,m,c}} \text{diag}(\mathbf{g}_{i,m,c}) \mathbf{F}_j \mathbf{P}_j \mathbf{1}_M, \\ \mathbf{V}_{i,m,e} &= \beta_T \sqrt{\varepsilon_{j,R,i,m,e}} \text{diag}(\mathbf{g}_{i,m,e}) \mathbf{F}_j \mathbf{P}_j \mathbf{1}_M. \end{aligned} \quad (52)$$

The objective function for IMB-sector is further reformulated as

$$y(\Psi_T) = \sum_{m=1}^M (\hat{I}_{1,m,c} + \hat{I}_{1,m,e}) + \sum_{m=1}^M (\hat{I}_{2,m,c} + \hat{I}_{2,m,e}), \quad (53)$$

which is continuous and differentiable. The constraint condition $\theta_{T,l} \in [0, 2\pi)$ can be equivalently expressed as the modulus of a complex exponential, where $|\phi_{T,l}| = |e^{j\theta_{T,l}}| = 1$. The phase shifts of STAR-RIS elements are confined to the unit circle in the complex plane. Therefore, the optimization problem in (33) is simplified as

$$\begin{aligned} \min_{\Psi_T} \quad & y(\Psi_T) \\ \text{s.t.} \quad & C8: |\phi_{T,l}| = 1, \quad \forall l = 1, \dots, L. \end{aligned} \quad (54)$$

By relaxing the constraint condition $C8$ to $\|\Psi_T\|_2^2 = L$, the optimal solution is given by

$$\hat{\Psi}_T^H = \frac{\sqrt{L} \sum_{i=1}^2 \sum_{m=1}^M \left(-I_{i,m,c} (\mathbf{V}_{i,m,c})^+ - I_{i,m,e} (\mathbf{V}_{i,m,e})^+ \right)}{2M}. \quad (55)$$

We still solve Ψ_T by the proposed RCG algorithm. The initial point $\Psi_{T,0} = \hat{\Psi}_T / |\hat{\Psi}_T|$. The Riemannian gradient, search direction and retraction are all calculated by using the similar method in (44), (46) and (48). We define $\nabla y(\Psi_T)$ as the Euclidean gradient of $y(\Psi_T)$, which can be given by

$$\begin{aligned} \nabla y(\Psi_T) &= \sum_{i=1}^2 \sum_{m=1}^M 2 (\mathbf{V}_{i,m,c} \mathbf{V}_{i,m,c}^H \Psi_T + \mathbf{V}_{i,m,c} (I_{i,m,c})^*) \\ &+ \sum_{i=1}^2 \sum_{m=1}^M 2 (\mathbf{V}_{i,m,e} \mathbf{V}_{i,m,e}^H \Psi_T + \mathbf{V}_{i,m,e} (I_{i,m,e})^*). \end{aligned} \quad (56)$$

B. User fairness analysis

After appropriately adjusting the precoding matrix of BSs, the phase shifts of STAR-RIS elements, we can obtain stronger channel gain and weaker interference. By utilizing the high SNR approximation in [37], the achievable rate of CEU in the m -th cluster is further expressed as

$$\hat{R}_{i,m,e} \approx \log_2\left(1 + \frac{\alpha_e^2}{\alpha_c^2}\right). \quad (57)$$

Adopting the fixed power allocation, when the power allocation factor of CCU reaches its maximum value, i.e. $\alpha_c = 1$ and $\alpha_e = 0$, the performance of the system is optimal. To ensure user fairness, it is necessary to dynamically adjust the power allocation factors based on the target rate of the CEU, i.e. $\hat{R}_{i,m,e} = R_{i,m,e}^*$. After algebraic transformation, the power allocation factors for CCU and CEU are obtained as follows:

$$\alpha_e^2 = \frac{2^{R_{i,m,e}^*} - 1}{2^{R_{i,m,e}^*}} \quad \text{and} \quad \alpha_c^2 = 1 - \alpha_e^2. \quad (58)$$

At this stage, the interference is effectively mitigated, the desired signal is enhanced, user fairness is ensured. All three sub-optimization problems have been resolved, yielding the solution to the optimization problem in (31). The detailed procedure is presented in **Algorithm 2**.

Algorithm 2 The proposed LSEM algorithm

Require: L, M , the target rate $R_{i,m,e}^*$,

the large-scale fading $\sqrt{\varepsilon_{1,1,m,c}}, \sqrt{\varepsilon_{2,2,m,c}}, \sqrt{\varepsilon_{1,1,m,e}}, \sqrt{\varepsilon_{2,2,m,e}}, \sqrt{\varepsilon_{1,2,m,c}}, \sqrt{\varepsilon_{2,1,m,c}}, \sqrt{\varepsilon_{1,2,m,e}}, \sqrt{\varepsilon_{2,1,m,e}}, \sqrt{\varepsilon_{1,R,1,m,c}}, \sqrt{\varepsilon_{2,R,2,m,c}}, \sqrt{\varepsilon_{1,R,1,m,e}}, \sqrt{\varepsilon_{2,R,2,m,e}}$,
the small-scale fading channel matrix $\mathbf{w}_{1,1,m,c}, \mathbf{w}_{2,2,m,c}, \mathbf{w}_{1,1,m,e}, \mathbf{w}_{2,2,m,e}, \mathbf{w}_{1,2,m,c}, \mathbf{w}_{2,1,m,c}, \mathbf{w}_{1,2,m,e}, \mathbf{w}_{2,1,m,e}$,
 $\mathbf{g}_{1,m,c}, \mathbf{g}_{2,m,c}, \mathbf{g}_{1,m,e}, \mathbf{g}_{2,m,e}, \mathbf{F}_1, \mathbf{F}_2$,
the reflected amplitude coefficient β_R and the transmitted amplitude coefficient β_T .

- 1: Compute $\hat{\mathbf{a}}_{1,m}$ and $\hat{\mathbf{a}}_{2,m}$,
 - 2: Initialize $k = 0, \Psi_{R,0} \in \mathcal{M}_{cc}^L$,
calculate $\mathbf{d}_0 = \text{grad}f(\Psi_{R,0})$,
 - 3: Calculate Ψ_R based on **Algorithm 1**.
 - 4: Compute the MRT beamforming vector $\hat{\mathbf{p}}_{i,m}$ based on (40),
 - 5: Calculate the MRT precoding matrix $\mathbf{P}_i = (\hat{\mathbf{p}}_{i,1}, \dots, \hat{\mathbf{p}}_{i,M})$.
 - 6: Compute the effective inter-cell interference $D_{1,m,c}, D_{1,m,e}, D_{2,m,c}, D_{2,m,e}$,
 - 7: Calculate the inter-cluster interference $B_{1,m,c}, B_{1,m,e}, B_{2,m,c}, B_{2,m,e}$,
 - 8: Compute the interference reflected by STAR-RIS $Q_{1,m,c}, Q_{1,m,e}, Q_{2,m,c}, Q_{2,m,e}$,
 - 9: Calculate all interference $I_{1,m,c}, I_{1,m,e}, I_{2,m,c}, I_{2,m,e}$ by (19).
 - 10: Compute $\mathbf{V}_{1,m,c}, \mathbf{V}_{1,m,e}, \mathbf{V}_{2,m,c}, \mathbf{V}_{2,m,e}$ by (52),
 - 11: Initialize $\hat{k} = 0, \Psi_{T,0} \in \mathcal{M}_{cc}^L$,
calculate $\hat{\mathbf{d}}_0 = \text{grad}y(\Psi_{T,0})$,
 - 12: Calculate Ψ_T based on **Algorithm 1**.
 - 13: Calculate the power allocation factors α_c^2 and α_e^2 by (58).
 - 14: **return** $\Psi_R, \Psi_T, \mathbf{P}_1, \mathbf{P}_2, \alpha_c^2, \alpha_e^2$.
-

TABLE I:

Compare the computational complexity of the proposed RCG algorithm with the majorization-minimization algorithm and the semidefinite relaxation algorithm.

Mode	Computational Complexity
semidefinite relaxation algorithm [41]	$O((L+1)^6)$
majorization-minimization algorithm [46]	$O(L^3)$
the proposed RCG algorithm	$O(L^{1.5})$

Based on **Algorithm 2**, we can calculate the achievable rate of all users. Furthermore, the SE of the cellular MISO-NOMA networks can be computed as follows

$$SE_i = \sum_{m=1}^M \left(\hat{R}_{i,m,c} + \hat{R}_{i,m,e} \right). \quad (59)$$

Since L passive STAR-RIS elements serve two cells at the same time, only STAR-RIS phase shifter needs power supply [43], [44], and the total dissipation power in two cells can be modeled as

$$P_e = 2(p\varepsilon_b + 2MP_U + P_{B,s}) + LP_L, \quad (60)$$

where p is the transmit power of BS, ε_b is the power amplifier efficiency of BS. $2P_U$ is the total power consumption at CCU and CEU in cluster m of cell i , the circuit power consumption at the BS is $P_{B,s}$. P_L is the circuit power consumption of each STAR-RIS controller. Then, we can express the EE as $EE = \frac{SE_1 + SE_2}{P_e}$.

C. Analysis of algorithm complexity and convergence

We propose a LSEM algorithm that utilizes two consecutive RCG algorithms, which effectively address the optimization problem in (31). Based on Theorem 4.3.1 cited in [45], it is demonstrated that both **Algorithm 1** and **Algorithm 2** converge to a critical point. Table I provides a comparative analysis of computational complexities. In the worst-case scenario, the computational complexity of the proposed RCG algorithm is $O(L^{1.5})$. In comparison, **Algorithm 1** exhibits substantially lower computational complexity than both the semidefinite relaxation and majorization-minimization algorithms.

V. NUMERICAL RESULTS

To validate the effectiveness of the proposed STAR-RIS assisted SSEIM design, numerical results are presented in this section. The simulation parameters are shown in Table II. Specifically, the direct link from BS to users is complex with many obstacles, resulting in the relatively large path loss exponent α_1 and α_2 . In order to improve the performance of cellular MISO-NOMA system, the signal can propagate more smoothly with fewer surrounding obstacles in the STAR-RIS link, thereby resulting in smaller α_3 and α_4 [47]. Accordingly, the direct link has abundant multipath signals, which results in a very small Rician factor \mathcal{K}_1 , whereas the larger Rician factor

of STAR-RIS \mathcal{K}_2 and \mathcal{K}_3 [21]. All the simulation results are averaged over 2×10^3 independent small-scale fading channel realizations.

TABLE II: Simulation parameters.

Target rate of the CEU	$R_{i,m,e}^* = 1.3$ bits/s/Hz [48]
Rician fading factor	$\mathcal{K}_1 = 1, \mathcal{K}_2 = 2, \mathcal{K}_3 = 3$ [21]
Distances	$d_{i,i,m,c} = 30\text{m}, d_{i,i,m,e} = 60\text{m},$ $d_{i,j,m,c} = 120\text{m}, d_{i,j,m,e} = 90\text{m},$ $d_{i,R} = 70\text{m}, d_{R,j,m,c} = 50\text{m},$ $d_{R,j,m,e} = 15\text{m}$
Path loss exponent	$\alpha_1 = \alpha_2 = 3.7, \alpha_3 = 3, \alpha_{4,c} = 2.5,$ $\alpha_{4,e} = 2.3$ [47]
Correlation coefficients	$r_d = 0, r_R = 0.5, r_{R,u} = 0.6$
Horizontal or vertical AoA/AoD	$\vartheta_R = \frac{\pi}{4}, \vartheta_{R,u,c} = \frac{\pi}{3}, \vartheta_{R,u,e} = \frac{\pi}{6}$
Number of STAR-RIS elements	$L = L_v L_h = 32 \times 32 = 1024$
Carrier frequency	$f = 2.4$ GHz
Transmission bandwidth	$BW = 1$ MHz
AWGN power	$\sigma^2 = -174 + 10 \log_{10}(BW)$ dBm
Number of transmit antennas	$M = 2$

In order to better illustrate the performance gain of our proposed STAR-RIS assisted SSEIM design, we also evaluate the performance of the following 4 baseline schemes:

- **Baseline 1 (RIS-aided SEB design):** We set $\beta_R = 1$ and $\beta_T = 0$. At this point, the STAR-RIS becomes a conventional reflecting-only RIS. In the cellular communication system, only the reflection of RIS can be utilized to enhance the desired signal.
- **Baseline 2 (RIS-aided IMB design):** We set $\beta_R = 0$ and $\beta_T = 1$. At this point, the STAR-RIS becomes a conventional transmitting-only RIS. In the cellular communication system, only the transmission of RIS can be utilized to mitigate the interferences.
- **Baseline 3 (random STAR-RIS):** The transmission and reflection phase shifts of STAR-RIS are obtained through random initialization.
- **Baseline 4 (without STAR-RIS):** In this case, there is no STAR-RIS in the MISO-NOMA cellular networks.

To better demonstrate the performance advantages of MRT precoding matrix, the following two precoding strategies are introduced:

- **Identity precoding matrix:** The signals are transmitted without any precoding adjustments.
- **ZF precoding matrix:** ZF precoding ensures that the signals intended for different users are orthogonal, which is designed to eliminate inter-user interference [49], [50].

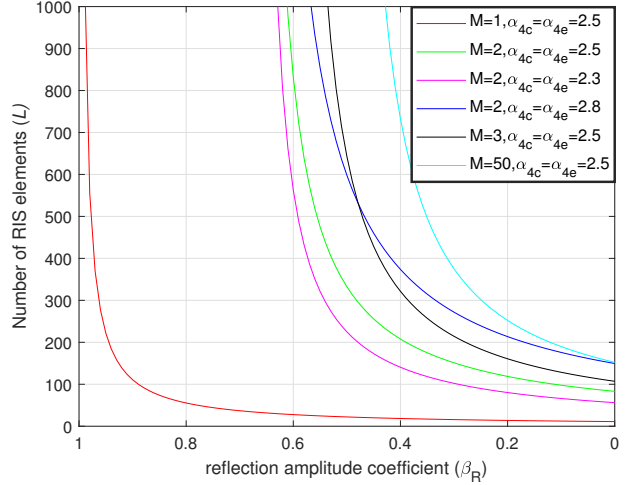


Fig. 2: Minimal required number of STAR-RIS elements for interference mitigation.

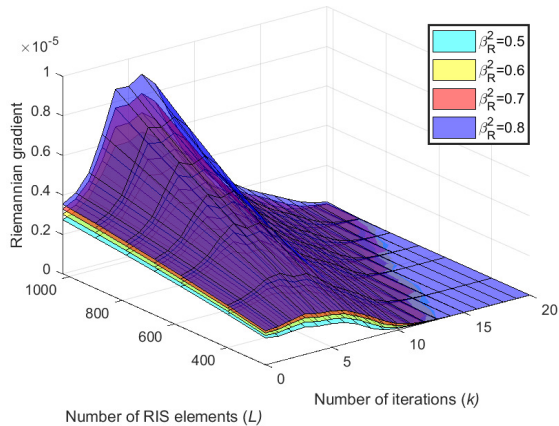
1) Minimal required number of STAR-RIS elements:

We study the minimal required number of STAR-RIS elements versus reflection amplitude coefficient with different numbers of TAs in Fig. 2, where the theoretical expression is derived in **Lemma 1**. As the reflection amplitude coefficient increases, we observe that the minimal required number increases rapidly to infinity. Besides, there is an upper bound of the reflection coefficient, which depends on the number of TAs. As the number of TAs increases, the upper bound value decreases. When the number of TAs is infinite, the upper bound is close to 0.5. When the reflection amplitude coefficient reaches the upper bound, no matter how many STAR-RIS elements are deployed, the interferences cannot be completely eliminated.

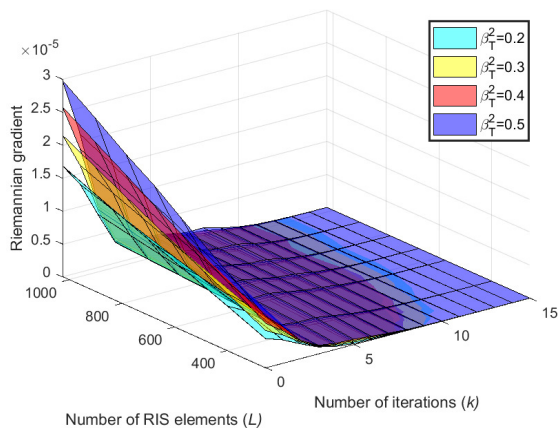
2) Convergence of the proposed RCG algorithm:

Fig. 3 presents a convergence analysis of the proposed RCG algorithm. Specifically, Fig. 3(a) illustrates the algorithm convergence when applied to solving the STAR-RIS reflection vector Ψ_R , while Fig. 3(b) demonstrates the convergence for the effective STAR-RIS transmission vector Ψ_T . The x-axis denotes the number of iterations, the y-axis represents the number of STAR-RIS elements, and the z-axis displays the Riemannian gradient of the objective function. The algorithm is considered to have converged when the Riemannian gradient falls below 10^{-6} .

As the number of STAR-RIS elements increases, the required number of iterations for algorithm convergence increases. As the reflection power coefficient β_R^2 of STAR-RIS increases, the required number of iterations for convergence of the RCG algorithm solving the STAR-RIS reflection vector increases. In the process of optimizing Ψ_R , the gradient of the objective function initially increases and subsequently decreases. Consequently, the algorithm convergence for SEB sector demands a higher number of iterations. Fig. 3 illustrates that algorithm convergence for the IMB sector requires about 10 iterations, while the SEB sector necessitates between 10 and 20 iterations to achieve convergence. It is associated



(a) SEB sector



(b) IMB sector

Fig. 3: Convergence of the proposed RCG algorithm with different number of STAR-RIS elements.

with the initial values selected for the algorithm. When the initial values of the optimization variables are close to the optimal solution, the algorithm requires fewer iterations to converge. Overall, the proposed RCG algorithm demonstrates strict convergence with a relatively low number of iterations needed.

3) Impact of the number of STAR-RIS elements:

In Fig. 4, we assess the impact of the number of STAR-RIS elements on the achievable rate, maintaining the transmit power at a constant 0 dBm. Note that as the number of STAR-RIS elements increases, the achievable rate of the CCU also increases. However, with the increase of STAR-RIS elements, the achievable rate of the CEU remains relatively constant. The phenomenon suggests that we can improve the SINR of the CCU by increasing the number of STAR-RIS elements, and thus improve the achievable rate of the CCU. However, the achievable rate of the CEU is determined primarily by the NOMA power allocation factors, which is independent of both the number of STAR-RIS elements and their reflection power coefficient. Furthermore, an analysis of the three solid lines in the figure reveals that the reflection and transmission power coefficient of STAR-RIS elements have a significant influence

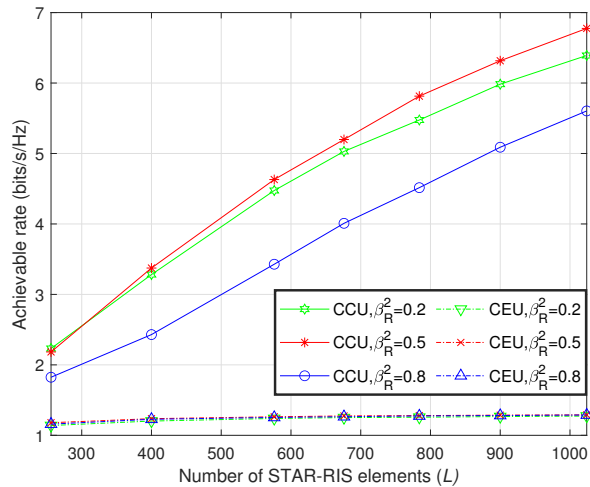


Fig. 4: Achievable rate versus the number of STAR-RIS elements.

on the proposed SSEIM design. Notably, when the reflection power coefficient of STAR-RIS is set at 0.8, the achievable rate for the CCU is substantially reduced.

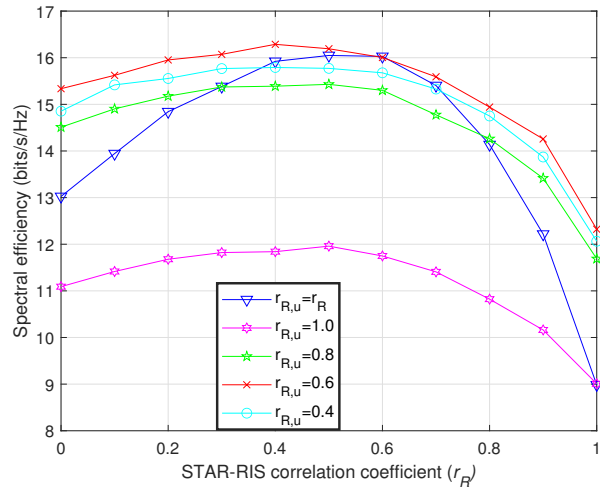


Fig. 5: SE versus the correlation coefficient when $\beta_R^2 = 0.5$.

4) Impact of the correlation coefficients:

Fig. 5 illustrates the spectral efficiency of STAR-RIS assisted cellular MISO-NOMA network versus the correlation coefficients $r_{R,u}$ and r_R . As the correlation coefficient of STAR-RIS r_R increases, SE initially shows an increase. It is because that a moderate increase in the STAR-RIS correlation coefficient r_R makes the phase adjustment more regular. Therefore, it is very necessary to miniaturize RIS array [22]. However, beyond a certain point, further increases in r_R lead to a decline in SE. It is due to the fact that the augmented spatial correlation lessens the spatial diversity [23]. Furthermore, Fig. 5 shows that as the correlation coefficient from STAR-RIS to users $r_{R,u}$ increases, the spectral efficiency continuously declines. Due to the restrictions on the possible phase shifts of STAR-RIS elements and the signal adjustment

of users, we observe an extremely poor spectral efficiency [24]. The analysis highlights the critical impact of correlation coefficients on the performance of spectral efficiency.

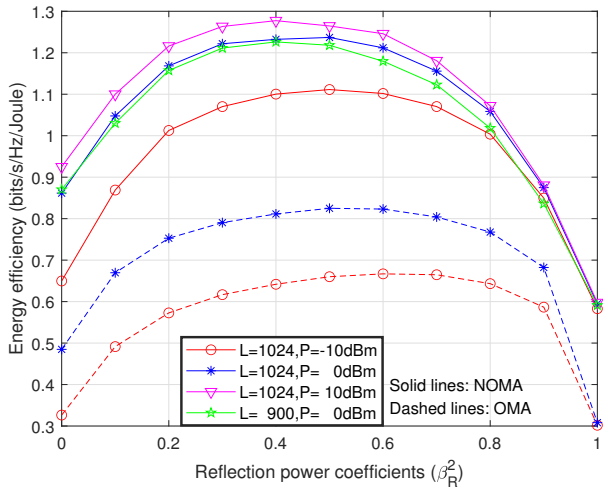


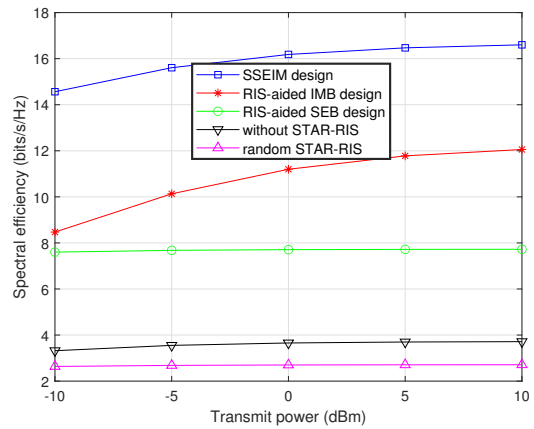
Fig. 6: EE versus the reflection power coefficients with different transmit power of BSs and different number of STAR-RIS elements, where the static power of users $P_U = 10\text{dBm}$, the static power of BS $P_{B,s} = 9\text{dBW}$, the amplifier efficiency at BS $\varepsilon_b = 1.2$.

5) Impact of the reflection coefficients:

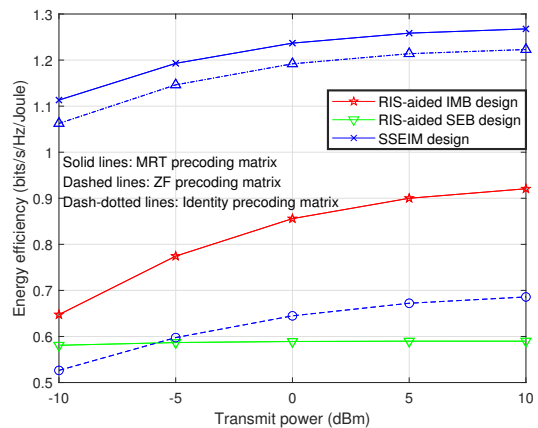
We focus on the energy efficiency in relation to the reflection power coefficient, as illustrated in Fig. 6. As the reflection power coefficient increases, the system's energy efficiency initially rises rapidly, then stabilizes, and eventually declines sharply. Because the MRT precoding matrix optimizes the active beamforming at BSs, high energy efficiency is achieved when the reflection power coefficient of STAR-RIS elements is within an optimal range $\beta_R^2 \in [0.2, 0.7]$. In view of Fig. 2, it is clear that there is a trade-off between the SEB-sector and IMB-sector. The optimal reflection coefficient is not necessarily capable of completely mitigating interference. Additionally, the blue curve above the green curve demonstrates that the energy efficiency improves as the number of STAR-RIS elements increases. The pink curve at the highest position indicates that a higher transmit power leads to greater energy efficiency. Furthermore, it can be known by comparing the dashed curves and the solid curves in Fig. 6 that the system energy efficiency of the SSEIM design in the NOMA network is superior to that of the OMA network. Based on (59) and (60), we can adopt an appropriate number of STAR-RIS elements, employ technologies like deep sleeping and sub-frame silence to achieve energy conservation in wireless networks without affecting system performance [20].

6) Compare with different baseline schemes:

Fig. 7(a) investigates the spectral efficiency of the proposed SSEIM design in comparison with four benchmark schemes: RIS-aided SEB design, RIS-aided IMB design, no STAR-RIS and random STAR-RIS. The blue curve at the highest position indicates that the proposed STAR-RIS assisted SSEIM design achieves significantly higher spectral efficiency than other



(a) SE versus the transmit power.



(b) EE versus the transmit power.

Fig. 7: Different baseline schemes in the case of the reflection power coefficient of STAR-RIS $\beta_R^2 = 0.5$, the number of STAR-RIS elements $L = 1024$.

baseline schemes, demonstrating its superior performance over traditional approaches. From Fig. 7(a), we can also draw the following conclusions: i) As the transmit power of BSs increases, the spectral efficiency of both the proposed SSEIM design and RIS-aided IMB design continually increases. However, the spectral efficiency of RIS-aided SEB design does not change significantly with increasing transmit power; ii) The STAR-RIS assisted design outperforms the design without STAR-RIS; iii) If the phase shifts of STAR-RIS elements are random, its performance is the worst; iv) In the STAR-RIS assisted cellular MISO-NOMA network using the MRT precoding matrix, the performance of RIS-aided IMB design is better than that of RIS-aided SEB design.

Utilizing the same parameters as above, Fig. 7(b) compares the energy efficiency of different baseline schemes and precoding strategies. Considering the MRT precoding matrix, ZF precoding matrix and identity precoding matrix, the solid blue line is significantly higher than the dashed and dotted lines. It indicates that the proposed MRT precoding matrix, which jointly optimizes the active beamforming at BSs and the passive beamforming of the STAR-RIS, achieves higher

energy efficiency than the ZF and identity precoding matrices. Additionally, the blue curve is much higher than the green and red curves, demonstrating that the proposed SSEIM design has a performance advantage, achieving higher energy efficiency than other baseline schemes. In summary, the SSEIM design based on the MRT precoding matrix exhibits the most superior energy efficiency performance.

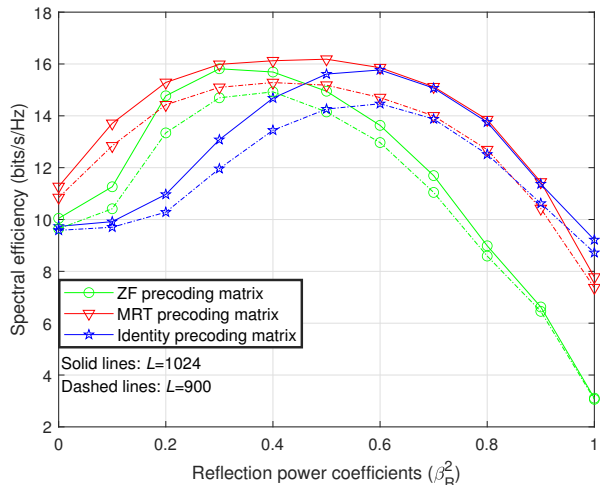


Fig. 8: SE versus the reflection power coefficients with different transmit power, different number of STAR-RIS elements as well as different precoding matrices.

7) Compare with different precoding matrices:

We plot the curves of system spectral efficiency versus the reflection power coefficient of STAR-RIS elements with different precoding matrices in Fig. 8. The solid lines consistently being above the dashed lines indicate that the spectral efficiency of the proposed SSEIM design improves as the number of STAR-RIS elements increases. No matter which precoding strategy is used, as the reflection power coefficient of STAR-RIS elements increases from 0 to 1, the system spectral efficiency first rises and then falls. When the reflection power coefficient reaches a specific value, the spectral efficiency attains its optimal level. By comparing the different colored curves, it can be seen that when using the MRT precoding matrix, the required reflection power coefficient to achieve optimal spectral efficiency falls within a range $\beta_R^2 \in [0.2, 0.8]$. Due to the active beamforming weights at BSs, the SE can maintain stability within this range. In contrast, when using the ZF precoding matrix and the identity precoding matrix, the required reflection power coefficient is a specific value. When the reflection power coefficient $\beta_R^2 \approx 0.3$ for the ZF precoding matrix or the reflection power coefficient $\beta_R^2 \approx 0.6$ for the identity precoding matrix, the desired signals are enhanced substantially and the interference signal is mitigated effectively, the SE reaches the peak value and the reflection coefficient reaches the optimal value. With further increasing of β_R , the SINR is dominated by the interference signals. At present, the interference can not be effectively mitigated.

Based on the above simulation results, two remarks are concluded.

Remark 1. Compared to the RIS-aided SEB and IMB designs, the proposed SSEIM design has the best performance on both spectral efficiency and energy efficiency, which demonstrates the superiority of the proposed SSEIM design.

Remark 2. The proposed SSEIM-aided network with MRT precoding matrix outperforms the SSEIM-aided network with the identity precoding matrix and ZF precoding matrix. It indicates that the MRT precoding matrix can reduce the limitations on the reflection and transmission coefficients of STAR-RIS in practical engineering.

VI. CONCLUSION

In this paper, we proposed a novel dual-sided STAR-RIS-assisted SSEIM design for the multiuser MISO-NOMA downlink cellular networks. Around the objective of maximizing the system spectral efficiency, we jointly optimized the transmission and reflection phase shifts at the STAR-RIS, the precoding matrix of BSs, and the power allocation factors of NOMA users. Specifically, we first maximized the effective channel power gain, and then minimized the interferences. Finally, we optimized the NOMA power allocation factors based on the target data rates. We proposed a LSEM algorithm, where both the non-convex unit modulus constraint subproblems were solved by the RCG algorithm. Numerical results illustrated that the STAR-RIS-assisted SSEIM design can significantly improve the SE and EE of the cellular MISO-NOMA networks. We also demonstrated that the MRT precoding matrix has the best performance compared to other precoding strategies. However, in practical scenarios, due to the constraints of factors like buildings and terrain, it is not easy to find a suitable deployment location. In addition, the protocols of existing communication systems need to be modified or optimized to make them compatible with STAR-RIS in order to achieve seamless integration and application. This is also the direction of our future research.

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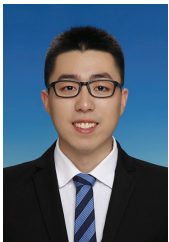
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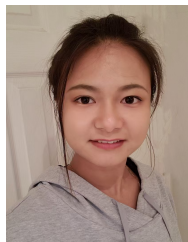
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