

1 **Multi-objective optimization of engineered cementitious composite**
2 **based on machine learning and generative adversarial network**

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49 **Abstract:** This study aims to establish a novel framework for mixture design
50 optimization of engineered cementitious composite (ECC) by first collecting two
51 original datasets of ECC's tensile stress and strain from the extensive and credible
52 literature. The datasets comprise a wide range of variables including cementitious
53 ingredients, 9 types of fiber and characteristics, admixtures, and experimental
54 conditions. The data augmentation is then performed using a tuned constraints-modified
55 Conditional Tabular Generative Adversarial Network (Tuned-CTGAN) to increase the
56 model accuracy and generalizability. The fitness functions of tensile stress and strain
57 are established based on four machine learning models with the hyperparameters tuned
58 by the Hunger Games search (HGS) algorithm. After the data augmentation, the values
59 of R^2 in their test sets are increased from 0.874 to 0.925 and from 0.772 to 0.889,
60 respectively. Subsequently, the third objective function (cost) is computed by
61 polynomials and four classes of constraints (Min-max, volume, ratio, and fiber) are set
62 up to define the variable's search space. A non-dominated sorting genetic algorithm
63 based on reference-point strategy (NSGA-III) is introduced to optimize the mixture
64 proportions of ECC by simultaneously optimizing tensile stress, tensile strain, and cost.
65 This paper combines the results of data augmentation, model prediction, and multi-
66 objective optimization for complex ECC design, which aims to provide a basis for
67 practical application.

68 **Keywords:** engineered cementitious composite; machine learning; generative
69 adversarial network; multi-objective optimization

70 1. Introduction

71 Engineered Cementitious Composite (ECC) is a strain-hardening cementitious
72 material recognized for its high tensile strength and ductility. When fibers are evenly
73 dispersed in the composite matrix and their volume is kept below 2%, ECC exhibits
74 strain-hardening behavior with multi-cracks under 100 μ m. ECC's tensile strength
75 typically ranges from 4 to 20 MPa, with a tensile strain capacity between 3 and 12%
76 [2]. The tensile properties of ECC are significantly influenced by the mixture design
77 and fiber types. The choice of fibers such as polyethylene fiber (PE), polyvinyl alcohol
78 fiber (PVA), polypropylene fiber (PP), and steel fiber (SF) and their specific properties
79 (strength, diameter, length, Young's modulus, oil coating) significantly affect ECC's
80 performance. For instance, PVA-ECC can reach a tensile strain of 5%, while PE-ECC
81 may achieve up to 13% [2, 3]. Determining the optimal mix for ECC to meet specific
82 tensile strength and strain poses a major challenge, mainly due to the dependence on
83 trial-and-error methods. Moreover, classical micro-mechanical design theories for ECC
84 can exhibit whether a mix exhibits strain hardening, while it fails to provide targeted
85 parameters [4, 5].

86 Nowadays, the rise of artificial intelligence (AI) and Machine Learning (ML) has
87 revolutionized the design process. Advanced ML models, such as neural networks
88 (ANN), support vector regression (SVR), and tree-based models, are now frequently
89 used to accurately predict concrete properties [6-8]. For instance, Shariati, Armaghani,
90 et al. (2021) [9] effectively used ANN and Extreme Learning Machine (ELM) to predict
91 the strength of concrete containing additives, while Feng et al. (2020) [10] leveraged
92 an adaptive boosting algorithm for greater predictive accuracy. The eXtreme Gradient
93 Boosting (XGBoost) algorithm, developed by Chen and Guestrin, represents a
94 significant advancement in the realm of gradient boosting machines [11]. It is

95 particularly effective in mitigating overfitting while enhancing computational
96 efficiency. Hunger Games Search (HGS) is an advanced meta-heuristic algorithm
97 inspired by the concept of 'Hunger-Driven Motivational State Competition', as first
98 introduced by Yang, Chen et al. [12]. In this study, the HGS algorithm is selected for
99 ML hyperparameter adjustment.

100 ML models in ECC design also suffer from limited generalization due to small
101 databases, as evident in Huynh et al.'s 2020 study on predicting geopolymer concrete
102 strength [13]. A potential solution is data augmentation using Generative Adversarial
103 Networks (GAN), an advanced algorithm based on the theory of a two-player game
104 (discriminator D and the generator G) [14]. While GANs have been extensively used
105 in computer vision, particularly for image generation, their application in augmenting
106 concrete datasets is still limited [15, 16]. Conditional Tabular GAN (CTGAN), a GAN-
107 based model, is particularly designed for synthesizing tabular data. CTGAN addresses
108 data imbalance in databases by using variational Gaussian mixture models for
109 continuous features and conditional generation for discrete ones. Therefore, the
110 generalization and accuracy of ML models are predicted to be improved by introducing
111 a Tuned-CTGAN model which is specifically designed for the ECC dataset. To
112 optimize multiple objectives under highly nonlinear constraints, a non-dominated
113 sorting genetic algorithm based on reference-point strategy (NSGA-III) was first
114 introduced by Deb and Jain (2014) [17]. This study proposed NSGA-III to optimize the
115 mixture proportions of ECC by simultaneously optimizing tensile stress, tensile strain,
116 and cost.

117 This study introduces a novel framework integrating Tuned-CTGAN for ECC data
118 augmentation, HGS optimized ML models for performance prediction, and multi-
119 objective optimization via NSGA-III for ECC design optimization. Through enhancing

120 model accuracy and enabling precise ECC mixture formulation, this study is expected
121 to contribute to the application of AI techniques to ECC, providing valuable insights
122 and practical tools for optimizing ECC mixtures with improved performance and cost-
123 effectiveness.

124 **2. Literature review and comparative analysis**

125 The adoption of AI techniques for predicting and optimizing the properties of ECC has
126 been significantly developed. This literature review synthesizes key contributions
127 between 2018-2024, highlighting the diverse approaches and outcomes in this domain,
128 as shown in [Table 1](#). It covers a diverse range of fiber materials, such as PVA, PE, and
129 steel fibers, each selected for their potential to enhance specific aspects of ECC
130 performance. The focus of ECC research has predominantly been on enhancing tensile
131 strength and ductility [\[18-20\]](#). The additional ECC properties such as self-healing
132 capacity (SC), freeze-thaw resistance (FR), and chloride ion permeability (CP) are also
133 gaining attention [\[21, 22\]](#).

134 Recent research has explored a variety of ML algorithms, including Random Forest
135 (RF), Support Vector Machine (SVM), and eXtreme Gradient Boosting (XGBoost). For
136 instance, Uddin, Shanmugasundaram [\[23\]](#) employed multiple ML techniques to predict
137 the compressive strength and tensile strain of ECC. The capability of ECC for self-
138 healing was modeled using ensemble ML algorithms by Alabduljabbar, Khan [\[24\]](#),
139 showcasing the potential of AI in enhancing the durability aspects of ECC. The
140 inclusion of hybrid and advanced ML models has also been noteworthy. [Tanyildizi \[25\]](#)
141 utilized hybrid deep learning models to predict the compressive strength of nano-silica-
142 modified ECC under high temperatures. Moreover, invertible neural networks (INNs)
143 was applied by Yu, Weng [\[5\]](#) for the performance-based design of ECC mixtures,
144 illustrating a novel approach to ECC formulation that aligns with specific mechanical

145 and sustainability requirements. However, only one group of mixture design can be
 146 obtained by one output. Besides, response surface methodology was also used to assess
 147 the importance of variables and optimize the mixture design of ECC [26-28].
 148 However, few studies focused on the data treatment before applying the ML or DL
 149 methods. According to the authors' review, Mahjoubi, Barhemat [19] utilized a decision
 150 tree algorithm based on the isolated forest method to remove anomalous data. Guo,
 151 Meng [29] conducted the Principal Component Analysis and Semi-empirical model to
 152 enlarge the database. A commonly used method in other publications is data
 153 normalization, which indicates that the data treatment research is limited. Therefore, to
 154 fill this gap, this study attempted to introduce a tuned-CTGAN model specifically
 155 designed for ECC to enlarge the raw database, enabling the training of more generalized
 156 and robust models. This approach is novel within the ECC optimization domain and
 157 allows for a better understanding of ECC's complex behavior. Besides, the majority of
 158 the research concentrates on a limited range of fiber types, predominantly PVA and steel
 159 fibers, without extensive analysis across a broader spectrum. This study investigated 9
 160 different fiber types and collected around 400 data points for both tensile strength and
 161 tensile strain.

162 In summary, while existing studies have laid a solid foundation in the application of AI
 163 for enhancing ECC's properties, this research introduces data augmentation method,
 164 optimization strategies, various fiber types, and large database that further the
 165 capabilities of AI in this field.

166 **Table 1.** The literature review and comparative analysis of recent ECC researches

Fiber type of ECC	Investigated properties and data points	Data treatment	ML prediction	Optimization design	References	Year
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9 fiber types (PP, PVA, etc.)	TS (429), TSt (392)	Tuned-CTGAN	HGS-XGBoost, Gradient Boosting Regressor, RF, SVR	NSGA-III	This study	2024
PVA, PE, PP, basal, glass fiber	CS (180), TSt (105)	-	RF, SVM, XGBoost, light gradient boosting machine, CatBoost, natural gradient boosting, MEMD-ADE-SVM	-	[23]	2024
PVA fiber	CS (100)	-	AE-ELM, AE-DT	-	[25]	2024
Not specified	SC (617)	-	AR, DT, BR	-	[24]	2023
PE fiber	TS (129), TSt (129)	-	ANN	INNs	[5]	2023
Not specified	SC (619)	-	SVM, XGBoost, RF	-	[30]	2023
Steel fibers (twisted, hooked, and smooth fibers)	TS (103), TSt (103)	-	ANN	-	[31]	2023
Steel fibers (straight, hooked-end, and spiral geometric)	Pull-out force and slip (382)	-	ANN	-	[32]	2023
Not specified	CS (182), TS (97), FS (50)	-	GEP	-	[20]	2023
PVA fiber	CS, TS, TSt, FS, EM, PR, DS (13)	-	RSM	RSM	[27]	2023
Polyacrylonitrile fiber	FR, CP (36)	-	RSM	NSGA-III	[28]	2023

PVA fiber	SC (617)	-	LR, ANN, CART, SVM, ensemble methods (bagging, AdaBoost, and stacking)	-	[21]	2023
Not specified	SC (617)	-	BR, SR	-	[22]	2023
PVA Fiber	CS (89)	-	ANN	-	[33]	2022
PVA fiber	CS (79), TS (36)	-	ANN	-	[34]	2022
PVA fiber	CS (151), FS (76), TS-TSt (44)	-	ANN	-	[35]	2022
PVA fiber	CS, FS, TS, TC (16)	-	RSM	RSM	[26]	2021
PVA, PP, PE, and steel fiber	CS (264), TS (244), TSt (237)	A decision tree algorithm based on the isolated forest method to remove anomalous data	SVM, AR, XGBoost	UNSGA-III and NSGA-III	[19]	2021
10 fiber types (PP, PVA, etc.)	TS (284), TSt (293), FS (189), FSt (166), CS (313), etc.	-	FDNN	-	[36]	2021
Chopped fiber	CS (387), TS (387), TSt (387)	Principal Component Analysis + Semi-empirical model	ANN, SVM, CART, XGBoost	-	[29]	2021
Steel fiber	CS (220), FS (220)	-	9 ML (RF, AR, etc.)	-	[37]	2021
PVA fiber	TS (36), TSt (36)	-	ANN	Numerical analysis	[18]	2019

	CS (24), TS					
PVA, steel	(44), FS	-	ANN	-	[38]	2018
fiber	(47), TSc					
	(54)					

167 Note: the abbreviation is as follows:

168 Algorithms: Random forest (RF), support vector machine (SVM), eXtreme Gradient
169 Boosting (XGBoost), categorical gradient boosting (CatBoost), AdaBoost regressor
170 (AR), decision tree (DT), bagging regressor (BR), Artificial neural networks (ANN),
171 gene expression programming (GEP), response surface methodology (RSM), linear
172 regression (LR), classification and regression tree (CART), stacking regressor (SR),
173 forest deep neural network (FDNN), autoencoder (AE), extreme learning machine
174 (ELM), multivariate empirical modal decomposition (MEMD), adaptive differential
175 evolution (ADE), Invertible neural networks (INNs), Unified NSGA-III (UNSGA-III).
176 Properties: compressive strength (CS), tensile strength (TS), tensile strain (TSt),
177 flexural stress (FS), flexural strain (FSt), self-healing capacity (SC), elastic modulus
178 (EM), Poisson’s ratio (PR), drying shrinkage (DS), Freeze–thaw resistance (FR),
179 chloride ion permeability (CP).

180 3. Database description

181 To accurately predict the generalized properties of ECC, it is imperative to
182 assemble a meticulously curated comprehensive database. This database must
183 encompass a broad spectrum of key variables, reflecting a general distribution. Its
184 establishment is grounded in the utilization of existing datasets coupled with an
185 extensive review of contemporary literature. This process adheres to stringent criteria
186 to ensure the reliability and relevance of the data included [3, 36, 39-92]:

187 (1) The literature references the use of Ordinary Portland Cement in producing
188 ECC;

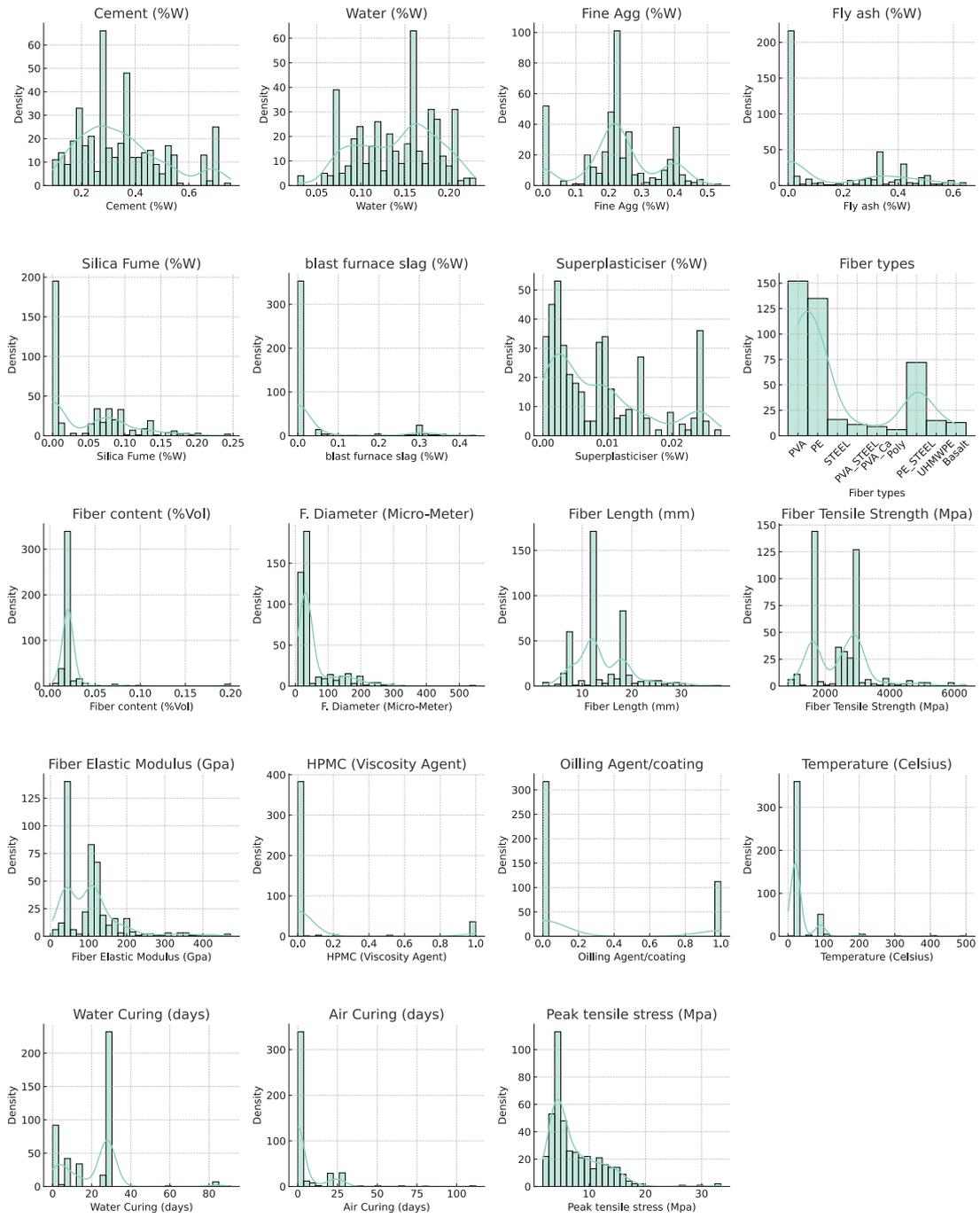
189 (2) For fine or coarse aggregates, natural aggregates with proper size distribution
190 are chosen over types like lightweight aggregate;

191 (3) To ensure data reliability, references are drawn from authoritative international
192 journals;

193 (4) The characteristics of fibers and other admixtures are clearly stated.

194 The database comprehensively records 18 ECC features and 2 outputs, namely
195 tensile stress and strain. The features fall into four main categories: main ingredients of
196 mortar normalized to a total weight of 1, including elements like cement, water, and fly
197 ash; fiber characteristics such as fiber type, volume proportion, and diameter;
198 admixtures including superplasticizer, viscosity agent, and oiling agent; and
199 experimental conditions covering aspects like temperature, water curing days, and air
200 curing days. The distribution plots of these features and output are depicted in [Figure](#)
201 [1](#).

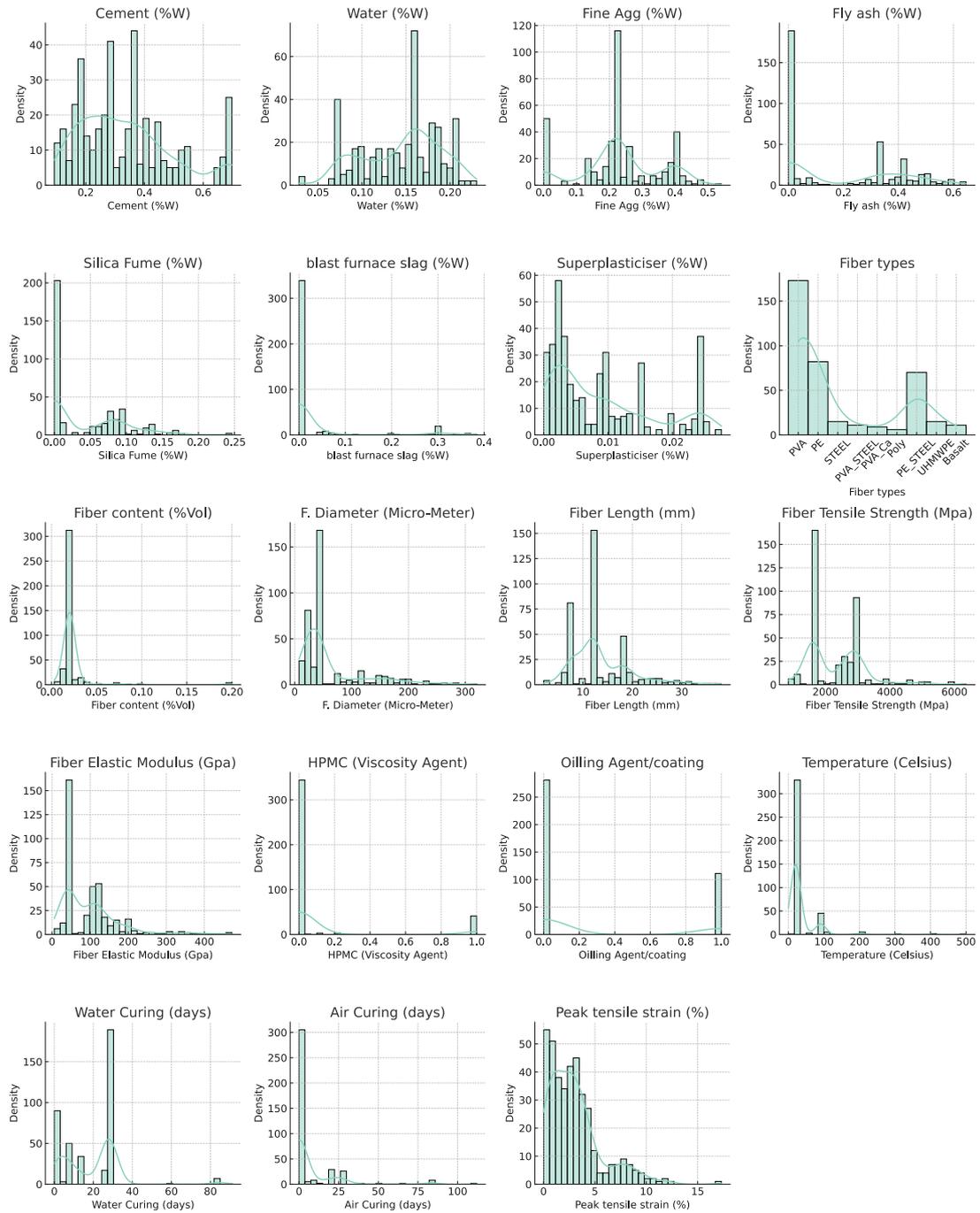
202 The database encompasses a wide array of fiber reinforcements, such as PE, PVA,
203 PP, basalt, steel, ultra-high molecular weight polyethylene fiber (UHMWPE), and
204 hybrid fibers like PE-steel, PVA-calcium carbonate whiskers, and PVA-steel. Each of
205 these selected features has been verified to significantly impact the strength and
206 ductility of ECC [\[2\]](#). The outputs of the dataset are the peak tensile stress (MPa) and
207 peak tensile strain (%). A statistical analysis of ECC stress and strain datasets is
208 summarized in [Appendix 1](#) and [Appendix 2](#).



209

210

(a)



211

212

(b)

213

Figure 1. The distribution plots of each feature and output in (a) the tensile stress

214

dataset and (b) the tensile strain dataset.

215

4. Methodologies

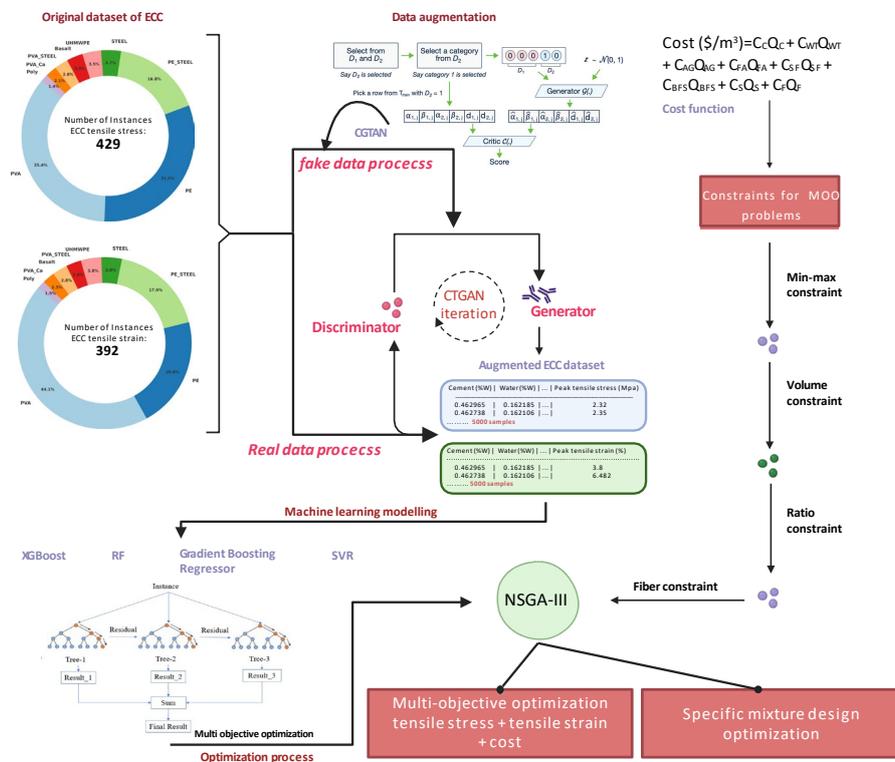
216

The methodology employed in this study consists of four progressive parts: ECC

217

database collection, data augmentation, ML modelling, and optimization process. The

218 database collection was demonstrated in Section 2 with 429 and 392 original tensile
 219 stress and tensile strain samples, respectively. The ECC database augmentation is
 220 achieved by combining the collected original data mentioned and the unsupervised
 221 learning algorithm - Tuned CTGAN. The primary objective of this part is to create more
 222 data to establish a robust machine learning model. The third part involves the
 223 development of the prediction model, wherein HGS based ML models are trained for
 224 ECC properties' prediction using both the original and synthesized database. The last
 225 part focuses on the mixture design optimization of ECC. Four classes of constraints
 226 (min-max, volume, ratio, and fiber) were established to define the search space. Then,
 227 a cost function was defined and NSGA-III was introduced to tackle the problem. The
 228 above-mentioned framework is expected to be valuable in accurately predicting ECC
 229 properties and reversely optimizing mixture design, as exhibited in Figure 2.



230

231 **Figure 2.** The flowchart of the ECC optimization framework comprising data

232 collection, data augmentation, ML modelling, and optimization process

233 4.1 Data augmentation

234 4.1.1 Concepts of Tuned-CTGAN

235 Introduced by Xu, Skoularidou, et al. (2019) [93], Conditional Tabular GAN
236 (CTGAN) is a GAN-based architecture tailored for synthesizing tabular data. It
237 effectively tackles a major challenge in augmenting tabular data for continuous columns:
238 handling non-Gaussian and multimodal distributions, an issue not adequately addressed
239 by traditional GANs like TableGAN. While traditional GANs typically employ min-
240 max normalization to scale continuous values to a range from -1 to 1, CTGAN adopts
241 a modality-specific normalization technique. This approach transforms continuous
242 values into a bounded vector by independently modelling each continuous column
243 using a Variational Gaussian Mixture (VGM) model.

$$\mathbb{P}_{C_i}(c_{i,j}) = \sum_{k=1}^{m_i} \mu_k \mathcal{N}(c_{i,j}; \eta_k, \phi_k) \quad (1)$$

244 where C_i and m_i are the i th continuous column and the mode number in the VGM;
245 in each mode, μ_k , η_k , and ϕ_k are the respective weight, mean, and standard deviation.
246 For each value $c_{i,j}$ in C_i , the model calculates the probability of $c_{i,j}$ from each mode
247 in the VGM as:

$$\rho_k = \mu_k \mathcal{N}(c_{i,j}; \eta_k, \phi_k), \quad k = 1, 2, \dots, m \quad (2)$$

248 It is assumed that the mode k with the highest probability is selected. This is
249 followed by a normalization process which can be written as follows:

$$\alpha_{i,j} = \frac{c_{i,j} - \eta_k}{4\phi_k} \quad (3)$$

$$\beta_{i,j} = [0, \dots, 0, 1, 0, \dots, 0] \quad (4)$$

250 where $\alpha_{i,j}$ is a normalized scalar within the range [-1, 1], and $\beta_{i,j}$ is a one-hot
251 encoding with the k th element set to 1 corresponding to the mode k . Thus, each value

252 in a continuous column is represented by a combination of scalar $\alpha_{i,j}$ for the
 253 normalized value and a one-hot vector $\beta_{i,j}$ to indicate the mode. This normalized data
 254 is then used as the input for the model.

255 When augmenting data in discrete columns of a table, an imbalance present in
 256 these columns in the original dataset may result in a skewed distribution of discrete
 257 outputs, commonly known as mode collapse. To effectively counter this issue, two
 258 distinct strategies are implemented: the introduction of a conditional generator and the
 259 application of sampling training. Both are strategically designed to promote a balanced
 260 representation of all categories within the discrete columns. In the case of the
 261 conditional generator, it is specifically trained to synthesize data reflecting the
 262 conditions associated with a specific value k^* in a specific column D_{i^*} . To represent
 263 this condition, a masking vector m_i is defined in the following manner:

$$m_i^{(k)} = \begin{cases} 1 & \text{if } i = i^* \text{ and } k = k^* \\ 0 & \text{otherwise} \end{cases} \quad (5)$$

264 Equation 6 represents the *cond* vector which is introduced to concatenate
 265 different masking vectors for all discrete columns D_1, \dots, D_{N_d} .

$$cond = m_1 \oplus m_2 \oplus \dots \oplus m_{N_d} \quad (6)$$

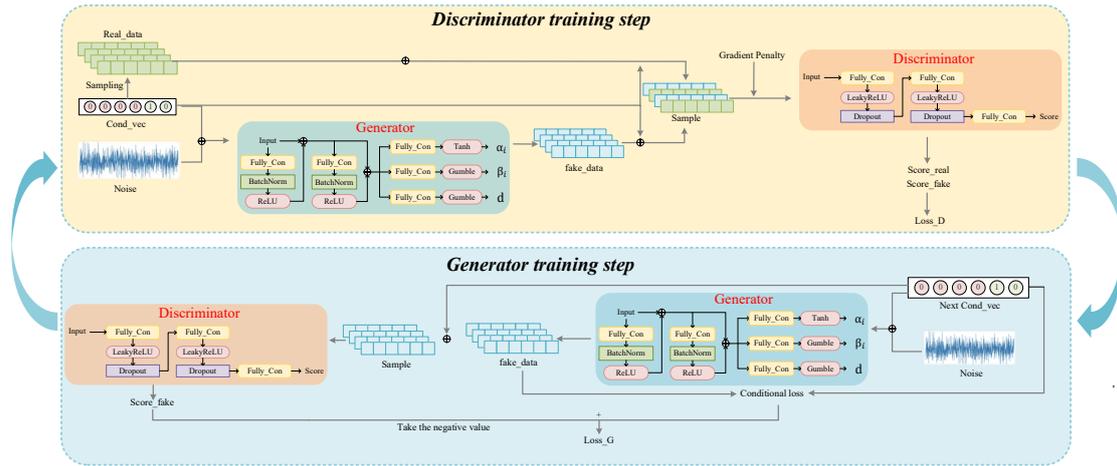
266 The *cond* vector is designed to facilitate the conditioning of specific column
 267 values through one-hot encoding. Following this, the conditional generator G operates
 268 by taking random noise along with the *cond* as its inputs. This setup compels G to
 269 adhere to the specified conditions, achieving this through the minimization of
 270 conditional loss, specifically cross-entropy.

271 4.1.2 Establishment of Tuned-CTGAN

272 In the Tuned-CTGAN framework, the architecture integrates a conditional
 273 generator G and a discriminator D . G is structured with two fully connected layers,

274 each layer being augmented with batch normalization and *ReLU* activation for
275 enhanced performance. Following these layers, a mixed activation function is utilized
276 to create synthetic row representations. Specifically, the continuous column values α_i
277 are processed through a *Tanh* activation, whereas the discrete column values d_i and
278 mode indicators β_i undergo activation via *Gumbel Softmax*. The architecture also
279 includes an *embedding_dim*, a critical hyperparameter set at 32 to enrich the
280 synthetic data generation with diversity. Furthermore, to optimize the training
281 efficiency of Tuned-CTGAN, the batch size, number of epochs, and learning rate are
282 carefully set to 50, 2000, and 2e-6, respectively.

283 Within the discriminator D of the Tuned-CTGAN model, a dual-layer fully
284 connected structure is implemented. These layers are succeeded by a dropout layer,
285 strategically designed to sporadically deactivate certain nodes, thereby addressing potential
286 overfitting challenges. *LeakyReLU* is selected as the activation function, enhancing the
287 model's capability to differentiate between data types. This is followed by another fully
288 connected layer tasked with scoring the current batch. The discriminator's layer sizes,
289 denoted as *discriminator_dim*, are set to (512, 512), where the higher dimensionality of
290 512 plays a pivotal role in accurately distinguishing between real and synthesized data.
291 Additionally, the discriminator's learning rate is calibrated at 0.0005. [Figure 3](#) visually
292 depicts the Tuned-CTGAN's architecture and its training procedure. Notably, the
293 *discriminator_steps* parameter is set to three, indicating that for every single update of
294 the generator, the discriminator undergoes three update cycles. During data generation, the
295 fiber parameters' boundaries are set based on the original data. These fiber parameters are
296 generated according to the normal distribution. This approach ensures a precise correlation
297 between fiber types and their traits, improving the synthetic data's reliability. The
298 pseudocode is shown in [Figure 4](#).



299

300

Figure 3. The training process and architecture of the Tuned-CTGAN model

Algorithm 1 Fiber Constraint for Synthetic Data Generation

Require: *desired_strength*, *desired_modulus*

- 1: Initialize dictionaries: *desired_strength*, *desired_modulus*
 - 2: **function** ISVALID(*column_names*, *data*)
 - 3: Extract *fiber_type*(*ft*), *fiber_tensile_strength*, *fiber_elastic_modulus* from *data*
 - 4: Initialize *valid_rows* as False array
 - 5: **for** *ft* in *desired_strength/modulus.dictionaries*() **do**
 - 6: Check if values are within range for strength and modulus
 - 7: Update *valid_rows* using OR operation
 - 8: **end for**
 - 9: **return** *valid_rows*
 - 10: **end function**
 - 11: **function** TRANSFORM(*column_names*, *data*)
 - 12: Extract *fiber_type*, *fiber_tensile_strength*, *fiber_elastic_modulus* from *data*
 - 13: **for** *ft* in *desired_strength/modulus.dictionaries*() **do**
 - 14: Calculate *avg_strength* and *std_strength*
 - 15: Generate new strengths using normal distribution
 - 16: Update *fiber_tensile_strength* for these rows
 - 17: Calculate *avg_modulus* and *std_modulus*
 - 18: Generate new modulus values using normal distribution
 - 19: Update *fiber_elastic_modulus* for these rows
 - 20: **end for**
 - 21: **return** *data*
 - 22: **end function**
 - 23: Create custom constraint class using ISVALID, TRANSFORM
-

301

302

Figure 4. The pseudocode of fiber constraint

303

304 **4.1.3 Evaluation metrics for CTGAN**

305 Evaluating the quality of data generated by GANs poses a challenge due to the
306 variability in outcomes produced by different evaluation metrics. This study proposes
307 a comprehensive approach combining visual, statistical, and ML based metrics for
308 assessing the quality of tabular data generation. The visual and statistical metrics are
309 detailed below, while the ML based metrics are thoroughly elaborated in [Section 4.2](#).

310 (1) Visual based metrics: This approach involves using visualization techniques to
311 intuitively compare real and synthetic data. In this study, three methods are introduced
312 for visual evaluation: Distribution plot, Cumulative Sum, and Correlation table. The
313 Distribution plot is used to assess the statistical properties and similarities of real and
314 synthetic datasets. Cumulative Sum offers a column-by-column visual comparison,
315 focusing on the distribution similarities. Lastly, the Correlation table is employed to
316 analyze the interrelationships between table columns, thereby gauging the generator's
317 efficacy in accurately modelling these relationships.

318 (2) Statistical based metrics: In this research, two statistical tests, KSTest and
319 CSTest are utilized for evaluation [\[94\]](#). KSTest uses the empirical Cumulative
320 Distribution Function (CDF) and the Kolmogorov–Smirnov test to assess continuous
321 features' distributions, mainly focusing on the maximal divergence between the
322 observed and expected CDF values. On the other hand, CSTest applies the Chi-squared
323 test to evaluate discrete columns' distributions, with its p-value indicating the
324 probability that values from two columns originate from the same distribution.

325 **4.2 Machine learning model establishment**

326 **4.2.1 XGBOOST**

327 The technique of XGBoost is built on the “boosting” idea, which combines the
328 prediction of weak learners with additive training approaches to build a powerful
329 learner. Boosting tree algorithms are based on the decision tree, which is known as the

330 classification and regression tree (CART). The structure of XGBoost is depicted in
 331 [Figure 5](#). For regression tasks, CART divides the dataset into two subsets at each level
 332 according to the boundary for one variable until reaching the tree's maximum depth set
 333 by users. It can be described as below:

$$R_1(j, s) = \{x \mid x^j \leq s\} \text{ and } R_2(j, s) = \{x \mid x^j \geq s\} \quad (7)$$

334 Mean squared error of each leaf node is calculated:

$$MSE_{node} = \sum_{i \in node} (\hat{y}_{node} - y^{(i)})^2 \quad (8)$$

$$\hat{y}_{node} = \frac{1}{m_{node}} \sum_{i \in node} y^{(i)} \quad (9)$$

335 where m_{node} is the number of instances in one node. The cost function for regression
 336 of CART can be expressed as:

$$J(k, t_k) = \frac{m_{left}}{m} MSE_{left} + \frac{m_{right}}{m} MSE_{right} \quad (10)$$

337 The algorithm will search for the best solutions for boundaries of variables to
 338 minimize the cost function. The prediction is then the average target value of all
 339 instances in one subset. The mechanism of XGBoost is to keep adding and training new
 340 trees to fit residual errors of the last iteration as shown in [Figure 5](#). A predicted value is
 341 assigned to each instance by adding all corresponding leaves' scores together:

$$\hat{y} = \phi(x_i) = \sum_{k=1}^K f_k(x_i) \text{ and } f_k(x_i) = w_{q(x)}, f_k \in \mathcal{L} \quad (11)$$

342 where K is the quantity of trees; $f_k(x_i)$ means the outcome of input x_i for the k th
 343 tree; $w_{q(x)}$ is the score for each leaf node; $q(x)$ denotes the number of leaf nodes; \mathcal{L}
 344 represents an assemble of all corresponding functions f_k .

345 The objective function of XGBoost contains two parts: the training error and the
 346 regularization, written as:

$$\text{obj}(\theta) = \sum L(\theta) + \sum \Omega(\theta) \quad (12)$$

347 where L is the loss function measuring the deviation of the predicted values from the
 348 actual values. Ω is the regularization function measuring the complexity of the training
 349 model in order to avoid overfitting.

$$\Omega(\theta) = \gamma T + \frac{1}{2} \lambda \|\omega\|^2 \quad (13)$$

350 where T represents the total number of leaf nodes and ω is the score of each leaf
 351 node. γ and λ are controlling factors employed to avoid overfitting.

352 When a new tree is created to fit residual errors of last iteration, the predicted score
 353 for the t th tree can be expressed as:

$$\hat{y}_i^{(t)} = \hat{y}_i^{(t-1)} + f_t(x_i) \quad (14)$$

354 The objective function is thus written as:

$$\mathcal{L}^{(t)} = \sum_{i=1}^n l(y_i, \hat{y}_i^{(t-1)} + f_t(x_i)) + \Omega(f_t) \quad (15)$$

355 An appropriate function, f_t , is replaced with the second-order Taylor polynomial
 356 of $f_t = 0$. Accordingly, the objective function can be approximated as:

$$\mathcal{L}^{(t)} \approx \sum_{i=1}^n \left[l(y_i, \hat{y}_i^{(t-1)}) + g_i f_t(x_i) + \frac{1}{2} h_i f_t^2(x_i) \right] + \Omega(f_t) \quad (16)$$

357 where g_i is the first-order derivative and h_i denotes the second-order derivative:

$$g_i = \partial_{\hat{y}_i^{(t-1)}} l(y_i, \hat{y}_i^{(t-1)}) \text{ and } h_i = \partial_{\hat{y}_i^{(t-1)}}^2 l(y_i, \hat{y}_i^{(t-1)}) \quad (17)$$

358 Since previous $(t - 1)$ trees' residual errors (y) have minimal influence on the
 359 modification of the objective function, [Equation 15](#) is then simplified as:

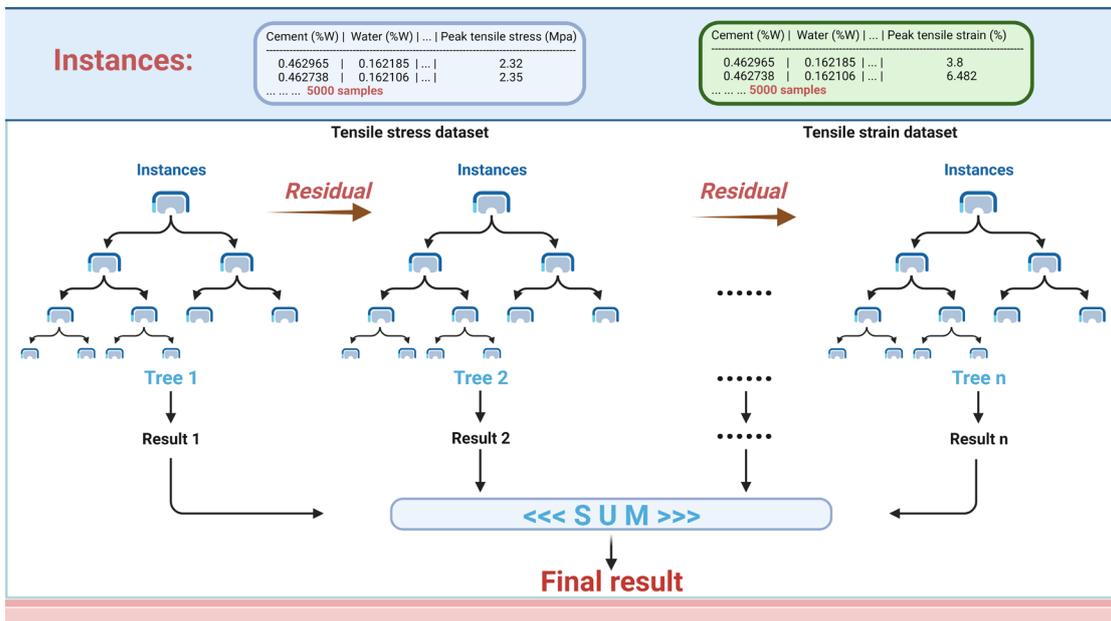
$$\tilde{\mathcal{L}}^{(t)} = \sum_{i=1}^n \left[g_i f_t(x_i) + \frac{1}{2} h_i f_t^2(x_i) \right] + \Omega(f_t) \quad (18)$$

360 As each instance will finally be classified into one leaf node, all instances that
 361 belong to the same leaf node can be reassembled as:

$$\text{obj}^{(t)} \approx \sum_{j=1}^T [(\sum_{i \in I_j} g_i)w_j + \frac{1}{2}(\sum_{i \in I_j} h_i + \lambda)w_j^2] + \gamma \quad (19)$$

362 Therefore, the optimum w and objective function obj are derived as:

$$w_j^* = -\frac{G_j}{H_j + \lambda} \text{ and } \text{obj} = -\frac{1}{2} \sum_{j=1}^t \frac{G_j^2}{H_j + \lambda} + \gamma T \quad (20)$$



363

364

Figure 5. The structure of XGBoost

365 4.2.2 Other ML algorithms

366 SVR is normally used to solve regression problems by constructing a model that
 367 attempts to fit the error within a certain threshold. Its main strategy involves finding a
 368 hyperplane in a high-dimensional space that best fits the data, with the flexibility to
 369 manage both linear and non-linear models through kernel tricks [95]. Gradient Boosting
 370 Regressor is another ML algorithm that builds sequential models, typically decision
 371 trees, where each tree corrects errors made by the previous ones [96]. It focuses on
 372 minimizing a loss function, iteratively adding trees that predict the residuals or errors

373 of prior trees to improve accuracy. This method excels in predictive accuracy even with
374 non-linear data and efficiently handles missing values. Random Forest is an ensemble
375 learning method that constructs multiple decision trees during training and outputs the
376 majority vote or average prediction of the trees for classification and regression tasks,
377 respectively [97]. It effectively handles large datasets and high-dimensional spaces,
378 offering robust performance and mitigating overfitting through its ensemble approach,
379 making it highly versatile across diverse applications. To compare the HGS-XGBoost
380 performance with other ML models, SVR, Gradient Boosting Regressor, and RF were
381 also introduced in this study.

382 **4.2.3 Hunger games search**

383 Hunger Games search (HGS) is an advanced meta-heuristic algorithm that
384 leverages strategies to discover diverse solution spaces to refine solutions towards
385 optimality. It was first introduced by Yang, Chen et al. [12]. Each group of
386 hyperparameters represents each individual and the fitness function is the loss function
387 (RMSE) of the XGBoost. The objective is to identify the best individual that minimizes
388 the RMSE when employing this group of hyperparameters for model training. “Hunger-
389 Driven Motivational State Competition” is the searching strategy of HGS. The key
390 advantage of HGS lies in its ability to efficiently navigate the search space and converge
391 rapidly to the optimal solution, thereby reducing computational time and resource usage
392 significantly. Considering the sources of food and the motions of species, a logical game
393 can be set up between various animals with the aim of winning the game and acquiring
394 the food. Equation 21 illustrates the foraging behaviours of individuals based on self-
395 dependent spirit ($Game_1$) or collaborative communication ($Game_2$ and $Game_3$).

$$\overrightarrow{X(t+1)} = \begin{cases} Game_1: \overrightarrow{X(t)} \cdot (1 + randn(1)), r_1 < l \\ Game_2: \overrightarrow{W_1} \cdot \overrightarrow{X_b} + \vec{R} \cdot \overrightarrow{W_2} \cdot |\overrightarrow{X_b} - \overrightarrow{X(t)}|, r_1 > l, r_2 > E \\ Game_3: \overrightarrow{W_1} \cdot \overrightarrow{X_b} - \vec{R} \cdot \overrightarrow{W_2} \cdot |\overrightarrow{X_b} - \overrightarrow{X(t)}|, r_1 > l, r_2 < E \end{cases} \quad (21)$$

$$E = \text{sech}(|F(i) - BF|), i = 1, 2, 3, \dots, n \quad (22)$$

$$\vec{R} = 2 \times shrink \times rand - shrink \quad (23)$$

$$shrink = 2 \times \left(1 - \frac{t}{T}\right) \quad (24)$$

396 where \vec{R} is in the range of $[-a, a]$; r_1 and r_2 are random numbers between 0 to 1;
 397 $randn(1)$ is a random number following a standard normal distribution; l is set as
 398 0.03 in this study; t denotes the current iteration and T is the maximum iterations;
 399 $\overrightarrow{W_1}$ and $\overrightarrow{W_2}$ are two hunger weights; $\overrightarrow{X_b}$ and $\overrightarrow{X(t)}$ represent the locations of the best
 400 and other individuals, respectively; sech is a hyperbolic function; $F(i)$ denotes the
 401 fitness value of each individual and BF is the current best fitness value.

402 Regarding the hunger role, $\overrightarrow{W_1}$ and $\overrightarrow{W_2}$ can be calculated as follows:

$$\overrightarrow{W_1(i)} = \begin{cases} hungry(i) \cdot \frac{N}{sum(hungry)} \times r_4, r_3 < l \\ 1, r_3 > l \end{cases} \quad (25)$$

$$\overrightarrow{W_2(i)} = (1 - \exp(-|hungry(i) - sum(hungry)|)) \times r_5 \times 2 \quad (26)$$

$$hungry(i) = \begin{cases} 0, F(i) == BF \\ hungry(i) + H, F(i) \neq BF \end{cases} \quad (27)$$

403 where $hungry(i)$ denotes the hunger degree of each individual; N is the total
 404 number of individuals; r_3 , r_4 , and r_5 are three random numbers from 0 to 1; $F(i)$ is
 405 the fitness value of each individual. Equation 27 means that the hunger degree is 0 for
 406 the best individual and a new hunger H will be added for other individuals.

$$TH = \frac{F(i) - BF}{WF - BF} \times r_6 \times 2 \times (UB - LB) \quad (28)$$

$$H = \begin{cases} LH \times (1 + r), TH < LH \\ TH, TH \geq LH \end{cases} \quad (29)$$

407 where WF is the worst fitness value in the current iteration; UB and LB are the
 408 upper and lower bounds of the feature space; LH is determined as the lower bound of
 409 the H (100 in this study). The pseudocode of HGS is represented in [Figure 6](#).

Algorithm 1 Pseudo-code of Hunger Games Search (HGS)

```

1: Initialize parameters  $N, T, l, D, sum(hungry)$ 
2: Initialize positions of Individuals  $X_i$  for  $i = 1, 2, \dots, N$ 
3: while  $t \leq T$  do
4:   Calculate fitness of all Individuals
5:   Update  $BF, WF, X_b, BF$ 
6:   Calculate  $hungry$  by Eq. (27)
7:   Calculate  $W_1$  by Eq. (25)
8:   Calculate  $W_2$  by Eq. (26)
9:   for each Individual do
10:     Calculate  $E$  by Eq. (22)
11:     Update  $R$  by Eq. (23)
12:     Update positions by Eq. (21)
13:   end for
14:    $t = t + 1$ 
15: end while
16: return  $BF, X_b$ 

```

410

Figure 6. The pseudocode of HGS

411

412 4.2.4 Model establishment

413 The ML models' hyperparameters are tuned by HGS in this study. Since the final
 414 utilized model is XGBoost, the model establishment process of XGBoost is described
 415 instead of the other ML models. When training XGBoost, some hyperparameters are
 416 crucial to the model predictive performance comprising *booster, objective, max_depth,*
 417 *eta, min_child_weight, subsample, colsample_bytree, learning_rate,*
 418 *num_parallel_tree, and n_estimators*. In this study, 'regression: linear' was determined
 419 for the hyperparameter objective because it was a typical regression task. After the trial
 420 experiment, the hyperparameters of *booster, eta, min_child_weight, subsample,*
 421 *colsample_bytree, num_parallel_tree* were set as 'gbtree', '0.1', '5', '0.7', '1', '1',

422 respectively. Besides, *max_depth*, *learning_rate*, and *n_estimators* were automatically
 423 optimized using HGS algorithm with the initial boundaries of [1, 100], [0.01, 1], and
 424 [1, 100], respectively. This is because these three hyperparameters are most important
 425 which significantly affect the model complexity, convergence efficiency, and
 426 overfitting/underfitting balance.

427 Once determining the hyperparameters, the XGBoost model was generated with
 428 the optimal values of *max_depth*, *learning_rate*, and *n_estimators* after 20 iterations on
 429 the training set (80% of the database). The fiber type, which is the eighth feature of the
 430 dataset, is transferred to one binary attribute using the One-hot-encoding function. Thus,
 431 the 18 features of the initial dataset were increased to 26 features. Subsequently, the
 432 optimal XGBoost model was tested on the test set (20% of the database) to ascertain its
 433 predictive efficacy. The XGBoost framework calculates the importance weight of each
 434 feature. If a certain feature is deemed to have minimal predictive significance, it is
 435 excluded in the subsequent training cycle.

436 4.2.5 Performance evaluation

437 In this study, three accompanying evaluating indicators aim to evaluate the
 438 precision of the ML model: correlation coefficient (R), mean absolute error (MAE),
 439 and root mean square error (RMSE). These indicators are calculated as follows [98]:

$$R = \frac{\sum_{i=1}^n (y_i^* - \bar{y}^*)(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (y_i^* - \bar{y}^*)^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}} \quad (30)$$

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i^* - y_i| \quad (31)$$

$$RSME = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i^* - y_i)^2} \quad (32)$$

440 where n is the n groups of data samples; y_i^* and y_i are the predicted and actual
 441 results; \bar{y}^* and \bar{y} illustrate the mean values of the predicted and actual results.

442 4.3 Multi-objective optimization

443 4.3.1 Objective function establishment

444 After the establishment of two XGBoost models, they are adopted as the objective
 445 functions for ECC's tensile stress and tensile strain, respectively. The third objective
 446 function (cost) is computed by polynomials as follows:

$$\begin{aligned}
 Cost(\$/m^3) = & C_C Q_C + C_{WT} Q_{WT} + C_{AG} Q_{AG} + C_{FA} Q_{FA} + C_{SF} Q_{SF} \\
 & + C_{BFS} Q_{BFS} + C_S Q_S + C_F Q_F
 \end{aligned} \tag{33}$$

447 In Equation 33, Q_C , Q_{WT} , Q_{AG} , Q_{FA} , Q_{SF} , Q_{ca} , Q_{BFS} , Q_S and Q_F denote the
 448 unit weight (kg/m^3) of cement, water, fine aggregate, fly ash, silica fume, blast furnace
 449 slag, superplasticiser, and fiber, respectively. Besides, C means the unit price ($\$/kg$)
 450 of each raw material of ECC, which is checked from Alibaba in China and summarised
 451 in Table 2. A simplified assumption was employed, utilizing the average cost of fiber,
 452 despite the recognition that fiber costs are influenced by parameters such as diameter,
 453 tensile strength, and elastic modulus, etc [99]. The fiber type, which is the eighth feature
 454 of the dataset, is transferred to one binary attribute using One-hot-encoding function.
 455 Therefore, the unit weight and cost of the specific fiber will be determined upon the
 456 fiber type selected.

457 **Table 2.** The unit weight and cost of each variable of ECC

Raw materials	Notation	Density (kg/m^3)	Notation	Unit price ($\$/kg$)
Cement	U_C	3100	C_C	0.59
Water	U_{WT}	1000	C_{WT}	0.0005

Fine Aggregate	U_{AG}	2600	C_{AG}	0.009
Fly ash	U_{FA}	2300	C_{FA}	0.027
Silica Fume	U_{FA}	2220	C_{SF}	0.82
blast furnace slag	U_{BFS}	2900	C_{BFS}	0.062
Superplasticiser	U_S	1100	C_S	1.07
Fiber type:				
Basalt		2670		3.42
PE		970		15.04
PE_Steel		4410		7.86
PVA		1300		3.2
PVA_Ca	U_F	1400	C_F	3.415
PVA_Steel		4575		1.94
PP		910		3.9
Steel		7850		0.68
UHMWPE		950		31.44

458 4.3.2 Constraints

459 In this study, the following four classes of constraints (Min-max, volume, ratio,
460 and fiber) were set up to define the search space in the MOO problem.

- 461 • Min-max constraint

462 Constraints were introduced to specify the range within which each input variable
463 can vary to avoid a covariate shift. The ranges of input features were limited to the
464 minimum and maximum values according to the datasets, as follows:

$$d_{imin} \leq d_i \leq d_{imax} \quad (34)$$

465 where d_{imin} and d_{imax} represent the lowest and highest value of the i th feature
466 ([Appendix 1](#) and [2](#)).

- 467 • Volume constraint

468 In the ECC matrix, the cumulative volume of each component, coupled with
469 inevitable air content for each blend, approximately equates to one cubic meter.

470 Therefore, the design domain should be restricted to exclude mixes deviating

471 significantly from a volume of one cubic meter. This was realized through a constraint
 472 that governs the volume of each mix design, termed the "volume constraint", as follows:

$$V_m = \left(\frac{Q_C}{U_C} + \frac{Q_{WT}}{U_{WT}} + \frac{Q_{AG}}{U_{AG}} + \frac{Q_{FA}}{U_{FA}} + \frac{Q_{SF}}{U_{SF}} + \frac{Q_{BFS}}{U_{BFS}} + \frac{Q_S}{U_S} + \frac{Q_F}{U_F} \right) \in [\alpha_{min}, \alpha_{max}] \quad (35)$$

473 where U_C , U_{WT} , U_{AG} , U_{FA} , U_{SF} , U_{BFS} , U_S and U_F are the density of cement,
 474 water, fine aggregate, fly ash, silica fume, blast furnace slag, superplasticiser, and fiber,
 475 respectively, specified in Table 2; α_{min} and α_{max} were set to 0.96 and 1.04,
 476 considering the variations in air content and disparities in ingredient densities across
 477 different studies.

478 • Ratio constraint

479 To ensure consistency within the dataset and prevent undue variations in
 480 properties, two ratio constraints were established. These constraints are crucial to
 481 mitigate potential complications arising from extreme water-to-binder (W/B) ratios that
 482 lie outside the raw database's scope, potentially affecting the concrete's fresh state.
 483 Consequently, the water to binder ratio and the fine aggregate to binder ratio were
 484 delineated as follows.

$$0.131 \leq \frac{\textit{Water}}{\textit{Cement} + \textit{Fly ash} + \textit{Silica fume} + \textit{Blast furnace slag}} \leq 0.568 \quad (36)$$

$$0 \leq \frac{\textit{Fine aggregate}}{\textit{Cement} + \textit{Fly ash} + \textit{Silica fume} + \textit{Blast furnace slag}} \leq 1.667 \quad (37)$$

485 • Fiber constraint

486 The type, diameter, length, tensile strength, and elastic modulus of fiber are crucial
 487 to the properties of ECC, simultaneously affecting the cost owing to totally different
 488 characteristics. They cannot be considered as unrelated features during the MOO

489 solving process, otherwise the characteristics fail to match the specific fiber. Therefore,
 490 this study introduced the boundary constraints corresponding to each fiber category, as
 491 shown in Table 3. In this case, the diameter, length, tensile strength, and elastic modulus
 492 were constrained according to the one binary attribute of the feature ‘fiber type’ using
 493 the One-hot-encoding function.

494 **Table 3.** The fiber constraints of ECC

Fiber type	F. Diameter (Micro-Meter)		Fiber Length (mm)		Fiber Tensile Strength (MPa)		Fiber Elastic Modulus (GPa)	
	Min	Max	Min	Max	Min	Max	Min	Max
Basalt	13	13	6	12	2600	2600	85	85
PE	12	78	6	38	2400	5200	66	158
PE_STEEL	54	279	8.9	34.5	1772	6360	115.8	379
PVA	35	40	8	12	900	1620	23	43
PVA_Ca	7.667	28.25	2.061	14.6	1929.6	4010.4	137.04	472.11
PVA_STEEL	60	192.7	7.68	16.3	1633.3	2608	82.1	155.12
PP	12	19.5	6	12	350	3700	4	6
STEEL	150	550	6	30	2428	5000	200	360
UHMWPE	18	25	12	13	3000	3000	100	114

495

496 4.3.3 Construction of optimizer

497 Regarding multi-objective optimization problems, an optimizer can seek within a
 498 set of compromise options in the objective space called the Pareto front to obtain the
 499 optimal solution [100]. The Pareto front implies the condition that one objective fails
 500 to be improved without worsening the other objectives. If A represents the group of
 501 feasible solutions and $\mathbf{x}^* \in A$ is one of the Pareto optimal solutions, there is no
 502 existence of $x \in A$ satisfy that:

$$f_k(\mathbf{x}) \leq f_k(\mathbf{x}^*) \text{ for } k = 1, 2, 3, \dots, t \text{ and} \quad (38)$$

$$f_k(\mathbf{x}) < f_k(\mathbf{x}^*) \text{ for at least one } k \quad (39)$$

503 Deb and Jain [17] introduced NSGA-III by replacing the crowding distance to a
504 reference point-based selection approach in NSGA II, significantly improving the
505 convergence speed and population diversity. Therefore, this study proposed NSGA-III
506 to acquire the above-mentioned Pareto front in a larger objective space. The procedure
507 of the establishment of NSGA-III started by randomly generating an initial population
508 (P_t) of size N . The iteration process is described as follows:

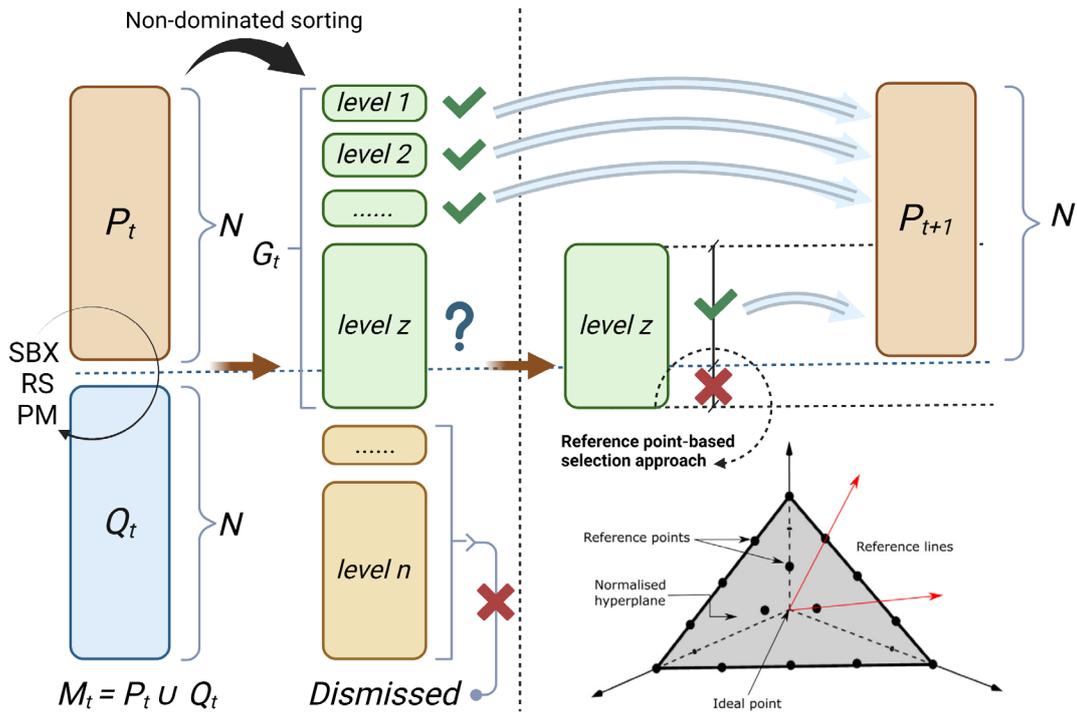
509 1. At t th iteration, an offspring population, denoted as Q_t , is derived from the
510 parent population P_t . This derivation employs techniques comprising simulated binary
511 crossover (SBX), random selection (RS), and polynomial mutation (PM), as described
512 in [17]. The population size for both P_t and Q_t remains consistent at N .

513 2. The populations P_t and Q_t are amalgamated to form a new population,
514 denoted as $M_t = P_t \cup Q_t$, which possesses a size of $2N$. Subsequently, the top N
515 individuals are chosen for the succeeding generation through a non-dominated sorting
516 mechanism. This process categorizes the elements of M_t into distinct non-domination
517 levels, represented as L_z .

518 3. A new population G_t is constructed by sequentially incorporating elements
519 from M_t across L_z levels until the population size either matches or surpasses N for
520 the first time, where the last level is called level z . The individuals from level z to the
521 end are excluded from consideration.

522 4. If the element size of G_t precisely matches N , all the individuals in the last
523 level z will be chosen for P_{t+1} , followed by the next iteration. If the size of G_t
524 exceeds N , the elements in the last level z will be sorted and selected according to the
525 reference point-based selection approach. By this approach, the size of P_{t+1} maintains
526 N and the population diversity is ascertained.

527 **Figure 7** depicts the environment selection of NSGA-III, showing non-dominated
 528 sorting and reference point-based selection in each iteration.



529

530

Figure 7. The environment selection of NSGA-III

531 **5. Results and discussion**

532 **5.1 Data augmentation**

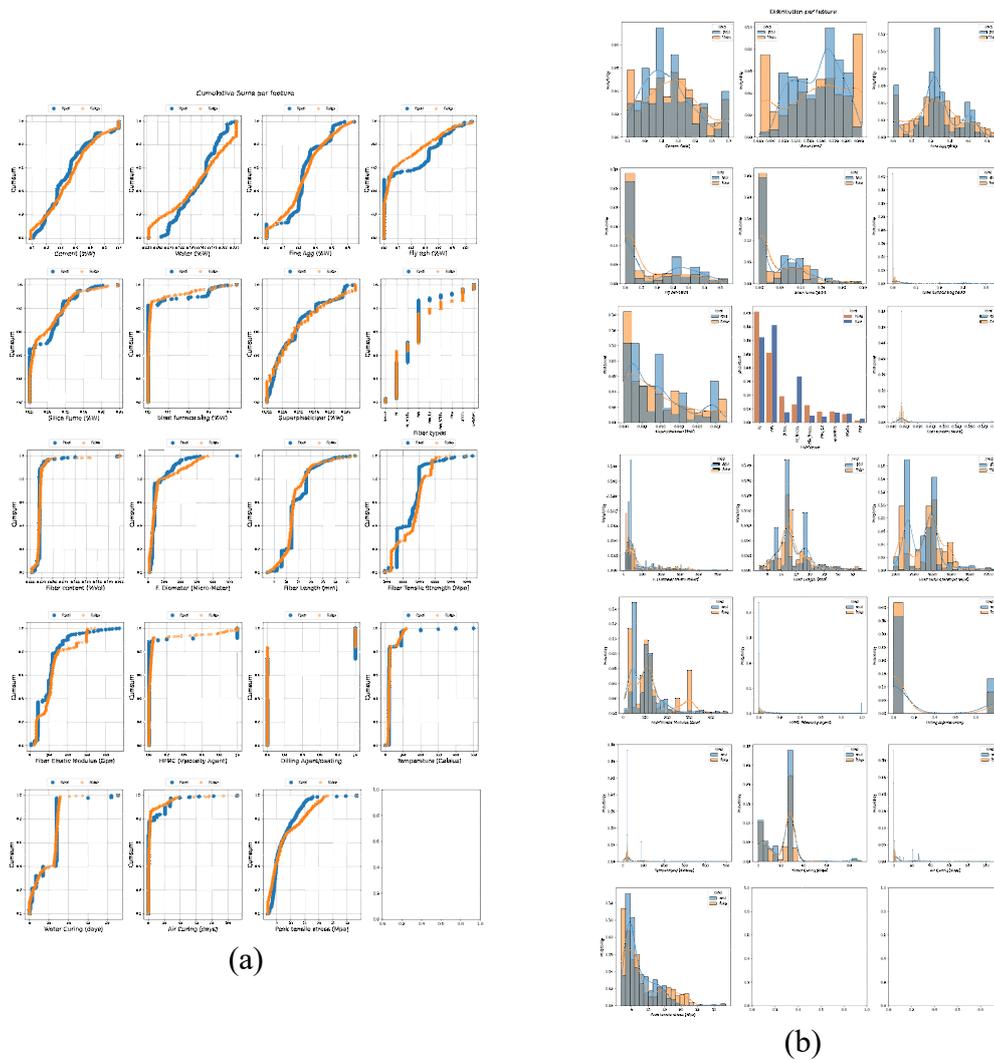
533 The Tuned-CTGAN augmentation technique was used to increase the size of the
 534 original tensile stress and strain datasets from 429 and 392 data records to 5000 each.
 535 The performance of the Tuned-CTGAN augmentation on the tensile stress and strain
 536 databases is depicted in **Figures 8** and **9**, respectively, through three visualization plots:
 537 the cumulative sum plot, distribution plot, and correlation table.

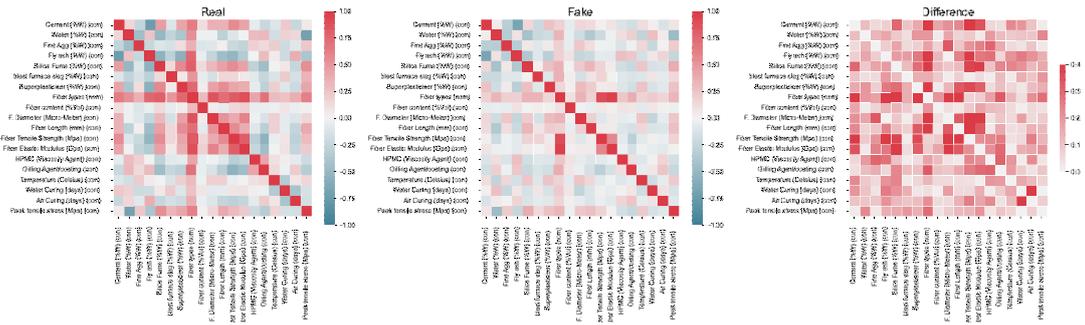
538 The cumulative plot for various features reveals a notable similarity between the
 539 original and synthesized datasets. For instance, the cumulative plot for the 'cement'
 540 feature exemplifies this similarity, as depicted in **Figures 8a** and **9a**. While the curves
 541 representing the original (in blue) and the generated data (in red) are not identical, their
 542 close proximity reflects the performance in capturing the statistical characteristics of

543 the original dataset. This phenomenon can be observed in the cumulative plots of the
544 other variables. Meanwhile, the distribution plots of the variables also demonstrate a
545 similarity in the probabilistic distribution of values between the original and
546 synthesized datasets. This means that values frequently observed in the original dataset
547 are generated with higher probability in the synthesized data, which is exhibited in
548 [Figures 8b](#) and [9b](#). It indicates that the data generation process effectively captures and
549 reproduces the underlying statistical tendencies of the original data. Besides, the
550 distribution of the fiber type (the single discrete variable) is well simulated by the
551 Tuned-CTGAN model. For instance, PE and PVA are the two most common categories
552 in the original database, and this is also reflected in the generated fake dataset. However,
553 the distribution of the fiber types is not strictly identical to the original database, mainly
554 due to the characteristics of Tuned-CTGAN. As mentioned earlier, a conditional
555 generator and sampling training applied in Tuned-CTGAN are used to tackle the
556 problem of mode collapse. This technology simultaneously partly neglects the actual
557 distribution of discrete features, increasing the sampling randomness and ultimately
558 leading to no identical distribution. Additionally, the distribution plot and cumulative
559 sum of the other fiber type related variables comprising fiber diameter, length, tensile
560 strength, and elastic modulus are mainly determined by the fiber type. This leads to the
561 same phenomenon of no identical distribution as that of fiber type.

562 The correlation table evaluates the association between each column of the table
563 as shown in [Figures 8c](#) and [9c](#). Apart from the relatively strong interdependency
564 between fiber types and their associated parameters, dependencies among other
565 parameters are comparatively weaker (below 0.25). This observation aligns with
566 expectations, as the characteristics of fibers inherently determine their parameters.
567 However, this strong interdependency may result in multicollinearity, reducing the

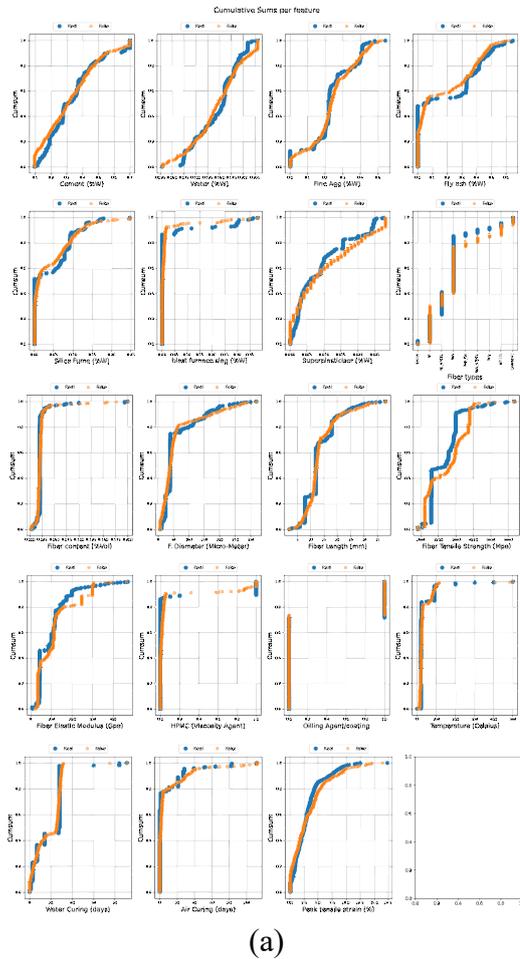
568 predictive performance and influencing design accuracy. To reduce the influence
 569 caused by multicollinearity, the generator's output is specifically directed by imposing
 570 constraints based on the selected fiber type in the training of Tuned-CTGAN.
 571 Meanwhile, these constraints are also imposed during the NSGA-III optimization
 572 process as mentioned in the previous section. In addition, the correlation tables between
 573 the original database and synthetic database depict a similar pattern with a relatively
 574 minor difference (the maximum of 0.3) for both the tensile stress and strain database.
 575 Therefore, the generator's performance in accurately modelling the relationships
 576 between columns has been assessed according to the visualization process.



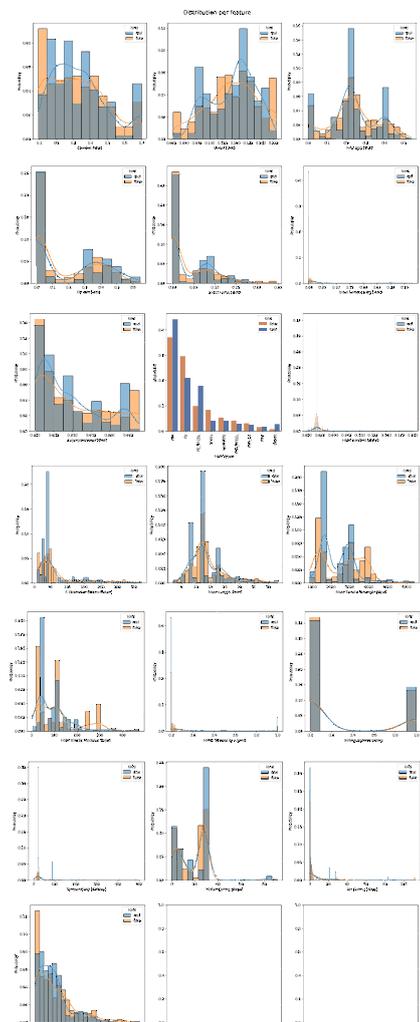


(c)

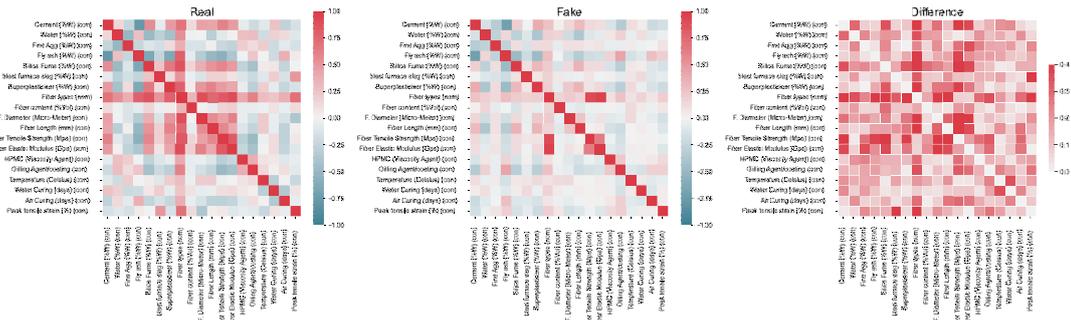
577 **Figure 8.** The cumulative (a), distribution (b), and correlation plots (c) for eighteen
 578 features before and after Tuned-CTGAN augmentation based on the dataset of tensile
 579 stress



(a)



(b)



(c)

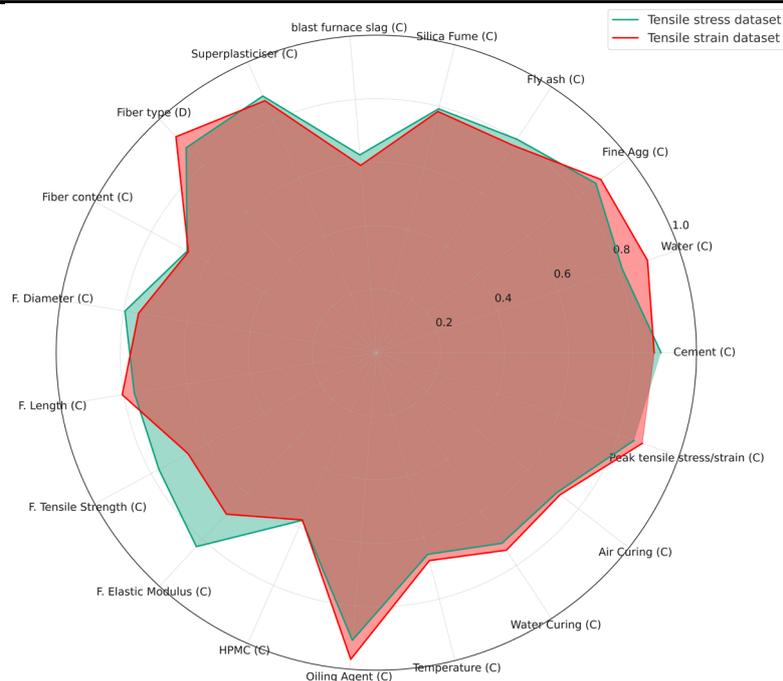
580 **Figure 9.** The cumulative (a), distribution (b), and correlation plots (c) for eighteen
 581 features before and after Tuned-CTGAN augmentation based on the dataset of tensile
 582 strain

583 The statistical based metrics (e.g., KSTest and CSTest) of the three data
 584 augmentation methods for both tensile stress and strain datasets are depicted in Table 4.
 585 The KSTest examines the distributions of continuous features, while the CSTest is used
 586 to evaluate distributions of discrete columns with the values depicted in Figure 10. For
 587 the KSTest, the results are expressed as $1 - \text{calculated value}$, so that a result closer
 588 to 1 indicates a slighter discrepancy between the real and generated distributions. In
 589 Table 4, the KSTest values of most variables in both stress and strain datasets are over
 590 0.7, indicating a relatively reliable outcome using Tuned-CTGAN data augmentation.
 591 The average metric values of 18 continuous variables and one output are 0.7795 and
 592 0.7764 on stress and strain datasets, respectively. These results explained the reliable
 593 data augmentation performance of Tuned-CTGAN, further verifying the conclusions
 594 acquired from the visualization plots.

595 **Table 4.** The statistical based metrics based on Tuned-CTGAN

Variables and outcome	Tensile stress dataset	Tensile strain dataset
Cement (C)	0.8892	0.8680
Water (C)	0.8122	0.8955
Fine Agg (C)	0.8687	0.8884
Fly ash (C)	0.8030	0.7800
Silica Fume (C)	0.7923	0.7836
blast furnace slag (C)	0.6250	0.5918
Superplasticiser (C)	0.8825	0.8664

Fiber type (D)	0.8773	0.9243
Fiber content (C)	0.6721	0.6677
F. Diameter (C)	0.7962	0.7530
F. Length (C)	0.7667	0.8047
F. Tensile Strength (C)	0.7722	0.6685
F. Elastic Modulus (C)	0.8299	0.6913
HPMC (C)	0.5763	0.5752
Oiling Agent (C)	0.9085	0.9687
Temperature (C)	0.6549	0.6752
Water Curing (C)	0.7169	0.7428
Air Curing (C)	0.7159	0.7276
Peak tensile stress (C)	0.8510	-
Peak tensile strain (C)	-	0.8785
Average value	0.7795	0.7764



596

597 **Figure 10.** The radar maps of Tuned-CTGAN on tensile stress and strain datasets

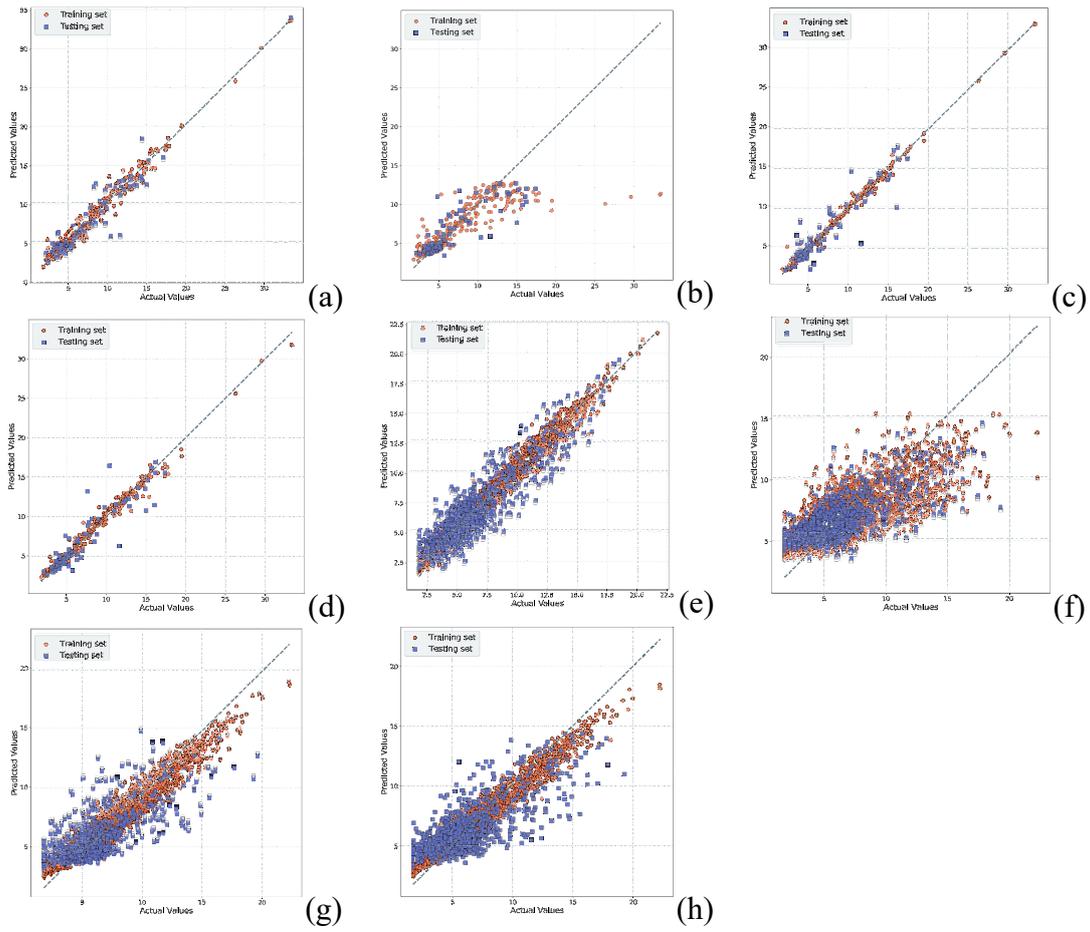
598 5.2 Model prediction

599 [Figures 11](#) and [12](#) illustrate the scatter plots of four ML models before and after
600 data augmentation with the x-axis denoting the actual values and the y-axis reflecting
601 the predicted values. The diagonal line displays a comparison between the actual and
602 predicted tensile stress or strain of ECC. The closeness of the data points to the diagonal
603 line is indicative of the accuracy of the predictions. A data point located near the
604 diagonal line indicates a minor difference between the real and predicted values,
605 demonstrating the accuracy of the forecasting model. Besides, the corresponding

606 evaluation indexes of four ML models before and after data augmentation are
607 summarized in [Tables 5](#) and [6](#), respectively.

608 Before the data augmentation, the XGBoost model indicates the highest predictive
609 accuracy in the stress dataset with the respective MAE, R^2 , and MSE values of 1.189,
610 0.874, and 1.425, as shown in [Table 5](#). Its performance in accurately predicting the ECC
611 stress can be verified in [Figure 11a](#) showing few outliers. The Gradient Boosting
612 Regressor and RF also demonstrate high predictive accuracy, achieving R^2 values of
613 0.847 and 0.846, respectively. In the strain dataset, RF model possesses the highest
614 predictive accuracy ($R^2=0.805$), followed by the XGBoost ($R^2=0.772$) and Gradient
615 Boosting Regressor ($R^2=0.757$), as shown in [Table 6](#). Thus, the tensile strain prediction
616 is observed to be more complex and challenging compared to the prediction of tensile
617 stress. The SVR models exhibit poor generalization ability in predicting both stress and
618 strain due to the low values of R^2 .

619 The obtained results are derived from the optimized ML models using the HGS
620 algorithm. After hyperparameters' tune, `max_depth`, `learning_rate`, and `n_estimators` of
621 XGBoost with the initial boundaries of [1, 100], [0.01, 1], and [1, 100], respectively are
622 determined as 44, 0.856, and 47 (stress dataset) and 39, 0.793, and 25 (strain dataset).
623 Besides, `n_estimators` and `max_depth` of Gradient Boosting Regressor in training stress
624 and strain are 78, 7 and 70, 7, respectively. Regarding the RF model, the two parameters
625 are set as 76, 11 and 94, 13, respectively. Besides, the kernel function used in the SVR
626 model is the Radial Basis Function.



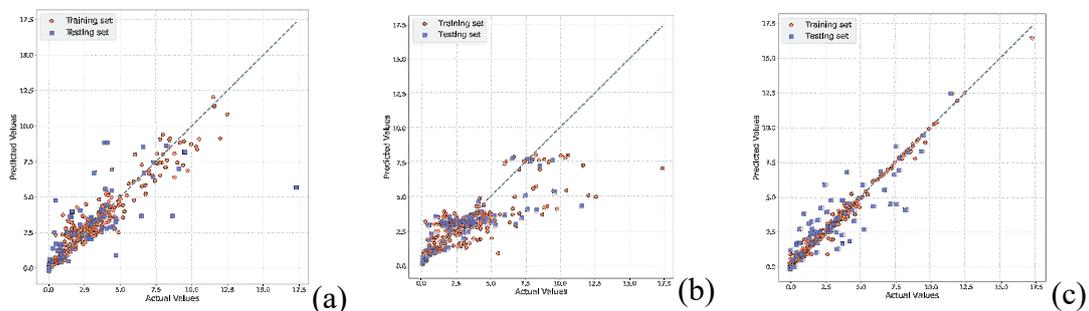
627 **Figure 11.** Training and testing accuracy of established stress prediction models
 628 before augmentation: (a) XGBoost (b) SVR (c) Gradient Boosting Regressor (d) RF
 629 and after augmentation: (e) XGBoost (f) SVR (g) Gradient Boosting Regressor (h) RF

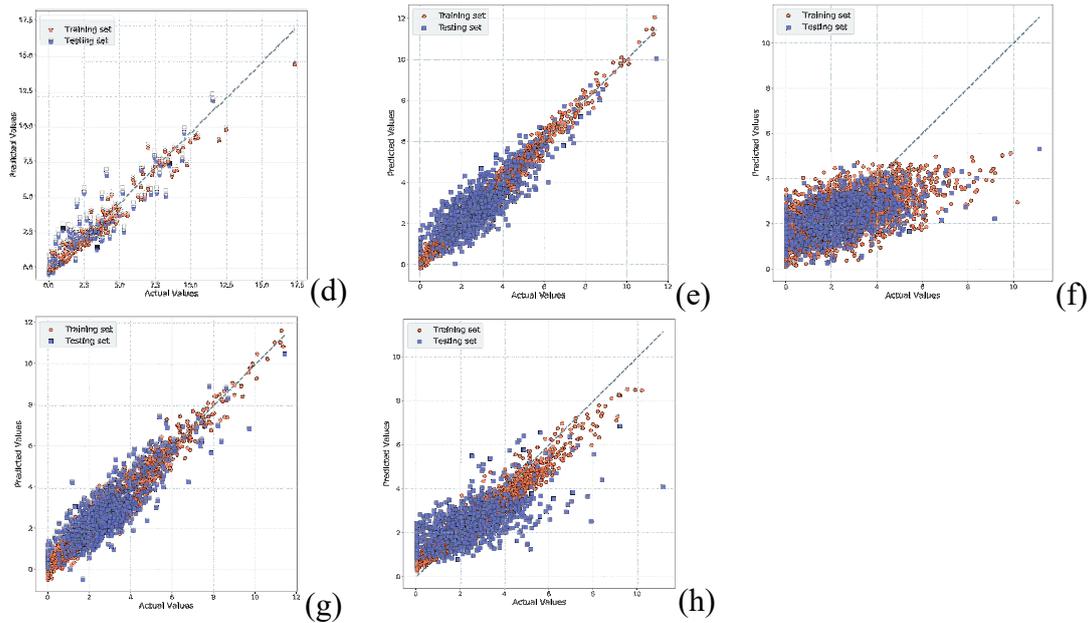
630 **Table 5.** The evaluation metric of varying ML models before and after tensile stress
 631 data augmentation

	XGBoost	SVR	Gradient Boosting Regressor	RF
Before data augmentation				
RMSE (trainset/testset)	1.667/1.425	2.871/2.216	0.352/1.534	0.593/1.539
MAE	0.998/1.189	1.374/1.442	0.180/0.990	0.389/0.951
R ²	0.881/0.874	0.627/0.680	0.994/0.847	0.984/0.846
After data augmentation				
RMSE	0.587/0.829	1.924/2.086	0.926/2.077	0.794/1.990
MAE	0.545/0.737	1.378/1.558	0.742/1.579	0.620/1.527
R ²	0.966/0.925	0.566/0.499	0.895/0.756	0.926/0.544

633 After the data augmentation, the tensile stress and strain data points are increased
634 to 5,000. In Figures 11a and 12a, the XGBoost model exhibited significantly improved
635 performance, especially in the strain dataset. The values of R^2 in the stress and strain
636 test sets are increased from 0.874 to 0.925 and from 0.772 to 0.889, respectively. The
637 other two evaluation indexes (MAE and MSE), are correspondingly reduced which
638 further verifies the efficacy of data augmentation. However, the evaluation indexes of
639 other ML models are worse after the data augmentation, with SVR and RF being
640 especially impacted. The possible reason is their poor capacity to resist overfitting when
641 handling complex datasets characterized by high feature dimensions and large volumes
642 of data. In contrast, XGBoost applies its regularization and optimization techniques to
643 overcome the overfitting problems.

644 It is acknowledged that the reliability of the proposed design hinges on the
645 precision of the established ML models. Inaccuracies in the predictive capability can
646 lead to considerable errors. The high values of R^2 of XGBoost models in this study
647 (0.925 and 0.889) on both tensile stress and strain datasets demonstrate the relatively
648 reliable predictive ability. In conclusion, XGBoost is finally established based on
649 CTGAN data augmentation and HGS hyperparameters' optimization, which is used as
650 the objective function in multi-objective optimization tasks.





651 **Figure 12.** Training and testing accuracy of established strain prediction models
 652 before augmentation: (a) XGBoost (b) SVR (c) Gradient Boosting Regressor (d) RF
 653 and after augmentation: (e) XGBoost (f) SVR (g) Gradient Boosting Regressor (h) RF

654 **Table 6.** The evaluation metric of varying ML models before and after tensile strain
 655 data augmentation

	XGBoost	SVR	Gradient Boosting Regressor	RF
Before data augmentation				
RMSE (trainset/testset)	1.612/1.414	1.513/1.628	0.286/1.296	0.528/1.160
MAE	0.912/0.845	0.884/1.065	0.169/0.912	0.338/0.888
R ²	0.833/0.772	0.660/0.616	0.912/0.757	0.958/0.805
After data augmentation				
RMSE	0.581/0.631	1.183/1.302	0.595/1.012	0.493/1.212
MAE	0.640/0.546	0.877/1.006	0.482/0.920	0.398/0.958
R ²	0.936/0.889	0.411/0.292	0.850/0.726	0.897/0.386

656

657 5.3 Multi-objective optimization

658 When implementing NSGA-III for multi-objective optimization, the water and air
 659 curing ages are respectively set as 28 and 0 days to guarantee the same curing method
 660 and time. Besides, although the fiber content in the original database ranged from 0.003
 661 to 0.3, the actual dosage is usually below 0.03 [92]. When fiber content is low, the

662 bridging stress is inadequate for supporting widespread crack propagation due to the
663 scarcity of fibers within the mortar matrix. When the tensile stress across a given
664 interface length falls beneath the matrix's cracking strength, this results in a reduction
665 of interface number that is unfavorable for crack spread [40]. In contrast, exceeding a
666 fiber content of 0.03 compromises the matrix's workability, causing issues like fiber
667 clustering and a greater occurrence of sizable voids. These problems significantly
668 detract from the composite's tensile strength [91]. Therefore, the upper limit of fiber
669 content in this study is set as 0.03.

670 [Figure 13](#) depicts the multi-objective optimization (maximizing peak tensile stress,
671 maximizing peak tensile strain, and minimizing cost) by NSGA-III for ECC
672 incorporating each kind of fiber. In these figures, a total of 100 Pareto points are
673 represented by dots and are widely distributed across the feasible objective space,
674 showcasing a reasonable range of stress, strain, and cost values. The original dataset
675 points are denoted by small crosses in the figures. By implementing constraints (Min-
676 max, volume, ratio, and fiber constraints), the obtained results are more practical and
677 reasonable. This distribution serves as a testament to the efficacy of NSGA-III in
678 addressing the complexities of multi-objective optimization problems. Within each plot,
679 three points correspond to the maximum tensile strain, minimum cost, and maximum
680 tensile stress among the Pareto points, where their corresponding mixture designs are
681 presented in [Tables 7 to 9](#).

682 Compared to the other fibers, the largest tensile strain is observed in PE
683 incorporated ECC with the largest strain value of 10.51%. The contents of cement,
684 water, fine aggregate, fly ash, silica fume, slag, and superplasticiser are 0.23, 0.19, 0.25,
685 0.25, 0.04, 0.06, and 0.01, respectively. The aggregate to binder ratio is 0.16 and the
686 water to binder ratio is 0.32. The tensile strain of 10.51% is higher than PVA-ECC

687 (6.45%) and is significantly higher than PP-ECC (2.73%) or Steel-ECC (2.08%). PE
688 fibers are distinguished by their exceptional ductility and ability to withstand significant
689 deformation without rupture [40]. This characteristic permits ECC incorporating PE
690 fibers to demonstrate strain-hardening behavior when subjected to tensile stresses, thus
691 improving tensile strain capacity. The inherent flexibility and toughness of PE fibers
692 enhance crack bridging capacities, enabling a more effective distribution of stress and
693 preserving structural integrity under loading conditions, resulting in a superior tensile
694 strain performance relative to ECC reinforced with PP, steel, or PVA fibers [39]. While
695 PP fibers exhibit flexibility, they lack the comprehensive elongation performance and
696 adhesion properties with the cement matrix exhibited by PE fibers. Conversely, steel
697 fibers offer reduced elongation capabilities despite their high tensile strength,
698 constraining the composite's ability to deform prior to failure. PVA fiber suffers from
699 the poor dispersion which affects its strain capacity and durability under tensile loading.

700 Apart from PE-ECC, the sum of binder content and values of water to cement ratio
701 in ECC incorporated with other fibers are all higher than 0.6 and below 0.3, respectively,
702 to achieve the highest peak tensile strain. It indicates that the high binder content and
703 low water to cement ratio are essential in ECC which is consistent with the previous
704 researches. When the binder content is low, the strength of the matrix decreases notably,
705 resulting in weaker bonding strength at the fiber-matrix interface. At specific fiber
706 concentrations, fibers may entirely detach from the matrix under tensile load,
707 eliminating the potential for strain hardening. Additionally, maintaining a low water to
708 cement ratio is crucial, primarily to ensure the mortar matrix remains dense.

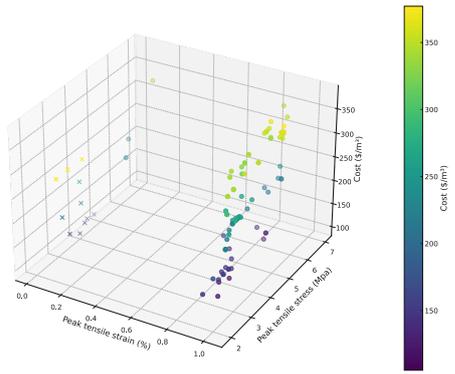
709 PE, steel, PE-Steel hybrid, and UHMWPE fibers are four types of reinforcement
710 that enable ECC composites to reach peak tensile stress levels of approximately 15MPa.
711 In contrast, the stress observed in ECC composites reinforced with other fibers is found

712 to be approximately half that of ECC composites reinforced with PE, Steel, or
713 UHMWPE fibers. This is mainly due to the properties of fiber and the fiber-matrix
714 structure. Steel fibers possess high tensile strength and stiffness, significantly
715 enhancing the composite's load-bearing capacity to facilitate the efficient stress transfer.
716 PE and UHMWPE fibers exhibit excellent tensile strength and elongation at break,
717 which are crucial for the composite's toughness, bond capabilities, and crack resistance.
718 The incorporation of PE-Steel hybrid fibers leverages the high stiffness and strength of
719 steel with the flexibility and toughness of PE, resulting in a composite that exhibits both
720 high peak stress and enhanced ductility [89]. The largest peak tensile stress is found as
721 15.25MPa for ECC incorporated with 1.5%vol PE_STEEL. The diameter, length,
722 tensile strength, and elastic modulus of PE_STEEL are 127 micro-meter, 20mm,
723 5481MPa, and 285GPa, respectively. However, these values are theoretical estimates,
724 given that PE_STEEL is a composite material consisting of PE fiber and Steel fiber. It
725 is assumed that these properties of a hybrid fiber can be estimated by averaging the
726 characteristics of the individual fibers according to their proportions in the mixture.

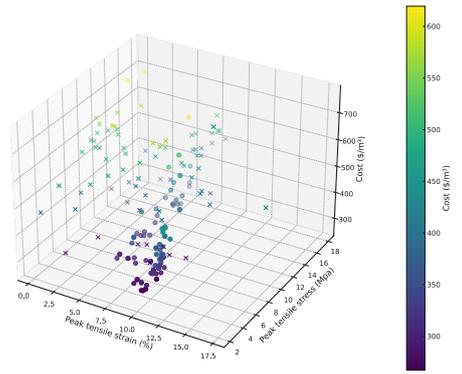
727 Within the 100 Pareto points, the mixture designs corresponding to the lowest cost
728 are summarized in [Table 10](#). The peak tensile strain and peak tensile stress are reduced
729 with the reduction of cost. The lowest cost can be found as 105 \$/m³ in Basalt-ECC
730 with a fiber content of 0.4%. The corresponding tensile stress and strain are 3.79MPa
731 and 0.89%, respectively. This variability in achievable properties allows for a range of
732 options to be considered and selected by the decision-maker based on specific project
733 requirements. Compared to Pareto points within multi-objective optimization, direct
734 optimization for specific mixture proportions is more practical in actual situations. In
735 generic multi-objective optimization tasks, the Pareto points are randomly generated
736 until the end condition is reached. For specific engineering applications, this may result

737 in numerous useless results that are not superior to the existing mixture design at all
738 these three objectives. Therefore, this study conducts directed optimization for two
739 samples of PE and PV (two typical fiber types). This can be achieved by setting up three
740 additional objective constraints, namely the lower limit of tensile stress and tensile
741 strain and the upper limit of cost. The actual and the optimized mixture designs are
742 shown in [Table 10](#). For instance, the strain, cost, and stress values of the chosen PVA-
743 ECC sample are 3.7%, 134.45\$/m³, and 4.8MPa, respectively. After optimization, these
744 objectives can be enhanced to 4.69%-122.58\$/m³-7.53 MPa, 3.82%-123.89\$/m³-5.41
745 MPa, and 3.74%-115.42\$/m³-7.22 MPa according to the established AI models and
746 constraints. Similarly, this direct optimization can be found in PE-ECC samples. In
747 cases of optimizing certain properties while keeping a strain or stress value constant,
748 the performance bounds can be adjusted strictly.

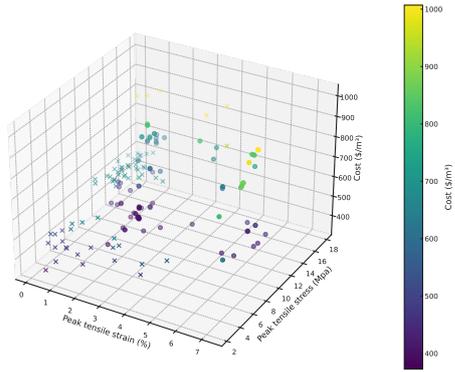
749 However, it is noted that the optimized designs represent local optima rather than
750 global optima. This implies the existence of alternative mixture designs that could
751 potentially yield equivalent or superior objective values. Besides, the optimized mixture
752 designs derived in this study can offer guidance for practical projects to a certain extent.
753 However, given that the data originate from literature, the model bias caused by
754 incomplete data is inevitable. Therefore, in practical engineering applications, actual
755 validation is required to ensure the reliability of the proposed designs. For attaining
756 more precise and globally optimal design mixtures, it is essential to compile a more
757 comprehensive database reflecting local materials and environmental conditions.



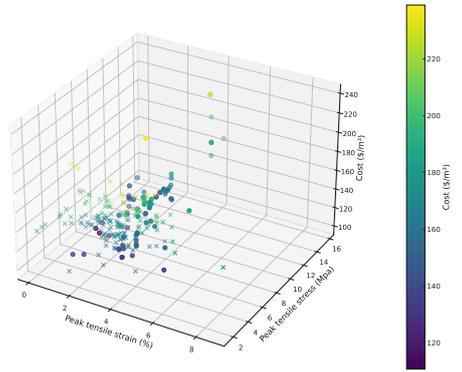
(a)



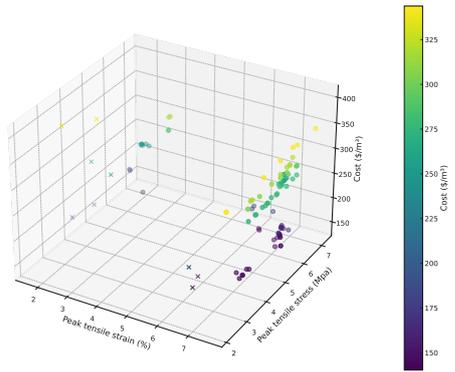
(b)



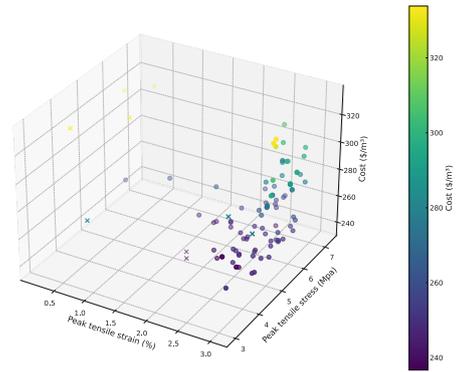
(c)



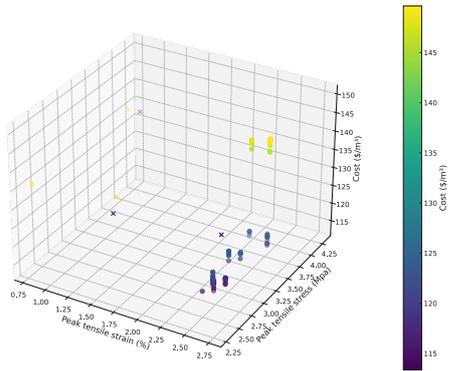
(d)



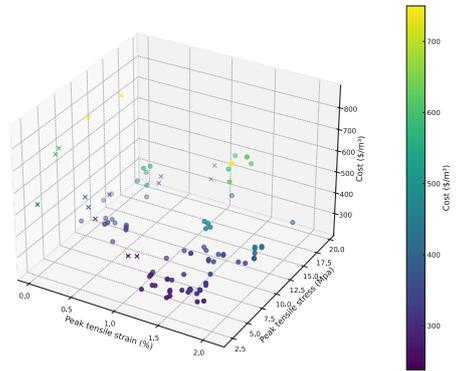
(e)



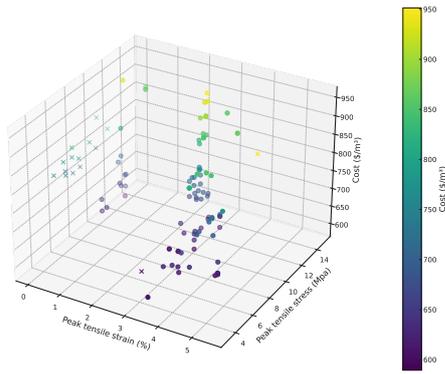
(f)



(g)



(h)



(i)

758 **Figure 13.** Multi-objective mixture designs of ECC for each fiber type from (a) to (i)

759

760 **Table 7.** The multi-optimization of strain-cost-stress for each fiber type (Max peak

761 tensile strain)

Cement (%W)	Water (%W)	Fine Agg (%W)	Fly ash (%W)	Silica Fume (%W)	Slag (%W)	Superplasticizer (%W)	Fiber types	Fiber content (100% Vol)	F. Diameter (Micro - Meter)	Fiber Length (mm)	Fiber Tensile Strength (Mpa)	Fiber Elastic Modulus (Gpa)	HPMC (Viscosity Agent)	Oiling Agent/coating	Temperature (Celsius)	Water Curing (days)	Air Curing (days)	Peak tensile strain (%)	Cost (\$/m ³)	Peak tensile stress (Mpa)
0.53	0.19	0.11	0.09	0.01	0.04	0.00	Basalt	0.018	13	10	2600	85	0	0	20	28	0	1.02	261.88	2.50
0.23	0.19	0.25	0.25	0.04	0.06	0.01	PE	0.012	47	23	3645	135	0	0	20	28	0	10.51	295.95	6.05
0.37	0.13	0.04	0.00	0.19	0.29	0.01	PE_STEEL	0.016	82	34	6248	152	0	0	20	28	0	7.24	1006.98	8.32
0.46	0.19	0.14	0.22	0.01	0.00	0.00	PVA	0.023	40	11	1340	36	0	0	20	28	0	6.45	183.83	4.25
0.13	0.17	0.20	0.46	0.00	0.00	0.00	PVA_Ca	0.020	22	14	2309	323	0	0	20	28	0	7.28	142.16	6.03
0.18	0.19	0.13	0.44	0.03	0.00	0.00	PVA_STEEL	0.026	99	8	2306	97	0	0	20	28	0	3.05	328.67	5.16
0.19	0.18	0.07	0.55	0.00	0.00	0.00	Poly	0.025	12	10	850	6	0	0	20	28	0	2.73	149.65	3.33
0.59	0.12	0.01	0.05	0.06	0.13	0.03	STEEL	0.025	234	11	3310	377	0	0	20	28	0	2.08	402.91	9.61
0.45	0.18	0.12	0.18	0.04	0.05	0.01	UHMWPE	0.021	21	13	3000	101	0	0	20	28	0	4.56	778.37	7.44

762

763 **Table 8.** The multi-optimization of strain-cost-stress for each fiber type (Min Cost)

Cement (%W)	Water (%W)	Fine Agg (%W)	Fly ash (%W)	Silica Fume (%W)	Slag (%W)	Superplasticizer (%W)	Fiber types	Fiber content (100% Vol)	F. Diameter (Micro - Meter)	Fiber Length (mm)	Fiber Tensile Strength (Mpa)	Fiber Elastic Modulus (Gpa)	HPMC (Viscosity Agent)	Oiling Agent/coating	Temperature (Celsius)	Water Curing (days)	Air Curing (days)	Peak tensile strain (%)	Cost (\$/m ³)	Peak tensile stress (Mpa)
0.49	0.20	0.27	0.03	0.00	0.02	0.00	Basalt	0.004	13	8	2600	85	0	0	20	28	0	0.89	105.48	3.79
0.23	0.19	0.23	0.25	0.02	0.07	0.02	PE	0.010	28	36	4649	137	0	0	20	28	0	9.38	267.05	3.53
0.48	0.11	0.34	0.00	0.02	0.03	0.01	PE_STEEL	0.007	221	33	5956	234	0	0	20	28	0	1.68	372.50	11.63
0.19	0.17	0.27	0.37	0.01	0.00	0.00	PVA	0.013	39	11	1429	36	0	0	20	28	0	1.27	110.70	6.54
0.13	0.17	0.21	0.48	0.00	0.00	0.00	PVA_Ca	0.020	28	12	2687	275	0	0	20	28	0	7.02	140.31	6.42
0.23	0.18	0.16	0.42	0.00	0.00	0.00	PVA_STEEL	0.020	138	11	2183	102	0	0	20	28	0	2.22	236.69	5.23
0.19	0.19	0.06	0.57	0.00	0.00	0.00	Poly	0.016	12	10	850	6	0	0	20	28	0	2.45	113.35	2.81
0.45	0.25	0.01	0.05	0.05	0.16	0.01	STEEL	0.010	308	27	4626	326	0	0	20	28	0	1.38	237.77	4.68
0.50	0.18	0.17	0.10	0.01	0.05	0.00	UHMWPE	0.016	18	13	3000	102	0	0	20	28	0	4.31	589.40	7.67

764

765 **Table 9.** The multi-optimization of strain-cost-stress for each fiber type (Max peak

766 tensile stress)

Cement (%W)	Water (%W)	Fine Agg (%W)	Fly ash (%W)	Silica Fume (%W)	Slag (%W)	Superplasticizer (%W)	Fiber types	Fiber content (100% Vol)	F. Diameter (Micro - Meter)	Fiber Length (mm)	Fiber Tensile Strength (Mpa)	Fiber Elastic Modulus (Gpa)	HPMC (Viscosity Agent)	Oiling Agent/coating	Temperature (Celsius)	Water Curing (days)	Air Curing (days)	Peak tensile strain (%)	Cost (\$/m ³)	Peak tensile stress (Mpa)
0.45	0.19	0.21	0.07	0.06	0.01	0.00	Basalt	0.020	13	8	2600	85	0	0	20	28	0	0.84	343.83	6.99
0.29	0.12	0.20	0.06	0.19	0.09	0.02	PE	0.012	44	8	3811	73	0	0	20	28	0	6.16	619.40	15.70
0.55	0.12	0.24	0.00	0.03	0.02	0.03	PE_STEEL	0.015	127	20	5481	285	0	0	20	28	0	3.91	712.26	15.25
0.27	0.12	0.27	0.28	0.02	0.00	0.00	PVA	0.013	35	8	1432	30	0	0	20	28	0	1.97	150.78	8.71
0.17	0.17	0.21	0.47	0.00	0.00	0.00	PVA_Ca	0.028	14	14	2034	313	0	0	20	28	0	1.67	183.82	6.58
0.25	0.16	0.24	0.35	0.01	0.00	0.00	PVA_STEEL	0.020	115	11	2326	94	0	0	20	28	0	2.51	255.13	7.24
0.19	0.18	0.07	0.55	0.00	0.00	0.00	Poly	0.025	12	10	850	6	0	0	20	28	0	2.73	149.65	3.33
0.41	0.12	0.14	0.05	0.05	0.16	0.03	STEEL	0.022	307	12	4602	383	0	0	20	28	0	2.04	359.37	15.80
0.26	0.10	0.31	0.15	0.14	0.01	0.01	UHMWPE	0.018	24	13	3000	113	0	0	20	28	0	0.19	864.94	14.87

768 **Table 10.** The direct optimization of strain-cost-stress for specific mixture design

Cement t (%W)	Water (%W)	Fine Agg (%W)	Fly ash (%W)	Silica Fume (%W)	Slag (%W)	Superc plasticis er (%W)	Fiber types	Fiber conten t (100% Vol)	F. Diame ter (Micro - Meter)	Fiber Length (mm)	Fiber Tensile Streng th (Mpa)	Fiber Elastic Modul us (Gpa)	HPMC (Visco sity Agent)	Oiling Agent/ coatin g	Tempe rature (Celsi us)	Water Curing (days)	Air Curing (days)	Peak tensile strain (%)	Cost (\$/m 3)	Peak tensile stress (Mpa)
0.16	0.16	0.23	0.45	0.00	0.00	0.00	PVA	0.020	39	12	1620	43	0	0	20	28	0	3.70	134.45	4.80
0.22	0.12	0.31	0.31	0.00	0.00	0.00	PVA	0.014	40	10	1152	28	0	0	20	28	0	4.69	122.58	7.53
0.24	0.18	0.46	0.13	0.01	0.00	0.00	PVA	0.015	36	9	1155	26	0	0	20	28	0	3.82	123.89	5.41
0.10	0.10	0.41	0.35	0.00	0.00	0.01	PVA	0.011	39	10	1240	33	0	0	20	28	0	3.74	115.42	7.22
0.37	0.17	0.45	0.00	0.00	0.00	0.01	PVA	0.025	39	12	1620	43	1	1	20	28	0	4.59	182.94	5.00
0.17	0.11	0.32	0.42	0.00	0.00	0.00	PVA	0.019	40	10	1238	43	1	1	20	28	0	4.93	136.58	6.52
0.21	0.09	0.36	0.30	0.01	0.00	0.00	PVA	0.020	40	10	1410	42	1	1	20	28	0	4.61	151.58	6.68
0.24	0.10	0.30	0.31	0.02	0.00	0.00	PVA	0.013	40	10	1609	27	1	1	20	28	0	4.80	143.20	8.87
0.70	0.21	0.00	0.00	0.08	0.00	0.02	PE	0.018	70	22	4698	142	0	0	20	28	0	3.50	509.28	3.10
0.32	0.15	0.15	0.29	0.06	0.04	0.00	PE	0.020	49	21	3405	122	0	0	20	28	0	5.80	462.16	5.31
0.23	0.15	0.08	0.23	0.13	0.18	0.00	PE	0.015	61	24	4562	68	0	0	20	28	0	6.95	501.08	3.22
0.32	0.15	0.15	0.30	0.06	0.04	0.00	PE	0.015	49	21	2822	122	0	0	20	28	0	6.09	389.84	4.47
0.53	0.12	0.20	0.00	0.13	0.00	0.01	PE	0.020	24	18	3000	120	0	0	23	28	0	7.00	633.40	7.10
0.44	0.12	0.12	0.12	0.09	0.11	0.00	PE	0.014	40	32	2528	114	0	0	20	28	0	7.96	449.44	7.88
0.27	0.13	0.23	0.16	0.08	0.13	0.02	PE	0.016	24	28	3689	79	0	0	20	28	0	8.80	462.35	9.16
0.29	0.11	0.13	0.07	0.06	0.30	0.02	PE	0.010	61	13	3078	123	0	0	20	28	0	7.35	400.36	10.55

769

770 **6. Conclusion**

771 ECC is a strain-hardening cementitious material with high tensile strength and
772 ductility mainly due to the fiber micromechanical reinforcement. This study proposes
773 a novel MOO framework to achieve a reliable and smart mixture design of ECC. The
774 main conclusions are drawn as follows:

775 (1) Data augmentation is performed using a Tuned-CTGAN on both tensile stress
776 and strain datasets. As evidenced by its high KSTest and CSTest values for 18 features,
777 the reliability of virtual data generation has been verified.

778 (2) The HGS algorithm is applied to automatically tune the hyperparameters of ML
779 models. The XGBoost and RF show the highest predictive accuracy in tensile stress and
780 strain datasets before the data augmentation, respectively.

781 (3) After the data augmentation, the evaluation indexes of SVR and RF become
782 worse. In contrast, the values of R^2 of XGBoost in stress and strain test sets are
783 increased from 0.874 to 0.925 and from 0.772 to 0.889, respectively.

784 (4) The NSGA-III successfully generates the Pareto front for multi-objective
785 (tensile stress, tensile strain, and cost) with four classes of constraints (Min-max,
786 volume, ratio, and fiber). It depends on the decision-maker to select the multi-objective

787 optimization solutions. Future research will conduct cost-based optimization,
788 incorporating a cost formula that takes into account fiber parameters and regions.

789 Future researches: Since the observed phenomenon showed a negative influence
790 of data augmentation on SVR, RF, and GBR, the possible reason is they are not suitable
791 to tackle big database tasks. The efficacy of data augmentation will be investigated on
792 deep learning algorithms in the future.

793 **Declaration of Generative AI and AI-assisted technologies in the writing process**

794 During the preparation of this work, the authors used ChatGPT-4 in order to
795 improve readability and language. After using this tool/service, the authors reviewed
796 and edited the content as needed and took full responsibility for the content of the
797 publication.

798 **Reference**

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Appendix

Appendix 1. Statistical analysis of variables for the original 429 ECC stress data

Variables	Minimum	Maximum	Mean	Std Dev	Skewness	Kurtosis
Cement (%wt)	0.093	0.755	0.347	0.157	0.726	-0.142
Water (%wt)	0.029	0.230	0.142	0.045	-0.230	-0.916
Fine Agg (%wt)	0.0	0.541	0.228	0.119	-0.159	-0.115
Fly ash (%wt)	0.0	0.646	0.170	0.201	0.631	-1.144
Silica Fume (%wt)	0.0	0.246	0.048	0.054	0.887	0.172
blast furnace slag (%wt)	0.0	0.439	0.040	0.100	2.373	4.044
Superplasticiser (%wt)	0.0	0.028	0.009	0.008	0.897	-0.333
Fiber content (100%vol)	0.003	0.200	0.023	0.019	7.393	61.218
F. Diameter (micro-meter)	7.667	550.0	59.391	62.945	2.716	10.630
F. Length (mm)	2.061	38.0	14.191	5.660	1.065	1.707
F. Tensile Strength (MPa)	850.0	6360.0	2450.852	885.831	0.965	2.062
F. Elastic Modulus (GPa)	6.0	472.11	104.209	74.905	1.970	5.361
HPMC	0.0	1.0	0.090	0.280	2.910	6.610
Oiling Agent	0.0	1.0	0.261	0.440	1.092	-0.812
Temperature (Celsius)	0.0	500.0	35.634	46.911	5.590	41.424
Water Curing (days)	0.0	91.0	20.186	14.505	1.287	5.359
Air Curing (days)	0.0	112.0	5.375	13.061	4.110	24.052
Peak tensile stress (MPa)	1.8	33.4	7.360	4.575	1.834	5.505

Appendix 2. Statistical analysis of variables for the original 392 ECC strain data

Variables	Minimum	Maximum	Mean	Std Dev	Skewness	Kurtosis
Cement (%wt)	0.093	0.698	0.337	0.160	0.754	-0.136
Water (%wt)	0.029	0.230	0.145	0.044	-0.373	-0.792
Fine Agg (%wt)	0.0	0.541	0.231	0.123	-0.195	-0.283
Fly ash (%wt)	0.0	0.646	0.191	0.210	0.427	-1.445
Silica Fume (%wt)	0.0	0.246	0.042	0.052	0.970	0.269
blast furnace slag (%wt)	0.0	0.384	0.028	0.085	3.010	7.562
Superplasticiser (%wt)	0.0	0.028	0.009	0.008	0.882	-0.493
Fiber content (100%vol)	0.003	0.200	0.023	0.020	7.117	56.303
F. Diameter (micro-meter)	7.667	320.0	61.875	59.667	1.964	3.279
F. Length (mm)	2.061	38.0	13.643	5.927	1.245	1.805
F. Tensile Strength (MPa)	850.0	6360.0	2342.169	915.499	1.211	2.300
F. Elastic Modulus (GPa)	6.0	472.11	99.956	78.215	1.941	4.836
HPMC	0.0	1.0	0.107	0.306	2.576	4.691
Oiling Agent	0.0	1.0	0.283	0.451	0.966	-1.072
Temperature (Celsius)	0.0	500.0	35.872	48.463	5.517	39.609
Water Curing (days)	0.0	91.0	19.209	14.912	1.493	5.530
Air Curing (days)	0.0	112.0	7.168	17.291	3.467	13.527

Peak tensile strain (%)	0.017	17.3	3.030	2.619	1.530	3.095
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