

1 **HIGHLIGHTS**

- 2 • The engine oil needs to enhance its properties to reduce the wear on the piston.
- 3 • The addition of CNC-CuO nanoparticles in the engine improved thermophysical
- 4 properties behaviour's performance at 0.5% concentration.
- 5 • The results can be beneficial for the heat transfer application, especially for
- 6 tribological

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11 **Improving the Thermophysical Properties of Hybrid Nanocellulose-Copper (II)**
12 **Oxide (CNC-CuO) as a Lubricant Additives: A Novel Nanolubricant for Tribology**
13 **Application**

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36 **ABSTRACT**

37 The primary objective of the present analysis is to investigate the thermophysical
38 properties of hybrid nanocellulose and copper (II) oxide nanoparticles added to engine
39 oil as a lubricant for piston ring-cylinder liner application. Kinematic viscosity, viscosity
40 index (VI) and dynamic viscosity have been performed for measurement of properties at
41 varying temperatures (ranging from 30°C to 90°C) and different concentrations (ranging
42 from 0.1% to 0.9% volume concentration). Thermal characteristics have been measured
43 using similar temperatures and concentrations to determine thermal conductivity and
44 specific heat capacity. In the results, as the concentration of the CNC-CuO nanoparticle
45 increases, the VI also increases. This proves the combination of CNC-CuO particles with
46 engine oil improves the lubricity of the base oil concerning its viscosity by 44.3%-
47 47.12%. The lowest and highest improvements in the dynamic viscosity were 1.34% and
48 74.81%. The highest increment of thermal conductivity ratio for the selected
49 nanolubricant was 1.80566% in the solid concentration of 0.1% at 90 °C. The specific
50 heat capacity of nanolubricant tends to reduce slightly with an increase in temperature.
51 Overall, the addition of CNC-CuO nanoparticle in the engine improved thermophysical
52 properties behaviour's performance at 0.5% concentration. The results can benefit the
53 heat transfer application, especially tribological.

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55 **KEYWORDS**

56 Thermophysical properties; Nanocellulose; Copper (II) oxide; Nanolubricant

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66 **ABBREVIATIONS**

AlO ₂	Aluminium oxide
TiO ₂	Titanium oxide
CuO	Copper Oxide
MWCNT	Multi walled carbon nanotube
CNC	Cellulose Nanocrystal
EG	Ethylene glycol
SAE	Society of Automotive Engineer
SiO ₂	Silica oxide
Cu	Copper
PAO	Polyalphaolefin
PTFE	Polytetrafluoroethylene
UV–vis	Ultraviolet
ZnAl ₂ O ₄	Zinc aluminium oxide
ASTM	American Standard Testing Method
MoS ₂	Molybdenum disulphate
MgO	Magnesium oxide
DSC	Differential scanning calorimeter
VI	Viscosity Index
C _p	Specific heat
CaO/Na ₂ O	Calcium oxide/sodium oxide

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72 **1.0Introduction**

73 The main benefits of nanolubricants are that they are resistant to temperature
74 compared to conventional additives and restricted tribochemical reactions [1]. It is
75 possible to use different kinds of nanoparticles, either organic or inorganic nanoparticles
76 [2]. Organic nanoparticles mainly include polymers, exosomes, liposomes, protein-based
77 nanoparticles, coal fly as, etc., while inorganic nanoparticles consist of silica
78 nanoparticles, metal nanoparticles, carbon nanotubes, quantum dots and so forth [3-7].
79 Organic-inorganic, or hybrid, nanoparticles have caught the interest of researchers due to
80 their potential applications because they can combine useful chemical, optical, and
81 mechanical properties while retaining the various benefits of nanolubricants. The
82 dispersion of these nanoparticles for tribological properties, such as Multi-Walled Carbon
83 Nanotube (MWCNT) or the latest research organic nanoparticle using coal fly ash hybrid
84 with different inorganic nanoparticles such as copper, alumina and silica, has piqued the
85 interest of researchers and academics in recent years, as it leads to friction and wear
86 reduction [10-12]. A hybrid nanoparticle comprises two or more nanoparticles that have
87 been synthesized and distributed in a base lubricant [8]. The main goal of creating hybrid
88 nanolubricants is to enhance the properties of materials so that they have significantly
89 better rheological properties than individual conventional nanolubricants [9].

90 On the other hand, not so much literature reports on using Cellulose Nanocrystal
91 (CNC) as a nanomaterial dispersant with any base fluid, particularly in lubricants. CNC
92 is non-toxic, biodegradable, and has a large surface area and high strength [8].
93 Nanocellulose emerges as an inexpensive and sustainable polymer material with
94 beneficial properties of oleophilic, optical transparency and mechanical performance,
95 both as films and aerogels, with a directive toward biodegradable, renewable, sustainable
96 and carbon-neutral polymer materials [9]. Nanocellulose-nanoparticle hybrid exploration
97 is still relatively sporadic but has increased significantly since the multifunctional
98 nanocellulose hybrid report [10, 11].

99 Nanotechnology has enhanced lubricant performance by using nanoparticles as
100 additives in lubrication systems since the advent of nanotechnology. The qualities of the
101 base oil can be enhanced or reduced by the additives present in the lubricating oil. The
102 effect depends on the nanoparticles' features, such as shape, size, and volume fraction
103 [12]. Many researchers reported improved viscosity changes in lubricating oil
104 functionalised with nanoparticles. They investigated the impact of lubricant viscosity

105 variation due to increasing nanoparticle additive concentrations and temperature [13-15].
106 They discovered substantial relationships between viscosity and temperature and
107 nanoparticle concentration; increasing temperature reduced viscosity while increasing
108 particle volume fraction increased viscosity of nano-lubricant. According to these
109 investigations, increasing the temperature and nanoparticle size or lowering the nanofluid
110 concentration reduces the nanofluid viscosity [16, 17]. Many publications in the literature
111 assessed varied concentrations below 1% and beyond 2%, demonstrating that there is no
112 optimal concentration for nanoparticles [18, 19].

113 Improved thermophysical properties of fluids, viscosity, thermal conductivity and
114 specific heat capacity have recently emerged as one of the most challenging problems for
115 researchers to solve. As a result, numerous research has been conducted on adding
116 nanoparticles to increase the conductivity of various fluids [20, 21]. Researchers have
117 also looked into the effects of various parameters on viscosity variations to study and
118 analyze the thermophysical attributes of various fluids after combining nanoparticles,
119 such as enhanced SAE40 oil with a mixture of MgO and MWCNT [22], enhanced 10W40
120 by CuO and MWCNT [23], Al₂O₃ and MWCNT for optimization goals [24, 25],
121 CaO/Na₂O [26], clove-treated MWCNTs and Al₂O₃ [27].

122 Previously, studies on the thermophysical properties of engine oil performance
123 using single component nanolubricants with CNC and CuO nanoparticles are available
124 in the literature [18, 28-31]. However, as mentioned, a single nanofluid does not include
125 all the characteristics compulsory for a specific purpose in some of the rheological and
126 thermal properties [32]. Hence, recent development in nanofluids research has developed
127 new nanolubricants with two or more types of nanoparticles dispersed in engine oil. The
128 nanolubricant's purpose is to improve natural wear and friction. When nanoparticles are
129 added to base oil, their concentration affects wear and friction. However, the
130 concentration limitation must be considered because the lubricants already contain
131 additives. More research is needed to improve the additive in lubricant, particularly on
132 the concentration of additive used and the constraints involved. Various nanoparticle
133 dispersions with differing nanoparticle material properties, shapes, sizes, and
134 concentrations have been extensively studied in the last decade. Most of these studies
135 have been carried out in polar base fluids like water, ethylene glycol (EG), and mixtures.
136 [33-36]. This paper aims to evaluate the thermophysical properties of CNC-CuO
137 nanolubricants for application in piston ring-cylinder liner contact for tribology
138 application. This research is important, stating that only a few studies are available on

139 organics-inorganics nanofluids based on manufacturing sector lubricants for viscosity
140 and thermal applications. The considerably low stated results on lubrication-based
141 nanofluids revolve around transformer oil, silicon oil, gear oil and heat transfer oil, and
142 there are inadequate studies on engine lubricants-based nanofluids. Furthermore, the
143 studies also revolve around single inorganic nanoparticles such as copper, aluminium,
144 zinc oxide etc.

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146 **2.0 Methodology**

147 **2.1 Preparation of nanolubricant**

148 SAE 40 was chosen as a base fluid for the nanolubricant. Blue Goose
149 Biorefineries Inc was a provider for the CNC with a 7.4% water weight concentration,
150 meaning the CNC is in gel form. Yuan, Fu [37] recommended spray drying as a suitable
151 practice in drying the suspension of nanocellulose. Copper oxide nanoparticles look like
152 brownish-black powder. It can be changed to metallic copper when reacting to hydrogen
153 or carbon monoxide at high temperatures. The present study considered the parameter for
154 concentration in volume per cent. Hence the conversion from weight concentration to
155 volume concentration is required for CNC and CuO single components of nanolubricant.
156 This study selected the two-step method to prepare nanolubricants, similar to the previous
157 study. The Yu and Xie two-step approach prepares five different nanolubricant samples
158 from 0.1% to 0.9% weight concentration. This technique consists of two steps: (i)
159 nanoparticle production in powder form and (ii) nanoparticle dispersion in base fluids to
160 generate a stable and homogeneous solution.

161 The CNC was synthesized into powder form to synthesise nanoparticles since its
162 form is barely an off-white cream structure. To dry CNC from the suspension, water
163 content from CNC suspension must be removed to sustain the nanofibrils size to the
164 nanoscale. Since CNC is hydrophilic, the CNC melts at high temperatures and dissolves
165 in any aqueous solvent [38]. A lab-scale blower was used for the spray drying process. It
166 was also carried out at 25°C relative temperature in an air-conditioning controlled room.
167 The flakes form of CNC are rapidly produced as its suspension is evaporated from the
168 hot air stream by the blower nozzle. The flakes are manually ground for about 60 minutes
169 to get the even powder form via porcelain mortar.

170 For the dispersion of the nanoparticles into the base fluid, the nanolubricants were
171 prepared at 70:30 CNC-CuO. The nanolubricants were prepared for different volume

172 concentrations from 0.1 to 0.9% at an optimum composition ratio in stage one. The
173 process flow and steps in the preparation of CNC-CuO nanolubricants as shown in Figure
174 1. Initially, in Step 1, the preparation of nanolubricants started with calculating the
175 required volume for dilution using Equation 1.

$$\phi = \frac{\left[\frac{W_p}{\rho_p} \right]}{\left[\frac{W_p}{\rho_p} + \frac{W_{bf}}{\rho_{bf}} \right]} \quad \text{Eq.1}$$

176 CNC and CNC-CuO nanolubricant were prepared with 0.1, 0.3, 0.5, 0.7 and 0.9% volume
177 fraction in 200 ml of base oil SAE 40. W_p indicates the nanoparticles' weight (grams), (ρ_p
178 indicates the density of the nanoparticles (g/cm³), (ρ_{bf} indicates the density for the base
179 fluid in g/cm³, and W_{bf} indicate the base fluid weight (grams). CNC with CuO powder
180 were then dry mixed to produce CNC-CuO nanoparticles. After that, the mixing process
181 of nanoparticles in the base fluid was done by using a stirrer in Step 2. The nanolubricant
182 was mixed up for 30 minutes, as suggested by other researchers [35, 39-42].

183 Hotplate magnetic stirrer was used for the initial dispersion process of CNC and CNC-
184 CuO nanoparticles into engine oil at medium stirring rate continuously for 1 hour at room
185 temperature. Each of the nanolubricant solutions then was left approximately for 2 hours
186 in an ultrasonic bath. This was a very important step to intensify the stability of the
187 nanolubricant. Furthermore, the sample of nanolubricants was subjected to the sonication
188 process.

189 **2.2 Stability Test for Nanolubricant**

190 Floating nanoparticles tend to be clustered due to large surface area and surface
191 reactions. It's a fact that the stability and dispersibility of nanolubricants are two
192 important criteria that affect their usage [39]. Various methods are used, such as
193 sedimentation, centrifugation, zeta potential, and spectral absorbency. These methods are
194 proposed to assess the stability of suspensions. For this paper, the sedimentation method
195 and visual absorbency analysis are done to analyze the stability. A stable suspended
196 nanoparticle is observed in the particle size of the supernatant particle as it remains
197 constant in the solution. Several researchers have adapted the sedimentation method in
198 their stability investigation [38, 40-43]. An 8 ml sample of nanolubricant was placed in
199 the test tube at a stationary state. The camera captured the sample and compared it with

200 the first day images over time. Then, the images of sedimentation over time for the
201 nanolubricant were captured on the first day of preparation and up until 30 days. Images
202 of the sedimentation behaviour changes and separation levels are recorded during this
203 period.

204 UV-Visualisation spectrophotometer is a straightforward, quick and cost-
205 effective method to quantitatively measure and characterize colloidal dispersion stability
206 conditions. This method is based on fluids absorption and is useful for analysing different
207 types of fluids dispersion but inappropriate for high volume concentrations of
208 nanoparticle dispersion. In this experiment, the device functioned at a steady wavelength
209 of 1200nm for every measurement of the nanolubricant sample. In this experiment, the
210 Pelkin Elmer UV-Vis spectrophotometer (model number TGA 4000) with a wavelength
211 range of 190 to 3300 nm was utilized in this investigation. The equipment has functioned
212 at a steady wavelength of 1200 nm for an individual sample of nano lubricant. A
213 transparent crystal cuvette is used to place the sample test inside the spaces. The
214 spectrophotometer provides six sample slots for measurement with one slot for reference
215 fluid, SAE 40, and another five for SAE 40. Before each measurement for precaution, the
216 cuvette was carefully cleaned using distilled water to avoid contamination with the
217 previous sample. UV-Vis spectrophotometer is utilized to determine the lessening light
218 beam after reflection from a sample surface or passing through a sample. The scattering
219 and absorption of light are determined by comparing the light power of the CNC-CuO
220 nanolubricant. The absorbance of the light, when directed to the sample test, will show
221 the existence of nanoparticles in the base fluid. In other words, densely populated
222 nanoparticles in the base fluid are projected to show considerable absorbance and lower
223 absorbance value due to fewer nanoparticles in the solution [44].

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232 2.3 Kinematic and Dynamic Viscosity

233 Kinematic viscosity data was performed following the American Standard
234 Testing Method (ASTM D445) through a temperature-constant bath of Cannon
235 Instrument Company, United States of America (Model CT-500 Series II) utilizing
236 Cannon-Fenske Routine Model crystal tube viscometer with 2 mm inner diameter
237 together with, Cole-Parmer Polystat economical constant temperature bath at a
238 temperature of 40°C. Thermal oil was utilized to obtain stable temperature distribution
239 inside the tube at 40°C, and 100°C for individual concentrations were determined
240 accordingly. The viscosity index (*VI*) calculates the difference in viscosity versus the
241 temperature. *VI* is an arbitrary measure for viscosity variation with temperature
242 differences. The *VI* values were determined according to the standard described in the
243 American Society for Testing (ASTM D-2270), based on the determination of the
244 kinematic viscosity. The *VI* is calculated from equation 2 below:

$$VI = 100 \frac{L - U}{L - H} \quad \text{Eq. 2}$$

245 where *U* is kinematic viscosity at 40°C while *L* and *H* are the values found in the ASTM
246 D2270 table from kinematic viscosity at 100°C.

247 The viscosity of the lubricant is a significant indicator for lubricating testing. A
248 commercial Brookfield DV-I prime viscometer was utilized to determine at dissimilar
249 rotation speed (rpm). This viscometer can also be utilized in Newtonian and non-
250 Newtonian liquids, ranging from small to large viscosity values (differing on the spindle,
251 range of 1 to 600 cP); however, this instrument is precise for low viscosity fluids (ranged
252 between 1 and 5 cP). The viscometer is a rotating type that uses a spindle submerged in
253 the nanolubricant sample. The 25mL volume of nanolubricant was added to the chamber
254 test and attached to the rheometer. Then the chamber and water jacket were carefully
255 attached to the rheometer spring with the spring deflection within 2 to 3%. The
256 nanolubricant sample was heated using a mixing water bath until reaching the required
257 temperature. The dynamic viscosity values were observed for the temperature range of
258 30 to 90°C. A Rheocalc software was utilized for the current viscosity values. The
259 viscosity was calculated by changing the speed of the spindle rotation. The measurement
260 was done three times to get the average values. Then, the setup was validated by
261 comparing the SAE 40 base oil at 30 to 90°C.

262 2.4 Thermal Conductivity and Specific Heat Capacity

263 KD2 Pro thermal property analyzer was used to measure the thermal conductivity
264 of the CNC-CuO nanolubricant. A single needle sensor named KS-1 was selected for the
265 thermal conductivity measurement. This sensor can measure the thermal conductivity of
266 liquids in the range of 0.002 to 2.00 W/m.K. The needle for the KS-1 sensor was inserted
267 into the sample bottle vertically at the centre and sealed with tape. Then the sample bottle
268 of nanolubricant was immersed in the water bath for approximately 10 minutes until the
269 temperature of the nanolubricants reached the bath temperature.

270 The KD2-Pro was calibrated using the Glycerin liquid provided by the
271 manufacturer before the experiments were conducted. The average Glycerin thermal
272 conductivity was recorded with 0.286W/mK at 25°C. The thermal conductivity was
273 conducted for a temperature between 30°C to 90°C. The measurement was done three
274 times, and the median value from three sets of data was obtained. The current thermal
275 conductivity measurement is measured in 15 minutes by the following reading for each
276 data set at various temperatures and volume concentrations. This step reduces the errors
277 during thermal conductivity measurement due to the temperature change along the sensor
278 in direct contact with the nanolubricant sample. The present thermal conductivity
279 measurement followed the ASTM D5332-08 and IEEE 442-03 standards.

280 To determine the specific heat capacity of the nanolubricant, a differential
281 scanning calorimeter (DSC), model DSC1000-/C from Linseis Messgeräte GmbH, Selb,
282 Germany, was employed. This DSC follows the standard method ASTM E1269-
283 11(2018). DSC is a thermal analysis technique examining how a material's heat capacity
284 (C_p) is changed over temperature. This equipment gives the highest possible accuracy
285 C_p by using heating rate temperature profiles. Nanolubricant is heated or cooled, and the
286 changes in its heat capacity are tracked during changes in the heat flow. A furnace that
287 can be heated up and cooled down homogenously is required to perform DSC. Two
288 crucibles contain nanolubricant samples, and the other one is the empty crucible that acts
289 as reference calorimeters that are equipped with high sensitive temperatures. When the
290 furnace is heated at a constant rate, heat flows through the crucible of the nanolubricant
291 sample and reference. The oven is purged with protective gas, nitrogen (N_2), at a 24
292 ml/min flow rate. The usage of N_2 also avoids ice formation at low temperatures and the
293 oxidation process. [45].

294

295 **3.0 Results and discussion**

296 **3.1 Stability of CNC-CuO nanolubricant**

297 The sedimentation observation was done by capturing images within a certain
298 period for the nanoparticles to sediment at the bottom of the test tube without any
299 disruption. The length of this test differs from days to months. Peng et al. reported the
300 deposit after 30 days for the silica and alumina nanoparticles scattered in paraffin
301 lubricant [46]. In a different study by Sui et al. (2016), the permanence of the nanosilica
302 enriched polyalphaolefin (PAO) lubricants was analyzed by storing the lubricants for 60
303 days [47]. Amiruddin et al. (2015) assessed the diffusion stability of SAE15W40
304 enhanced with nanohBN for 60 days. Dubey ran this test for 7 days in PTFE-based
305 nanolubricants [48]. Thus, various test intervals have been stated by investigators for
306 various nanoparticle and lubricant permutations. Hence, it is worth saying that the main
307 idea for the selection of test time is based upon examining uncommon dispersion
308 behaviours of lubricant samples. It can also be said that the test can be completed when
309 the naked eye observes the deposits. The height of the solid-liquid interface of the
310 supernatant layer of the samples was observed periodically. From the statement above,
311 the period of observation was recorded at week one and at week 4. All samples were kept
312 in test tubes and set aside undisturbed throughout the observation period and were
313 observed periodically for any visual changes. Figure 1 shows the sedimentation
314 observation in week 1. The samples were mixed well with no settlement of nanoparticles
315 at the bottom of the test tube at week 1. After the 4th week, the supernatant layer is at the
316 top of the solution. Therefore, CNC-CuO nano lubricant was observed to be stable for up
317 to one month or more, as shown in Figure 2.

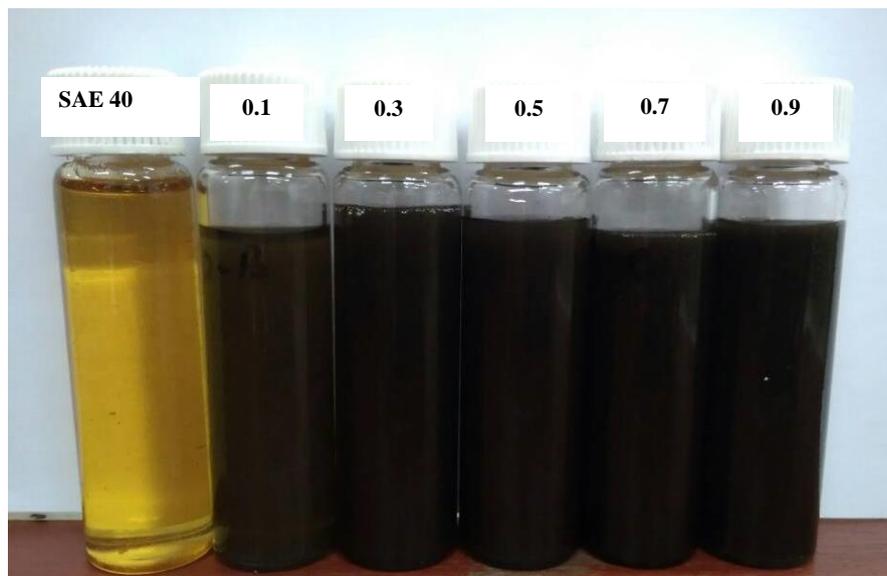


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319 Figure 1 Sedimentation observation at week 1

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323 Figure 2 Sedimentation observation at week 4

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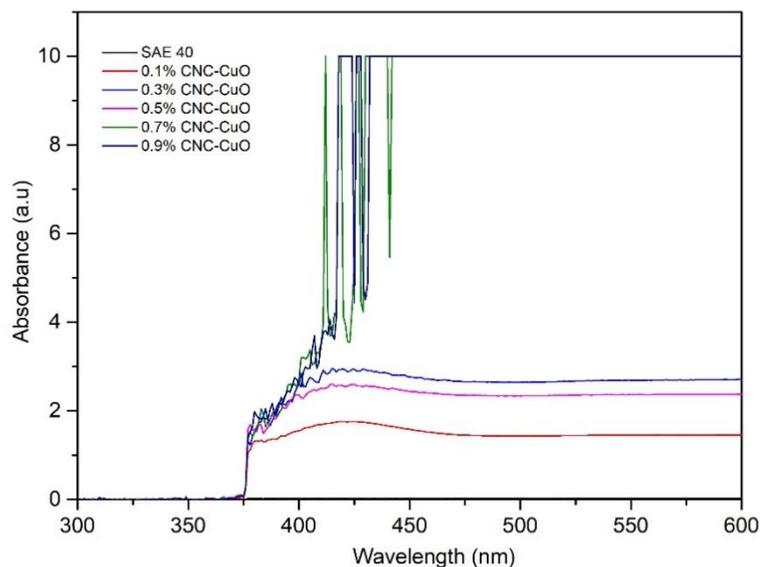
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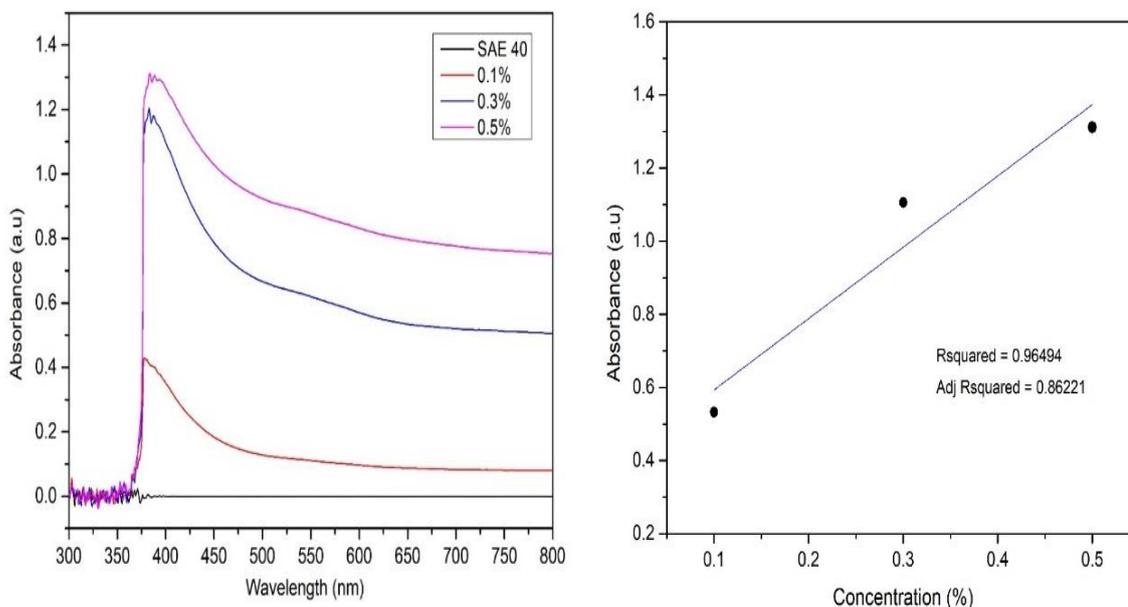
330 Next presents the data UV-Vis spectrophotometer for CNC-CuO nanolubricants.
331 The gamut pattern at numerous volume concentrations of CNC-CuO lubricant is shown
332 in Figure 3. The peak absorbance can be seen from 0.1% to 0.5%. The peak position is
333 broadened due to the increase in CNC-CuO nanoparticle concentration. As can see in
334 Figure 3 as well, 0.7% and 0.9% show asymmetrical distribution due to the limitation of
335 UV-Vis spectrometry. UV Vis functions well on liquid and solutions, but if the sample
336 is made of a suspension of solid particles in liquid and has darker solutions, the sample
337 scatters the light more; thus, the data obtained will be biased. Thus, it proves that 0.5%
338 is the optimum concentration for CNC-CuO stability, and further experiments will only
339 discuss three concentrations.



340
341 Figure 3 UV Vis spectrophotometer for CNC-CuO

342 As nanoparticles deposited in nanofluid, the absorbance in the supernatant part
343 declined with concentration. The association among these two variables is stated as the
344 Beer-Lambert law. The law states a linear relationship between the concentration and
345 the absorbance of the liquid, which allows the concentration of a mixture to be
346 determined by evaluating its absorbance [49]. This principle suggests that weightage
347 intensity is linearly related to absorbance. As seen in Figure 4, the highest absorbance
348 values of CNC-CuO nanolubricant with three distinct concentrations were found over a
349 wavelength of 380-383 nm. Using corresponding absorbance values from each
350 concentration, a linear correlation between absorbance and concentration of colloids was
351 obtained, as shown in Figure 4, with the R^2 at 0.96494. This is as per the Beer-Lambert

352 law.



353

354 Figure 4 UV Vis spectrum for 0.1% to 0.9% concentration

355 Figure 5 shows the amount of the highest absorbance per week. It indicates that
356 the small concentration of nano lubricants sediment is faster due to rapid agglomeration
357 [50]. The absorbance ratio signals the ratio of the last absorbance at a specific
358 sedimentation time to the initial absorbance of the mixture. The ideal absorbance ratio is
359 100%, representing good stability during the deposit period. As Hajjar et al. [51]
360 discussed, the more the ratio is to 1 with the increase of the sedimentation times affect
361 the stability of the test. Equation 3 determines the final absorbance ratio:

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$$A_r = \frac{A}{A_o} \quad \text{Eq.3}$$

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364 where A_r denote the absorbance ratio, A denotes the final absorbance, while A_o denotes
365 initial absorbance. According to Figure 6, 0.1% shows the closest absorbance ratio to
366 one; thus, 0.1% concentration shows the most stable nanolubricant, followed by 0.5%,
367 and the least stable nano lubricant is 0.3% concentration.

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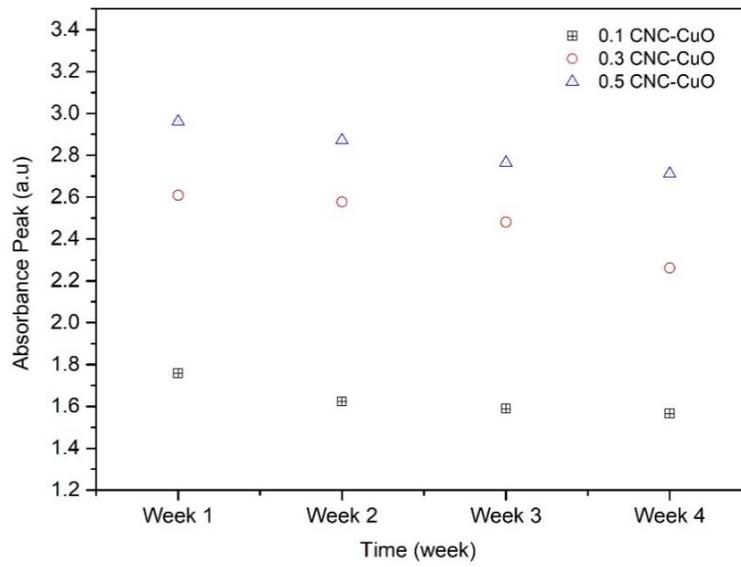
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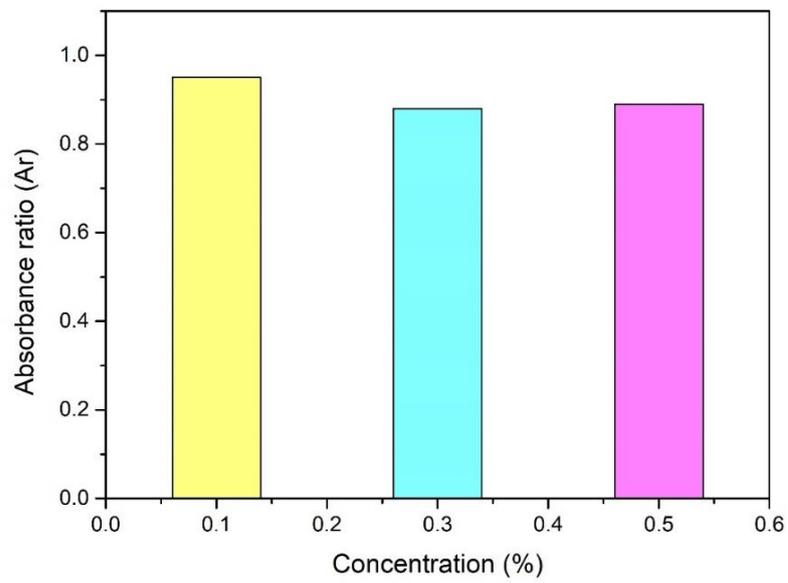
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375 Figure 5 Absorbance peak for one month

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378 Figure 6 Absorbance ratio for 0.1%, 0.3% and 0.5% concentration.

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383 3.2 Kinematic Viscosity and Viscosity Index

384 The main physical criteria for determining the condition of the oil is engine oil
385 viscosity. The viscosity in a lubricant depends primarily on the operating temperature.
386 Determining kinematic viscosity is vital for the ability of a lubricant to lubricate contact
387 surfaces efficiently. Nanoparticle dispersion can greatly affect the viscosity of the base
388 lubricant, which is a key factor in determining load-bearing potential and viscous friction
389 [51] (Kotia, Borkakoti, & Ghosh, 2017). The viscosity of the base oil and various additive
390 samples are taken out using Capillary Viscometer based on the ASTM D445 standard. In
391 kinematic analysis, the concentration of nanoparticles in volume and temperature were
392 evaluated as the two controllable parameters that were effective for engine oil. Kinematic
393 viscosities were resolved at 40°C and 100°C.

394 Figure 7 shows the viscosity increment in percentage when CNC-CuO
395 nanoparticles are added to the engine oil in different concentrations at 40°C and 100°C.
396 The mathematical relation for the viscosity increment measurement is calculated by using
397 equation 4.

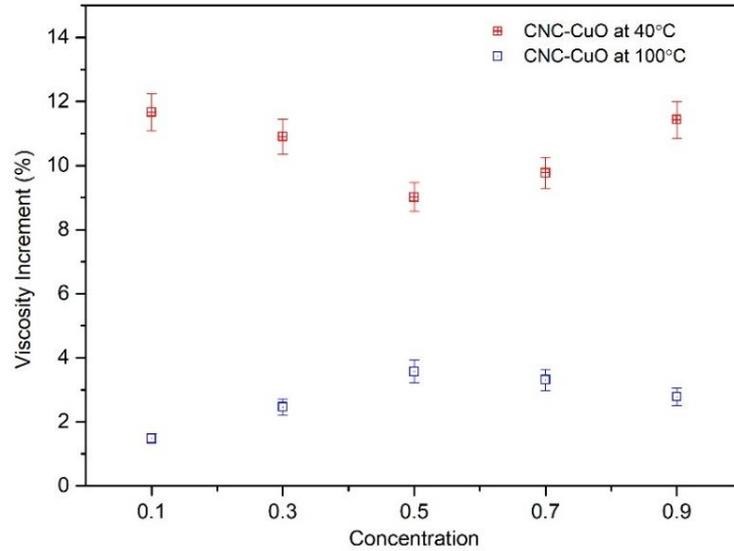
$$\begin{aligned} & \text{Viscosity Increment (\%)} && \text{Eq.4} \\ & = \frac{\text{Nanolubricant viscosity} - \text{Engine oil viscosity}}{\text{Engine oil viscosity}} \times 100 \end{aligned}$$

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403 Figure 7 Viscosity increment at 40°C and 100°C

404 At 40°C, the viscosity increment decreases until 0.5% concentration and starts to
 405 rise at 0.7% concentration. In contrast with 100°C, the viscosity increment is increased
 406 to 0.5% and starts to decrease at 0.7% of CNC-CuO. The graph also shows that the
 407 viscosity of all lubricants reduces with the temperature rise. This is owing to the
 408 deterioration of the intermolecular strength of attraction among base fluid molecules [52].
 409 The rise of nanoparticles in the liquid results in agglomeration on the surface, causing
 410 molecular collision. This improves nanolubricant viscosity. The collision of the
 411 molecular forces in increasing temperature reduces the viscosity of the nano lubricant
 412 [13]. The relative viscosity of nanolubricant with the change in temperature for various
 413 concentrations is shown in Figure 8. Equation 5 shows the mathematical relation for
 414 getting relative viscosity.

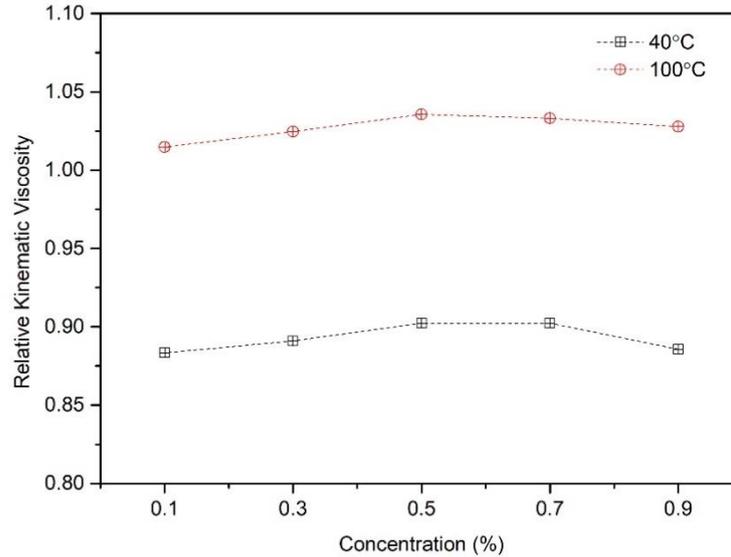
$$\mu_r = \frac{\mu_{nl}}{\mu_{bf}} \quad \text{Eq.5}$$

415 μ_r is relative viscosity, μ_{nl} is nanolubricant viscosity, and μ_{bf} is base fluid kinematic
 416 viscosity. From the relation, it can be observed that the increment in relative viscosity
 417 depends on the fluid viscosity considered for the analysis.

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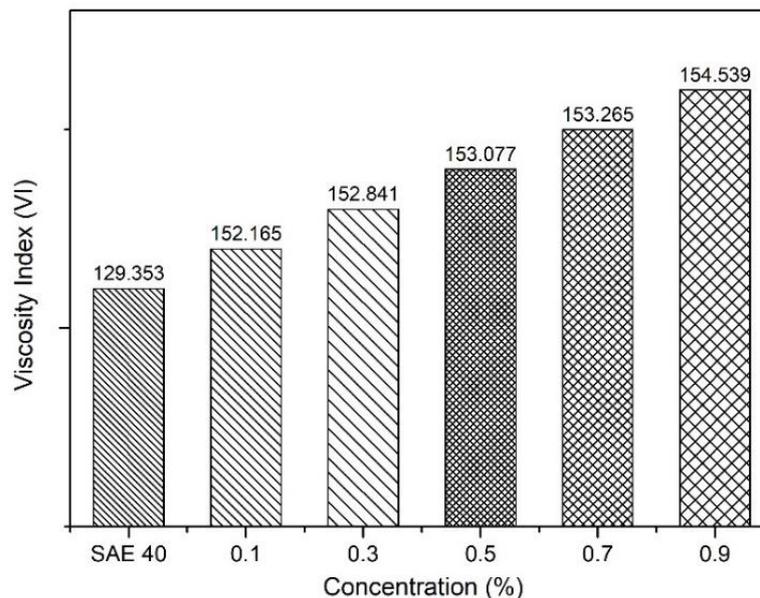
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422 Figure 8 Relative kinematic viscosity at 40°C and 100°C

423 Figure 8 shows the maximum change for the 0.5% CNC-CuO nanoparticles
 424 concentration at the highest temperature of 100°C. When the fluid's viscosity increases
 425 with the addition of the nanoparticles, a higher value is observed in relative viscosity with
 426 0.5% CuO nanoparticles addition [53]. Due to this viscosity reduction in relative
 427 kinematic viscosity at 0.5%, it was easy for nanoparticles to enter between the oil layers
 428 and the CNC and CuO nanoparticles acting as catalysts. Furthermore, the nanoparticles'
 429 almost spherical form influenced their rheological behaviour. Similarly, the viscosity of
 430 the CNC-CuO nanolubricant was only slightly reduced. Viscosity friction was reduced
 431 thanks to the low viscosity reduction. The low viscosity decrease helped to lessen viscous
 432 friction. The fewer viscosity decrease in the nanolubricants confirmed the CNC and CuO
 433 nanoparticle's effect on decreasing friction and thus lowering the frictional energy losses
 434 [54]. Oil viscosity is a required indication for lubricating analysis due the viscosity of
 435 a lubricant is directly linked to its ability to decrease friction on contact surfaces.
 436 Normally, a low viscous lubricant is desired [55]. The engine oil pump works with low
 437 energy to move a low viscous liquid. If the lubricant has a high viscosity, it requires a
 438 substantial amount of energy to work; oppositely, if it is too thin, the surfaces will come
 439 in contact, and friction increases [56]. The viscosity index (VI) was analysed to recognise
 440 which lubricant demonstrates better properties, as shown in Figure 9. The lower the VI,
 441 the better the viscosity difference of the oil with heat. Higher VI is required to
 442 demonstrate better friction and wear [57]. This proves that the CNC-CuO nanoparticle

443 combined with engine oil improved the lubricity of the base oil viscosity by 44.3%-
444 47.12%.

445 The higher viscosity index meant that it was more resistant to lubricant film
446 thinning and had better fuel efficiency in an automotive engine. Figure 9 presents the
447 viscosity of blended engine oil SAE 40 with CNC nanoparticles at increased
448 concentration. It is clear that using nanoparticles of CNC and CuO as additives with
449 blended engine oil also decreases the kinematic viscosity at 40°C and 100°C, which has
450 considerably lower kinematic viscosities than engine oil SAE 40. It is also evident that
451 the viscosity of nanolubricant decreases with increasing temperature. This is possibly due
452 to a deterioration of attractive intermolecular forces that permits more rapid movement
453 of suspended particles in the nano lubricants and offers less resistance to motion [58].
454

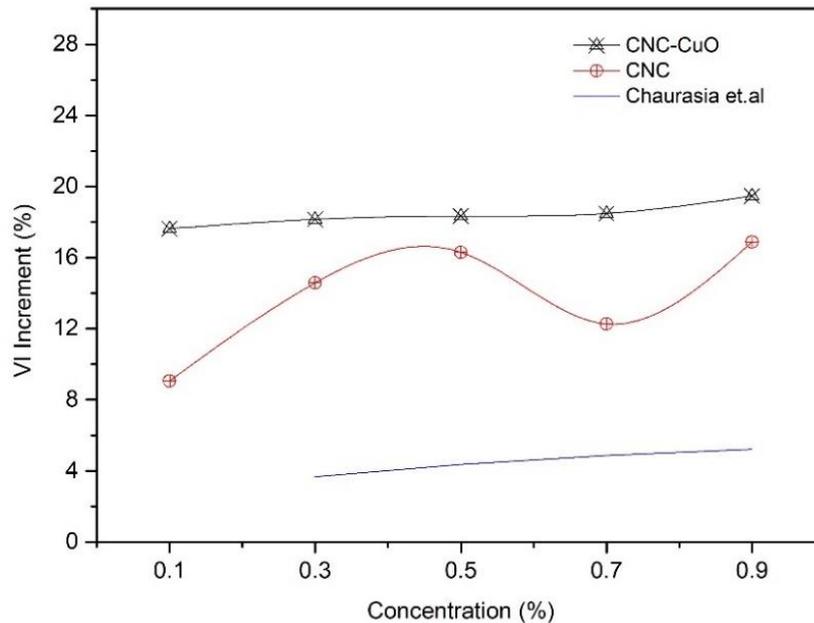


455

456 Figure 9 Viscosity index for CNC-CuO nanolubricant at all concentrations,

457 Figure 10 shows the comparison between CNC-CuO, CNC and Chaurasia et al. that use
458 CuO nanoparticles as additives. The graph clearly shows that CNC-CuO shows the
459 highest VI increment for all concentrations compared to other nanolubricant. The
460 maximum VI increment was obtained at 0.9 concentration. The last changes in viscosity
461 index increase were studied at lesser concentrations and temperatures. These variations
462 happened due to a greater molecular collision rate at an elevated temperature [53]. There
463 will be molecular interchange in a liquid similar to what occurs in a gas, but there are
464 additional significant attractive, cohesive forces between the molecules of a

465 liquid. Liquid viscosity is affected by both cohesion and molecular interchange. When
466 the temperature of a liquid rises, it reduces the cohesive forces while increasing the rate
467 of molecular interchange. The former causes a decrease in shear stress, whereas the latter
468 causes an increase. As a result, as the temperature increases, the viscosity of liquids
469 decreases. When temperatures rise, viscosity increases in gases and decreases in liquids
470 and drag force decreases [59].



471

472 Figure 10 VI compares CNC-CuO and CNC nanolubricant with the previous researcher.

473

474 3.3 Dynamic Viscosity

475 The rheological behaviour of nanofluids is a concern to many researchers,
476 whether it is Newtonian or Non-Newtonian fluids. For example, [60] reported that the
477 viscosity directly depends on the shear rate, while in contrast, [61] suggested that the
478 viscosity of nanofluid is impartial to the shear rate. Based on the statement, nanofluid's
479 Newtonian or Non-Newtonian behaviour can be recognized by investigating the relation
480 between shear stress and shear rate. According to Esfe et al., the recognition of Newtonian
481 and Non – Newtonian fluid behaviour can be determined by its type of internal resistance,
482 viscosity to shear rate [62]. The researcher in this approach investigated the dependence
483 of viscosity on shear rate. Independence of fluid's viscosity on the shear rate indicated
484 that the fluid is similar to Newtonian fluids' behaviour. Still, viscosity dependency on

485 shear rate suggests that fluid has a close behaviour to non- Newtonian fluids. Liquids in
486 which viscosity reduces with rising shear rates are known as pseudoplastic fluids, while
487 fluids in which viscosity rises with rising shear rate are called dilatant fluids.

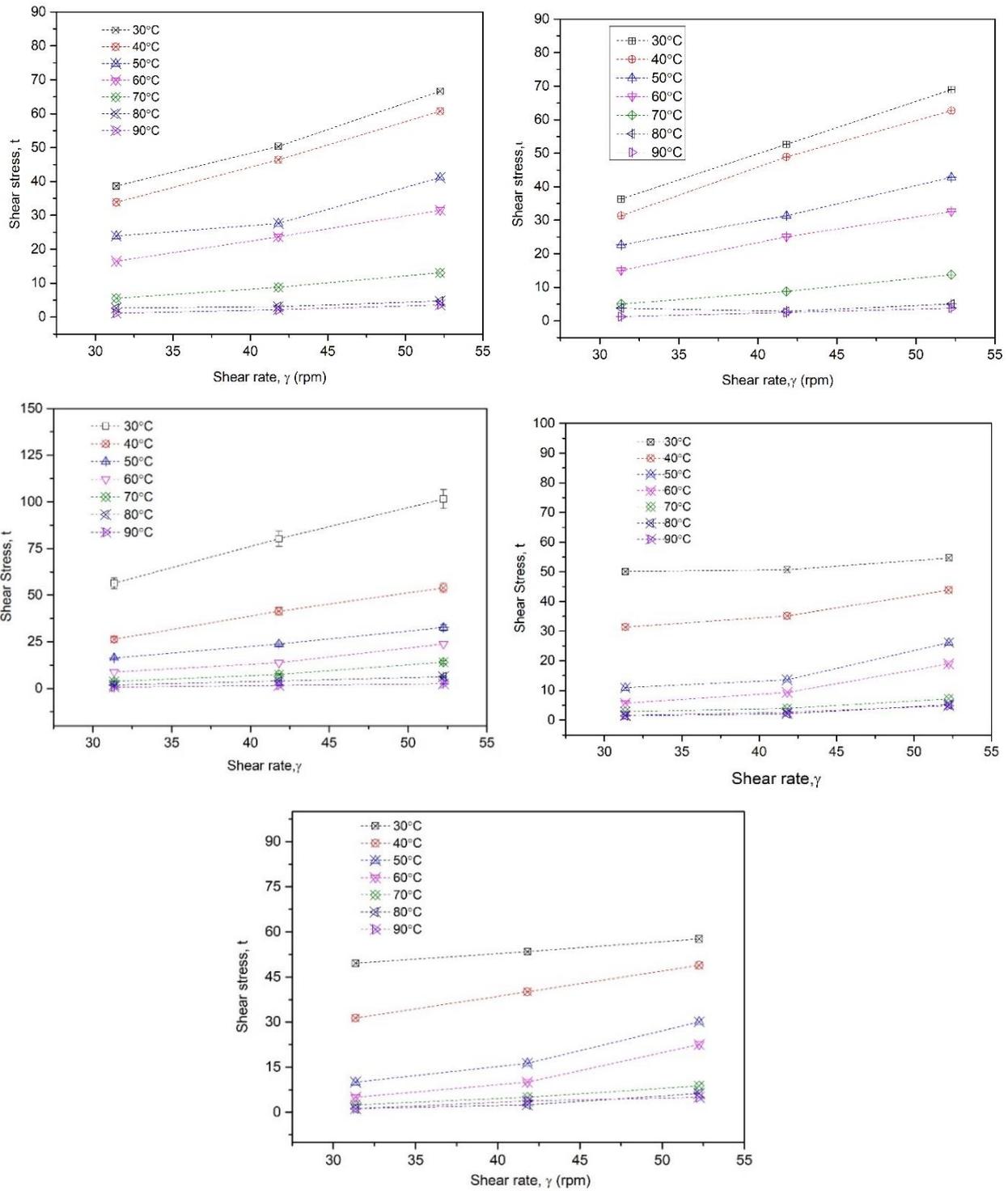
488 Various discussions have been made on the rheological performance of nanofluids,
489 whether it is Newtonian or non-Newtonian fluids. For example, [51] reported that the
490 viscosity of a mixture containing Al₂O₃ is independent of the shear rate. At the same
491 time, Kabelac and Kuhnke [60] indicated that the shear rate promptly impacts the
492 viscosity of such a solution. Thus, recognizing whether the nanofluid is Newtonian or
493 non-Newtonian is the first step to researching the rheological performance of CNC-CuO
494 nanolubricant. The Newtonian behaviour of nanofluids can be expressed as follows:

495

$$\tau = \mu\gamma \quad \text{Eq.6}$$

496

497 The shear stress of CNC-CuO nanolubricant concerning shear rate and temperature at the
498 concentration of 0.1% has been shown in Figure 12. Where τ represents the shear stress,
499 μ represents the dynamic viscosity, and γ represents the shear strain. Based on the figure,
500 it can be assumed that under the circumstances of the present investigation, the studied
501 nanolubricant exhibits Newtonian behaviour.



502

503 Figure 11 Variation of shear stress versus shear rate for CNC-CuO at a different

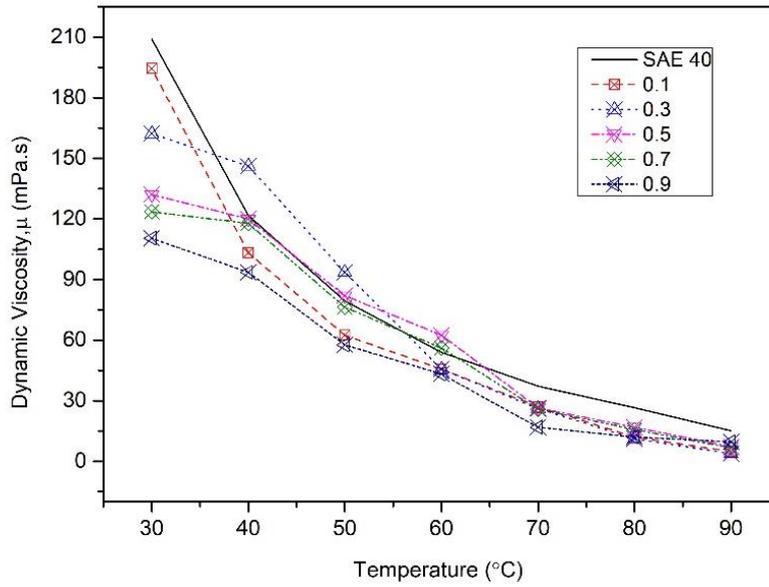
504 concentration from 0.1% to 0.9%

505 **3.3.1 Dynamic Viscosity in Different Temperatures and Concentration**

506 Figure 12 displays the dynamic viscosity of CNC-CuO engine oil nanolubricant
507 regarding temperature in different solid mixtures. Raising the temperature leads to lessening
508 the dynamic viscosity of the examined nanolubricant in each solid concentration. It is to note
509 that raising the solid concentration at a continuous temperature improves the nanofluid's
510 dynamic viscosity. This rise is substantial in low temperatures contrasted to the higher ones.
511 The dynamic viscosity of the examined nanolubricant concerning solid concentration in various
512 temperatures has been displayed in Figure 13.

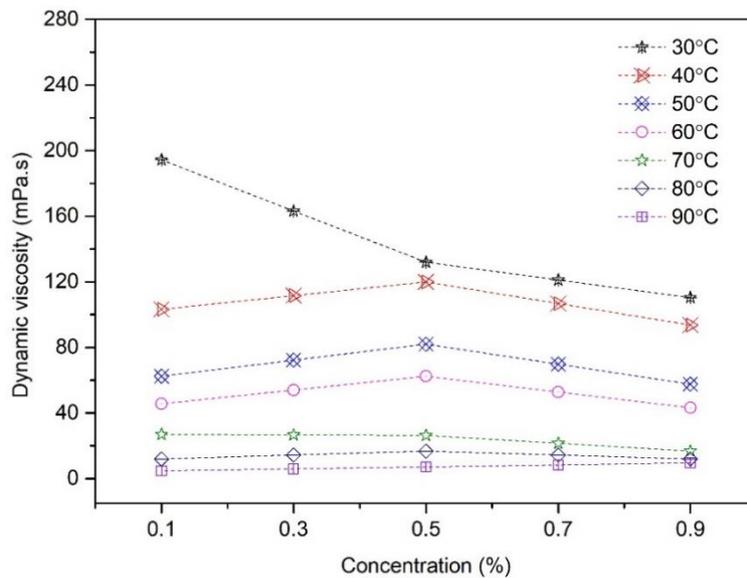
513 According to [63], viscosity is affected by the adhesive forces among liquid molecules.
514 In accordance, the molecules are impacted by a larger quantity of energy at a greater
515 temperature, affecting the adhesive forces. As a result, higher energy molecules can move more
516 freely. The higher occurrence of molecular collision per unit volume and per unit time affects
517 resistance against the movement of the liquid. Decreased intermolecular forces are driven by
518 increased temperature and lower resistance to the liquid movement. Therefore, the viscosity of
519 Newtonian nanofluid reduces with rising temperature. Brownian motion is another cause for
520 switching the viscosity with the temperature and volume fraction. The impact of nanoparticles'
521 Brownian movement on the nanofluid viscosity after the increasing temperature is
522 understandable. Nanoparticles and the base fluid now have easy molecular movements, and the
523 possibility of intermolecular collision is decreased in nanoparticles with the temperature rise.
524 Moreover, the intermolecular gap between nanoparticles and the base fluid improves with the
525 temperature rise, thus lowering the resistance to movement and viscosity.

526
527



528

529 Figure 12 Dynamic viscosity at the increasing temperature at different concentration



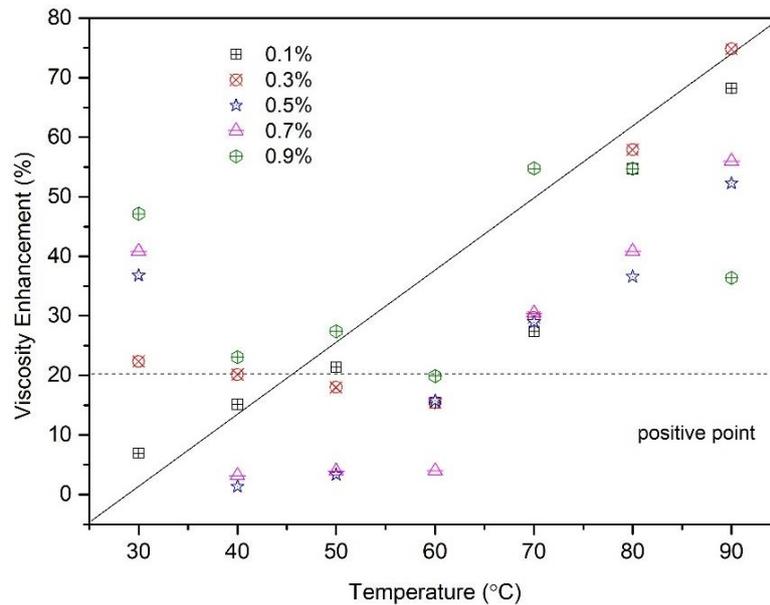
530

531 Figure 13 Dynamic viscosity at the increasing concentration for different temperature

532 Figure 14 shows the difference in viscosity improvement concerning temperature in
 533 several solid concentrations. The calculation of viscosity enhancement can be denoted as
 534 below:

535

$$= \pm \left(\frac{\mu_{nl} - \mu_{bf}}{\mu_{bf}} \times 100 \right)$$



536

537 Figure 14 Viscosity enhancement at increasing temperature for different concentrations.

538 From Figure 14 that the maximum improvement in viscosity in solid concentrations of
 539 0.3% at 90°C, while in solid concentrations of 0.25% and 0.5%, the highest rise occurred at the
 540 temperature of 35 °C. Hence, it's interesting to note that an increase in dynamic viscosity of
 541 the examined nanolubricant at a solid concentration of at all concentrations except 0.9%
 542 concentration at 40°C temperatures, 0.1% at 30°C, 0.7%, 0.5% and 0.9% at 60°C and 0.3%,
 543 0.5% and 0.7% at 50°C was fewer than 20% which can be assumed as an optimistic fact in
 544 manufacturing and engineering application of this nanolubricant [64]. Thus, the minimum and
 545 maximum enhancement in the dynamic viscosity was 1.34% and 74.81%, which occurred at
 546 the temperature of 40°C and 90°C and solid concentrations of 0.5% and 0.3%, respectively

547

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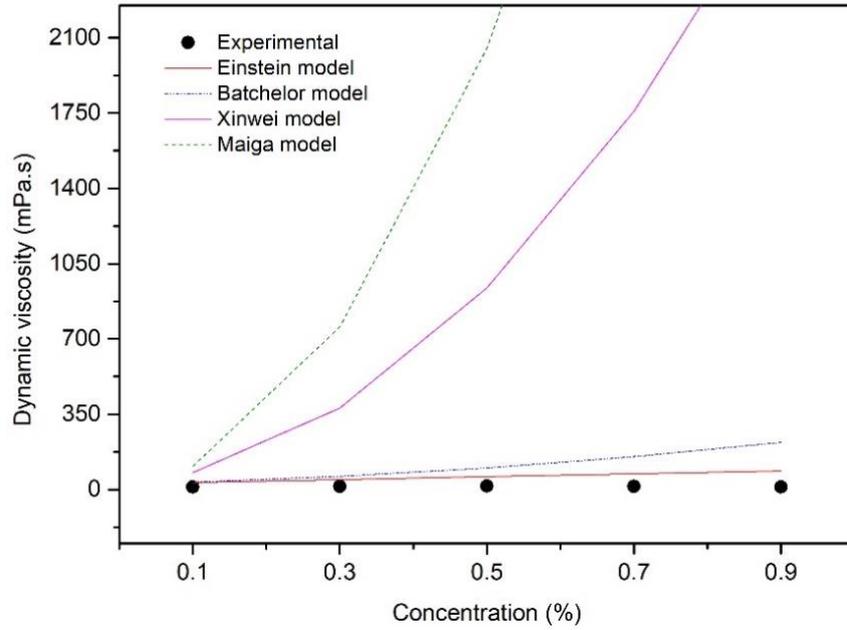
552 **3.3.2 Difference Between Hypothetical Model and Experimental Data**

553 Many hypothetical models to calculate the dynamic viscosity of nanolubricant have
 554 been suggested by researchers. In this analysis, 4 frequently used models are analysed;
 555 Einstein, Batchelor, Wang and Maiga are selected to examine their capability to calculate the
 556 dynamic viscosity of the examined nanolubricant and assess their results with the experimental
 557 data. Table 1 displays the selected theoretical models.

558 Table 1 Selected theoretical models to predict the dynamic viscosity

	Model	Description	Proposed by
559	$\mu_{nf} = (1 + 2.5\varphi)\mu_{bf}$	Foresee the viscosity of a	[65]
560		suspension, including	
561		globular particles in	
		solid concentrations less	
		than 5%	
	$\mu_{nf} = (1 + 2.5\varphi + 6.2\varphi^2)\mu_{bf}$	Foresee the dynamic	[66]
		viscosity of a suspension	
		containing rigid globular	
		particles	
	$\mu_{nf} = (1 + 7.3\varphi + 123\mu^2)\mu_{bf}$	Foresee the dynamic	[67]
		viscosity of nanofluids	
	$\frac{\mu_{nf}}{\mu_f} = 1 - 0.19\varphi + 306\varphi^2$	The relation was obtained	[68]
		by executing a least-square	
		curve fitting method of	
		experimental.	

562
 563 The contrast between the chosen theoretical models and experimental data is shown in
 564 Figure 15. Neither model can calculate the nanofluid's dynamic viscosity in an accurate value.
 565 Therefore, it is necessary to suggest a model that can calculate the nanofluid's dynamic
 566 viscosity in the appropriate accuracy range. Table 2 shows the error analysis between model
 567 from previous researcher compared to experimental data.



568

569 Figure 15 Comparison between theoretical models from previous researchers and current
 570 experimental data

571

Below are the error analysis compared to the previous model and experimental result.

$$POAE (\%) = \left(\frac{\text{Experimental value} - \text{Model value}}{\text{Experimental value}} \right) \times 100 \quad \text{Eq.8}$$

572

573 Table 2: Error analysis between previous researcher model and experimental in percentage

Concentration	Einstein Model	Batchelor Model	Xinwei Model	Maiga Model
0.1	176.0625	189.7551667	553.716	792.4548333
0.3	222.0729167	324.7681944	2524.434167	5142.058819
0.5	254.9375	499.45	5484.35	12110.63875
0.7	406.1145833	965.2331944	12116.68583	27654.7716
0.9	617.7625	1726.871167	23575.12	54822.96567

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579 **3.4 Thermal Conductivity**

580 The thermal conductivity of liquids is an important thermal property that influences
581 heat transfer performance. The improvement in thermal properties of nanolubricants will drive
582 the system to operate at utmost efficiency, especially in the internal combustion engine.
583 Researchers attempted to enhance the reduced thermal conductivity of the standard heat
584 transfer fluids by scattering several nanoparticles in the base fluid, mainly in engine oil [64,
585 69-71]. Therefore, the thermal conductivity enhancement of CNC-CuO nanolubricants was
586 investigated under three conditions; (i) Different concentrations of nanoparticles dispersed in
587 engine oil. (ii) Nanolubricants at optimum concentration with the variation of temperature, and
588 (iii) Nanolubricants with various types of nanolubricant at constant volume concentration.

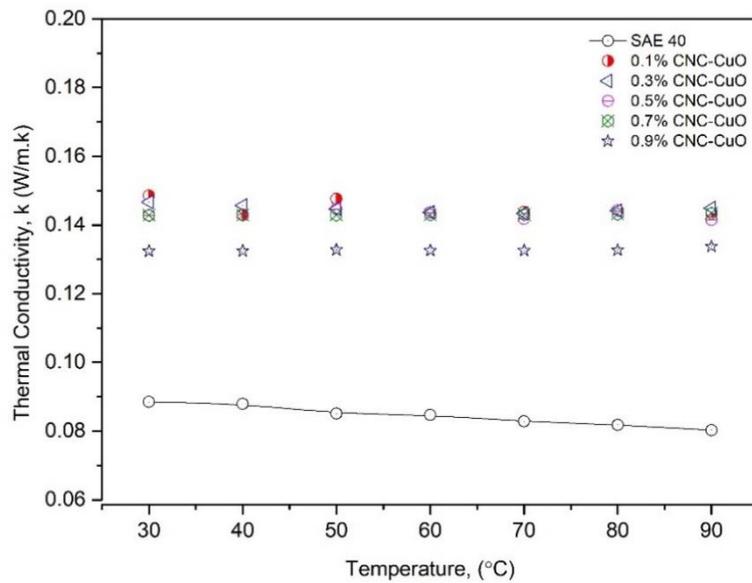
589

590 **3.4.1 Thermal Conductivity in Different Temperatures and Solid Concentration**

591 The thermal conductivity of CNC-CuO nanolubricant with different concentrations
592 (0.1% to 0.9%) is defined with a temperature varying from 30°C to 90°C. Figure 16 and Figure
593 17 show the temperature-related results of the thermal conductivity of the chosen nanoparticle
594 proportions. According to both figures, the thermal conductivity value shows an erratic
595 outcome as the temperature increases. With a concentration of 0.5%, the value of thermal
596 conductivity at 50°C has risen. The trend decreases gradually until 90°C. As for 0.9%, the
597 thermal conductivity increases marginally up to 90°C. Hence, the combination between carbon-
598 based nanoparticles (CNC) and metallic (CuO) as the thermal conductivity amount displays
599 the consistent growth pattern for CNC nanolubricant, as shown in Figure 18.

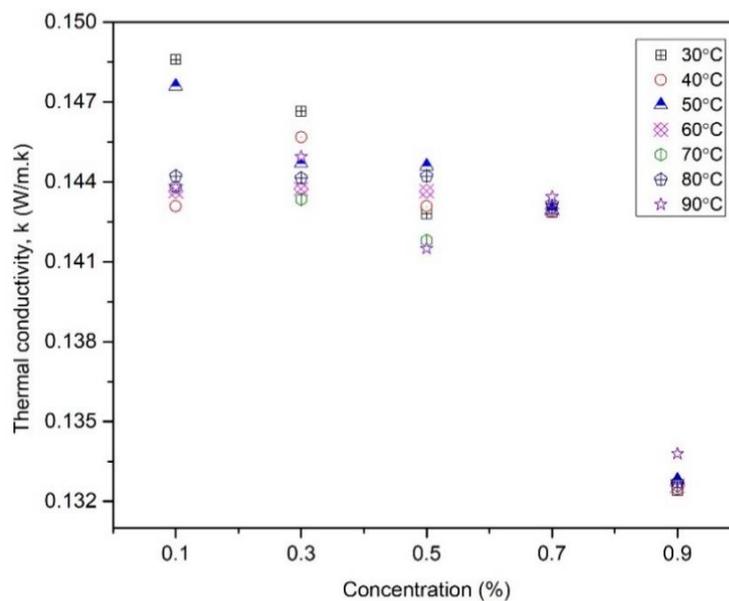
600 In contrast, Aberoumand et al. show a consistent decreasing pattern for CuO
601 nanolubricant [72, 73]. Despite the inconsistent pattern for CNC-CuO nanolubricant as the
602 temperature increases, all concentrations for CNC-CuO nanolubricant show better results than
603 the base fluid (SAE 40). This outcome is because the mean path between each of the
604 nanoparticles was high when the nanolubricants were at smaller concentrations and higher
605 temperatures, consequently reducing the collision probability. When the fluid heats, the
606 Brownian movements of molecules strengthen and thus, the consequent interaction between
607 the molecules increases. The fast motions of the particles due to an expansion in temperature
608 also affect the clumping of the particles, which boosts the possibility of impacts among the
609 particles. As a result, the improvement of the thermal conductivity. Another reason can be

610 because the near-field radiation was strongly affected by the thermal conduction as the
 611 temperature of the nanolubricant increased [74].



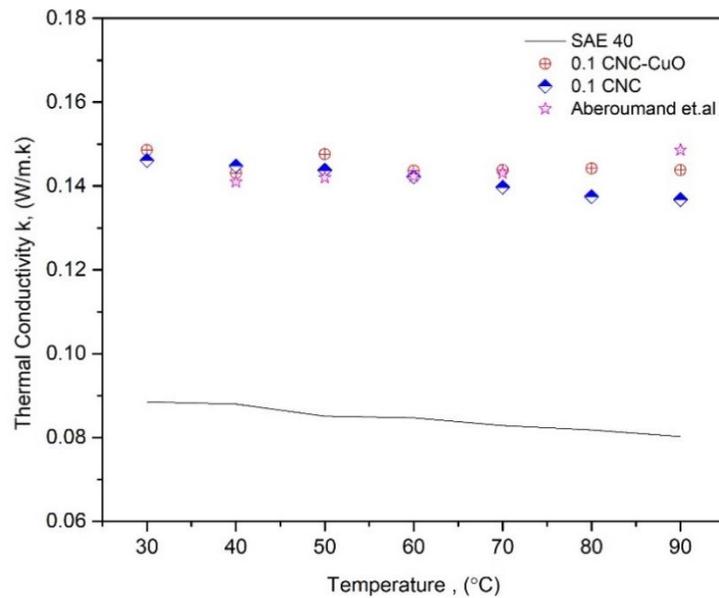
612
 613 Figure 16 Thermal conductivity of CNC-CuO at different concentrations and increasing
 614 temperature

615



616
 617 Figure 17 Thermal conductivity versus different concentrations at increasing temperature

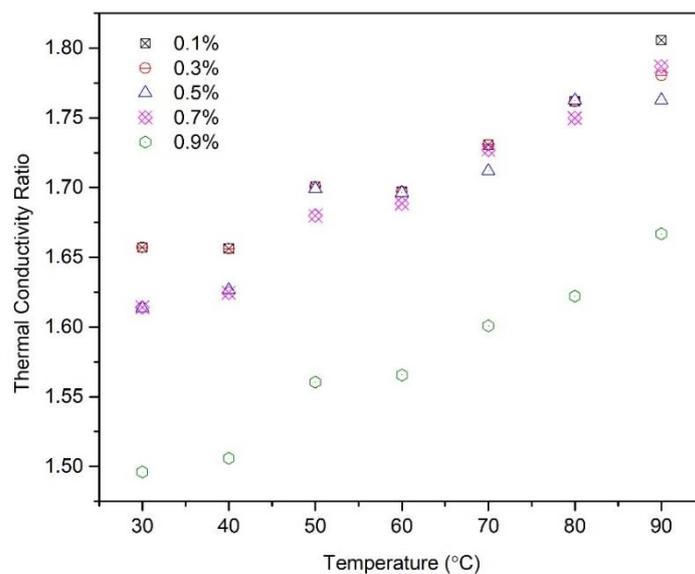
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621

622 Figure 18 Thermal conductivity result of CNC, CNC-CuO and CuO nanolubricant [73] better
623 than the base fluid

624 Figure 19 displays the ratio of thermal conductivity given by, $\left(\frac{k_{eff}}{k_b}\right)$ In a function of
625 temperature for all the corresponding solid concentrations. The ratio improves with
626 temperature and with the increase of solid concentration. The maximum value of the thermal
627 conductivity ratio in the chosen nanolubricant is around 1.80566 for a solid concentration of
628 0.1% at 90°C. The most important cause for the improvement of thermal conductivity is the
629 existence of a layer in the solid-liquid boundary, and particle clumping provides directly to the
630 improvement of thermal conductivity. The molecules of lubricant appear closer to the element
631 and forms encrusted shapes. It behaves like a solid surface and plays a role as a thermal bridge
632 between particles and oil molecules. Furthermore, the thermal conductivity of particles is
633 higher than the lubricant. As the concentration rises, the particles are close enough to improve
634 the phenomenon of heat transfer among the nanoparticles due to a rise in Brownian movements
635 [75].



637

638 Figure 19 Thermal conductivity ratio of CNC-CuO nanolubricant with the temperature at
639 different concentrations

640 3.4.2 Comparison concerning Hypothetical Model and Experimental Data

641 Hypothetical simulations to forecast the thermal conductivity of nanolubricant are
642 suggested by many researchers. In this study, the most generally used models, are Hamilton
643 and Crosser and Yu Choi model, are selected to assess their ability to forecast the thermal
644 conductivity of the studied nanolubricant and assess its results with the experimental data.
645 Hamilton-Crosser (H-C) proposed the basic model to measure thermal conductivity at the
646 solid-liquid condition. The models predict the thermal conductivity at the solid phase ratio
647 greater than 100 [76]. Another method to calculate thermal conductivity was also proposed by
648 Yu and Choi [77]. Table 3 shows the description of the theoretical model.

649

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656 Table 3 Theoretical model from previous researchers with the description

Model	Description	Proposed by
$k_{eff} = \left(\frac{k_p + (n-1)k_f + (n-1)\phi(k_p - k_f)}{k_p + (n-1)k_f - \phi(k_p - k_f)} \right) k_f$	<p>The model assumption is the discontinuous phase is spherical</p>	[76]
$k_{eff} = \left(\frac{kp + 2kf + 2\phi(kp - kf)(1 + \beta)2}{kp + 2kf - \phi(kp - kf)(1 + \beta)3} \right) kf$	<p>Modified Maxwell's equation, introducing the effect of the interfacial layer. They assume that the nanolayer impact is significant for small particles (r - h)</p>	[77]

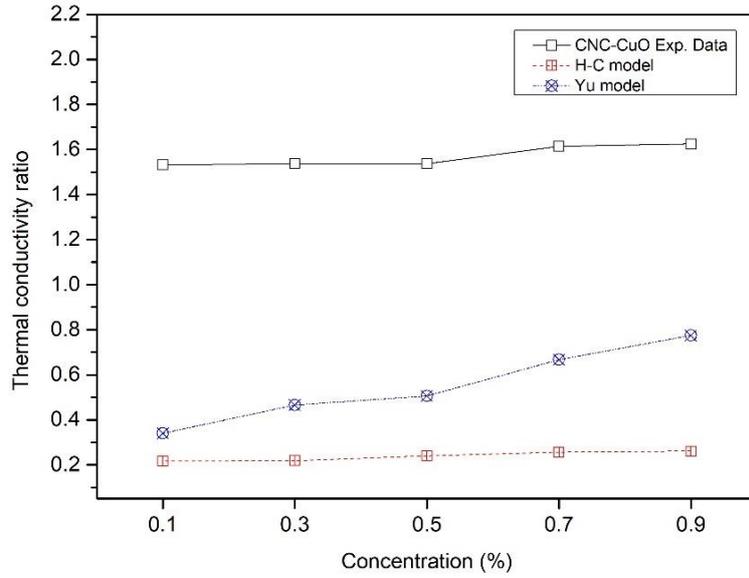
657 From both equations, the empirical shape factor (n) is as below:

$$n = \frac{3}{\phi}$$

Eq. 9

658 where the ϕ denotes the surface area ratio of a sphere with a volume of the surface area
 659 nanoparticles, from the H-C equation, the value of n is 2 (spherical nanoparticles) β in denotes
 660 the ratio of the thickness of nanolayer with the real particle radius, these two equations then
 661 were used to compare the enhance thermal conductivity ratio. Figure 20 compares the
 662 theoretical model with the current experimental data. It is obvious from the figure that both of
 663 the equations from the previous study's H-C and Yu-Choi models underestimate the viable
 664 thermal conductivity of the nanolubricant. The reason is because of the impact of prime
 665 parameters; for example, the nanoparticle size and the interfacial layer were not acknowledged
 666 on the thermal conductivity of the nanolubricant. The effective thermal conductivity of
 667 nanolubricant relies upon the nanoparticles' thermal conductivity as well as the base fluid, the
 668 concentration of nanoparticles, shape and thickness of nanoparticles. Table 4 shows the error
 669 analysis of thermal conductivity model and experimental result.

670



671

672 Figure 20 Comparison between theoretical from the previous researcher compared to

673 CNC-CuO experimental data.

674 Table 4: Error analysis between previous researcher model and experimental thermal

675 conductivity model in percentage

Concentration	H-C Model (%)	Yu Model (%)
0.1	77.99093	70.61376
0.3	78.46741	63.52852
0.5	76.48986	60.84944
0.7	76.93715	54.01294
0.9	76.8401	47.96168

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685 **3.5 Specific Heat Capacity**

686 The specific heat (C_p) is the main property of thermophysical for the thermal model. It
687 can be said that specific heat is necessary for assessing a specific-phase heat transfer. The
688 specific heat is also utilized to evaluate additional properties such as thermal expansion
689 coefficient and isothermal compressibility [78]. Thus, specific heat measurements and
690 corresponding models are required to apply the nanolubricants to heat transfer applications. In
691 the present study, similar to thermal conductivity, the specific heat capacity enhancement of
692 CNC-CuO nanolubricants was investigated under three conditions; (i) Different concentrations
693 of nanoparticles dispersed in engine oil. (ii) Nanolubricants at optimum concentration with the
694 variation of temperature, and (iii) Nanolubricants with various types of nanolubricant at
695 constant volume concentration.

696

697 **3.5.1 Specific Heat Capacity at Different Temperatures and Solid Concentration**

698

699 Figure 21 displays the difference in experimental findings for median specific heat
700 capacity versus temperature in the base fluid (SAE 40) and CNC-CuO nanolubricant at
701 different concentrations. Oil, in addition to a higher specific heat capacity rate, shows a reduced
702 temperature rise for the total absorption of heat energy; hence, the greater value of C_p in the
703 lubricant is improved in heat transfer [79]. Hence, the specific heat capacity of the
704 nanolubricants is an essential criterion for enhancing the load-carrying threshold of the system.
705 The temperatures in the supporting gaps of the bearings are lesser in the place where the
706 specific heat capacity of engine oil is elevated; hence, the heat capacity is elevated in the same
707 operational situation [80]. According to figure 21, 0.1%, 0.3%, and 0.5% show a better value
708 of the C_p than the base oil, while 0.7% and 0.9% are below the base fluid. This result indicates
709 that 0.5% is the optimum concentration for better C_p . Figure 22 displays the specific heat
710 capacity against concentration. The specific heat capacity (C_p) of fluid significantly affects
711 regulating heat amount or rate of heat transfer in thermal systems. From Figure 23, the specific
712 heat capacity of the nanolubricant decreases as volume concentration improves. This reduction
713 in specific heat with improving volume concentration is constant with the findings in the
714 literature on numerous nanofluids [81, 82].

715

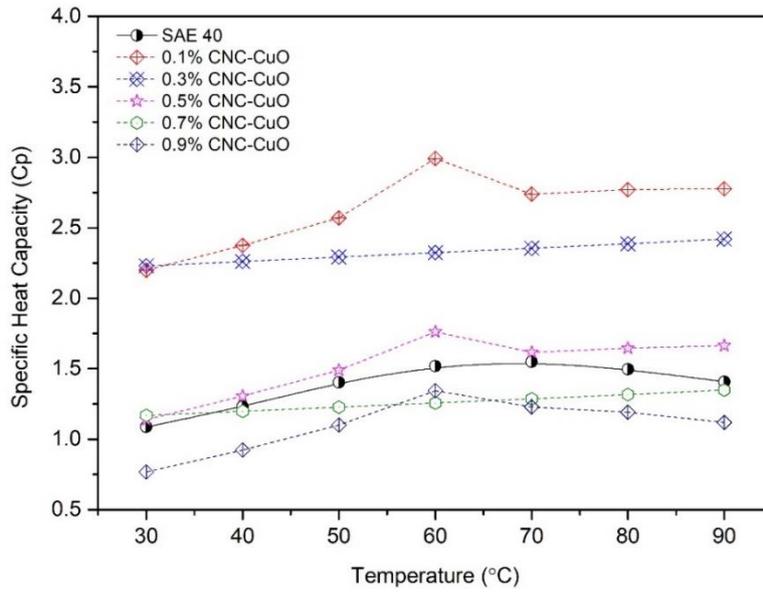
716 According to both graphs, after 0.5% concentration, the increase in nanoparticle volume
717 concentration in nanolubricants will certainly decrease the specific heat capacity of the
718 nanolubricants. The specific heat capacity of nanolubricant tends to lessen marginally with a

718 temperature rise. Thus, the rise in the specific heat with temperature examined in Figure 23 is
719 in line with the number of nanoparticles that appeared in the base fluids. The flawed geometric
720 character of the nanoparticles impacts the specific heat of nanoparticles, eventually producing
721 a discrepancy between the specific heat capacity of the particles and the bulk material [83]. As
722 heat increases, the specific heat capacity of the nanoparticles rises and can go beyond that of
723 the bulk material by twice as much [84]. The bigger difference in the straight-line exhibited by
724 the 50/50 lubricant/surfactant blend as associated with the base lubricant is theorized to be
725 affected by some surfactant aggregation. Surfactants have a larger propensity for accumulation
726 at high concentrations [85].

727 Figure 23 shows the comparison between base oil (SAE 40) with a single nanoparticle:
728 CNC nanolubricant, CNC-CuO nanolubricant and Saeedinia et al [86] conduct the specific heat
729 capacity experiment for CuO nanoparticle with the base oil. According to the graph, the
730 specific heat capacity was improved when nanoparticles were added. This might be due to the
731 nanoparticle size, where CuO shows the smallest size, followed by CNC-CuO and CNC.
732 Greater specific heat capacities for nanoparticles are likely when particles' size is reduced [84,
733 85]. In a previous study of nanoparticles, specific heat rates are only available up to 80°C,
734 suggesting that the high operating temperatures of nanolubricants have many hidden areas that
735 need to be examined further. A high surface area per unit mass of nanoparticles is
736 recommended to improve the interfacial thermal resistance among the nanoparticles and
737 neighbouring liquid molecules. This elevated interfacial thermal resistance performs as extra
738 thermal space due to the interfacial contact of the vibration energies among nanoparticle atoms
739 and the interfacial molecules. This occurrence can cause a rise in the specific heat of
740 nanolubricant [86].

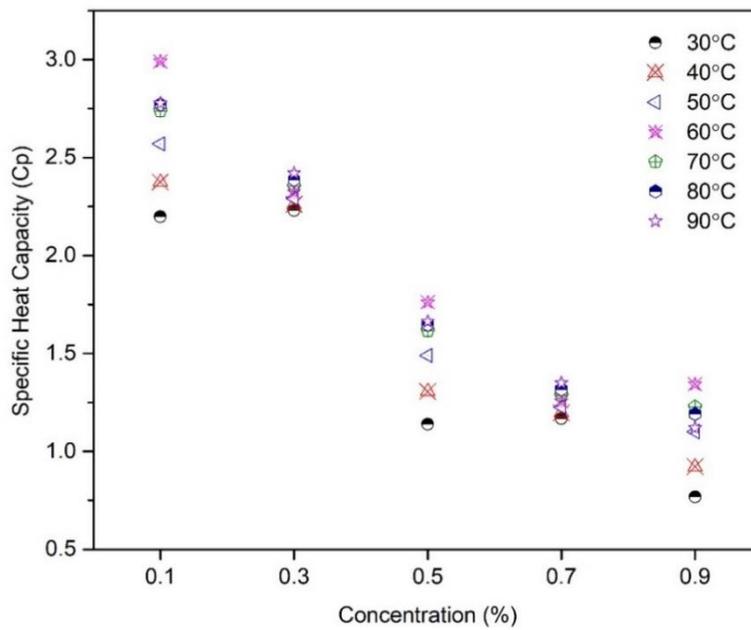
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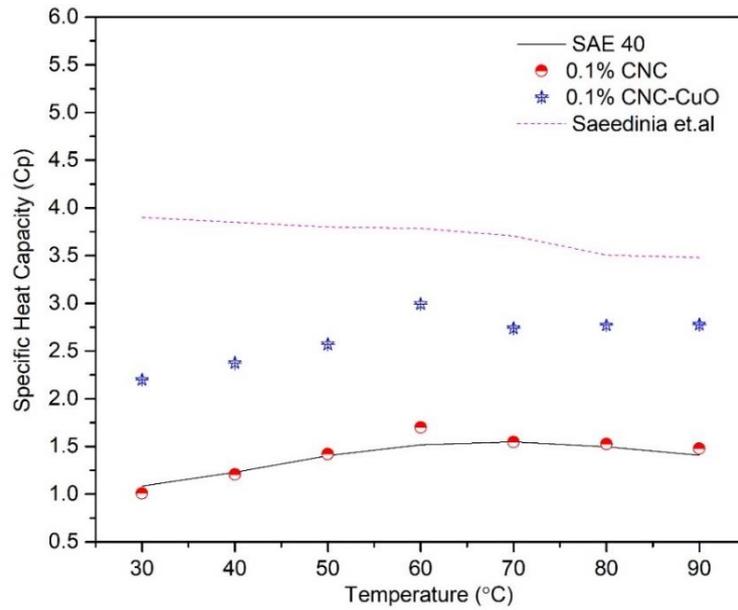
743 Figure 21 Specific heat capacity of CNC-CuO at different concentrations

744
745



746 Figure 22 Specific heat capacity at different concentration

747
748



749

750 Figure 23 Comparison between specific heat capacity of CNC-CuO with the base fluid

751 (SAE 40), CNC nanolubricant and [87] at 0.1% concentration

752

753 3.5.2 Comparison between Theoretical Model and Experimental

754 As mentioned before, the experiments and models about specific heat capacity are not
 755 widely discussed. Forecasting the specific heat capacity of the nanofluids can help investigators
 756 enhance their knowledge of the heat holding properties of the nanofluids. Here, two generally
 757 used models, Pak and Cho and Xuan and Rotzel, are selected to analyze their ability to forecast
 758 the specific heat capacity of the studied nanolubricant and evaluate their results with the
 759 experimental data. Table 5 shows the chosen theoretical models. Like thermal conductivity,
 760 predicting the specific heat capacity of nanolubricant depends on numerous important
 761 parameters, such as nanoparticles concentration, the temperature of nanolubricants and the type
 762 of nanoparticle material.

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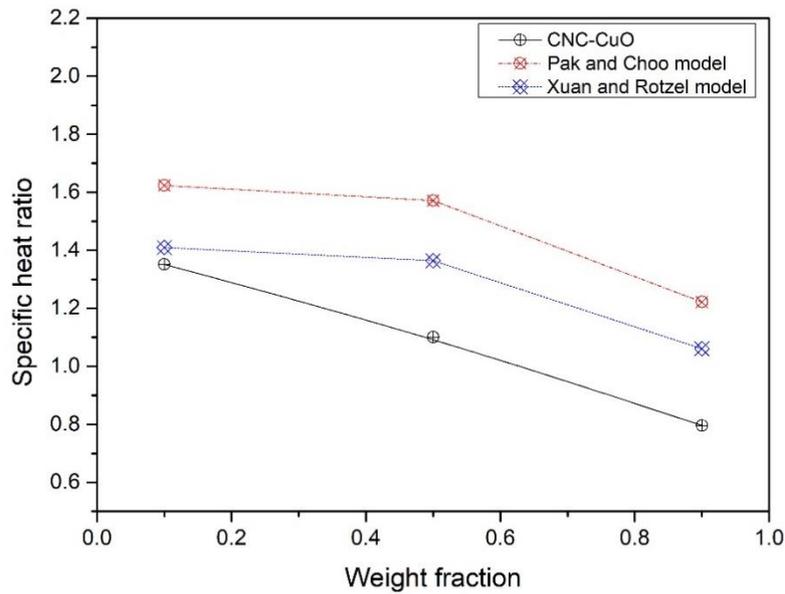
768

769

770 Table 5 Theoretical model for specific heat capacity.

Model	Description	Proposed by
$C_{pnf}, Pak and Cho$ $= \phi C_{pp} + (1 - \phi) C_{pf}$	The specific heat capacity model significantly deviates from the experimental.	[88]
$(\rho C_p)_{nf}, Xuan and Rotzel =$ $\phi(\rho C_p)_p + (1 - \phi)(\rho C_p)_f$	Extension of Maxwell's equation, introducing empirical factor n, where $n = 1/4$ $3/J$ and J is particle sphericity.	[89]

771
 772 According to Table 5, the [88] model is the volume fraction weighted model, and the
 773 [89] model is the mass fraction weighted model. The first model assumes that the specific heat
 774 is equivalent to the volume fraction weighted average of the specific heats of the base fluid and
 775 nanoparticles. This is similar to the mixing theory for ideal gas mixtures. The mass fraction
 776 weighted model's second mode is centered on thermal equilibrium. The specific heat
 777 corresponds to the mass fraction weighted average of the specific heat of the base fluid and the
 778 nanoparticles. The two models generate similar results for tiny nanoparticle concentrations but
 779 differ significantly as the nanoparticle concentration rises. Figure 24 shows both models'
 780 specific heat capacity ratios compared with experimental data. Figure 24 Xuan and Rotzel
 781 model shows the closest to the experimental data compared to Pak and Cho model. This data
 782 complies with the previous researchers. Researchers have shown that the mass fraction
 783 weighted model exhibits better agreement for nanofluid-specific heat data [90-93]. Table 6
 784 shows the error analysis between model for specific heat capacity with the experimental data.



785

786 Figure 24 Specific heat ratio at different literature models for CNC-CuO nanolubricant

787 Table 6: Error analysis between previous researcher model and experimental for specific
 788 heat capacity model in percentage (%)

789

Concentration	Pak and Cho Model	Xuan and Rotzel Model
0.1	20.33761171	4.915597073
0.3	31.32113058	14.20325588
0.5	41.52994184	23.07747541
0.7	46.14309876	27.43899236
0.9	51.79905878	33.20940229

790

791 According to [94], for small nanoparticle concentration, the models will exhibit nearly
 792 the same result as the experimental but diverge greatly as the concentration increases. The
 793 classical numerical calculations do not correctly foresee the experimentally achieved values of
 794 specific heat capacity and viscosity. This is because the models do not contain all the aspects
 795 impacting the rheological performances in the nanofluids. Based on other research, the thermal
 796 equilibrium models, which presume that a thermal equilibrium occurs among the base fluid
 797 and the nanoparticles, are a better numerical forecaster of specific heat capacity than the
 798 blending concept. Lately, the “nanolayer effect” has been contemplated in some models for
 799 the specific heat of molten-salt nanofluids. The nanolayer effect implies the trend of liquid
 800 molecules creating an ordered, thin (a few nanometers), solid-like layer on the nanoparticle
 801 shell. This is believed to impact the heat exchange between the liquid and the nanoparticle [95].

802 Even though there are few findings on the nanolayer effect, it is crucial in verifying nanofluids'
803 thermal conductivity, but its importance for the specific heat is not well realized. Nonetheless,
804 a few findings have indicated that the nanolayer effect in specific heat is particle size-
805 dependent, i.e., the result is further important for tinier nanoparticles [36]. As the measurements
806 have indicated that the particle size does not have an apparent impact on the specific heat it is
807 acceptable to hypothesize that the nanolayer effect for the specific heat, can be ignored.

808

809 **4.0 Conclusion**

810 In the present study, the thermophysical properties and the comparison between the theoretical
811 model and the experimental data of the thermophysical properties have been discussed.
812 Furthermore, the effects of temperature and varied concentrations on
813 Stability, dynamic viscosity, thermal conductivity and specific heat capacity of the CNC-CuO
814 nanoparticle added to engine oil have been studied. The experiments were carried out in
815 temperatures ranging from 30°C to 90°C and volume concentrations ranging from 0.1% to
816 0.9%. Based on the experimental measurements, the following can be concluded:

- 817 1) The samples were mixed well with no settlement of nanoparticles at the bottom of the
818 test tube at week 1. After the 4th week, the supernatant layer is at the top of the solution.
819 Therefore, CNC-CuO nano lubricant was observed to be stable for up to one month or
820 more
- 821 2) According to the UV-Vis spectrophotometer result, 0.1% shows the closest absorbance
822 ratio to one; thus, 0.1% concentration shows the most stable nano lubricant compared
823 followed by 0.5%, and the least stable nano lubricant is 0.3% concentration.
- 824 3) According to the viscosity index result (VI), as the concentration of CNC-CuO
825 nanoparticles increases, the VI is higher, proving that CNC-CuO nanoparticles added
826 with engine oil did improve the lubricity of the base oil regarding its viscosity by
827 44.3%-47.12%.

- 828 4) The minimum and maximum enhancement in the dynamic viscosity was 1.34% and
829 74.81%, respectively, which occurred at the temperature of 40°C and 90°C and solid
830 concentrations of 0.5% and 0.3%, respectively
- 831 5) The thermal conductivity ratio increase with temperature and with the increase of solid
832 concentration as well. The maximum increase of thermal conductivity ratio of the
833 selected nanolubricant was found to be 1.80566 for a solid concentration of 0.1% at
834 90°C.
- 835 6) For specific heat capacity, 0.1%, 0.3% and 0.5% show a better value of the C_p than the
836 base oil, while 0.7% and 0.9% are below the base fluid. This result indicates that 0.5%
837 is the optimum concentration for better C_p .
- 838 7) The main findings of the stability and thermophysical properties of CNC-CuO are
839 usable for the tribology application in terms of determining how to improve engine oil
840 efficiency through the heat transfer and flow behaviour of nanolubricants

841 4.1 Credit authorship contribution statement

842 **Sakinah Hisham:** Conceptualization, Methodology, Validation, Formal analysis, Investigation,
843 Data Curation, Writing - Original Draft, Visualization. **K. Kadirgama, D. Ramasamy:**
844 Conceptualization, Methodology, Validation, Formal analysis, Investigation, Resources, Writing -
845 Review & Editing, Visualization, Supervision. **Mohd Kamal Kamarulzaman, R. Saidur:**
846 Conceptualization, Investigation. **Talal Yusaf:** Review & Editing

847 4.2 Declaration of competing interest

848 The authors declare that they have no known competing financial interests or personal
849 relationships that could have appeared to influence the work reported in this paper.

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854

855 4.4 References

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