The Effect of Sand and Dust Storms (SDSs) and Rain on the Performance of Cellular Networks in the Millimeter Wave Band

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ABSTRACT Future cellular systems are expected to use millimeter-wave (mm-Wave) frequency bands in addition to the existing microwave bands under 6 GHz. Severe weather conditions, including sand and dust storms (SDSs) and heavy rainfalls, challenge reliable communications over wireless links at those higher frequencies. In such conditions, besides frequency-dependent path-loss, radio signals experience additional attenuation. The SDS attenuation is related to visibility, receiver distance to the storm origin point, soil type, frequency, temperature and humidity. On the other hand, the rainfall attenuation is affected by rainfall rate, polarization, carrier frequency, temperature and raindrop size distribution. Leveraging on experimental measurements carried out in previous works, a novel unified mathematical framework is introduced in this paper to include SDS/rainfall-dependent attenuation in the performance evaluation of terrestrial wireless cellular networks in terms of coverage probability, bit error rate (BER) and achievable rate in the mm-Wave band. Extensive numerical results are presented to show the effects of the different SDS/rainfall parameters on performance, showing that the degradation due to SDS is generally higher than that due to rain and may cause a reduction of even six orders of magnitude in the average achievable bit rate when the frequency increases from 28 to 38 GHz.

INDEX TERMS Cell Planning, Cellular Networks, mm-Wave Band, Performance Analysis, Rainfall, Sand and Dust Storm.

I. INTRODUCTION

Due to the high demands and expectations envisioned for future generations of cellular networks, exploiting higher frequencies in the mm-Wave bands seems to be inevitable [1]. Furthermore, the forthcoming 5th generation (5G) cellular communications technology is a diverse and heterogeneous network in terms of base stations (BSs) and operating frequency bands. Machine-to-machine (M2M) [2], device-to-device (D2D) [3], and low power wide area (LPWA) communications are examples of what 5G is supporting. In general, most research in the aforementioned areas in the context of 5G heterogeneous networks assume regular weather conditions. Since 5G is going to be deployed worldwide, it is critical to investigate cellular networks’ performance in extreme weather conditions, such as heavy rainfalls and sand and dust storms (SDSs).

The main effect of rainfall and precipitation on wireless signal transmission is an increase of signal attenuation [4], [5], which is usually quantified in terms of the measured rain rate during a given time percentage. Attenuation per
unit length curves for frequencies between 3 and 100 GHz for different rainfall rates can be found in [6]. Also, scattering and phase fluctuations effects caused by rainfall on the performance of a wireless link using multiple antennas has been investigated [7]. The attenuation and scattering in radio links due to rain is predicted from rainfall rate statistics with a 1-min integration, and a method to obtain the rainfall rate exceeded for any given time percentage and for any location at 1-min integration time has been established by ITU-R and presented in [8]. Also, methods to estimate 1-min rain rate by making a better use of the available data are discussed in [9], [10]. In [11] a modified effective rainfall rate method is proposed to include the prevailing wind direction during rainy conditions as an additional parameter for the prediction of rain attenuation. Studies on attenuation due to rainfall have shown that, in non-tropical regions with rainfall rates lower than 100 millimeter per hour (mm/h), the attenuation due to rainfall does not contribute significantly to the overall path loss for short distance wireless links below 200 m [5]. However, for higher frequencies or distances, or in tropical areas with rainfall rates above 100 mm/h, the attenuation due to rain cannot be ignored. For instance, for a Tx-Rx (transmitter to receiver) distance of 200 m with a rain attenuation of 25 mm/h at 28 GHz, the rain attenuation is 1.4 dB, which can be neglected when compared to the distance-dependent path loss of around 80 dB. However, the rainfall rate in tropical areas such as Kolkata, India, reaches 100 mm/hour at almost 0.01% of the time, which causes a significant attenuation, greater than 10 dB, for the mentioned 200 m distance at 28 GHz [5]. In [12], rain attenuation and drop size distribution measurements are presented at 77 and 300 GHz for up to 20 mm/h rainfall rate. Intense heavy rainfall and large raindrop sizes are studied in [13]–[15]. In [13], the rain rate and rain attenuation at 26 GHz are evaluated by means of experimental measurements in Malaysia on a 5G microwave radio link, and rainfall is categorized based on drizzle, showers and thunderstorms according to its rainfall rate and compared with ITU-R predictions, reporting a total rain attenuation over 1.3 km of 34 dB, while results in [14] show that 18.4 dB/km of rain attenuation can be expected at 38 GHz. Also in Malaysia, the rainfall attenuation is investigated in [16] at 38 GHz, where measurement data were simultaneously collected for rainfall rate and received signal level in 1-minute time over a 300 m path length, reporting an attenuation of 15 dB for an average rain rate of 125 mm/h, which was obtained at 0.01% of the time, while the rain attenuation can be as high as 25.78 dB for a rain rate of 210 mm/h [17]. On the other hand, the rain attenuation fitting distribution at 25.84 and 77.52 GHz mm-Wave 5G bands are studied in [18], and the collected measurement data are presented for short-range links over a year. Additionally, a one-year rain attenuation measurement at 73.5 GHz for a 1.8 km link is presented in [19] that resulted in a maximum attenuation of 40.1 dB for a maximum rain rate of 108 mm/h.

While some parts of the world face heavy rainfalls and precipitations, in other areas SDSs constitute a major challenge for reliable wireless transmission. Wide semi-desert regions and areas with sparse vegetation in America, North Africa and the Middle East experience this harsh atmospheric conditions. Moreover, desertification due to natural or anthropogenic factors results in an increasing rate of occurrence of SDSs [20]–[22]. In these areas, small sand or dust particles1 can be lifted a few meters above the ground level during an SDS, which reduces visibility and, in extreme cases, causes interruption of public services such as power lines and telecommunication networks. SDSs are often characterized in terms of the “Visibility” parameter, which depends on the distance of the point of interest to the source of the storm and the height of the point of interest from the ground level. It is also related to the mass of dust per cubic meter of air and is given in kilometers unit [23]. Thus, wireless communication channel characteristics change in SDS conditions, and, accordingly, the performance of operating wireless systems is affected, as an extra attenuation due to SDS has to be considered, for which different models can be found in the related technical literature. The SDS attenuation has been usually estimated using the Rayleigh approximation [24]–[26] and the Mie solution to Maxwell’s equations (Mie scattering) [27]–[29] for solving the forward scattering amplitude function of a single particle. These methods assume specific particles geometries (spheres, ellipsoids, cubes, etc.) and do not include multiple scattering effect or mutual interaction among particles and their random distribution and orientation. Also, although it is known that the size distribution of dust particles in an SDS can be characterized with a lognormal distribution [26], most SDS attenuation models rely on deterministic values of the Visibility parameter. For these reasons, alternative approaches to SDS attenuation estimation have been proposed, including empirical [30] and statistical [31] models. In our work, we have used the approach in [32] to model SDS attenuation, which is obtained by using the effective material property technique.

Coverage, achievable throughput and bit error rate (BER) are important performance metrics for cellular networks [33]–[35], which are greatly affected by the channel characteristics between the BS and the user equipment (UE). In this regard, rainfall and SDS result in a decrease of the received signal-to-noise ratio (SNR) compared to the clear sky situation. As these atmospheric conditions become more frequent due to global warming, they have to be considered in the design of cellular networks, which were originally designed and deployed without considering such phenomena. For the users, this consequently results in a lower than expected coverage and average achievable throughput, as well as a higher error rate. Performance analysis papers considering rainfall and SDS are very scarce. The effect of SDS on the attenuation of GSM signals is studied in [35], while the impact of rainfall have been investigated for the performance of wireless power transfer [36] and BER in a point-to-point

1Particles with a radius smaller than 60 μm are defined as dust, and larger than that are referred to as sand [23].
wireless link [37]. To the best of our knowledge, no prior work has investigated coverage, achievable throughput and BER degradation of cellular networks due to rainfall and SDS. This is however an immediate need as the performance evaluation of these metrics provide insights on the effect of harsh atmospheric conditions on network design and the cost of alleviating such conditions on network performance.

In this paper a novel unified mathematical framework is introduced to include SDS/rainfall-dependent attenuation in the performance evaluation of wireless cellular systems in terms of coverage, achievable throughput and BER. We assume the location of BSs to be modeled by a Poisson point process (PPP), which is considered in the context of stochastic geometry [38] and which is more realistic than a grid type of BS deployment. We then use distance, precipitation and visibility-dependent path-loss models to evaluate the aforementioned performance metrics at mm-Wave bands. Moreover, multipath propagation results in the reception of multiple replicas of the transmitted signal causing fast variations of the received power as users move. This multipath fading is known to generally have a detrimental impact on cellular performance and it is explicitly considered in the presented analysis, which also constitutes a novelty with respect to previous SDS/rainfall related works. Our analysis provides exact expressions for the degradation of performance metrics as a function of the parameters characterizing the network layout and the instantaneous channel gain. The developed approach further enables network designers with options (e.g., the average number of extra BSs to be deployed per unit area and/or higher BS transmit power) to compensate for the performance degradation due to SDS and rainfall. Specifically, the following key contributions are presented in this paper:

- Exact mathematical expressions are derived for the coverage probability, achievable bit rate and BER of terrestrial wireless cellular networks in the mm-Wave band assuming random BS locations, frequency-dependent path-loss, SDS/rainfall attenuation and Rayleigh multipath fading. The attenuation (in dB/km) due to SDS and rainfall is used as input parameter.
- Extensive numerical results are presented to show the effects of the different SDS/rainfall parameters on performance of the analyzed cellular networks at the system level.
- The cost of provisioning a certain level of performance, in terms of the excess transmission power at the BSs, in the presence of SDS or rainfall is analyzed.

The rest of the paper is organized as follows: Section II describes the system and channel models. Section III presents mathematical derivations for evaluating coverage, achievable rate and BER degradation in terms of visibility and rainfall rate. In Section IV, simulation results are presented, followed by the conclusions in Section V.

II. SYSTEM AND CHANNEL MODEL

We consider the downlink of a cellular network where the BSs are distributed throughout the network according to a homogeneous 2-dimensional Poisson point process (PPP) that results in Voronoi cells [38], $\Phi$, with density $\lambda$ (number of BSs per unit area). It is assumed that UEs connect to their closest BS, which are considered to be equipped with omnidirectional antennas. Users are also assumed to be distributed according to a PPP distribution, $\Phi_u$, with density $\lambda_u$ (number of users per unit area). Distributions $\Phi$ and $\Phi_u$ are assumed to be mutually independent. The probability density function (PDF) of the distance between a user and its nearest BS, $r$, is then expressed as follows [39]:

$$f_R(r) = 2\pi\lambda r \exp(-\lambda\pi r^2).$$

(1)

It is further assumed that the BS transmit power is $P$ watts and UEs are allocated orthogonal channels via one of the orthogonal multiple access schemes, hence there is no inter-user interference.

A. SAND/DUST AND RAINFALL DEPENDENT PATH-LOSS MODELS

1) Sand and Dust

The severity of SDSs is often characterized in terms of the visibility parameter, $V$, which is expressed, in kilometers, as [23]

$$V = \sqrt[2]{\frac{C_s}{M}},$$

(2)

where $M$ is the mass of sand and dust in kilograms per cubic meter of air, and $C_s$ and $\rho_s$ are constants that depend on the distance of the receiver to the storm’s origin point, type of soil and climate conditions.

We follow in this subsection the approach in [32] to
characterize the signal attenuation due to SDS. Assuming the mass density of soil particles to be \( m_d \), the volume fraction occupied by sand and dust particles in a storm is obtained as

\[
V_f = m_d / V^0.
\]

The equivalent complex relative permittivity of SDSs is calculated as

\[
e^{eq} = \epsilon_{air} + \frac{3V_f}{1 - V_f} \left( \epsilon_{sd} - \epsilon_{air} \right) / \left( \epsilon_{sd} + 2\epsilon_{air} \right)
\]

where \( \epsilon_{sd} \) is the complex relative permittivity of sand and dust, for which a number of frequency-dependent values in the range of 3 - 100 GHz are given in [32], and \( \epsilon_{air} \) is the relative dielectric constant of air. Using (4), the SDS-dependent path-loss in dB is also expressed as

\[
\zeta_{k, db}(V, r) = \frac{k_v}{\lambda_0} \left[ \frac{\epsilon_{eq}}{2} \left( \sqrt{1 + \tan^2 \delta} - 1 \right) \right]^{0.5} r
\]

where \( \Theta_{SDS} \) is given in dB/km, \( k_v = 0.017372\pi \), \( \tan \delta \) is \( \epsilon_{eq}/\epsilon_{eq} \), and \( \lambda_0 \) is the wavelength of the radio wave.

2) Rainfall

The attenuation due to rain, \( \Theta_{Rain} \), in (dB/km), is obtained using a power-law relationship as [4], [40]

\[
\Theta_{Rain} = a_{Rain} \times \tilde{R}^{b_{Rain}},
\]

where \( \tilde{R} \) is the rain rate in mm/h and \( a_{Rain} \) and \( b_{Rain} \) are parameters. Thus, the rainfall-dependent path-loss is expressed as

\[
\zeta_{k, db}(\tilde{R}, r) = \Theta_{Rain} \times r,
\]

where \( r \) is given in km, and parameters \( a_{Rain} \) and \( b_{Rain} \) are a function of different factors such as polarization, carrier frequency, temperature and raindrop size distribution, which can be obtained from experimental measurements [4].

Values for \( a_{Rain} \) and \( b_{Rain} \) for horizontal, vertical and circular polarization, and for all path geometries, are calculated in [40], for frequencies, \( f \) (GHz), in the range 1-1000 GHz, as

\[
\log_{10}(a_{Rain}) = \sum_{j=1}^{4} a_j \exp \left[ - \left( \frac{\log_{10} f - b_j}{c_j} \right)^2 \right] + m_a \log_{10} f + c_a,
\]

\[
b_{Rain} = \sum_{j=1}^{5} a_j \exp \left[ - \left( \frac{\log_{10} f - b_j}{c_j} \right)^2 \right] + m_b \log_{10} f + c_b,
\]

where values for the coefficient constant \( a_j, b_j, c_j, m_a, c_a, m_b \) and \( c_b \) are given in Tables 1-4 in [40].

The rain rate provides a measure to characterize different rainfall environments. Thus, for heavy rains, \( 10 \leq \tilde{R} \leq 50 \) mm/h is expected, whereas in tropical areas \( \tilde{R} \) reaches higher values [41]. For instance, in Malaysia, due to its tropical location, the monthly average rain rate is around 200 mm/h during the wet season [42].

B. CHANNEL MODEL

The complex baseband signal amplitude of the frequency-flat fading channel between the \( k \)-th UE to its corresponding BS can be expressed as [43]

\[
h_k = \frac{1}{\alpha_k(r)\zeta_k(r)} h_{\text{w},k}, \quad 1 \leq k \leq K,
\]

where \( \alpha_k(r) \) and \( \zeta_k(r) \) denote, respectively, the distance-dependent and rainfall/SDS-related attenuation, \( K \) denotes the total number of users in a cell, \( r \) denotes the UE-BS distance and \( h_{\text{w},k} \) denotes the channel’s small scale Rayleigh fading, i.e., \( h_{\text{w},k} \) are independent and identically distributed (i.i.d.) zero-mean, unit-variance complex Gaussian random variables, \( \mathcal{CN}(0,1) \).

In the case of SDS, \( \zeta_k(r) \) is a function of the visibility (\( V \)) in the area where user \( k \) is located. In the case of rainfall, \( \zeta_k(r) \) is a function of the rainfall rate (\( \tilde{R} \)). Fig. 1 shows a sample cellular network downlink layout in these conditions.

For the distance dependent path-loss in millimeter-wave frequencies, we adopt the model given in [44] as follows:

\[
\alpha_{k(db)}(r) = A + B \times 10\log_{10}(r),
\]

where parameters \( A \) and \( B \) depend on BS and UE heights, and non-line-of-sight (NLOS) channels are assumed. Table 1 shows path loss parameters, \( A \) and \( B \), for measurements collected in New York City at 28 GHz and Austin, Texas, at 38 GHz, with different BS antenna heights [44].

<table>
<thead>
<tr>
<th>Frequency</th>
<th>TX Height (meter)</th>
<th>RX Height (meter)</th>
<th>( B )</th>
<th>( A ) (dB)</th>
</tr>
</thead>
<tbody>
<tr>
<td>28 GHz</td>
<td>7</td>
<td>1.5</td>
<td>3.73</td>
<td>75.85</td>
</tr>
<tr>
<td>28 GHz</td>
<td>17</td>
<td>1.5</td>
<td>4.51</td>
<td>59.89</td>
</tr>
<tr>
<td>38 GHz</td>
<td>8</td>
<td>1.5</td>
<td>1.28</td>
<td>115.17</td>
</tr>
<tr>
<td>38 GHz</td>
<td>23</td>
<td>1.5</td>
<td>0.12</td>
<td>118.77</td>
</tr>
<tr>
<td>38 GHz</td>
<td>36</td>
<td>1.5</td>
<td>0.41</td>
<td>116.77</td>
</tr>
</tbody>
</table>

In order to evaluate network’s performance, we now define an overall attenuation parameter which depend on distance \( r \), encompassing distance-dependent path-loss \( (\alpha_{k, dB}) \) and SDS/rainfall attenuation \( (\zeta_{k, dB}) \).

**Definition:** The overall attenuation due to distance and rainfall/SDS-based path-loss for the \( k \)-th user is expressed as

\[
L_{k, db}(r) = \alpha_{k, db}(r) + \zeta_{k, db}(r)
\]

\[
= L_c + L_{kg} \ln (r) + L_{fr},
\]

\[\text{where}\]

\[\text{in dB} \]
Proposition 1. Let $P_{C}(T)$ and $\hat{P}_{C}(T)$ be, respectively, the coverage probability under SDS/rainfall and in normal weather conditions, i.e., without SDS/rainfall. The average degradation of coverage probability in a cellular network in SDS or rainfall conditions is given by

$$\Delta P_{C}(T) = \hat{P}_{C}(T) - P_{C}(T)$$

where $\Delta P_{C}(T)$ is the absolute degradation of coverage probability in a cellular network in SDS/rainfall conditions, $\hat{P}_{C}(T)$ is the coverage probability for SDS/rainfall conditions, and $P_{C}(T)$ is the coverage probability for normal weather conditions.

Equation (12) shows that the total power loss in dB is a function of $r$ and $\ln(r)$, whereas in clear sky conditions only the dependence on $\ln(r)$ is present, i.e., the distance dependent path-loss in watts is a function of $r^B$ in the latter case.

Simultaneously considering both SDS/rainfall and distance-dependent attenuation in network performance analysis is a novel contribution of this work, yielding accurate and realistic results for the assumed harsh propagation conditions. For all environment related parameters of $L_{k,db}(r)$, we use values obtained from experimental measurements in the mm-Wave band given in [32, 40] and [44].

III. PERFORMANCE ANALYSIS

We use a cellular downlink network model and an SDS/rainfall attenuation-dependent channel model for the performance analysis carried out in this section in terms of coverage probability, average achievable rate and BER.

The received SNR at the $k$-th user considering SDS/rainfall is given by

$$\Gamma_k = \frac{P[h_k]^2}{N_0}$$

where $P$ is the BS transmitted power, in watts, incorporating all power gains and losses (antenna gains, cable losses, etc.) and $N_0$ is the noise power at the receiver.

A. COVERAGE PROBABILITY

The coverage probability under SDS/rainfall is defined as

$$P_{C}(T) = \mathbb{E}\left\{\text{Pr}\{\Gamma_k > T\}\right\},$$

where $T$ is a predefined threshold that depends on the receivers’ sensitivity, and $\mathbb{E}$ represents the expected value with respect to distance $r$, distributed according to (1), and fading. The coverage probability without SDS/rainfall is defined as $\hat{P}_{C}(T) = \mathbb{E}\left\{\text{Pr}\{\hat{\Gamma}_k > T\}\right\}$, where $\hat{\Gamma}_k = \frac{P[h_k]^2}{N_010^{-L_{k,db}(r)}/10}$, and $L_{k,db}(r) = L_c + L_{lg} \ln(r)$.

Proposition 2. Let $P_{C}(T)$ and $\hat{P}_{C}(T)$ be, respectively, the coverage probability under SDS/rainfall and in normal weather conditions, i.e., without SDS/rainfall. The average degradation of coverage probability in a cellular network in SDS or rainfall conditions is given by

$$\Delta P_{C}(T) = \hat{P}_{C}(T) - P_{C}(T)$$

where $\Delta P_{C}(T)$ is the absolute degradation of coverage probability in a cellular network in SDS/rainfall conditions, $\hat{P}_{C}(T)$ is the coverage probability for SDS/rainfall conditions, and $P_{C}(T)$ is the coverage probability for normal weather conditions.

Proof. See Appendix A.

B. ACHIEVABLE RATE

The average achievable rate is defined as

$$\overline{R} = \mathbb{E}\left\{\log_2(1 + \Gamma_k)\right\},$$

and the degradation of the average achievable rate ($\Delta \overline{R}$) is defined as the difference between the achievable rates in clear sky, $\overline{R}_0$, and with SDS/rainfall, $\overline{R}$, i.e.,

$$\Delta \overline{R} = \mathbb{E}\left\{\log_2(1 + \hat{\Gamma}_k)\right\} - \mathbb{E}\left\{\log_2(1 + \Gamma_k)\right\}.$$
where, from (14),

\[ f_{\gamma}(\gamma) = e^{-\gamma}, \]

we can write

\[
P_{E} = \int_{0}^{\infty} \int_{0}^{\infty} P_{E}(\gamma, r) f_{\gamma}(\gamma) f_{R}(r) d\gamma dr,
\]

which can be rewritten in terms of the defined constants \( \hat{\mu}_{0}, \hat{\mu}_{1} \) and \( \hat{\mu}_{2} \) as

\[
\bar{R}(P, N_{0}, \lambda) = \mathbb{E}_{r} \left\{ \int_{0}^{\infty} \log_{2} \left( 1 + \frac{P_{\gamma}}{N_{0}10^{L_{x, a}(r)/10}} \right) e^{-\gamma d_{r}} \right\}, \quad (23)
\]

which is considered a random variable, the average BER can be calculated by setting \( \hat{\mu}_{2} = 0 \) in (24)

\[
P_{E} = 2\pi \lambda \int_{0}^{\infty} \sum_{m=1}^{M} \alpha_{m} \int_{0}^{\infty} \left( \frac{2\beta_{m}P_{\gamma}}{N_{0}10^{L_{x, a}(r)/10}} \right) e^{-\gamma d_{r}} \] 

\[ \times e^{-\gamma|d_{r}|} \] \[ \times e^{-\gamma d_{r}} dr. \]

The inner integral in (28) can be solved by parts in closed-form, yielding

\[
P_{E} = 2\pi \lambda \int_{0}^{\infty} \sum_{m=1}^{M} \alpha_{m} \int_{0}^{\infty} \left( \frac{2\beta_{m}}{\mu_{0}r^{\mu_{1}}e^{\mu_{2}r}} \right) e^{-\gamma d_{r}} dr \times e^{-\gamma |d_{r}|} \] 

\[ \times \frac{1}{2} \left( 1 - \frac{\beta_{m}}{\mu_{0}r^{\mu_{1}}e^{\mu_{2}r} + \beta_{m}} \right) r^{e^{-\gamma d_{r}}} dr, \]

which after some manipulation can be written as in (27). \( \square \)

IV. NUMERICAL RESULTS

In this section numerical results are presented to investigate the effect of rainfall and SDS on the performance of cellular downlink. Throughout this section, we assume a noise PSD of \( N_{0} = -70 \text{ dBm} \) \( (N_{0} = 10^{-7} \text{ mw}) \) a bandwidth of \( BW = 2600 \text{ MHz} \) (Band 7 - Telstra / Optus for 4G), and, for coverage calculations, a threshold \( T = 0.01 \), unless otherwise stated.

**TABLE 2:** Parameters of rain effect for different frequencies [40].

<table>
<thead>
<tr>
<th>Frequency</th>
<th>( a_{\text{Rain}} )</th>
<th>( b_{\text{Rain}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>24 GHz</td>
<td>0.1425</td>
<td>1.0101</td>
</tr>
<tr>
<td>28 GHz</td>
<td>0.2051</td>
<td>0.9679</td>
</tr>
<tr>
<td>38 GHz</td>
<td>0.4001</td>
<td>0.8816</td>
</tr>
<tr>
<td>75 GHz</td>
<td>1.1048</td>
<td>0.7221</td>
</tr>
</tbody>
</table>

The parameters in (11) are borrowed from Table 1 for \( h_{\text{BS}} = 7 \text{ m} \) and \( h_{\text{UE}} = 1.5 \text{ m} \), where \( h_{\text{BS}}, h_{\text{UE}} \) represent the heights of BS and UE, respectively. Also, parameters of rain effect for horizontal polarization at 24, 28, 38 and 75 GHz are listed in Table 2 [40], while for SDS, \( c_{sd} \) values for different frequencies are taken from Table 3 [32] and find \( \epsilon_{sd}^{*} \) for different visibility values, \( V \), via (3) and (4) for \( m_{sd} = 9.43 \times 10^{-9} \) and \( \rho_{s} = 1.07 \) [32], which are used to obtain the SDS related path-loss \( \zeta_{k,dB}(r) \) in (5).

Fig. 2 shows the average coverage probability degradation due to SDS/rainfall, defined as the difference between coverage probability with and without SDS/rainfall conditions. The summations in (16) are truncated to 15 terms, as higher \( k \) and \( j \) values in the summations indexes have a negligible effect on results. It can be observed that, as expected, either decreasing SDS visibility, in Fig. 2a, or increasing rain rate, in Fig. 2b, increase attenuation and hence decrease coverage. On the other hand, increasing \( \lambda \) decreases the distance of
users to their corresponding BS. Since the attenuation due to SDS and rainfall, as well as the path loss, are related to distance, increasing $\lambda$ reduces the loss. For instance, comparing the curves in Fig. 2a corresponding to $\lambda = 0.001$ and $\lambda = 0.005$ for a SDS visibility of $10^{-1}$ km, reveals that the coverage probability is 0.62 less than the case of clear weather (no SDS) for $\lambda = 0.001$, i.e., $\Delta P_{C} = 0.62$. However, when a larger number of BSs are deployed (i.e., $\lambda = 0.005$), users will be served by BSs which are closer to them; therefore, the loss of coverage probability reduces to 0.26. In the case of rainfall, for $\lambda = 0.001$ it can be observed in Fig. 2b that $\Delta P_{C} = 0.009$, while for $\lambda = 0.005$, $\Delta P_{C} = 0.0004$, which represents more than an order of magnitude difference with respect to the former case.

Fig. 3 shows coverage and average rate as a function of rainfall rate and average SNR, respectively, considering 28 and 38 GHz.

<table>
<thead>
<tr>
<th>Frequency</th>
<th>$\epsilon_{sd} = \epsilon_{sd}' - j\epsilon_{sd}''$</th>
</tr>
</thead>
<tbody>
<tr>
<td>24 GHz</td>
<td>3.6-j0.65</td>
</tr>
<tr>
<td>37 GHz</td>
<td>4.0-j1.3</td>
</tr>
<tr>
<td>100 GHz</td>
<td>3.5-j1.64</td>
</tr>
</tbody>
</table>

TABLE 3: Complex permittivities of SDS for different frequencies [32].
and 38 GHz. Fig. 3a depicts the coverage probability versus rainfall rate. It is observed that, for both frequencies, the coverage probability decreases with increasing rainfall rate, showing a higher slope for 38 GHz. For instance, for a rainfall rate of $\bar{R} = 50$ mm/h, the coverage probabilities at $f = 28$ GHz and $f = 38$ GHz are $P_C = 0.878$ and $P_C = 0.578$, respectively. Also, comparing the results at $\bar{R} = 150$ mm/h and $\bar{R} = 0$ mm/h (no rainfall) reveals that for the case of $f = 28$ GHz, the coverage probability decreases 0.015 (from 0.884 in $\bar{R} = 0$ to 0.869 in $\bar{R} = 150$). However, this degradation is higher (around 0.035) at $f = 38$ GHz. Fig. 3b shows the average achievable bit rate vs. SNR considering SDS. It can be seen that the average achievable bit rate is considerably reduced by as much as 6 orders of magnitude when the frequency increases from 28 to 38 GHz. To obtain the average throughput results of this figure, $\lambda = 0.05$, $V = 0.05$ km for SDS and Bandwidth = 2600 MHz (Band 7 - Telstra / Optus for 4G) have been considered.

Fig. 4 shows the excess transmission power, referred to as cost, required to reach a target coverage probability in the presence of SDS and rain, with respect to the power required in clear sky conditions. Fig. 4a shows the cost with respect to visibility for an SDS scenario. As an example, for target coverage probabilities of 0.8 and 0.9, considering $10^{-2}$ km visibility, the power costs are 50 and 250 watts, respectively. On the other hand, Fig. 4b shows that, at a rainfall rate of 50 mm/h, increasing the target coverage probability from 0.8 to 0.9 leads to an almost 5-fold increase in power cost. Comparison between Figs. 4a and 4b also suggests that the SDS effect is more significant than the rain effect and will impose a higher cost to the system.

Fig. 5 compares analytical and simulation results of coverage probability vs. SNR threshold for SDS and clear sky conditions. As it be can seen in the figure, analytical results agrees with simulations. It can also be observed that the coverage degradation due to SDS is more significant at low SNR thresholds. Fig. 6 depicts the average rate degradation due to SDS and rainfall for 0.05 km visibility and 50 mm/h rainfall rate, respectively. Results show that, for severe weather conditions, the average rate degradation due to SDS is considerably higher than that due to rain.

The average bit error rate in the presence of SDS/rainfall is represented in Fig. 7 for BPSK modulation computed from (27) with $M = 1$, $\alpha_1 = 1$ and $\beta_1 = 2$. The exact average BER versus the signal power to noise ratio ($P/N$) is plotted for different values of cell density ($\lambda = 0.5, 1$) and verified by Monte-Carlo simulations. It can be observed that increasing the cell density yields lower BER, due to the reduced average distance of users to their serving BS. The figure also shows that the obtained BER in SDS condition is higher than under rainfall, and both of them are significantly worse (higher BER) than the "No SDS/Rain" case, when the signal is only weakened by path loss.

**V. CONCLUSION**

In this paper, the effect of sand and dust storms (SDSs) and rainfalls on the performance of cellular networks in the mm-Wave band is investigated. A novel unified mathematical framework has been presented in order to analyze the power cost that the system has to pay to overcome the counterproductive effects of these atmospheric phenomena so that the same performance is achieved as in clear weather. Specifically, we focused on coverage probability, average achievable rate and average BER of the system and provided exact expressions for the performance degradation. Numerical results were provided to study the effects of various atmospheric phenomena on the performance of cellular networks.
FIGURE 5: Average coverage probability vs. target SNR threshold, with $\lambda = 0.001$, $P = 1$ W, $N_0 = 10^{-10}$ W and $V = 0.05$ Km for SDS in $f = 28$ GHz.

FIGURE 6: Degradation of average maximum achievable bit rate vs. SNR (dB) for $f = 28$ GHz, $\lambda = 0.001$ and bandwidth of 2600 MHz (Band 7 - Telstra / Optus for 4G).

FIGURE 7: Average BER in the presence of SDS/Rain at $f = 28$ GHz with BPSK modulation, path loss parameters $B = 3.73$, $A = 75.85$ dB, $V = 1$ km, $R = 50$ mm/h, and $\lambda = 0.5$ for the case no SDS/Rain.

parameters, including the density of deployed cells, visibility (in SDS conditions) and rainfall rate (in rain conditions). The presented results show that, when comparing severe rain (high rain rate) with severe SDS (low visibility), the loss of performance in SDS is higher than in the case of rainfall. This is in agreement with the results presented in [31], where SDS attenuation is compared with rain and gaseous attenuation at 22 GHz, and it is shown that SDS attenuation is much higher than others. It must be remarked that rainfall and SDS attenuation modeling for 5G/6G frequency bands, including mm-Wave and Teraherz, is an open research area, and the proposed mathematical framework is expected to provide a useful tool where different attenuation models can be tested at the network level. Such comparison is left for future research.

APPENDIX A: PROOF OF PROPOSITION 1

Proof. To obtain the coverage probability we can write

$$P_c(T) = \mathbb{E}\{\Gamma_k > T|r\} \quad (30a)$$

$$= \int_{r>0} \Pr \left\{ \frac{P|h_{w,k}|^2}{N_0 10^{L_{k,\mathrm{dB}}(r)/10}} > T|r \right\} f_R(r)dr \quad (30b)$$

$$= \int_{r>0} \Pr \left\{ |h_{k,w}|^2 > \frac{T N_0}{P} 10^{L_{k,\mathrm{dB}}(r)/10} \right\} f_R(r)dr \quad (30c)$$

$$= \int_0^{\infty} 2\pi r \exp \left( - \frac{T N_0}{P} 10^{L_{k,\mathrm{dB}}(r)/10} \right) \exp \left( -\lambda \pi r^2 \right) dr. \quad (30d)$$

Note that substituting $L_{k,\mathrm{dB}}(r)$ from (12) yields

$$10^{L_{k,\mathrm{dB}}(r)/10} = 10^{C_r/10 + C_{\ell}/10 + L_{\ell} \ln(r)/10} \quad (31)$$

In (30), we assume that $|h_{k,w}|$ and $|h_{k,w}|^2$ follow Rayleigh and exponential distributions, respectively. By substituting
We then use the exponential series, then the integral in (32) can be rewritten as

\[ P_c(T) = \sum_{k=0}^{\infty} \sum_{j=0}^{\infty} \left( \frac{-\mu_0}{k!} \right)^j \frac{(k\mu_2)^j}{j!} \int_0^{\infty} x^{k+j+1} \times 2\pi r \lambda \times \exp(-\lambda \pi r^2) dr \]

\[ = \sum_{k=0}^{\infty} \sum_{j=0}^{\infty} \left( \frac{-\mu_0}{k!} \right)^j \frac{(k\mu_2)^j}{j!} \left( \lambda \pi \right)^{-\frac{k+j+2}{2}} \Gamma \left( \frac{k+j+2}{2} \right) \]

(34)

The coverage probability without SDS and rain effects (clear sky conditions) is then obtained by setting \( \mu_2 = 0 \) as

\[ \hat{P}_c(T) = \sum_{k=0}^{\infty} \left( \frac{-\mu_0}{k!} \right)^j \left( \lambda \pi \right)^{-\frac{j}{2}} \Gamma \left( \frac{j+2}{2} \right) \]

(35)

And subtracting (35) from (36) completes the proof. 

\[ \hat{P}_c(T) = \sum_{k=0}^{\infty} \left( \frac{-\mu_0}{k!} \right)^j \left( \lambda \pi \right)^{-\frac{j}{2}} \Gamma \left( \frac{j+2}{2} \right) \]

(36)

REFERENCES


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