

Where are the magnetar binary companions? Candidates from a comparison with binary population synthesis predictions

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ABSTRACT

It is well established that magnetars are neutron stars with extreme magnetic fields and young ages, but the evolutionary pathways to their creation are still uncertain. Since most massive stars are in binaries, if magnetars are a frequent result of core-collapse supernovae, some fraction are expected to have a bound companion at the time of observation. In this paper, we utilise literature constraints, including deep Hubble Space Telescope imaging, to search for bound stellar companions to magnetars. The magnitude and colour measurements are interpreted in the context of binary population synthesis predictions. We find two candidates for stellar companions associated with CXOU J171405.7–381031 and SGR 0755–2933, based on their *J-H* colours and *H*-band absolute magnitudes. Overall, the proportion of the Galactic magnetar population with a plausibly stellar near-infrared counterpart candidate, based on their magnitudes and colours, is between 5 and 10 per cent. This is consistent with a population synthesis prediction of 5 per cent, for the fraction of core-collapse neutron stars arising from primaries which remain bound to their companion after the supernova. These results are therefore consistent with magnetars being drawn in an unbiased way from the natal core-collapse neutron star population, but some contribution from alternative progenitor channels cannot be ruled out.

Key words: stars: neutron – stars: magnetars – binaries: general

1 INTRODUCTION

Magnetars comprise a class of highly magnetised young neutron stars, with magnetic field strengths up to 10^{15} G (Kouveliotou et al. 1998). They are typically discovered when they produce γ -ray or X-ray bursts during active episodes; their nature is also confirmed through the detection of their persistent X-ray emission (Kaspi & Beloborodov 2017). Some were originally classified as soft gamma repeaters (SGRs), others as anomalous X-ray pulsars (AXPs), but both populations are now believed to be manifestations of the same phenomenon (Thompson & Duncan 1996). Approximately 30 are currently known; two are in the Magellanic clouds (one each, Olausen & Kaspi 2014), while the rest reside in our Galaxy. Their very rare Giant Flares are bright enough to be seen at extragalactic distances (Hurley et al. 2005; Palmer et al. 2005); two originated from mag-

netars in the Milky Way and a handful have been identified in other galaxies (e.g. Hurley et al. 2010; Burns et al. 2021).

Measurements of magnetar spin periods P and period derivatives \dot{P} imply extremely young ages of 10^3 – 10^5 yr, under the assumption of a surface dipole field and magnetic braking. These estimates are unreliable for magnetars, since the fundamental assumption of a constant magnetic field (and hence braking index) is shown to vary significantly (Younes et al. 2017). However, these are upper limits for their decaying magnetic fields, leading to *overestimates* of their true ages. The young magnetar ages are further backed up by their associations with star forming regions and supernova remnants (e.g. Munro et al. 2006; Gelfand & Gaensler 2007; Nakano et al. 2015). Moreover, current sophisticated methods now exist that account for their magnetic field decay, in addition to particle winds and gravitational wave emission (Mondal 2021).

Despite some associations with HII regions and supernova remnants, around half of the magnetar population have not yet been associated with a high-mass progenitor (Olausen & Kaspi 2014).

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This may be attributed to detection biases due to e.g., dust, source crowding, and high column densities. There are, however, magnetars for which there is no obvious association with recent star formation despite a relatively clear sightline (see e.g., SGR 0501+4516 which lies in the Galactic anti-centre direction). Putative non-core-collapse production channels include binary neutron star mergers and the accretion or merger induced collapse of ONe white dwarfs resulting in magnetars (Duncan & Thompson 1992; Levan et al. 2006; Ablimit 2021).

The rarity of magnetars (Kouveliotou et al. 1994; Beniamini et al. 2019) raises questions about their origin. Are specific conditions required to generate neutron stars with such strong magnetic fields? If their magnetic fields decay fast enough, it may be that a large fraction of core-collapse supernovae result in magnetars (Nakano et al. 2015; Beniamini et al. 2019), which then may decay into X-ray dim isolated neutron stars (XDINS, Jawor & Tauris 2021) before fading beyond detection limits. Correspondingly, if magnetars are intrinsically rare, particular evolutionary pathways may be required. Suggestions include core-collapse following main sequence mergers (Schneider et al. 2020), rapid core rotation pre-collapse (White et al. 2021), and non-core collapse channels, as mentioned above.

Owing to their large energy reservoirs, magnetars have also been invoked as the central engines in a variety of transients, from compact object mergers, which produce short gamma-ray bursts (GRBs, Bucciantini et al. 2012; Gompertz et al. 2013; Rowlinson et al. 2013; Gompertz et al. 2014; Metzger & Piro 2014; Zou et al. 2021), core-collapse long GRBs (Wheeler et al. 2000; Komissarov & Barkov 2007; Metzger et al. 2011), superluminous supernovae (Kasen & Bildsten 2010; Woosley 2010; Metzger et al. 2015) and fast blue optical transients (Prentice et al. 2018; Mohan et al. 2020). Many fast radio burst models also implicate magnetars (e.g. Lyubarsky 2014; Metzger et al. 2019), a connection strengthened by the discovery of low-luminosity FRBs from the Galactic magnetar SGR 1935+2154 (CHIME/FRB Collaboration et al. 2020; Bochenek et al. 2020; Younes et al. 2021). The host environments of extragalactic FRBs are broadly representative of where we expect to find young neutron stars (Heintz et al. 2020; Safarzadeh et al. 2020; Bochenek et al. 2021; Mannings et al. 2021; Chrimes et al. 2021; Bhandari et al. 2021; Katz 2021). However, there is also evidence that FRBs do not follow the cosmic star formation rate density (James et al. 2020; Zhang & Zhang 2021), and there are other objects which seem inconsistent with core-collapse magnetars. For example, assuming that magnetars do produce FRBs, Tendulkar et al. (2021) find that FRB 20180916B is too offset from a nearby star forming region to be a young ejected magnetar. Subsequently, FRB 20200120E was located in a globular cluster outside M81 (Kirsten et al. 2021). Since globular clusters have old stellar populations, a young core-collapse magnetar explanation for this source is challenging (Lu et al. 2021; Kremer et al. 2021).

It remains unclear which progenitor channels contribute to magnetar production, or if any particular channel dominates their formation rate. If we assume that magnetars are drawn from the natal core-collapse neutron star population in an unbiased way, then some fraction should have a bound companion star. The majority of massive stars are in binaries (e.g. Sana et al. 2014), and not all supernovae in binaries unbind the system, as evidenced by the existence of binary neutron star and black hole mergers, X-ray binaries and pulsars in binaries.

In this paper, we use published photometry of counterpart candidates in conjunction with distance and extinction estimates to determine whether any of the Galactic magnetar near-infrared (NIR) counterparts could be a bound companion star. We determine the fraction of the population that could plausibly have a bound compan-

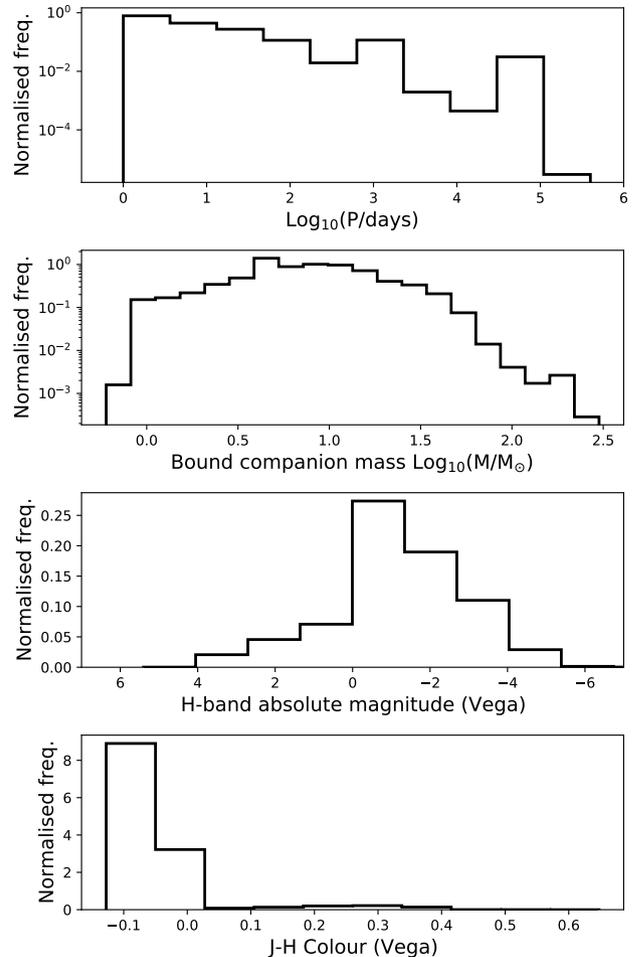


Figure 1. The predicted orbital period, mass, H -band absolute magnitude and $J-H$ colour distributions for bound companions to natal neutron stars. The median absolute H -band magnitude is -1.2 , and the median colour is -0.08 . The axes of the top two panels are on a log scale to clearly show the distribution shape across the full range of parameter space.

ion, and compare these results to population synthesis predictions for the fraction of neutron stars born with a bound secondary companion.

The paper begins with population synthesis predictions in Section 2, and an exploration of the major sources of uncertainty in these predictions. We describe the sample selection in Section 3, before applying distance modulus and extinction corrections in Section 4, allowing us to compare population synthesis predictions with observations in Section 5. We summarise the results in Section 6, discuss our findings in Section 7 in the context of magnetar progenitor and evolutionary models, and conclude in Section 8. All magnitudes are quoted in the Vega system, where conversions from AB magnitudes (Oke & Gunn 1983) have been made using `stsynphot`¹ for Hubble Space Telescope (*HST*) data. AB magnitudes are obtained by adding 0.8227, 0.9204, 1.0973, and 1.2741 to Vega magnitudes for F110W, F125W, F140W and F160W respectively. For J , H and K -band filters, the conversions of Blanton & Roweis (2007) are used.

¹ https://github.com/spacetelescope/stsynphot_refactor

2 BINARY POPULATION SYNTHESIS

2.1 Predictions

To establish predictions for the fraction of neutron stars born in primary supernovae, and the fraction of those with a surviving bound companion, we make use of the population synthesis code BPASS (Binary Population and Spectral Synthesis, Eldridge et al. 2017; Stanway & Eldridge 2018, v2.2.1). BPASS consists of thousands of binary and single stellar evolution models across a grid of masses, mass ratios, orbital periods, and metallicities. Each model is assigned a weighting, corresponding to how often it is predicted to occur in a $10^6 M_{\odot}$ stellar population, with the initial weightings based on observations of Galactic populations (Moe & Di Stefano 2017).

For a fiducial estimate, we use the default BPASS model weightings and broken power law initial mass function (IMF), with a maximum zero age main sequence mass of $300 M_{\odot}$, and gradients of -1.30 ($0.1-0.5 M_{\odot}$) and -2.35 ($0.5-300 M_{\odot}$, based on Kroupa et al. 1993). Solar metallicity (a metal mass fraction of 0.02) is assumed. To identify models which produce neutron stars in core-collapse, we require in the final time step of each model (i) a total mass $> 2.0 M_{\odot}$, (ii) a CO core mass $> 1.38 M_{\odot}$, (iii) a non-zero ONe core mass, and (iv) a remnant mass in the range $1.38 < M_{\text{rem}} < 3.0$ (see also Eldridge et al. 2017, 2019; Chrimes et al. 2020; Briel et al. 2021). We then sum the weightings for all models which satisfy these criteria, and examine the contributions from different model types (single, primary, bound secondary, unbound secondary). To identify how many primary neutron stars are born with a bound companion, the weightings for secondary star models whose companion is a neutron star at $t = 0$ are summed. We find that around half of all neutron stars are born in the supernovae of primary stars in binaries. Another ~ 25 per cent arise from single stars or mergers, and the remaining ~ 25 per cent from secondary stars.

Around ~ 10 per cent of neutron stars born from primaries remain bound after the supernova. We therefore predict that the fraction of natal neutron stars with a bound, pre-supernova companion is $f_{\text{bound}} = 0.05$. Figure 1 shows the predicted $\text{Log}_{10}(P/\text{days})$, $\text{Log}_{10}(M/M_{\odot})$, H -band absolute magnitude and $J-H$ colour distributions for bound companions to neutron stars, in the first time step of secondary BPASS models. The bulk of the colours correspond to massive main sequence companions, with the smaller, redder bump arising from a minority of models where the secondary has already evolved off the main sequence when the primary goes supernova. This is in qualitative agreement with previous predictions for surviving supernova companions (e.g. Kochanek 2009; Zapartas et al. 2017).

We focus on NIR colours because of the available observational constraints on Galactic magnetar counterparts. Since the population lies predominantly in the Galactic plane, and out to large distances (> 10 kpc), high extinctions typically render the optical magnitudes of magnetar counterparts extremely faint (with only a few detections reported). Conversely, there ~ 15 (depending on the confidence of the association) counterpart candidates in the H -band (see Section 3). Since the companions to natal neutron stars are primarily expected to be massive, un-evolved main sequence stars, other works in this area - for example searches for surviving companions to supernovae - typically use bluer optical bands (Maund et al. 2016). While such companions will be intrinsically fainter in the NIR, typically by ~ 2 magnitudes compared to the optical, just $A_V \sim 2$ of extinction negates this advantage. Approximately two magnitudes of optical extinction is the lowest value inferred for any Galactic magnetar (see Section 4), and as extinction increases, the NIR becomes relatively more favourable. Combined with many more detections of magnetar

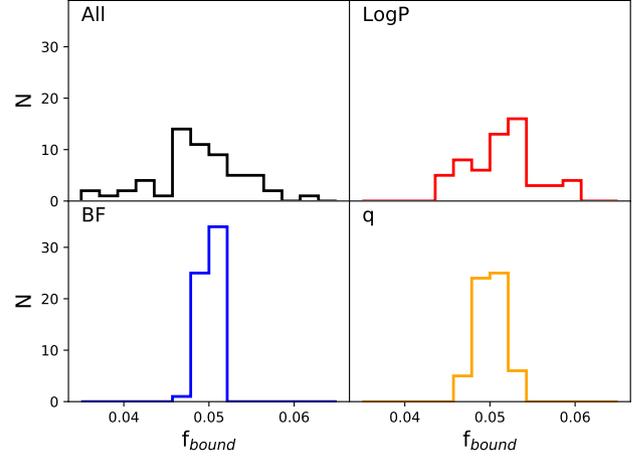


Figure 2. How the prediction for f_{bound} varies with 60 different realisations of the input distributions, drawn through bootstrap re-sampling (as in Stanway et al. 2020). Default assumptions yield $f_{\text{bound}} = 0.05$. The upper left distribution arises from varying the orbital periods ($\text{Log}_{10}(P/\text{days})$, labelled LogP), mass ratios (q) and binary fraction (BF) simultaneously. Orbital periods are the largest individual contributor to the uncertainty.

counterparts in the NIR compared with the optical, this justifies our focus on the NIR as the best wavelength range in which to search for companions.

2.2 Uncertainties

Previous estimates for f_{bound} have varied, in part due to uncertainties on the population synthesis input distributions (for details of how BPASS handles binary dynamics following a supernova, see Tauris & Takens 1998; Eldridge et al. 2011). For example, Eldridge et al. (2011) predict that the number of neutron stars born from primaries which remain bound is a few per cent. The choice of binary fraction, initial period and mass ratio distributions will change f_{bound} , as will the assumed natal kick distribution.

Stanway et al. (2020) investigated the impact of uncertainties in the BPASS input parameters on the integrated light of stellar populations. Using the same set of iterations across orbital period, mass ratio and binary fraction, and drawing from the observed distribution of these inputs in the Galactic stellar populations, we determine the impact on f_{bound} . The default period distribution (LogP), binary fraction (BF) and mass ratio (q) distributions are based on table 13 of Moe & Di Stefano (2017) as follows,

(i) LogP: A period distribution is applied in each of the five mass bins studied by Moe & Di Stefano (2017). For example, 0.095 ± 0.018 of Solar mass stars have a companion with $\text{Log}P=4.5-5.5$ (P in days), whereas 0.30 ± 0.09 of stars above $16 M_{\odot}$ have a companion in this range,

(ii) BF: defined as one minus the single star fraction in each mass bin. The BF in each mass bin has an associated observational uncertainty, e.g. the single star fraction for Solar-type stars is 0.60 ± 0.04 , and among the most massive stars it is 0.06 ± 0.06 ,

(iii) q : the mass ratio distribution is a broken power law following $p_q \propto q^\gamma$, which varies in each LogP and (primary star) mass bin. For example, the probability p_q of a mass ratio in the range 0.3–1.0 for Solar mass primaries in a binary with $\text{Log}P=5$ is given by $\gamma = -0.5 \pm 0.3$. In the mass ratio range 0.1–0.3, $\gamma = 0.3 \pm 0.4$.

Finally, the elevated fraction of twin systems is taken into consideration, and the distributions are interpolated across the BPASS model grid. Randomly sampling these input distributions within the quoted uncertainties (assuming Gaussian uncertainties, as fully described in Stanway et al. 2020) yields the results shown in Figure 2. Uncertainty on the initial orbital periods of massive binaries is the largest source of binary parameter uncertainty in f_{bound} . The result when all uncertainties are varied together is 0.049 ± 0.005 , the wider spread showing that there are correlated uncertainties between the parameters.

We also investigate the impact of assuming different neutron star natal kick velocities - the kick distributions of Hobbs et al. (2005) and Igoshev (2020) yield very similar f_{bound} values of 0.049 and 0.050. Igoshev et al. (2021) also found little difference between these kicks in terms of the Be star mass distribution in X-ray binaries. The kick of Bray & Eldridge (2016, 2018), however, gives a substantially larger value of 0.23. For an observational comparison, we refer to Kochanek (2021) who performed a *Gaia* search for unbound companions to 10 supernova remnants. Combining these results with a previous search for surviving bound companions in supernova remnants, they find that 0.036–0.197 (90 per cent confidence, excluding triple systems) of core-collapse neutron stars are born in primaries which remain bound post supernova. This figure also agrees well with the results of the StarTrack binary population synthesis code (yielding 0.05, assuming an 84 per cent binary fraction; Kochanek et al. 2019) and binary_c ($0.11^{+0.07}_{-0.09}$, assuming 22 per cent of massive binaries merge before the first supernova, Renzo et al. 2019). Therefore, the prediction of $f_{\text{bound}} = 0.05$ is consistent with other population synthesis codes and observational constraints.

3 SAMPLE SELECTION

Our sample consists of the 23 Galactic magnetars (excluding the Magellanic clouds) which have imaging detections or limits, and a distance estimate. Of the 31 objects listed in the McGill magnetar catalogue (Olausen & Kaspi 2014)², CXOU J010043.1–721134 and SGR 0526–66 are in the Large and Small Magellanic clouds respectively, while SGRs 1801–23 and 1808–20 have neither imaging nor a distance estimate. Swift J1818.0–1607 and PSR J1846–0258 have no photometric data while SGR 1833–0832 and AX J1818.8–1559 do not have a distance estimate. The full list of magnetars in the sample, and the photometry used, is provided in Table 1. Most sources have *HST* F160W (*H*) and F125W (*J*) observations, as reported in Chrimes et al. (2022). The NIR counterparts are localised, where possible, through astrometric alignment of a *Chandra* X-ray localisation with the *HST* images, by finding common sources in the field or doing so through an intermediate image. The RMS residuals of this translation, combined with the source centroiding uncertainty, determines the size of the error circle in the *HST* frame. In other cases, a radio localisation is used (for which the absolute astrometric uncertainty of *HST* dominates), or simply the absolute astrometric uncertainty of the X-ray observations, if no common sources could be found and no alternative positional measurements were available. Shortened magnetar names, as indicated in this table, are used hereafter. Given the population synthesis predictions, we would expect 1 ± 1 (Poisson uncertainty only) of the 23 objects in the sample to have a bound companion. This prediction holds under the assumptions that (i) the young age estimates are broadly correct (since the probability of a companion going supernova within the age of the

magnetar is extremely low) and (ii) they are drawn from the natal core-collapse neutron star population in an unbiased way.

4 EXTINCTIONS AND DISTANCES

Since the photometry in Table 1 is reported in terms of dust attenuated apparent magnitudes, we must now correct the observed photometry for the distance and dust extinction along the magnetar sight-lines, in order to compare with the un-attenuated, absolute magnitude predictions of BPASS.

We adopt the primary distance estimates listed in the McGill catalogue (Olausen & Kaspi 2014, and reference therein)². These are derived using a variety of methods, including neutral hydrogen column densities/red clump stars (e.g., Durant & van Kerkwijk 2006b), dispersion measures (e.g., Levin et al. 2010), and associations with objects that have a well-measured distance (such as supernova remnants, molecular gas clouds, or young clusters Corbel et al. 1999; Bibby et al. 2008). In a few cases the distance is derived by assuming that the magnetar is in a spiral arm along that line of sight. In this instance, and any others where the distance uncertainty is not quantified, we assume a 15 per cent error (the mean uncertainty of those that are quantified, and large enough to account for spiral arm width). For SGR 1935, we adopt the estimate of Bailes et al. (2021), which is derived from the dispersion measure and is constrained to $1.5 < d < 6.5$ kpc. All distance estimates adopted and their sources are provided in Table 2.

To infer the reddening due to dust, $E(B - V)$, we try two methods in the following order of preference,

(i) If the magnetar lies above declination -30° , we check the extinction estimate from the Bayestar 3D dust map of Green et al. (2019, G19), using the DUSTMAPS python package (Green 2018). These maps do not have 100 per cent coverage of the Galaxy, and are only reliable out to a certain distance along each sight-line because stars (in the input surveys *Gaia*, Pan-STARRS and 2MASS) need to be detected in order to infer an extinction. To determine whether the extinction estimates are reliable, we compare the total cumulative extinction along each sight-line to the 2D extinction estimate from the Schlafly & Finkbeiner (2011, SF11) dust maps. Where these totals are comparable, we adopt the 3D map estimate at the distance of the magnetar. If there is a large discrepancy (greater than a 50 per cent difference in A_V) we move on to the next method. An extreme example is SGR 1745 towards the Galactic centre, where we have $A_V \sim 3$ from Bayestar and $A_V \sim 300$ from the 2D map.

(ii) The neutral hydrogen column density N_{H} is known to be proportional to visual extinction A_V . Predehl & Schmitt (1995, PS95) find $A_V = N_{\text{H}} / [(1.79 \pm 0.03) \times 10^{21} \text{ cm}^{-2}]$. Many magnetars have an X-ray derived N_{H} estimate, but the uncertainties on this number are typically large, and the $N_{\text{H}}-A_V$ relation itself has some scatter. This method therefore more accurately probes the direct sight-line to the magnetar, but is typically less precise.

For the first method, the uncertainty on the extinction is correlated with the uncertainty on the distance. For example, if a 3D estimate is used, the upper bound on the extinction is the dust map value at $d + \delta d$. The N_{H} inferred A_V values depend on X-ray measurements and we treat them independently from the distance estimate.

In Figure 3 we plot N_{H} versus A_V for each magnetar with a N_{H} measurement. If a 3D dust map or cluster-based extinction is used, that value is plotted. For example, we adopt a value based on observations of the Wd1 cluster for CXOU J1647 (Clark et al. 2014). If an A_V-N_{H} value is adopted, the 2D value for that sight-line is

² <http://www.physics.mcgill.ca/~pulsar/magnetar/main.html>

Table 1. The full magnetar sample considered in this paper (23 objects). Photometry (Vega magnitudes) for the most likely counterpart(s) is listed in each case. Shortened magnetar names, as in the first column without brackets, are used throughout this paper. The criteria for selection are a distance estimate and imaging. 1RXS J1708 has three candidate counterparts in (or just outside) the X-ray error circle (see [Chrimes et al. 2022](#)), the candidates A and B are labelled following [Israel et al. \(2003\)](#) and [Durant & van Kerkwijk \(2006a\)](#). The magnitudes listed here are the primary ones used (i.e. for the colour-magnitude diagram), other values from the literature are also plotted later in [Figure 4](#), following references in the McGill catalogue ([Olausen & Kaspi 2014](#))².

Magnetar	<i>H</i> -band (Vega)	<i>J</i> -band (Vega)	Instrument/survey	Filter(s)	Reference
4U 0142(+61)	20.80±0.01	21.72±0.01	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
SGR 0418(+5729)	>25.12	>26.08	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
SGR 0501(+4516)	22.56 ^{+0.06} _{-0.07}	23.33±0.07	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
1E 1048(.1–5937)	22.15±0.20	>24.08	<i>HST</i> /NICMOS	F160W+F110W	Tam et al. (2008)
1E 1547(.0–5408)	>20.22	>22.45	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
PSR J1622(–4950)	22.39±0.05	23.95±0.08	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
SGR 1627(–41)	20.48±0.01	21.97±0.01	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
CXOU J1647(10.2–455216)†	21.0±0.1	23.5±0.2	VLT/NAO	<i>H, J</i>	Testa et al. (2018)
1RXS J1708(49.0–400910) A	18.77±0.01	20.61±0.01	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
1RXS J1708(49.0–400910) B	20.58±0.01	22.37±0.02	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
1RXS J1708(49.0–400910) C	21.80±0.08	23.71 ^{+0.14} _{-0.16}	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
CXOU J1714(05.7–381031)	17.45±0.01	19.01±0.01	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
SGR 1745(–2900)	>15.97	>18.98	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
SGR 1806(–20)	21.75±0.75	>21.1	Keck/NIRC2, VLT/NAOS	<i>K_p, J</i>	Tendulkar et al. (2012) , Israel et al. (2005)
XTE J1810(–197)†	21.67±0.12	22.92±0.22	Gemini/NIRI	<i>H, J</i>	Testa et al. (2008)
Swift J1822(.3–1606)	19.76±0.01	21.04±0.02	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
Swift J1834(.9–0846)	21.74±0.02	23.21±0.03	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
1E 1841(–045)	20.80±0.4	>22.10	Magellan/Panic	<i>H, J</i>	Durant (2005)
3XMM J1852(46.6+003317)★	18.85±0.01	21.97±0.02	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
SGR 1900(+14)†	21.17±0.50	-	Keck/NIRC2	<i>H</i>	Tendulkar et al. (2012)
SGR 1935(+2154)	~24	-	<i>HST</i> /WFC3	F140W	Levan et al. (2018) , Lyman et al. (2022)
1E 2259(+586)	22.52±0.04	23.61±0.05	<i>HST</i> /WFC3	F160W+F125W	Chrimes et al. (2022)
SGR 0755(–2933)★★	9.52±0.01	9.69±0.01	2MASS	<i>H, J</i>	Doroshenko et al. (2021)
AX J1845(.0–0258)	>21	-	NTT	<i>H</i>	Israel et al. (2004)
SGR 2013(+34)	>18.5	>19.3	PAIRITEL	<i>H, J</i>	Bloom (2005)

★ - Reddest object in large error circle, unlikely to be the counterpart ([Chrimes et al. 2022](#)), ★★ - a possibly unrelated HMXB ([Doroshenko et al. 2021](#))

† - has *HST* imaging in [Chrimes et al. \(2022\)](#), not used due to non-detections or single-band imaging

indicated. The [Predehl & Schmitt \(1995\)](#) relation is also shown. The quoted scatter on the A_V - N_H relation is a significant underestimate, if the differences between the 3D dust map values and N_H derived values are representative. The difference might partly arise due to gas and dust local to the magnetars, not captured by the dust map spatial resolution (variable, but between 3–14 arcmin for Bayestar), explaining the tendency for the 3D dust map values to be lower than the N_H estimates. The standard deviation of the relative differences between the 3D dust map and N_H derived extinctions, i.e. $\Delta A_V/A_V$, is 0.34. This is indicated in [Figure 3](#) by the grey shaded region on the A_V - N_H relation. We plot this region equally either side of the relation, although there is a clear bias towards A_V - N_H values exceeding dust map values.

The total 2D extinctions greatly exceed the N_H estimates as expected, bar one case at low A_V , putting an upper limit on the degree to which local, unresolved dust/gas enhancement is contributing to the higher N_H derived estimates. Since the N_H and 3D map methods agree to within ~30 per cent, this also implies that the distance estimates are reasonable, since the extinction is a function of distance for the 3D map estimates. In each case, we choose the most reliable method as described above, where the 3D map values are correlated with distance and both the quoted scatter and N_H uncertainties are included if [Predehl & Schmitt \(1995\)](#) is used. We note that in both cases, the extinction uncertainties may be underestimated, but that they will be no more than ~30 per cent in any case.

Finally, we convert visual A_V extinctions into $H, J, F160W, F140W, F125W$ and $F110W$ extinctions using the effective wavelengths of these filters and the python `EXTINCTION` module ([Barbary](#)

[2016](#)), assuming $R_V = 3.1$ and a Fitzpatrick extinction curve ([Fitzpatrick 1999](#)). The extinction values using each method, and the adopted values, are listed in [Table 2](#).

5 COMPARISON WITH POPULATION SYNTHESIS PREDICTIONS

We now compare the observed colours and magnitudes of the candidate bound companions to the predictions from [Section 2](#).

5.1 H-band magnitude comparisons

Using the distance estimates in [Table 2](#), the absolute magnitudes of NIR counterpart candidates can be calculated. As a first step in comparing the predictions of [Section 2](#) to observations, we instead correct the *H*-band absolute magnitude distribution for bound companions ([Figure 1](#)) for the distance and extinction of each magnetar. These dust attenuated apparent magnitudes are compared to observations in [Figure 4](#). Dashed vertical lines enclose 95 per cent of the *H*-band magnitude probability. Uncertainties on the correction to the BPASS outputs are indicated by error-bars on the lower (brighter) percentile. In calculating these uncertainties (provided in [Table 2](#)), we assume for dust-map derived extinctions that the distance and extinction uncertainties are correlated, i.e. the upper distance error is used with the upper extinction error to derive the maximum correction within the uncertainties, and vice versa. In every other case we assume that the uncertainties are uncorrelated, taking the average of the upper

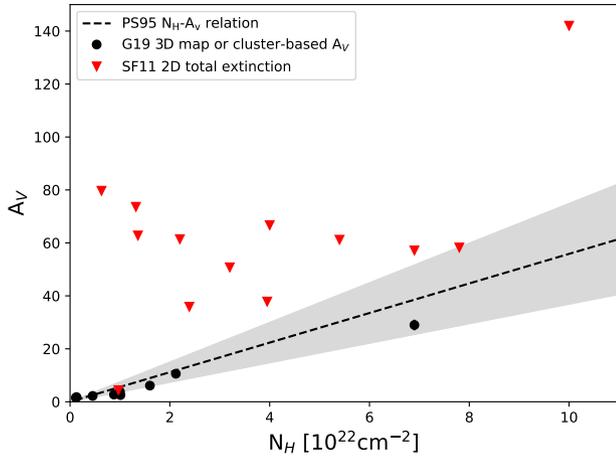


Figure 3. Extinction as a function of N_{H} derived from (i) magnetar distance estimates and the 3D maps of Green et al. (2019, G19), or a cluster association-based extinction estimate if available, (ii) the $N_{\text{H}}-A_{\text{V}}$ relation of Predehl & Schmitt (1995, PS95) and (iii) the total integrated line of sight extinction out of the Galaxy Schlafly & Finkbeiner (2011, SF11). We adopt 3D dust map estimates if they are reliable, if not and no cluster-based estimate is available, then the $N_{\text{H}} - A_{\text{V}}$ relation is used. The shaded region around the $A_{\text{V}}-N_{\text{H}}$ relation corresponds to the typical ~ 0.3 relative difference between 3D dust map and N_{H} derived estimates.

and lower distance and extinction uncertainties if they are asymmetric. The observed magnitudes are either from *HST* measurements (F140W is drawn on this figure as F160W, F110W as F125W) or other observations from the literature (if not *HST* they are assigned to H, J or K , whichever is the closest match) as indicated in Table 1. Although SGR 1806 does not have a H -band detection, if we assume it has a similar intrinsic $H-K = 1$ colour to other counterparts, combined with 2 magnitudes more extinction in H than K ($A_{\text{V}} = 29$), this places it a few magnitudes outside the lower (in terms of luminosity) percentile.

5.2 Colour-magnitude comparisons

While informative, single-band magnitudes are only part of the information available. To add further constraints, we now examine the colours of the counterpart and candidates. For those sources which have observations in H and J and a detection in at least one, we apply the distance and extinction corrections to the *magnetar* photometry and place this on a colour-absolute magnitude diagram in Figure 5. Here we show BPASS predictions for a Solar metallicity stellar population at 10^7 yrs. Ages of a few tens of Myr correspond to the expected lifetimes of supernova progenitors, hence our choice of 10^7 yr, but comparisons with populations at 10^6 yr and 10^8 yr are also provided in Appendix A.

The corrected magnetar measurements are coloured by the method used to derive the extinction. Horizontal dashed lines mark the upper and lower luminosity percentiles enclosing 95 per cent of the distribution, previously adjusted in each case in Figure 4. Vertical dashed lines represent the same for the predicted $J-H$ colour distribution of bound companions. The box enclosed by these 4 lines is therefore where companion stars are predicted. However, we plot the whole stellar population at the given age underneath for two reasons. Firstly, this is in order to be agnostic about the properties of any bound companions, which represent a subset of the wider stellar population. For example, as companions to massive stars, they will

be biased to higher masses since very high mass ratio systems are disfavoured (Moe & Di Stefano 2017). However, by plotting the whole population, we are open to the possibility of companions outside of the predicted range, either because the predictions are inaccurate, or because magnetar progenitor systems are atypical. Secondly, if a source does not fall on the shaded regions (where each shading level represents an order of magnitude difference in the number density of sources), this is indicative of either,

- Genuinely non-stellar colours, assuming the adopted d and A_{V} are at least approximately correct, or,
- A chance alignment, where the source in the localisation error circle is unrelated to the magnetar, and hence the wrong distance and extinction is being applied,

where ‘non-stellar’ is defined as colour-magnitude properties which are inconsistent with stars undergoing nuclear fusion (any phase from the main sequence through to core-collapse or white dwarf formation), or white dwarfs. Examples of non-stellar emission in this context include magnetospheric or debris disc emission. We now discuss the placement of the counterparts in this parameter space after distance and extinction correction, and the implications in each case.

There are three cases where the wrong corrections have likely been applied for the sources in the error circle. These are SGR 1627, PSR J1622 and Swift J1834, which have very large uncertainties due to large and uncertain N_{H} measurements. None the less, they are unphysically blue (the right panel of Fig. 5 is zoomed out to show this). Given the high extinction on these sight-lines, it is likely that these are foreground chance alignments, and therefore the distance and extinction corrections are much too high. This is also seen by the direction of the extinction vector, which traces back to the main sequence - the region of highest probability density - for these sources.

At first glance, the three sources in (or just outside, we have added source B of Israel et al. (2003) and Durant & van Kerkwijk (2006a) to compare) the 1RXS J1708 error circle also look like chance alignments, since they cannot all be counterparts. However, Israel et al. (2003) claim that their source A (the brightest of the three) is non-stellar in $J-H$, $J-K$ colour space. Durant & van Kerkwijk (2006a) showed that source B can only be shifted into the cloud of stellar sources if an A_{V} of ~ 20 is assumed, inconsistent with the column density extinction estimate (and consistent with the main sequence offset shown in Figure 5). It is therefore unclear which is associated with 1RXS J1708, but it is likely that two are anomalously red because they are background chance alignments with an insufficient distance/extinction applied, whereas the other is the magnetar counterpart, with a non-stellar SED. AX J1818.0-1607 is a similar case, for which this was shown to be a plausible scenario by Chrimes et al. (2022). In any case, all of the 1RXS J1708 candidates are outside the bound companion magnitude range.

There are another nine sources below the population synthesis bound companion limit. 4U 0142, 1E 2259 and SGR 0501 are unambiguously the counterpart based on precise localisations and a lack of other sources in the immediate vicinity. 1E 2259 stands out as being unusually red, whereas 4U 0142 does not, despite previous claims of a dusty debris disc. We attribute this to the J and H bands used, which are not as sensitive in this case to the upturn which becomes more significant from the K -band into the mid-infrared (e.g. Muñoz-Darias et al. 2016). The source associated with Swift J1822 is also in this faint, red area of parameter space.

1E 1841, 1E 1048 and SGR 1806 all have J -band non-detections and hence their colours are lower limits. For 1E 1048 this is a constraining limit which places it in the same faint, red region of param-

Table 2. Details for each of the 23 magnetars with a distance estimate and imaging, including distance estimates, and extinctions calculated using the two methods outlined in the text. The majority of this information is as provided in the McGill magnetar catalogue and references therein [Olausen & Kaspi \(2014\)](#)², with some additions and updates. The extinction used for each magnetar is in bold, and listed in the final column with the uncertainty. For dust-map derived extinctions, the upper extinction uncertainty corresponds to the upper distance uncertainty, and vice versa.

Magnetar	Dist. [kpc]	Distance reference	Total A_V SF11 (tot. G19)	A_V at d G19	A_V-N_H PS95	A_V used with uncertainty
4U 0142	3.6±0.4	Durant & van Kerkwijk (2006b)	4.90 (4.93)	3.79	5.59	3.79 ^{+0.40} _{-0.25}
SGR 0418	2±0.3†	Van der Horst et al. (2010)	2.25 (2.17)	1.55	0.64	1.55±0.01
SGR 0501	2±0.3†	Lin et al. (2011)	3.45 (3.62)	2.73	4.92	3.79 ^{+0.15} _{-0.39}
IE 1048	9.0±1.7	Durant & van Kerkwijk (2006b)	3.75	-	5.42	5.42±0.11
1E 1547	4.5±0.5	Tiengo et al. (2010)	43.42	-	17.88	17.88 ^{+1.15} _{-0.41}
PSR J1622	9±1.35†	Levin et al. (2010)	53.22	-	30.17	30.17 ^{+8.91} _{-7.84}
SGR 1627	11±0.3	Corbel et al. (1999)	125.4	-	55.87	55.87 ^{+11.21} _{-11.22}
CXOU J1647	3.9±0.7	Kothes & Dougherty (2007)	30.61	10.66 [1]	13.35	10.66±0.40
1RXS J1708	3.8±0.5	Durant & van Kerkwijk (2006b)	53.84	-	7.60	7.60 ^{+0.25} _{-0.26}
CXOU J1714	13.2±1.98†	Tian & Leahy (2012)	31.36	-	22.07	22.07 ^{+0.91} _{-0.87}
SGR J1745	8.3±0.3	Bower et al. (2014)	301.66 (3.34)	unreliable	75.42	75.42 ^{+3.58} _{-3.53}
SGR 1806	8.7 ^{+1.8} _{-1.5}	Bibby et al. (2008)	45.5 (6.85)	29 [2]	38.55	29±2
XTE J1810	2.5 ^{+0.4} _{-0.3}	Ding et al. (2020)	60.05 (5.43)	unreliable	3.52	3.52±0.29
Swift J1822	1.6±0.3	Scholz et al. (2012)	12.75 (9.73)	2.21	2.53	2.21 ^{+1.18} _{-1.32}
Swift J1834	4.2±0.3	Leahy & Tian (2008)	96.78 (4.55)	unreliable	98.27	98.27 ^{+19.11} _{-20.13}
IE 1841	8.5 ^{+1.3} _{-1.0}	Tian & Leahy (2008)	52.86 (5.61)	unreliable	12.29	12.29 ^{+0.60} _{-0.59}
3XMM J1852‡	7.1±1.07†	Zhou et al. (2014)	65.17 (9.89)	unreliable	7.63	7.63 ^{+0.05} _{-0.07}
SGR 1900	12.5±1.7	Davies et al. (2009)	11.05 (10.94)	10.60	11.84	10.60 ^{+0.07} _{-0.03}
SGR 1935	4.0±2.5	Bailes et al. (2021)	13.13 (8.58)	6.11	8.94	6.11 ^{+0.28} _{-0.31}
IE 2259	3.2±0.2	Kothes & Foster (2012)	3.82 (3.22)	2.54	5.64	2.54 ^{+0.04} _{-0.03}
SGR 0755	3.5±0.2	Doroshenko et al. (2021)	2.6 (2.39)	1.77	0.73	1.77 ^{+0.09} _{-0.05}
AX J1845	8.5±1.28	Torii et al. (1998)	50.35 (5.58)	unreliable	43.58	43.58 ^{+12.87} _{-10.09}
SGR 2013	8.5±1.32	Sakamoto et al. (2011)	5.64 (6.20)	5.36	6.13	5.36 ^{+0.56} _{-1.24}

† - distance uncertainty unquantified, 15 per cent assumed, ‡ - Reddest source in error circle

[1, 2] - extinctions from cluster associations ([Clark et al. 2014](#); [Eikenberry et al. 2004](#)).

eter space as the other counterparts. 1E 1841 has H and K imaging presented by [Testa et al. \(2008\)](#) and the likely counterpart is identified as their source 9, due to 4σ K -band variability. We therefore adopt the H and J -band measurements of the same object in [Durant \(2005\)](#), labelled there as source B. The shallow J -band limit means that the $J-H$ colour is relatively poorly constrained. The source placement is outside of the predicted companion magnitude range and marginally consistent with the predicted colours. For SGR 1806, which has a K -band detection ([Tendulkar et al. 2012](#)) and limits in H and J ([Israel et al. 2005](#)), we first assume a $H-K$ colour of one. This is typical of the intrinsic colours of known counterparts (see e.g. the least extinguished examples in Figure 4) and is consistent with the $H > 19.5$ limit. Correcting for the distance and extinction then places it at $M_H \sim 5$. Given the $J > 21.1$ limit, the high extinction ($A_V = 29$) yields an unconstraining $J-H > -3.6$ colour limit.

Although there is HST imaging for CXOU 1647, this is only in one band (F140W, [Chrimes et al. \(2022\)](#)), so we adopt the $J = 23.5 \pm 0.2$ and $H = 21.0 \pm 0.1$ measurements of ([Testa et al. 2018](#)) instead. The last of the eight sources with colour information to lie below the population synthesis prediction for bound companion H -band magnitudes is XTE J1810. The counterpart is not detected in 2018 HST F160W and F125W imaging ([Chrimes et al. 2022](#)), so we use measurements from [Testa et al. \(2008\)](#) instead. Because the source is variable, we chose just the first epoch (MJD 52900) of observations presented ($H = 21.67 \pm 0.12$, $J = 22.92 \pm 0.22$).

Finally, there are two sources which are notably different from the cloud of objects in the lower right of Figure 4. Not only do they lie in the magnitude range predicted for companions, but they also have stellar colours. These are SGR 0755 and CXOU J1714. The star

associated with SGR 0755, as previously discussed, is too bright to measure from the HST images, so 2MASS ([Skrutskie et al. 2006](#)) magnitudes are adopted. This system, 2SXPS J075542.5–293353, is an HMXB ([Doroshenko et al. 2021](#)). However, it remains an open question whether the accretor could be a magnetar ([Popov 2022](#)), or whether the magnetar burst came from a different source in the BAT error circle. The counterpart candidate for CXOU J1714 is unambiguous, well localised, and has stellar colours, albeit slightly bluer than predicted for neutron star companions. The source also stands apart from previously established counterparts in terms of its X-ray to NIR power law index ([Chrimes et al. 2022](#)). Unless the distance and extinction are drastically overestimated for this magnetar, the source is clearly distinct from previously confirmed non-stellar counterparts.

6 SUMMARY OF RESULTS

Out of the 23 sources considered in this sample, 3 are unconstrained in terms of their H -band magnitude - AX J1845 only has a limit that does not preclude a bound companion, SGR 1745 also has an unconstraining limit, and we deem 3XMM J1852 as unconstrained given the poor localisation. The overall results, including colour information where available, are summarised in Table 3. Here we list whether the observations for each source can rule out or allow for the possibility of a bound companion. Of the 20 that have a magnitude constraint, 2 are plausibly bound companions based on their absolute magnitude and colour. These are SGR 0755 and CXOU J1714. CXOU J1714 is slightly outside the colour predictions but is other-

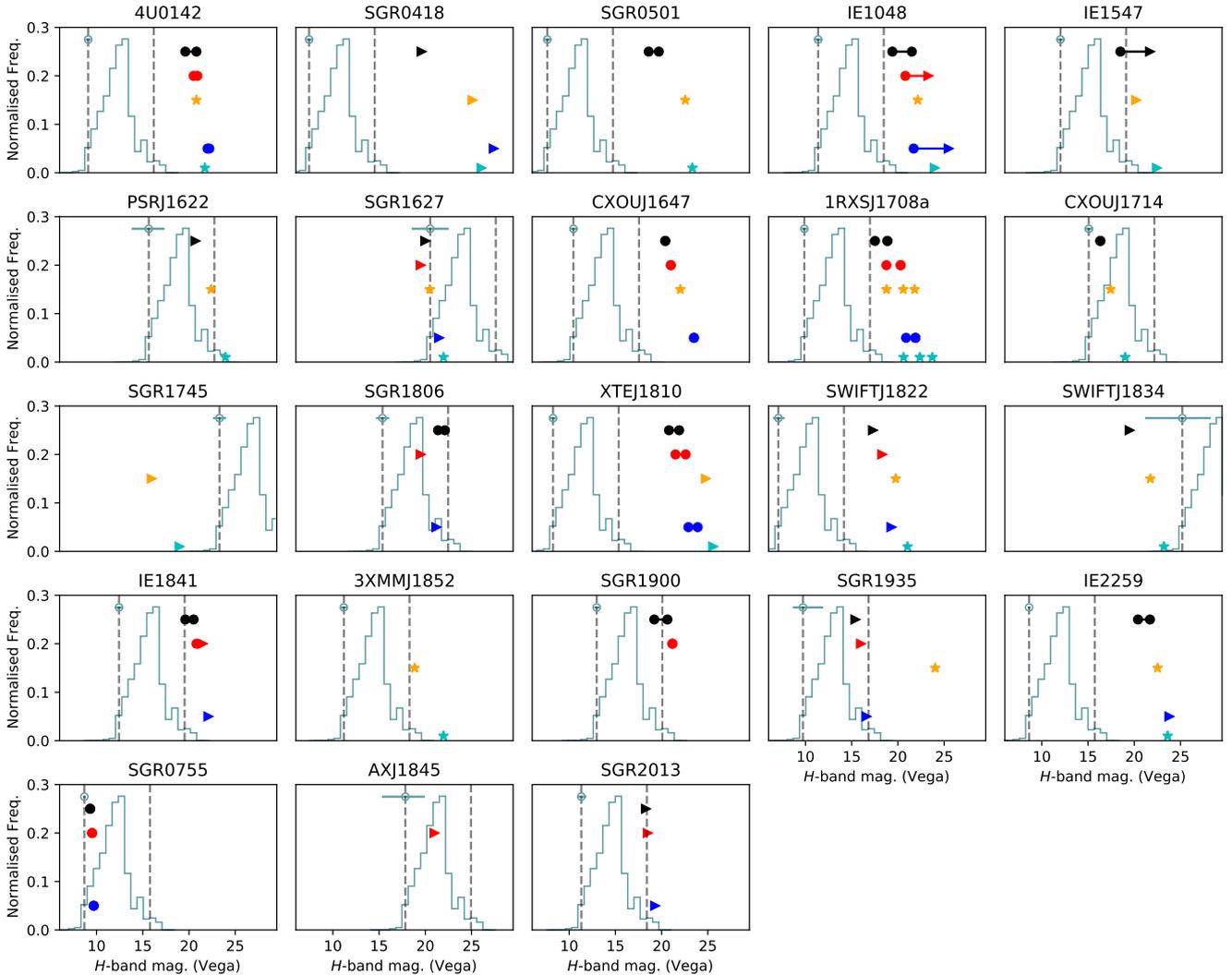


Figure 4. Photometry for the 23 magnetars with a distance estimate, compared to BPASS predictions for the apparent magnitudes of bound companions (histogram), assuming the distance and extinction estimates in Table 2. The 2.5 and 97.5 percentiles (enclosing 95 per cent of the distribution) are indicated by vertical lines, the lower percentile has an errorbar indicating the uncertainty on the distribution due to distance and A_V uncertainties. Previously reported apparent magnitudes (uncorrected) are indicated by the black points (K -band, arbitrarily placed at $y = 0.25$), red (H -band, 0.2) and blue (J -band, 0.05). If the source is variable and a range of values have been reported, the brightest and faintest magnitudes previously reported are joined by a line. If two separate sources have previously been measured as candidates, they are plotted separately. Triangles represent upper limits. The *HST* F160W (F125W) photometry listed in Table 2 is plotted in orange (cyan) at $y = 0.15$ ($y = 0.01$).

wise well within the magnitude range expected. SGR 0755 satisfies both criteria. IE 1841 is not far ($\sim 2\sigma$) outside the lower magnitude bound, but the colour limit also precludes most of the $J-H$ distribution, so we deem it inconsistent with predictions.

Of the two candidates, which appear distinctly bright and blue in this parameter space, SGR 0755 is an X-ray binary, and it is possible that the magnetar is actually elsewhere in the BAT error circle (Doroshenko et al. 2021). CXOU J1714 is perhaps the most promising bound companion candidate. We can therefore constrain the fraction of magnetars with a bound companion to 0.05–0.10 (1–2 out of 20). This range is quoted at 95 per cent confidence since both the localisation uncertainties and bound companion magnitude predictions are at 95 per cent. This bound companion fraction is consistent with population synthesis predictions for a regular core-collapse origin, as discussed in Section 2. If there is a contribution amongst this population from non-core-collapse channels, it cannot be very large

before the bound companion fraction among the remainder disagrees with predictions. For instance, if 5/20 do not have a core-collapse origin, the bound fraction amongst the rest would be 7–13 per cent, which would imply a bias towards magnetar production in primary stars, assuming that $f_{\text{bound}} = 0.05$ is accurate for the wider neutron star population.

7 DISCUSSION

7.1 Bound companion candidates

7.1.1 SGR0755

A system of particular interest here is 2SXPS J075542.5–293353, a HMXB which may (or may not) be harbouring SGR 0755 (Doroshenko et al. 2021). If this is a magnetar accreting from a

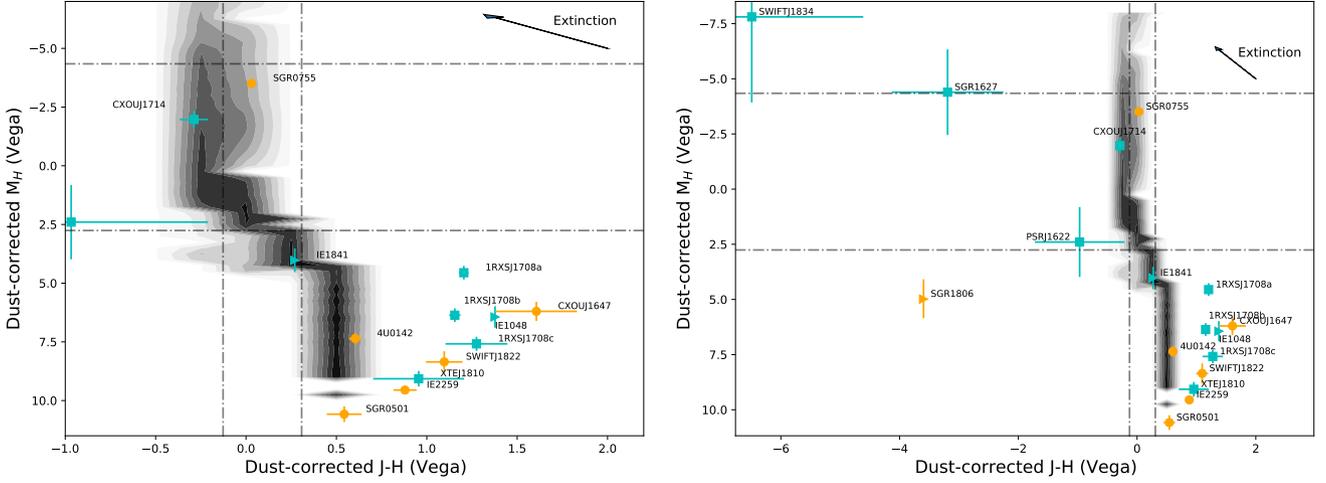


Figure 5. A NIR colour magnitude diagram for a Solar metallicity stellar population at 10 Myr. The right hand panel zooms out to show SGR 1806, PSR J1622, SGR 1627 and Swift J1834 (whose extinctions are large and uncertain). Extinctions derived from 3D dust map/cluster extinctions, or the A_V - N_H relation, are labelled with orange circles or cyan squares respectively. Immediately post primary supernova, 95 per cent of all bound companion H -band magnitudes lie in the region bounded by the horizontal dot-dashed lines, and 95 per cent of their $J-H$ colours lie between the vertical dashed lines. The reddening vector is indicated in the upper right - for a fixed apparent magnitude and observed colour, the inferred absolute magnitude and intrinsic colour move in this direction with increasing extinction. Objects that lie away from the shaded regions either have intrinsically non-stellar colours, or the incorrect distance and extinction applied (i.e., they are chance alignments). The underlying density contours (an order of magnitude in number density per level) were plotted with the python package for BPASS, HOKI (Stevance et al. 2020).

high mass companion, it would be the first such system identified (some works claim that such systems are highly unlikely to form, since accretion would dampen the magnetic field, or at least that accretion does not power magnetar emission e.g. King & Lasota 2019; Doroshenko et al. 2020). While it may be a chance coincidence that this HMXB lies in the BAT error circle derived from the SGR 0755 discovery burst, it could also be that the burst came from this system even if does not contain a magnetar (there are several X-ray pulsars known in HMXBs e.g. Salganik et al. 2021). There are also models which predict magnetar survival (i.e. avoiding rapid magnetic field decay) in certain accreting systems (Igoshev & Popov 2018; Bozzo et al. 2022). For example, the orbital and spin periods measured for 2SXPS J075542.5–293353 agree with the magnetar X-ray binary model predictions of Xu et al. (2021). Unfortunately, we cannot compare the age of the magnetar in this system with an estimate age of the star, because the P/\dot{P} age becomes unreliable in an accreting system. Furthermore, the lack of an independent magnetar distance estimate precludes a comparison with the *Gaia* distance of 3.5 ± 0.2 kpc (EDR3, *Gaia* Collaboration et al. 2016, 2021).

7.1.2 CXOUJ1714

The other magnetar with a coincident NIR source consistent with being a massive stellar companion is CXOU J1714. It has an inferred absolute magnitude consistent with BPASS predictions for a bound companion, and although bluer than the predicted colours, it is still consistent with being stellar in nature. This source is much fainter than the donor in 2SXPS J075542.5–293353, and has not yet been unambiguously identified as stellar in nature. In principle, there might be an orbital period signature in the X-ray lightcurve of the magnetar, if the emission is somehow coupled to interactions with the companion. Figure 1 shows the BPASS prediction for the orbital periods of bound neutron star-massive companion systems. X-ray observations of CXOU J1714 are somewhat sparse, with 11 epochs since its identification as a magnetar in 2010 (Sato et al. 2010). There

are also a handful of preceding epochs, where the target was the surrounding supernova remnant CTB 37B (Gotthelf et al. 2019). The 3.8s period of the magnetar is clear, and there is clear evidence for variability over timescales of \sim years within these data (Sato et al. 2010). However, whether there is day-week timescale periodicity in this long term variation, as predicted in a bound system, remains to be seen.

We also search for catalogues containing the NIR source associated with CXOU J1714. A *Gaia* star lies 2.7 arcsec away from the centre of the *CXO* localisation of CXOU J1714, and appears in the *Gaia* - neutron star association catalogue of Antoniadis (2021). No proper motion or parallax is available for this source, due to its faint 20.9 G -band magnitude. Given the good *CXO* localisation of the magnetar (ruling the star out as a bound companion), and given the extinction of $A_V \sim 22$ along the magnetar sight-line, it would have an unphysically luminous absolute G -band magnitude of ~ -10 if placed at the same distance and extinction as the magnetar (i.e., as a companion).

The only optical/NIR catalogue in which the NIR source at the position of CXOU J1714 is detected, is the VVV Infrared Astrometric Catalogue (Smith et al. 2018). It has VVV magnitudes of $H = 17.3 \pm 0.1$ and $J = 19.1 \pm 0.3$, agreeing well with our measurements (see Table 2), given the bandpass differences. The source has a VVV proper motion measurement of 6.3 ± 3.1 mas yr $^{-1}$. Following Verbunt et al. (2017) and using the same model parameters as Lyman et al. (2022), we correct for the relative motion due to Galactic rotation and the peculiar velocity of the Sun. The IAU standard of 220 kms $^{-1}$ is assumed for the Galactic rotation at both the Solar location and the source (reasonable given that all locations considered are outside the central few kpc of the Galaxy, Clemens 1985). The resultant transverse velocity in the local standard of rest (LSR) of the source is 349 ± 151 kms $^{-1}$, where the 1σ uncertainty is derived from 10^5 Monte Carlo trials with Gaussian uncertainties on U , V and W (the Solar peculiar motion components), μ_α and μ_δ (the observed proper motion components) and distance d . This is a high value which is more typical of the Galactic pulsar population, but the lower limit is

Table 3. A summary of the results. Whether each source is plausibly a bound companion based on the H -band or location on the colour-magnitude diagram (CMD), is indicated. The tolerance for being consistent in Figure 4 is extended beyond the plotted percentiles according to the indicated uncertainty on the distance and extinction corrections. 3/23 are unconstrained. Of the remaining 20, two have apparently stellar properties broadly consistent with expectations for bound companions (CXOU J1714 and SGR 0755, for which the bright star is a confirmed HMXB, but may but a chance alignment with the magnetar in question).

Magnetar	Plausible from H mag?	Plausible from CMD?	Classification
4U 0142	N	N	Non-stellar
SGR 0418	N	-	Non-stellar
SGR 0501	N	N	Non-stellar
1E 1547	N	-	Non-stellar
IE 1048	N	N	Non-stellar
PSR J1622	Y	N	Non-stellar**
SGR 1627	Y	N	Non-stellar**
CXOU J1647	N	N	Non-stellar
IRXS J1708	N	N	Non-stellar
CXOU J1714	Y	Y	Possibly stellar
SGR J1745	Unconstrained	-	Unconstrained
SGR 1806	N*	N	Non-stellar
XTE J1810	N	N	Non-stellar
Swift J1822	N	N	Non-stellar
Swift J1834	N	N	Non-stellar**
IE 1841	N	N	Non-stellar
3XMM J1852	Unconstrained	-	Unconstrained
SGR 1900	N	-	Non-stellar
SGR 1935	N	-	Non-stellar
IE 2259	N	N	Non-stellar
SGR 0755	Y	Y	Stellar
AX J1845	Unconstrained	-	Unconstrained
SGR 2013	N	-	Non-stellar

★ - Assuming an intrinsic $H-K = 1$

★★ - extremely blue unattenuated colours, high likelihood of chance alignment

consistent with the upper end of compact remnant-massive star bound systems, specifically high-mass X-ray binaries (Mirabel et al. 2002; Atri et al. 2019; Igoshev et al. 2021). If we instead adopt a distance of 5 kpc - the lowest distance estimated for CXOU J1714 before it was revised upwards by association with the CTB 37 supernova remnant complex (Tian & Leahy 2012) - the transverse velocity estimate drops to $140 \pm 67 \text{ km s}^{-1}$, entirely consistent with bound systems. If we change the distance, the inferred absolute magnitude is only affected by a change in distance modulus because the extinction is derived from the column density. Consequently, at 5 kpc, the source is 2.1 magnitudes fainter, which still places it firmly in the stellar region of parameter space in Figure 5. Although a lower distance is preferred given the VVV proper motion measurement of the NIR source and the typical systemic velocities of X-ray binaries, the large uncertainties mean a reasonable velocity cannot be ruled out even at $d = 13.2 \text{ kpc}$.

7.2 Pre-main sequence stars

Another possibility, if the companion is significantly less massive than the magnetar progenitor, is that it may still be in a pre-main sequence (PMS) period of evolution. The NIR variability of PMS stars is well-established (e.g. Carpenter et al. 2001; Eiroa et al. 2002; Alves de Oliveira & Casali 2008), and several magnetar counterparts

are variable. The variations in PMS stars are thought to be due to changes in the disc accretion rate, structure, and clumpy circumstellar dust distributions. Although the time-scales of PMS evolution of low-mass stars are indeed comparable to the entire life-times of massive O stars (tens of Myr; Palla & Stahler 1993) – with the magnetar’s life-time adding an insignificant amount of time – this scenario would invoke the need for a somewhat extreme mass ratio binary. This scenario is disfavoured due to the initial binary parameter distributions (Sana et al. 2012), and the preference for these systems to unbind upon primary supernova. However, we know such systems can occur, due to the existence of low-mass X-ray binaries, so the pre-main sequence scenario cannot be ruled out.

7.3 Comparison with pulsars

In addition to the population synthesis predictions of Section 2, we can also compare our results to the pulsar population. Seven per cent of pulsars in the ANTF catalogue are listed as having a main sequence companion (Manchester et al. 2005)³. However, this number is highly uncertain due to detection and follow-up biases - some may be obscured by dust, while others have not had deep observations to establish the presence of a companion, or lack thereof. Antoniadis (2021) performed a cross-match between the *Gaia* DR3 catalogue and 1534 pulsars. They find that the binary fraction of young pulsars (defined as being un-recycled and with magnetic field strength $> 10^{10} \text{ G}$) is < 5 per cent, under the assumption that all pulsar stellar companions with orbital periods of $< 50 \text{ yr}$ and brighter than 20.5 mag should have been identified. However, some systems with bound companions will manifest as X-ray binaries. We note that the ages of HMXBs, typically tens of Myrs, (inferred from kinematics and cluster associations, e.g. Coleiro & Chaty 2013) are more typical of (young) pulsars (Manchester et al. 2005) than magnetars (Olausen & Kaspi 2014). This might suggest that more pulsar bound companions will be ‘missing’ (because these systems are instead identified as XRBs) than magnetar bound companions. The lifetimes of bound companions also suggest that they will leave the main sequence on a similar time-scale to the ages of HMXBs, consistent with this scenario. Overall, the population synthesis, pulsar and magnetar estimates for f_{bound} are all broadly consistent with ~ 5 per cent.

7.4 Other constraints and future progress

The origin of magnetars has been probed in a variety of ways, from investigating their colours/spectral energy distributions (SEDs) as in this work, their proper motions, and associations with recent star formation/supernovae. The results presented here do not require non-core-collapse channels to explain the Galactic population, and this is backed up by previous studies which point towards core-collapse as the dominant channel (e.g. Beniamini et al. 2019; Burns et al. 2021). However, some contribution from other channels cannot be excluded. For example, accretion or merger induced collapse magnetars are predicted on theoretical grounds (Duncan & Thompson 1992; Levan et al. 2006; Margalit et al. 2019; Gautam et al. 2021; Ablimit 2021), and are a possible explanation for FRB202001E, which resides in a globular cluster (Kirsten et al. 2021; Lu et al. 2021). If the majority of magnetars are born in core-collapse events, it is still uncertain whether this is a typical outcome, or if it requires specific pre-collapse conditions (this is largely dependent on how rapidly their magnetic fields decay, Nakano et al. 2015; Beniamini et al. 2019).

³ <https://www.atnf.csiro.au/research/pulsar/psrcat/>

Another avenue to compare magnetars with other neutron stars is their proper motions. Thus far a handful have measured proper motions, (Tendulkar et al. 2012; Deller et al. 2012; Tendulkar et al. 2013; Ding et al. 2020). Lyman et al. (2022) also add the proper motion of SGR 1935 to this distribution, making use of the stability and spatial resolution of *HST*. The sample remains small, but they show that there is currently no statistically significant difference between magnetar and pulsar proper motions.

Potential further tests include searching for unbound (runaway) companions. A runaway companion to magnetar CXOU J1647 in the young star cluster Westerlund-1 has been claimed (Wd1-5, a blue supergiant, Clark et al. 2014). Due to the carbon rich composition and over-luminous nature of Wd1-5, they infer an evolutionary history in which the (initially slightly less massive) secondary evolves more rapidly following accretion, polluting the primary with carbon rich Wolf-Rayet winds, before going supernova and unbinding the system. Wd1-5 has $H \sim 8.5$, at the upper end of the population synthesis predictions for bound companions (Fig. 4). We predict that 90 per cent of primary neutron stars should have unbound from their companion following the supernova (47 per cent of core-collapse neutron stars overall, including single stars and mergers). The unbound companions will have a range of velocities, and some will be runaways with velocities of hundreds of kms^{-1} . These numbers are less prone to low number statistics and may provide a more robust constraint on magnetar progenitors, but the large number of possible matches means that finding magnetar-secondary pairs is not trivial. Wd1-5 was selected due to its high radial velocity from spectroscopy, but tracing back proper motions may still be a promising route to identifying associations (e.g. Fraser & Boubert 2019). We leave searches for unbound runaway companions, which requires significant additional analyses beyond the scope of this paper, for further studies. However, we qualitatively note that the bound companion search presented here also rules out a fraction of this parameter space, namely unbound companions with small natal kicks.

Another constraint is the masses of the progenitors. For magnetars in a stellar cluster, these can be inferred by ageing the cluster with the red supergiant luminosity distribution. Assuming (i) that the magnetar age is (much) less than the progenitor evolutionary time, and (ii) that the cluster is coeval, the age of the cluster corresponds to a progenitor mass range (e.g. Davies et al. 2009). Progenitor mass estimates range from $> 40 M_{\odot}$ (CXOU J1647, SGR1806 Muno et al. 2006; Bibby et al. 2008) down to $\sim 15\text{--}20 M_{\odot}$ (SGR1900, 1E1841 Davies et al. 2009; Borkowski & Reynolds 2017). Supernova remnant associations can also be used to estimate the progenitor mass, based on modelling of the remnant itself. For example, Zhou et al. (2019) use spatially resolved X-ray observations of supernova remnants to infer progenitor masses of less than $20 M_{\odot}$ for magnetars 1E 1841, SGR 0526–66 and 1E 161348–5055. If these progenitor mass distributions can be expanded, comparisons can be made to the overall massive star IMF and pre-SN masses, to see if magnetars represent a biased subset.

In this work, we have assumed Solar metallicity for the progenitors. If they are biased to lower metallicities, this could be reflected in the progenitor masses and delay times distributions. Quantifying the metallicity of the parent stellar populations is plausible aim, particularly for sources which have cluster associations, e.g. CXOU 1647 in Westerlund 1 (approximately Solar, Crowther et al. 2006).

Finally, spectra or SEDs of magnetar counterparts can conclusively determine their nature. They can distinguish stellar from non-stellar, particularly if the SED extends into the *K*-band and beyond, where dusty debris discs start to dominate the spectra (Wang et al. 2006). The nature of any stellar companion can also be distinguished. The

colours of O-stars and lower-mass pre-main sequence stars differ considerably in the NIR, and also differ from non-thermal/disc models. Characterisation of the NIR SED, as well as a better understanding of the time-scales and amplitude of variability in these sources, would therefore be able to better determine if the emission can be explained by a companion. In principle, neutron star-mass companions could be inferred from radial velocity measurements of bound stellar candidates, but this becomes increasingly difficult at higher mass ratios. Given the locations of magnetars in the Galactic plane, and the associated dusty sight-lines, magnetar spectroscopy and even SED construction is also challenging, but the possibilities will broaden with the advent of *JWST* (*James Webb Space Telescope*, Gardner et al. 2006).

8 CONCLUSIONS

In this paper, we have employed photometry of candidate magnetar counterparts to identify any bound companion stars among the Galactic population. Distance and extinction estimates are used to infer intrinsic colours and absolute magnitudes, which are compared to predictions from binary population synthesis. We find that 5–10 per cent of the Galactic population could plausibly have a bound companion, corresponding to one or two NIR counterparts which appear stellar in nature. One of these is associated with SGR 0755–2933 and has been identified as a high mass X-ray binary, but it remains unclear whether the accretor in this system is the magnetar, or if this is a chance alignment. The other is the counterpart to CXOU J171405.7–381031. These numbers are consistent with binary population synthesis predictions, assuming that the dominant magnetar formation channel is through core-collapse. Further observations are needed to determine if magnetars arise ubiquitously from core-collapse events or a biased subset of this population, and to what extent alternative progenitor channels contribute.

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⁴ <https://www.astropy.org>

and photometry of astronomical sources (Bradley et al. 2021). This research has made use of the SVO Filter Profile Service (<http://svo2.cab.inta-csic.es/theory/fps/>) supported from the Spanish MINECO through grant AYA2017-84089 (Rodrigo et al. 2012; Rodrigo & Solano 2020).

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DATA AVAILABILITY

Based on observations made with the NASA/ESA Hubble Space Telescope, obtained from the data archive at the Space Telescope Science Institute. STScI is operated by the Association of Universities for Research in Astronomy, Inc. under NASA contract NAS 5–26555. These observations are associated with programs 14805, 15348 and 16019 (Levan). The scientific results reported in this article are based on data obtained from the Chandra Data Archive.

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APPENDIX A: COLOUR-MAGNITUDE DIAGRAMS AT OTHER AGES

In this appendix, we show colour-magnitude diagrams at two other ages, 10^6 yr and 10^8 yr, covering the majority of the age range where core-collapse supernovae are expected (Figure A1). Along with Figure 5, we therefore show the range of stellar population colours and magnitudes at the expected age of bound companions to recently born core-collapse neutron stars, agnostic to any prior assumptions about the expected properties of bound companions.

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