Super Dual Auroral Radar Network Expansion and its Influence on the Derived Ionospheric Convection Pattern

M.-T. Walach¹, A. Grocott¹, F. Staples^{2,3}, E. G. Thomas⁴

5	¹ Lancaster University, Lancaster, LA1 4YW, UK
6	² formerly at Mullard Space Science Laboratory, University College London, Holmbury St. Mary, RH5
7	6NT, UK
8	³ Department of Earth, Planetary, and Space Sciences, University of California, Los Angeles, CA, USA
9	⁴ Thayer School of Engineering, Dartmouth College, Hanover, NH 03755, USA

10

1

2

3

4

Key Points:

11	- We identify changes in derived convection maps when PolarDARN and StormDARN $$
12	are added, and show the impact of different processing
13	• Derived convection parameters are highly susceptible to processing variables and
14	which radars are included
15	• We show how the number of backscatter echoes per map is critical to the integrity
16	of the maps, and discuss how this impacts map quality

Corresponding author: M.-T. Walach, m.walach@lancaster.ac.uk

17 Abstract

The Super Dual Auroral Radar Network (SuperDARN) was built to study ionospheric 18 convection and has in recent years been expanded geographically. Alongside software de-19 velopments, this has resulted in many different versions of the convection maps dataset 20 being available. Using data from 2012 to 2018, we produce five different versions of the 21 widely used convection maps, using limited backscatter ranges, background models and 22 the exclusion/inclusion of data from specific radar groups such as the StormDARN radars. 23 This enables us to simulate how much information was missing from older SuperDARN 24 research. We study changes in the Heppner-Maynard boundary (HMB), the cross po-25 lar cap potential (CPCP), the number of backscatter echoes (n) and the χ^2/n statistic 26 which is a measure of the global agreement between the measured and fitted velocities. 27 We find that the CPCP is reduced when the PolarDARN radars are introduced, but then 28 increases again when the StormDARN radars are added. When the background model 29 is changed from the RG96 model, to the most recent TS18 model, the CPCP tends to 30 decrease for lower values, but tends to increase for higher values. When comparing to 31 geomagnetic indices, we find that there is on average a linear relationship between the 32 HMB and the geomagnetic indices, as well as n, which breaks when the HMB is located 33 at latitudes below $\sim 50^{\circ}$ due to the low observational density. Whilst n is important in 34 constraining the maps (maps with n > 400 data points are unlikely to differ), it is in-35 sufficient as the sole measure of quality. 36

37

Plain Language Summary

The ionosphere, where space begins and the atmosphere ends, moves as a result 38 of the Earth's magnetic field coupling with the Sun. The Super Dual Auroral Radar Net-39 work (SuperDARN) was built around the Earth's magnetic poles to study this phenomenon, 40 known as ionospheric convection. Combining many line-of-sight convection measurements, 41 we are able to build global maps of ionospheric convection from SuperDARN data. This 42 encapsulates dynamics which are central to space weather phenomena. SuperDARN, which 43 has been gathering data for decades, has over time undergone numerous transformations, 44 including the development of new processing software and more radars being added to 45 the network. Using data from the years 2012 to 2018, we perform a statistical analysis 46 on processed SuperDARN convection maps for the entire dataset and assess systemat-47 ically how the dataset has changed over the years. We consider how the addition of more 48

⁴⁹ data and differences to the convection mapping procedures can affect scientific studies

⁵⁰ in the context of this large database.

51 **1** Introduction

The Super Dual Auroral Radar Network (SuperDARN) consists of high-frequency 52 coherent scatter radars built to study ionospheric convection by means of Doppler-shifted, 53 pulse sequences and has been widely used in space physics and ionospheric research (e.g. 54 Greenwald et al., 1995; Ruohoniemi & Greenwald, 1996; Chisham et al., 2007; Nishitani 55 et al., 2019). SuperDARN data are continuously available from 1993, with the network 56 having expanded over time from one radar (built in 1983) to 23 radars in the Northern 57 hemisphere, 13 in the Southern hemisphere and more under construction (Nishitani et 58 al., 2019). This expansion has allowed for a greater area to be covered by SuperDARN 59 (i.e. down to magnetic latitudes of 40°) with at least 16 different look directions along 60 which each radar can sample different ranges (Nishitani et al., 2019) in the Northern hemi-61 sphere. Line-of-sight measurements by this large-scale network of radars can be combined 62 and used to construct a picture of high-latitude ionospheric convection on time scales 63 of 1-2 minutes (Ruohoniemi & Baker, 1998). The radars can be grouped into high-latitude 64 radars (the original network), polar-latitude radars (or PolarDARN), and mid-latitude 65 radars (or StormDARN). Nishitani et al. (2019) provides a summary from a historical 66 northern hemisphere perspective: high-latitude radars, at magnetic latitudes of $50-70^{\circ}$ 67 were first built, starting in 1983 with the Goose Bay radar, followed by the PolarDARN 68 radars (covering 70-90° magnetic latitude), and the expansion to mid-latitudes (\sim 40-50°), 69 starting in 2005 with the Wallops Island radar. Over time new radars have improved global 70 ionospheric convection mapping by increasing the number of measurements and look di-71 rections. 72

The most commonly used SuperDARN data product by the space science and iono-73 spheric research community is the convection maps. Convection maps are large scale maps, 74 showing ionospheric convection around the magnetic poles. In order to produce these 75 maps, several data processing steps have to be undertaken. Data from different radars 76 are combined, which allows for the exclusion of data from particular radars or the spec-77 ification of a range limit for the scatter. For example, slow moving E-region scatter can 78 and should be removed by setting the minimum range gate limit to 800 km (Forsythe 79 & Makarevich, 2017; Thomas & Shepherd, 2018). It has become apparent that far range 80

-3-

data beyond 2000 km may also be problematic owing to geolocation uncertainties in the 81 range finding algorithm (Chisham et al., 2008). Once the data has been chosen and com-82 bined, a fitting algorithm is applied which fits an electrostatic potential in terms of spher-83 ical harmonic functions to the data (Ruohoniemi & Greenwald, 1996; Ruohoniemi & Baker, 84 1998). To find the optimal solution for the spherical harmonic coefficients, a singular value 85 decomposition (e.g. Press, W. H. and Teukolsky, S. A. and Vetterling W. T. and Flan-86 nery B. P., 2007) is minimised. When this fitting is performed, typically a background 87 statistical convection model (hereafter referred to as just the background model), param-88 eterised by a mix of IMF conditions and solar wind velocity depending on the model used, 89 to infill information in the case of data gaps. This method is also known as the 'Map Po-90 tential' technique. With the expansion of the radar network, as well as data processing 91 software improvements, the resulting data product has undergone several changes. 92

Several models are available for the 'Map Potential' method, most notably Ruohoniemi 93 and Greenwald (1996) generated the most widely used background model, which was sub-94 sequently implemented in the RST, the Radar Software Toolkit (e.g. SuperDARN Data 95 Analysis Working Group, Thomas, Ponomarenko, Billett, et al., 2018). This background 96 model was thus used by most SuperDARN users when generating convection maps and 97 used in many scientific studies. Ruohoniemi and Greenwald (1996) used data from the 98 Goose Bay radar to derive the background statistical model. Since then however, many 99 more radars have been added to SuperDARN. This raises the question of how much of 100 an effect changing the background model has on the convection map dataset, which was 101 investigated by Shepherd and Ruohoniemi (2000). The main conclusion from Shepherd 102 and Ruohoniemi (2000) was that the solution becomes insensitive to the choice of sta-103 tistical model when the data coverage is high. Since then, Ruohoniemi and Greenwald 104 (2005) produced an updated version of their background model using data from 9 radars, 105 but this was not implemented into RST, thus keeping the RG96-model the default which 106 was used by the community. Since then, a number of updated background models, such 107 as Pettigrew et al. (2010), Cousins and Shepherd (2010) and Thomas and Shepherd (2018) 108 have been produced. The Pettigrew et al. (2010) and Cousins and Shepherd (2010) mod-109 els were not implemented into RST until version 4.1 (SuperDARN Data Analysis Work-110 ing Group, Thomas, Ponomarenko, Bland, et al., 2018). Soon after, the background model 111 by Thomas and Shepherd (2018) was released, which is now standard in RST since ver-112 sion 4.2 (SuperDARN Data Analysis Working Group, Thomas, Ponomarenko, Billett, 113

-4-

et al., 2018). The RG96 and TS18 models are thus the most widely used and we will fo-

¹¹⁵ cus our analysis on these background models.

- In this paper we conduct a large scale data analysis to assess systematically how the SuperDARN convection map dataset has changed over the years and how this may have affected the derived convection maps.
- ¹¹⁹ We specifically probe the effects of the following changes:
- 120 1. Inclusion of the backscatter range limits
- 121 2. Addition of the PolarDARN data
- 3. Addition of the StormDARN data
- 4. Updating of the background statistical model

Comparing different versions of input dataset allows for a large-scale analysis of systematic changes and in particular, how the introduction of new StormDARN and PolarDARN data modifies the convection maps on a large scale, which has implications for use of the maps in scientific studies.

In particular, we discuss measures of map quality in the context of these changes, as well as the placement of the Heppner-Maynard boundary (the lower latitude convective boundary which is used to constrain the maps).

131

2 Data and Method

To provide a meaningful large scale comparison of different versions of the Super-DARN dataset, we process Northern hemisphere data to create different versions of the SuperDARN convection maps for the same time period (2012-2018).

To make SuperDARN convection maps we process the raw data using the Radar
 Software Toolkit (RST (SuperDARN Data Analysis Working Group, Thomas, Ponomarenko,
 Bland, et al., 2018)), which can be broken down into 5 steps:

- Fitacf files, which include the line-of-sight velocity data, are produced from the raw radar data by applying version 2.5 of the FITACF function (SuperDARN Data Analysis Working Group et al., 2019).
- 2. The data from one hemisphere (in our case, the Northern hemisphere) are then
 gridded onto an equal area latitude-longitude grid (see equation 1 from Ruohoniemi

¹⁴³ & Baker, 1998) and split into typically one or two minute cadence records. The ¹⁴⁴ grid we use for this analysis is in the AACGM coordinate system (version 2 by Shep-¹⁴⁵ herd, 2014). Historically it has almost always been the case that all ionospheric ¹⁴⁶ data measured by the radars were added to the grids. As discussed below, we ex-¹⁴⁷ plore changing the range limit by setting the minimum range gate limit to 800 km ¹⁴⁸ and the far range data limit to 2000 km.

3. A Heppner-Maynard boundary (HMB) (Heppner & Maynard, 1987), the low-latitude 149 boundary of the convection pattern where the flows approach zero, can either be 150 specified or be chosen using backscatter measurements. This is to constrain the 151 convection pattern when the spherical harmonic fit is applied (Shepherd & Ruo-152 honiemi, 2000). For typical two minute cadence convection maps, it is appropri-153 ate to find the lowest latitude where three radar velocity measurements are greater 154 than 100 ms^{-1} to define the HMB (Imber et al., 2013). This boundary is circu-155 lar around the nightside and oval-shaped on the dayside, such that it moves to higher 156 latitudes. Previous to Shepherd and Ruohoniemi (2000), a fully circular bound-157 ary was used, which was deemed to create unrealistic flows at lower latitudes when 158 the radar network was expanded. To make all the convection maps (D0 to D4), 159 using RST, the HMB (Heppner & Maynard, 1987; Shepherd & Ruohoniemi, 2000) 160 was chosen using the default method using the functional form Shepherd and Ruo-161 honiemi (2000), using the thresholds above. 162

- 4. A background model is selected based on solar wind conditions and model vec-163 tors are added to the grid. For this, we use solar wind data from the ACE space-164 craft, which has been time-lagged to the magnetosphere using the algorithm from 165 Khan and Cowley (1999) which takes magnetosheath transit time into account. 166 We add the model, specifying a fitting order of 6 with a 'light' doping level for the 167 background convection model, which means a minimum reliance is placed on the 168 background model. Newer background models (Thomas & Shepherd, 2018; Pet-169 tigrew et al., 2010; Cousins & Shepherd, 2010) are all generated using a fitting or-170 der of 8, whereas Ruohoniemi and Greenwald (1996) was generated using a sixth 171 order fit. 172
- 5. Finally, the 'Map Potential' technique is applied. We use the technique from Ruohoniemi
 and Baker (1998) to fit electrostatic potentials to the combined measured and model
 velocity vectors as spherical harmonic functions.

-6-

Using the steps outlined above, we first create the dataset (D0) with the high-latitude radars only, which is then modified by changing one aspect for each subsequent dataset. This allows us to contrast the impact of each change in the dataset. The basic data processing is the same for all the datasets, except for the differences outlined in Table 1. The specific processing commands and options used for the data processing can be found in the appendix of this paper.

Two versions of the gridded map files were created (e.g. step 2 to 5 is repeated) 182 to see how changing the backscatter range limits affects the dataset. One version of the 183 gridded files was created with added backscatter range limits and one without any range 184 limit. By only including data from a minimum range of 800 km and a maximum far range 185 of 2000 km, we try to eliminate all possible E-Region scatter and all backscatter with 186 higher uncertainties in range and azimuth (i.e. projected location) (Chisham et al., 2008; 187 Forsythe & Makarevich, 2017; Thomas & Shepherd, 2018). On a statistical level, we ex-188 pect this method to remove most of the data with higher uncertainty, but this method 189 will also remove some good quality data as a substantial amount of scatter comes from 190 ranges greater than 2000 km. Applying these range limits may not remove all E-region 191 scatter or all scatter with uncertain locations, but currently no better method for a large 192 statistical dataset exists. The version of gridded files with backscatter range limits is used 193 for D1-D4 and the one without a range limit is used for D0. The gridded map files were 194 resolved into two minute records and used the Chisham virtual height model (Chisham 195 et al., 2008). 196

Dataset versions D0 and D1 include the same radars, whereas for D2 and D3, more radars were included (see Table 1). For the selection of PolarDARN and StormDARN groupings the list provided by Table 1 in Thomas and Shepherd (2018) was used. The list provided in Thomas and Shepherd (2018) demonstrates that most of the StormDARN radars were built after the high-latitude and PolarDARN radars.

202

204

For D4, we keep the selection of radars the same as D3, but use the background model from Thomas and Shepherd (2018) (TS18) instead of the one from Ruohoniemi and Greenwald (1996) (RG96).

Having established this archive of 2-minute resolution convection map files, we then extract a set of measured parameters with which to quantify the ionospheric convection. The HMB latitude and cross polar cap potential (CPCP) describe the spatial extent and

-7-

strength of the convection and allow us to examine how changes in the processing might 208 affect conclusions of scientific studies, whereas the number of backscatter echoes per map 209 or the average number of backscatter points per radar allows us to study how changes 210 affect coverage. In this study, we define the HMB latitude as the latitude of the fitted 211 boundary on the nightside and we also investigate how this parameter changes along-212 side the minimum latitude where backscatter is obtained (Λ_{min}) , which can be along any 213 magnetic local time or longitude. We would thus expect the difference between the two 214 parameters to be positive for well constrained maps (i.e. Λ_{min} is at a lower latitude than 215 the HMB), but to be negative when either the minimum latitude of observations is on 216 the dayside (where the HMB shifts to higher latitudes) or an indicator that the HMB 217 is not constrained by data. We also show how the different processing affects the χ^2/n -218 statistic, which is often used as a global measure of map quality. 219

The χ^2 parameter is a result from the singular value decomposition, which is minimised when the spherical harmonic fitting is performed to find the optimal solution for the coefficients. Ruohoniemi and Baker (1998) define this as

223

$$\chi^2 = \sum_{i=1}^{N} \frac{1}{\sigma_i^2} [\mathbf{V}[i] \cdot \hat{\mathbf{k}}[i] - W_i]^2, \qquad (1)$$

where $\mathbf{V}[i]$ is the fitted velocity vector at the grid cell position i, σ_i^2 is standard devi-224 ation of the fitted velocity vector at $i, \hat{k}[i]$ is the direction of the velocity vector, W_i are 225 the uncertainties associated line-of-sight velocity uncertainties and the dot product thus 226 provides the projection of the velocity onto the line-of-sight direction. χ^2/n was intro-227 duced by Ruohoniemi and Baker (1998) as a measure of the goodness of fit of the spher-228 ical harmonic expansion to the measured line-of-sight velocity data, where a value of 1 229 would indicate a good match and higher values would indicate a worse match. In this 230 study we explore how this parameter varies and we discuss if it is an adequate measure 231 of map quality. We discuss why χ^2/n might change and what these changes might mean 232 for the quality of the convection maps. 233

Additionally, we also discuss the relationship between the HMB latitude and measures of geomagnetic activity, such as the Auroral Lower index (AL), the Auroral Electrojet index (AE) and the Symmetric Horizontal index (Sym-H) (Davis & Sugiura, 1966; Iyemori, 1990). These are derived from ground-based magnetometer measurements and are a proxy for the magnetospheric activity in response to the dayside driving and in²³⁹ ternal dynamics (Davis & Sugiura, 1966; World Data Center for Geomagnetism in Ky-

oto et al., 2015). We also consider the relationship between the CPCP and Φ_D , the day-

side reconnection rate, which is calculated from the IMF B_{YZ} component, the solar wind

speed, V_X , and IMF clock angle, θ , (Milan et al., 2012; Walach et al., 2017):

$$\Phi_D = 3.3 \times 10^5 V_x^{4/3} B_{YZ} \sin^{9/2} \frac{1}{2} \theta \tag{2}$$

We compare these parameters from D0 to D3 with D4, the most modern set-up, 244 which we use as our control dataset. We compare D0 and D4 to see how the lack of a 245 range limit, PolarDARN, StormDARN and an updated background model affects the 246 convection maps. We compare D1 to D4 to see how the lack of PolarDARN, StormDARN 247 and an updated background model affects the convection maps, and a D2 to D4 com-248 parison allows us to investigate the lack of StormDARN and an updated background model 249 affects the convection maps. Finally, a comparison between D3 to D4 allows us to see 250 the effects on the convection maps of changing the background model only. Overall, this 251 allows us to see which changes take us closer to the control dataset, D4. The timeseries 252 data extracted from the SuperDARN convection maps is condensed into probability dis-253 tribution functions (PDF) for each parameter. Our approach allows us to further inves-254 tigate how changing one parameter affects the convection maps (e.g. comparing the PDF 255 of D1 and D4 to the PDF of D0 and D4 of the same parameter shows how adding range 256 limits affects the dataset). In section 3.5 we also explore by how much the fitted Super-257 DARN velocities can increase after adding StormDARN. In the following section, we show 258 the PDFs, which enable us to compare the effects of changing the dataset on each pa-259 rameter in turn. A selection of example convection maps, that illustrates some of the dif-260 ferences that result from changing the datasets, are shown in the Supporting Informa-261 tion (Figure S1). 262

263 3 Results

This section shows the probability distribution functions for the parameters discussed above. We compare the results from each dataset with the control dataset (D4) and discuss the parameters in turn.

-9-

Version	Introduced difference	Background	high-	range	PolarDARN	StormDARN
		model	radars	limits	radars	radars
D0	High-latitude radars ^{a}	RG96	yes	no	no	no
	only					
D1	Added range limits:	RG96	yes	yes	no	no
	800-2000 km					
D2	Added PolarDARN	RG96	yes	yes	yes	no
	$radars^b$					
D3	Added all other (i.e.	RG96	yes	yes	yes	yes
	StormDARN radars) ^{c}					
D4:	Changed the back-	TS18	yes	yes	yes	yes
Con-	ground model					
trol						
set						

 Table 1.
 Differences between the comparison datasets

 a High-latitude radars: King Salmon, Kodiak, Prince George, Saskatoon, Kapuskasing,

Goose Bay, Stokkseyri, Pykkvibaer, Hankasalmi.

^bPolarDARN radars include: Inuvik, Rankin Inlet, Clyde River, Longyearbyen.

 $^c\mathrm{Storm}\mathrm{DARN}$ radars include: Hokkaido West, Hokkaido East, Adak West, Adak East, Christmas Valley West,

Christmas Valley East, Fort Hays West, Fort Hays East, Blackstone, Wallops Island.

267

3.1 The Heppner-Maynard Boundary

Figure 1 shows the probability distribution functions comparing the HMB latitude between models with the difference between the HMB latitude and Λ_{min} . The occurrences of the example maps in Fig. S1 are indicated in the probability distribution functions by the light blue crosses (and green square for comparison of Fig. S1 g and h).

Fig. 1a shows the comparison between D0 and D4. Whilst for a large proportion 272 of the data (38%) the HMB does not differ $(\pm 1^{\circ})$, 44% of the data lie above the line of 273 unity. For these instances the HMB is placed at a higher latitude in D4 than in D0. This 274 is mostly prominent when the HMB for D0 is above latitudes of 59° (40% of the time). 275 This could be due to a number of reasons, which we will discuss in section 4. We also 276 see a saturation of points in D0 at a HMB latitude of 60° , which is where the bound-277 ary is drawn if not enough data is available (due to low data coverage or no slow scat-278 ter being observed). The RG96 model has two boundaries where the HMB can be drawn 279 when not enough data is available: 60° and 55° , whereas TS18 interpolates between back-280 ground model solutions, so there are less discrete groupings in the HMB locations. Fig. 281 1b shows the HMB latitude comparison between D1 and D4. Adding range limits brings 282 the HMB distribution closer to the D4 dataset, but the saturation at 60° remains, which 283 means the HMB is most likely relying on the background fitting. This could be due to 284 a lack of StormDARN data. Now including the PolarDARN data, Fig. 1c shows the D2 285 dataset once more moving closer to the D4 dataset: The HMB moves to higher latitudes 286 in D2 for 27% of the time. The HMB moves to higher latitudes in D2 if it cannot be de-287 fined by data in D1. For the majority of maps however (72%), the HMB does not dif-288 fer at all when adding PolarDARN data. For D3 and D4, the HMB values are largely 289 the same as the raw input data do not differ, except for times when the HMB cannot 290 be defined. For brevity, we have chosen not to show this plot, as these cases are extremely 291 rare (3% of cases). For D4, these cases will be defined by the background model and vary 292 smoothly due to the interpolation in the background model between distinct bins, whereas 293 for D3 (due to the parametrization in RG96), they will be defined as two distinct lat-294 itudes, as defined by the model: 60° (96% of instances) and 55° (4% of instances), where 295 the 60° is the default and 55° is defined for strong, southward IMF (6 nT<| B |<12 nT; 296 $90^{\circ} < \text{clock angle} < 270^{\circ}$). 297

-11-



Figure 1. Probability distribution functions comparing the HMB latitude for (a) D0; (b) D1; (c) D2 with D4; and the difference between the HMB latitude and Λ_{min} for (d) D0; (e) D1; (f) D2 with D4. The occurrences of the example maps in Fig. 1 are indicated in the PDFs by blue crosses and green square.

Fig. 1d shows the difference between the HMB latitude and Λ_{min} for D0 against 298 D4. This difference is mostly positive for both D0 and D4, which means that the HMB 299 sits poleward of Λ_{min} and is thus well constrained. Fig. 1e shows the same parameter, 300 but comparing D1 and D4. Having added range limits, more data is in the top left quad-301 rant of the plot than previously, where D1 is negative and D4 is positive. For these data, 302 introducing range limits means the HMB is not well-defined in D1, but it is remedied 303 in D4. Fig. 1f shows the same parameter, but comparing D2 and D4. Adding the Po-304 larDARN data moves a considerable proportion of these data with negative HMB- Λ_{min} 305 and more datapoints cluster around 0, meaning that for these maps, the fitting is likely 306 to be better constrained. It is worth noting however that even when this parameter is 307 at 0, the HMB is not necessary bounded due to no observations being available equa-308 torward. 309

310

3.2 Number of Backscatter echoes

Figure 2 shows probability distribution functions for n, the number of backscatter echoes and the average n per radar.

Fig. 2a shows n for D0 versus D4. Going from D0 to D4, the number of backscatter points largely increase (67% of the time), though sometimes n decreases (32% of the time), which means the introduction of range limits reduces n by more than the combined addition of Polar and StormDARN increase it by. Introducing range limits (see Fig. 2b), means that for all instances, n is either higher or the same in D4 as in D1 and the same is true for D2, after the PolarDARN data have been added (see Fig. 2c).

Fig. 2d shows that the number of backscatter points per radar is on average higher 319 for D0 than D4. After introducing range limits, however (Fig. 2e), this is true for a slightly 320 smaller proportion of the data. After adding the PolarDARN data (Fig. 2f), we see that 321 despite a large proportion of the data still lying below the line of unity, the gradient of 322 the relationship has increased which means that the number of backscatter echoes per 323 radar is higher for the StormDARN than the PolarDARN. By comparing Fig. 2d to e 324 and f, we find that number of backscatter echoes per radar is lower for PolarDARN than 325 the older radars in the network (D0 and D1). 326

327

3.3 CPCP and χ^2/n

Figure 3 shows a comparison between the different datasets and D4 for the CPCP 328 (a to d) and χ^2/n (e to h). We immediately see that the CPCP varies little on average. 329 Fig. 3a shows that the observed CPCP is on average smaller for D4 than D0 (54% of the 330 time), but can increase or decrease from D0 to D4. When the CPCP increases (going 331 from D0 to D4), it increases by more on average (8 kV median increase; 10 mean increase; 332 92 kV maximum increase; 8 kV standard deviation of the increase) than the average de-333 crease (7 kV median decrease; 8 kV mean decrease; 98 kV maximum decrease; 5 kV stan-334 dard deviation of the decrease). The increases happen however less frequently than the 335 decreases (46%) of the time, compared to the 54% of the time). We see vertical striations 336 in the data in Fig. 3a, which is due to the CPCP being discretely quantized by the RG96 337 model bins when the model influence is strong, whereas for TS18 interpolation between 338 model bins occurs. Fig. 3b shows the CPCP distribution for D4 and D1. Not much varies 339 after introducing range limits, but we find that the striations are more pronounced. Com-340



Figure 2. Probability distribution functions comparing the number of backscatter echoes for
(a) D0; (b) D1; (c) D2 with D4; and the average backscatter echoes per radar for (d) D0; (e) D1;
(f) D2 with D4. The occurrences of the example maps in Fig. S1 are indicated in the PDFs by blue crosses and green square.

paring D1 and D4 and looking at the vertical spread, it is possible for the CPCP to in-341 crease by more than 30 kV, though the majority of data lies below the unity line and 342 is likely to decrease by less than ~ 30 kV. Adding in the PolarDARN data (Fig. 3c) moves 343 the D2 CPCP closer to the D4 CPCP, but there is still some spread. We see less of the 344 vertical striations in the CPCP for D2 than previously, which means the background model 345 has reduced influence. Fig. 3d shows the CPCP comparison between D3 and D4. After 346 adding StormDARN data, there is little variation in the distribution in comparison to 347 Fig. 3c. At the lower range $(0 \sim 50 \text{ kV})$, the CPCP is likely to decrease as we change the 348 background model from RG96 to TS18 (this occurs 42% of the time as opposed to the 349 increase which occurs 29% of the time). For the higher range (>50 kV) however, the CPCP 350 is likely to increase when we change model from RG96 (D3) to TS18 (D4) (this occurs 351 16% of the time as opposed to the decrease which is 13%). Overall, TS18 thus provides 352 a lower CPCP 55% of the time and a higher CPCP 45% of the time for the same data. 353 The majority of data lies below the unity line and is likely to decrease by less than ~ 30 354 kV. 355

Fig. 3e shows χ^2/n for D0 and D4. Most of the distribution lies between 1 and 10 356 for both datasets. We find that for the times when χ^2/n is larger in D4 than D0, n for 357 D4 tends to small numbers (<200; 102 median; 123.13 mean). Fig. 3f shows the same 358 distribution, but for D1 and D4. Changing the data from D0 to D1, the split between 359 increases and decreases is approximately equal (45% of χ^2/n increasing and 50% of χ^2/n 360 decreasing). Adding the PolarDARN data (Fig. 3g), shows a slightly slimmer distribu-361 tion in the y-direction, meaning that the parameter in D2 has moved closer to D4. The 362 distribution moves yet closer to D4, after we add the StormDARN data (Fig. 3h). Al-363 though not immediately obvious, 64% of the data lie below the line of unity (in compar-364 ison to 36% of data above the line) in Fig. 3h, meaning the fitting error is on average 365 reduced when making the convection maps using TS18 in comparison to RG96. 366

367

3.4 Differences in Velocity after Adding StormDARN

Computing the velocities for D3 at the HMB latitude location in D2 can be used as an indicator of how much the map has changed at specific locations and gives us an idea of how quantitatively different the convection maps might be without the Storm-DARN radars. Choosing the HMB allows us to see the maximum expected variation. We explore this in more detail now.



Figure 3. Probability distribution functions comparing the CPCP for (a) D0; (b) D1; (c) D2 ;(d) D3 with D4; and the χ^2/n distribution for (e) D0; (f) D1; (g) D2 ;(h) D3 with D4. The occurrences of the example maps in Fig. S1 are indicated in the PDFs by blue crosses and green square.



Figure 4. Probability distribution function of the velocity for D3, extracted at the noon, dusk, midnight and dawn locations where D2 would have had the HMB. Dashed lines show the medians for each distribution. Shaded regions indicate the boundaries of the lower and upper quartiles (25% and 75%).

Figure 4 shows the velocities, extracted from the D3 convection maps for the lo-373 cations where the D2-HMB intersects with the noon, dusk, midnight and dawn merid-374 ians. After adding the StormDARN data, the maps differ considerably at the locations 375 where the HMB would have otherwise stipulated that there be zero flow. The histograms 376 show that at dawn, the effect is the least noticeable and that there is a 1 in 2 chance that 377 the velocity measured in D3 has increased by 120 m/s or less, whereas this increases to 378 190 m/s for midnight and 220 m/s and 230 m/s for noon and dusk, respectively. In 8%379 of cases (which equates to over 22000 maps), adding StormDARN increases the D2-zero 380 flow regions at midnight to > 400 m/s at midnight, which indicates a considerable dif-381 ference to the convection pattern. 382



Figure 5. Probability distribution functions comparing D3 and D4 datasets: (a) CPCP difference versus n, (b) n versus D4 HMB, (c) Sym-H versus D4 HMB. The black dashed line show the line at 0 and the yellow crosses show the median for the associated bins and the error bars represent the upper and lower quartiles of the distributions (75% and 25%).

3.5 Number of Backscatter Points in Context

383

We have already shown most of the differences which happen to the derived convection maps when changing the background model. Figure 5 shows further data on how changing n in D3 and D4 relates to parameters of interest (e.g. CPCP variation, HMB and Sym-H).

Figure 5a shows the CPCP difference against n. We find that the CPCP shows the 388 least variability for maps with a high number of backscatter points, which means that 389 there is a model dependency which decreases as n increases. For example, at n=200, the 390 median and standard deviation are 0.87 kV and 8.88 kV, whereas at n=400, the median 391 and standard deviation are 0.04 kV and 6.50 kV, respectively. The yellow crosses and 392 error bars (which are indicative of the median and upper or lower quartiles) illustrate 393 further that the distribution is narrowing as n increases. While using the TS18 model 394 tends to result in a lower CPCP for less constrained maps, it can also overall result in 395 a significantly larger CPCP than with RG96 Fig. 5b shows the D4 HMB latitude against 396 n. It shows that the HMB is likely to move closer to the equator as the number of backscat-397 ter echoes increases. This is again illustrated by the yellow crosses and error bars. Fig. 398 5c shows the HMB latitude against Sym-H. There is a dependence in the HMB moving 399 to lower latitudes as Sym-H becomes more negative. Panels b and c show a seemingly 400 linear trend with HMB, which seems to break at low latitudes, but this is not supported 401 by the yellow crosses, which show the medians for each bin. 402

403

3.6 Changes to Convection Mapping Since the Original Auroral Radars

Since the SuperDARN radar network was first built, new additions to the network 404 have resulted in differences to the convection map dataset. In this section we compare 405 D0 and D4 further to see this historical comparison in context. Figure 6 shows further 406 distributions comparing D0 and D4 in the context of geomagnetic activity. Fig. 6a shows 407 the differences in the CPCP between D4 and D0 against the dayside reconnection rate, 408 Φ_D . The differences in the CPCP tend to be smaller for high solar wind driving (high 409 Φ_D). Similarly, Fig. 6b shows the differences in the HMB against AE and Fig. 6c shows 410 the estimates in the HMB against AL. Panels b and c show that differences in the HMB 411 tend to be smaller when the auroral electrojet indices, AE and AL are enhanced. Figs. 412 6d and e show the D0 and D4 HMB against AL. These include yellow and blue crosses 413 which represent the median fits for each AL bin with the error bars showing the lower 414 (25%) and upper (75%) quartiles of the distributions, allowing us to compare D4 (yel-415 low) with D0 (blue). This shows very clearly that when we use D0, we are less likely to 416 observe a low HMB at enhanced (low) AL, which is not to mean that these occurrences 417 do not exist, but simply that the SuperDARN fitting with the original dataset means 418 we are less likely to observe them. In Figs. 6f and g, we provide a similar comparison for 419 the D4 and D0 CPCP with respect to Φ_D . Here, we use the vertical bins to calculate 420 the upper and lower quartiles and the medians. We show error bars for every fifth bin 421 only due to the point density. This comparison shows that for D4 we are more likely to 422 observe a higher CPCP at higher values of Φ_D than for D0. In fact, at a Φ_D of 100 kV, 423 the median CPCP for D4 is at \sim 75 kV and \sim 65 kV for D0. The median curve has a 424 different shape for the two datasets: The bulk of the distribution is at low values of so-425 lar wind driving where the median values are very similar but at higher values, the dis-426 tributions differ. Both have a logarithmic shape to them and neither appear like a lin-427 ear fit would suffice to describe the trend in the dataset. Finally in panel h, we show the 428 ratio between the CPCP normalised by Φ_D for both datasets. This shows that the ra-429 tio between the two versions of the CPCP and dayside driving are proportional to each 430 other. It also shows that these ratios increase logarithmically and that the CPCP dif-431 ferences with respect to Φ_D in D0 are likely to be similar to D4. 432

-19-



Figure 6. Probability distribution functions comparing the entire D0 and D4 datasets: (a) Φ_D versus the CPCP difference, (b) AE versus HMB difference, (c) AL versus HMB difference, (d)AL versus D0 HMB and (e) D4 HMB, (f) D0 CPCP versus Φ_D , (g) D4 CPCP versus Φ_D and (h) CPCP normalised by Φ_D . The crosses show the median in the x- or y-direction for each y- or x-bin (where applicable) with the yellow showing the fit for D4 and blue showing the fit for D0. Error bars represent the lower and upper quartiles of the distributions (25% and 75%, respectively). Black dashed lines either show the lines of unity or the line at 0. -20-

433

3.7 Identification of Minimum Map Reliability

When using SuperDARN maps in research, a frequent question is "How reliable is this map?" and often n is used to answer this question. If n is high, the maps are often deemed more reliable, but is there a universal limit for n, which can be used to select reliable convection maps?

To attempt to answer this question statistically, we present in Figure 7a the PDF 438 of the ratio of χ^2/n between D4 and D0 on a logarithmic scale against the difference in 439 n. It shows that as the map fitting becomes more constrained (i.e. the ratio of D4 and 440 D0 χ^2/n comes closer to 1), the difference in n is likely to become smaller. As the ra-441 tio of χ^2/n becomes larger, the difference in n in also very small. This means that an 442 increase in n does not necessarily translate to an improved map. In fact, the width of 443 the distribution peaks in the y-direction (and differences in n are more likely to happen) 444 for maps that are not already well constrained. Fig. 7a shows that maps where χ^2/n does 445 not differ much (i.e. ratio close to 1), the differences in n are also very small, but can 446 also be large. Figure 7b and c show the ratio of the two χ^2/n on a logarithmic scale ver-447 sus n in D4 and n in D0. There is a trend for χ^2/n ratio moving away from 1 as n de-448 crease. In both D4 and D0, there is no clear uniform break-point in n, where χ^2/n ra-449 tio becomes smaller and the maps are better constrained in D4 than D0. We also find 450 that as n increases, χ^2/n is likely to be smaller for D4 than D0, however there is less spread 451 and the peak is more pronounced for D0 than D4. We also note that the tail in the dis-452 tributions of D4 n and D0 n versus the ratio in χ^2/n are not symmetrical around 0. We 453 will discuss these results further in the discussion section. 454

- 455 4 Discussion
- 456

4.1 Effect of Changing Range Limits on Derived Convection Maps

Adding range limits is intended to remove E-region scatter (i.e. scatter which moves slower than F-Region scatter), which can be assessed by direct comparison between D0-D4 and D1-D4. If we consider a simple situation where adding a range limit removes scatter moving slower than the F-region ExB velocity, then this should increase overall convection in the maps and thus the CPCP should increase. However, the blanket removal approach means that the removed scatter can also be faster than the average F-region flows, which can lead to counter-intuitive results. This will be discussed in further de-



Figure 7. Probability distribution functions comparing the D0 and D4 datasets: The ratios of χ^2/n on a logarithmic scale versus (a) the differences in n, (b) D4 n and (c) D0 n. The black dashed line show the line at 0 (horizontal lines) or 1 (vertical lines).

tail later in this section. The applied range limits also remove far-range scatter from slant 464 range > 2000 km, which avoids potential errors in geolocation of LOS measurements at 465 far range gates. Whilst this seems like it should constrain the spherical harmonic solu-466 tion, Thomas and Shepherd (2018) have shown that the opposite is true for a dataset 467 that is limited in latitudinal coverage: Figure 11 in Thomas and Shepherd (2018) shows 468 how range limits impacts the data coverage afforded by the high-, polar-, and mid-latitude 469 radars. For example, when data from beyond 2000 km slant range are removed from the 470 high-latitude radar dataset, which is comparable to our D0 to D1 variation, then the so-471 lution poleward of $\sim 76^{\circ}$ magnetic latitude is purely reliant on the statistical model be-472 cause no measurements are possible. This is to be expected and will be the same for our 473 D0 to D1 comparison. Imposing the range-limit will also reduce the number of backscat-474 ter echoes in the maps but we also see that the number of backscatter echoes are not solely 475 responsible for map quality. 476

Chisham and Pinnock (2002) conclude that the contamination from non-F-region 477 scatter does not usually have a large impact on the global characteristics of the Super-478 DARN convection maps. However, they did show that it has a significant effect on mesoscale 479 features in the convection maps. Our study supports these findings in terms of the larger 480 scale characteristics. We find that for the analysed time period, the CPCP is > 10% dif-481 ferent 5% of the time and the CPCP is < 10% different 95% of the time. Whilst less than 482 5% seems like a small set of observations, this does comprise more than 80000 maps, so 483 it may be important on a case-study basis. 484

-22-

Chisham and Pinnock (2002) further showed that removing E-region scatter may 485 not always result in more accurate convection maps. Whilst most E-region scatter is be-486 lieved to move slower than F-region scatter, this may not always be the case: Forsythe 487 and Makarevich (2017) used SuperDARN data from the Southern hemisphere and showed 488 that E-Region scatter can be of a similar order of magnitude as F-Region scatter (~ 200 489 m/s or larger). They also showed however that whilst F-Region scatter tends to have 490 a Gaussian velocity profile, the E-Region velocity distribution is highly asymmetric, ow-491 ing to the Farley-Buneman and gradient drift instabilities being the main drivers. This 492 may be the reason why Chisham and Pinnock (2002) find that removing E-region scat-493 ter does not always improve convection maps, but the study by Forsythe and Makare-494 vich (2017) provides clear evidence why removing this scatter makes scientific sense. Our 495 method of adding range limits follows the strategy of Thomas and Shepherd (2018), though 496 they used this method for statistical convection maps and this may not always be prac-497 tical for instantaneous convection maps. Whilst the method employed here to remove 498 far range backscatter is a broad-brush approach and also removes valid data, future al-499 ternatives could include the use of either calibrated elevation angles (which involves mea-500 suring the elevation angles using interferometry) or a more accurate virtual height model. 501

We have to consider the possibility that removing the far-range scatter reduces the integrity of the maps: The uncertainty in the geolocation of far-range scatter is expected to be of the order of ~ 100 to 200 km when using the Chisham virtual height model, which approximately equates to between one to two grid cells. Given that for an order 6 SHA fit the spatial resolution of the maps is relatively low, this level of spatial uncertainty is small.

To reduce measurement uncertainty, we remove both potential E-region scatter and scatter from far range gates. We find that by introducing range limits, the normalised Chi-squared distribution of the map fitting procedure, χ^2/n is increased 74% of the time and decreased 26% of the time.

Sometimes, reducing the number of backscatter points by introducing range limits will increase the HMB to higher latitudes due to removing lower-latitude scatter but more importantly, this difference will reduce E-region scatter at lower-latitudes and thus reduce the probability of choosing a HMB at a low latitude. For the subset of observations where this is most likely the case (i.e. the difference between the HMB and Λ_{min}

-23-

are greater in D0 than in D1 and the HMB is at a lower latitude in D0 than in D1), the 517 median n is higher (D0: 128 and D1: 56) than the median for the entire dataset (D0: 518 93 and D1: 40). Other portions of the dataset which may indicate a worse fitting con-519 tain the population where χ^2/n increases: here, the median n is less (D0: 86 and D1: 520 38) than the medians for the entire dataset (D0: 93 and D1: 40). Both these statistics 521 suggest, that n is not a good predictor for how good the fit is once range limits have been 522 introduced if χ^2/n is used as a quality-of-fit indicator. Alternatively, we suggest that this 523 illustrates a problem with χ^2/n and that it may not be the perfect indicator for qual-524 ity. We propose that in the future, a better measure for map quality is sought. Further 525 work is required to decide what this may be and is also necessary to evaluate which range 526 limits would be the best choice for creating convection maps. 527

528

4.2 Effect of PolarDARN Radars on Derived Convection Maps

Adding PolarDARN to the dataset increases the coverage, so we would expect the CPCP to be better constrained and n to increase.

We find that adding the PolarDARN radars decreases the CPCP on average, which 531 could indicate that the CPCP is overestimated without good polar cap coverage or that 532 adding PolarDARN causes an underestimation. The latter has also been shown by Mori 533 et al. (2012), who compared the velocity measurements from PolarDARN radars to CADI 534 ionosonde measurements, as well as comparing the CPCP. Adding range limits to our 535 processing will remove any slow-moving E-Region scatter, which may increase the CPCP. 536 Without polar cap measurements, it is more likely that the CPCP is estimated inaccu-537 rately, which is illustrated by the example maps in Fig. S1 (c and d). 538

We also find that the difference between the HMB and Λ_{min} either stays the same 539 or tends to increase when the polar radars are added to the dataset. Whilst we would 540 expect PolarDARN measurements mostly to be poleward of the observations from the 541 original high-latitude radars (particularly after introducing range limits), this does not 542 seem to be the case, which is most likely due to the limited local time observations in 543 the original (D0) maps. We also find that the HMB tends to stay the same or move pole-544 ward when adding the polar radars. This indicates that for a number of maps, the HMB 545 was not well defined as we would not expect the introduction of PolarDARN data to move 546 the HMB at all. Whilst this indicates that the HMB was not always necessarily well con-547

strained prior to the introduction of the PolarDARN data, it also indicates that observations near the pole are important when producing the maps.

Adding the PolarDARN radians to the dataset can increase or decrease χ^2/n . This 550 parameter only tends to increase for D2 if it was low for D1 and tends to decrease for 551 D2 if it is also high for D1. This suggests that the maps where the fitting is not partic-552 ularly good for D1, improve when adding PolarDARN data, but there are also a num-553 ber of maps where this fitting parameter decreases. Overall however, we find that the 554 difference between the HMB and Λ_{min} has a tendency to increase, which means the HMB 555 is constrained by data at a lower latitude. The median n increases from 40 to 108 when 556 adding the PolarDARN radars, which is a considerable increase in scatter. 557

558

4.3 Effect of StormDARN on Derived Convection Maps

Adding StormDARN radars improves the coverage of data at lower latitudes, we expect the HMB to move equatorward and the CPCP to be better estimated.

We find that the StormDARN radars add less data to the maps (on average), than the polar or high latitude radars, but nevertheless, adding their data to the maps generally improves the map quality. χ^2/n almost always decreases and the HMB tends to be better estimated. Adding StormDARN data tends to add low velocity scatter in lower turbulence regions, which better constrains the spherical harmonic expansion and leading to the decrease in χ^2/n .

Thomas and Shepherd (2018) made a new background model and showed that in-567 troducing the StormDARN radars could increase the CPCP by as much as 40% (for the 568 most strongly southward IMF conditions) due to the high-latitude radars only being able 569 to image a proportion of the convection zone necessary to estimate the CPCP. It is worth 570 noting that Thomas and Shepherd (2018) found very little difference in the CPCP for 571 weak to moderate solar wind driving because the low-latitude convection boundary re-572 mained within the FOV of the high-latitude radars. We find that, without using the TS18 573 model, but by simply including the StormDARN radars, the CPCP does indeed increase 574 more often (12% of times) than decrease (8% of times) but the maximum difference seen 575 is a 45% decrease when the CPCP varies from 34.70 kV in D2 to 19.19 kV in D3. 576

⁵⁷⁷ By investigating the D3 velocity measured at the HMB location of D2, we find that ⁵⁷⁸ for 33% of cases the velocity variation is less than 200 m/s, but for a considerable num-⁵⁷⁹ ber of maps (8%, which equates to over 22000 maps), the velocity variation is > 400 m/s ⁵⁸⁰ at midnight, which indicates a considerable variation to the convection pattern. This means ⁵⁸¹ that without the StormDARN radars, the velocities at Λ_{HMB2} could have an uncertainty ⁵⁸² of more than 190 m/s over half the time at midnight, which is considerable, assuming ⁵⁸³ the HMB placement is constrained by data.

However, we have to consider the possibility that the HMB placing is not always 584 as good as we would like: Many convection maps from the post-StormDARN era (such 585 as the map shown in Fig. S1h, for example) show large amounts of low velocity mid-latitude 586 convection in the nightside ionosphere, which does not seem to improve the convection 587 map. We postulate that these streams are associated with magnetic flux frozen into the 588 plasmasphere (the inner part of the magnetosphere located just above the ionosphere) 589 (Ribeiro et al., 2012). As the plasmasphere corotates with Earth, radars should not mea-590 sure Doppler velocities associated with the rotation due to their fixed geographic loca-591 tion. However, if this co-rotation is not perfectly in sync with Earth's rotation then it 592 may be possible to measure low Doppler velocities (tens-hundreds of ms^{-1}). While more 593 transient in nature, over- or under-shielding scenarios may also lead to uncertainties in 594 the HMB latitude determination when including the StormDARN radar data (e.g. Nishida, 595 1968; Nishitani et al., 2019): When this happens, the electric field formed at the inner 596 edge of the plasma sheet and associated with the region 2 field-aligned currents coun-597 teracts the effects of the solar wind-driven magnetospheric convection at sub-auroral lat-598 itudes. Whilst these scenarios may lead to uncertainty of the HMB placement, they are 599 understood to be exceptional circumstances and not well enough understood to be ex-600 plicitly taken into account when determining the HMB (Nishitani et al., 2019). Further-601 more, it is important to keep in mind that the HMB is a boundary condition, introduced 602 to facilitate the fitting process and may in reality be different to our simplified circular 603 shape. 604

605 606

4.4 Effect of Changing the Background Model on Derived Convection Maps

When changing the background model from RG96 to TS18 we might expect a more realistic fit due to a background model parametrization with more variables. The TS18

-26-

model not only uses the IMF magnetic field strength and direction, but this model parametriza-609 tion also includes the solar wind's electric field and the Earth's dipole tilt, which results 610 in 120 model bins that are trilinearly interpolated between to achieve smoother transi-611 tions, as opposed to the rigid 24 model bins chosen by RG96. The χ^2/n distribution in-612 dicates that sometimes this expected improvement is the case, however sometimes the 613 fitting is worse (i.e. χ^2/n increases), which is primarily the case for low n maps. Over-614 all, we find (in Fig. 3 and 5) that the largest differences in the CPCP are produced when 615 the CPCP was already high in D3 and these tend to occur when n is low. In fact, a higher 616 n, means smaller likelihood of observing a difference in CPCP. Thomas and Shepherd 617 (2018) compared the statistical averages over a ~ 7 year period and found that the CPCP 618 can differ by as much as 40%, when StormDARN radars are included in the convection 619 model, which is equivalent to a difference of 32 kV for a CPCP of 80 kV without the Stor-620 mDARN radars. In comparison, this study compares individual 2-min maps over a sim-621 ilar \sim 7 year period and shows that when using this model, the maximum observed per-622 centage difference in the CPCP is however a much larger difference: a reduction of 63%623 for a CPCP across this study of 49 kV in D3, which reduces to 18 kV in D4. The largest 624 increases we find in CPCP when going from D3 to D4 is 57 kV, which happens for a CPCP 625 of 33 kV in D3 and is a smaller difference than the smallest decrease (44 kV), which hap-626 pens for a CPCP of 78 kV in D3. 627

Fig. 5 and 6 show that both AL and Sym-H show a linear trend in the likelihood 628 of observations with HMB: As the HMB tends to lower latitudes, the values in AL and 629 Sym-H tend to be enhanced until the HMB reaches a latitude of $\sim 50^{\circ}$, at which point 630 the observational likelihood reduces drastically overall. We also find that at HMBs $<50^{\circ}$, 631 n is likely to be smaller in general also, which means the observations in this HMB range 632 are less dense and less well constrained. This is not surprising, as not all radars are ca-633 pable of measuring HMBs $<50^{\circ}$. Furthermore, the coverage from radars at mid-latitudes 634 is sparser as the radars tend to, on average, return less backscatter per radar than the 635 higher latitude radars. 636

We also explored how adding the newest radars to the dataset, affects the convection maps (D0 to D4 comaprison). This shows that the HMB is more likely to be found at lower latitudes (50-40°) for D4 due to the lower observational latitude limit of the data. This means that the HMB is more likely to be observed at lower latitudes when the auroral electrojet indices (AL and AE) are enhanced. It is possible that the observational

-27-

peak in AL and HMB, which shifts from \sim -400nT in D0 to \sim -300nT in D4 and \sim 66° in D0 to \sim 50° in D4, respectively, is still limited by radar coverage and it is possible that the decreasing trend we see in the median should continue (see crosses in Fig. 6d and e). It is important to note however, that AL and AE are measured by 12 magnetometer stations and the current system which they measure may well move equatorward during times of high activity. This will mean that the values shown are an underestimate rather than a true estimate.

The RG96 model was built only using the data from the Goose Bay radar, which 649 is located at a high-latitude and thus part of our D0 set. Whilst it is one of the oldest 650 operating radars in the network (and thus a lot of data is available), the RG96 model 651 was constrained in magnetic latitudes from 65-85° (Ruohoniemi & Greenwald, 1996). It 652 is therefore interesting to find χ^2/n reduced, when adding the StormDARN radars. This 653 shows that the data is important in generating the convection map files, but from com-654 paring D3 and D4 we show that the model can also make a difference. It is however worth 655 noting that due to its limited data ingestion, the RG96 model was not built to be used 656 with a radar network that extends to mid-latitudes, whereas TS18 was. Regardless of 657 the χ^2/n statistic not always decreasing for the variation from D3 to D4, the RG96 model 658 does not account for as wide a variety of solar wind driving, dipolar tilt and latitudinal 659 changes of the pattern and it thus makes more sense to use the TS18 model for the ex-660 tended dataset, especially when including data from the midlatitudes. 661

662

4.5 The Importance of Parametrizing the HMB

Much more than just flow velocities are affected by the HMB placement. The lo-663 cation of the HMB determines the boundary of the fitting, but if the CPCP is kept the 664 same, the convection strength estimate will differ. Similarly, if the flows are kept the same, 665 the CPCP will differ. Having a reliable HMB is therefore paramount to having a reli-666 able map. We have seen variations of the HMB location of up to 35° (e.g. Fig. 1) when 667 StormDARN radar data are included. This shows that there is a great uncertainty in 668 the placement of the HMB and good spatial coverage is paramount to ascertain the re-669 liability of this. 670

In either case, the HMB may need to be redefined. Currently, the HMB is calculated to be where velocity measurements suggest the electric field is zero, however low

-28-

velocity measurements associated with imperfect co-rotation will also have an associated
non-zero electric field. This suggests the HMB would not give the boundary of the convective regions associated with opening and closing of magnetic flux or that the boundary presents as a gradual variation.

A further alternative to the HMB fitting could be the original fitting by Heppner 677 and Maynard (1987), who used spacecraft passes to determine the HMB location. This 678 parameterization not only provides a non-circular fit, but also one parametrized by Kp, 679 so it could be used as an alternative for the HMB fitting. The planetary K-index, Kp, 680 is a measure of global geomagnetic activity (e.g. Matzka et al., 2021, and references therein). 681 Whilst this is one of the most extensively used indices, it is a 3 hourly index, which is 682 a long timescale in the context of ionospheric convection. There is a reason why we do 683 not produce convection maps at a 3-hourly cadence: ionospheric convection can and usu-684 ally does differ on much shorter timescales. For example, Walach and Grocott (2019) and 685 Walach et al. (2021) showed that during very active times, such as geomagnetic storms, 686 ionospheric convection and in particularly the location of the HMB, varies on timescales 687 of minutes and we thus do not advise to use a Kp parameterized HMB model. Walach 688 and Grocott (2019) showed that during geomagnetic storms, which can also be described 689 as extremely driven times, the HMB can move to latitudes as low as 40° , which Super-690 DARN radars prior to the mid-latitude expansion were not able to observe. 691

Fogg et al. (2020) provide an alternative fit for the HMB using AMPERE data, and show that the HMB may be placed at too low latitudes when StormDARN data are available. This might indicate that a changing HMB is not always an improvement when it moves equatorward in D3. It is however worth noting that the fitting by Fogg et al. (2020) does not include mid-latitude data and their fitting stops at 55°, so further analysis is necessary, which will be the subject of a future study.

Sub-auroral Polarization Streams (SAPS) are one of the main phenomenon studied with the StormDARN radars (e.g. Kunduri et al., 2017, 2018), which may also affect HMB parametrization. They consist of fast azimuthal streams, measured below auroral latitudes on the nightside (Kunduri et al., 2018). The possibility of the midlatitude radars observing either auroral flows in an expanded pattern, or sub-auroral flows in a smaller sized pattern, is an important distinction, which we have not studied in this paper but warrants further investigation. Kunduri et al. (2018) studied these flows in great

-29-

detail and found that their occurrence and flow speed tends to increase with higher geomagnetic activity. To this date, SAPS have not been explicitly taken into account in the background SuperDARN models (e.g. RG96 and TS18) and it is thus likely that their effects are averaged over. We know that SAPS will occur at or near the lower latitudinal boundary of the convection patterns (e.g. Kunduri et al., 2018), but further investigation is necessary to understand how they fit in with the general convection pattern and in particular, how they affect HMB determination.

712

4.6 The Importance of Backscatter Echoes

Historically, n has on average increased due to the expansion of SuperDARN. Nev-713 ertheless, when we compare our most historic version of the dataset (D0) with the ver-714 sion that includes all new radars, as well as updated processing techniques (TS18 and 715 range limits), we show that sometimes n decreases (Fig. 2a). This is thus solely due to 716 introducing range limits. Whilst adding the newer radars to the dataset can in some cases 717 increase n by 500 or more, adding range limits can reduce n by 100. We have shown that 718 n is an important parameter in constraining the convection pattern (e.g. HMB or CPCP): 719 In particular, we find that if n is high, the CPCP is less likely to differ(i.e. the maps are 720 constrained well) and the HMB is more likely to be found at lower latitudes (see Fig. 5). 721

⁷²² When using SuperDARN maps, the reliability of the map is important and often ⁷²³ this has been tied to n. If n is high, the maps are often deemed more reliable (e.g. Imber ⁷²⁴ et al. (2013) identified 200 to be a low threshold number for good convection maps but ⁷²⁵ Fogg et al. (2020) chose 400 as threshold for an acceptable number of grid cells contain-⁷²⁶ ing data and Lockwood and McWilliams (2021) used a threshold of 255 for specifying ⁷²⁷ the transpolar voltage). This raises the question of whether there is a universal thresh-⁷²⁸ old for n, which can be used to select reliable convection maps?

In Fig. 7b and c we show that when n is large, χ^2/n is unlikely to differ between the two datasets (the χ^2/n ratio tends to unity). However, in Fig. 7a we also show that this ratio is closest to unity when the difference in n between the two datasets is large (>200). This means that large differences in n between the datasets can have little impact on χ^2/n .

We see that for smaller $n \ (< 200)$, the map fitting is more sensitive to differences between the datasets $(\chi^2/n \text{ varies by a factor of up to } 40)$. In Fig 7a we see that when ⁷³⁶ n is the same in both datasets the χ^2/n ratio can we large or small (either D0 or D4 be-⁷³⁷ ing better constrained). In general, χ^2/n is likely to be larger in D4 than in D0 (the dis-⁷³⁸ tributions of χ^2/n ratio are skewed towards positive values in Fig. 7b and c).

Overall, whilst the biggest differences in χ^2/n are found only for n < 200, there is no clear threshold of n above which χ^2/n becomes completely insensitive to differences between the datasets, but we show that if we choose n > 400, χ^2/n is unlikely to differ by much and thus the map fitting is less sensitive to changes in the dataset.

Fig. 7b and c shows that the spread of observations becomes larger for small n and 743 the χ^2/n ratio approaches 1 for higher n. This means that for high $n, \chi^2/n$ is likely to 744 remain the same, so for small n, the maps are more likely to change when comparing D0 745 and D4. This could be due to a number of reasons, but we suggest one main cause: D4 746 includes data over a larger spatial range but for a sixth order SHA, only 49 vectors are 747 required to constrain the fitting. This is to say that a sixth order SHA can be fully de-748 scribed by 49 vectors if they are spaced appropriately. As more vectors are added (e.g. 749 from the midlatitude radars), it is likely that they are adding detail that the sixth or-750 der cannot resolve and and thus χ^2/n is not changing drastically. 751

This study has not considered the spatial distribution of n in detail, which is likely 752 to further influence map quality. Coverage at a range of local times and latitudes is likely 753 to better constrain the map fitting procedure and this is something which needs to be 754 explored further. SuperDARN map quality is inherently difficult to assess without an 755 independent dataset and the definition of quality can be different, depending on the type 756 of scientific study (e.g. for a case study, spatial distribution may be a crucial measure 757 of quality). Another way to understand quality is to consider quantitative error estimates. 758 The SuperDARN assimilatice mapping technique from Cousins et al. (2013) for exam-759 ple, readily provides uncertainty estimates on the potential at all spatial points. 760

761

4.7 Geomagnetic Conditions and SuperDARN Observations

762

We have shown in Fig. 5 and 6 that when AL and Sym-H are enhanced, and the

HMB is at lower latitudes, n tends to also be high. It is worth considering the under-

763 764

lying physics and how these parameters are related.

-31-

The expanding and contracting polar cap paradigm (e.g. Siscoe & Huang, 1985; 765 Lockwood, 1991; Lockwood & Cowley, 1992; Milan, 2015; Walach et al., 2017, and ref-766 erences therein) requires the polar cap to increase in size when the dayside reconnection 767 rate exceeds the night reconnection rate. This implies that the CPCP also increases 768 when dayside driving is high. We have shown that this is mostly the case, although there 769 are some deviations to this relationship, which we attribute to noise and errors in solar 770 wind propagation. It has long been discussed whether or not the relationship between 771 the dayside driving and the CPCP is linear and whether or not the CPCP saturates be-772 yond a threshold (e.g. Hill et al., 1976; Reiff et al., 1981; Doyle & Burke, 1983; Wygant 773 et al., 1983; Shepherd, 2007; Mori & Koustov, 2013, and references therein). Shepherd 774 et al. (2002) and Shepherd (2007) discuss this in great detail and showed, using Super-775 DARN CPCP measurements, that during high solar wind driving (when the reconnec-776 tion electric field is above 5.5 mV/m), the CPCP saturates. 777

Mori and Koustov (2013) talk about a SuperDARN "quantization" effect, whereby 778 for high CPCP where the observational density is low and not all maps are well constrained. 779 In this case, the CPCP oftentimes takes on the values of the underlying model, which 780 are quantized bins for RG96. We see this quantization very clearly in Figs. 3a, 3b, 3c 781 and to some extent in Figs. 3d and 6f for RG96, but the quantization problem is solved 782 for TS18, which interpolates between solutions of the background model. Whilst this is 783 not the focal point of our study, we find that as Φ_D increases, the CPCP also increases. 784 Similar to Shepherd (2007), we note that observational density is an important factor 785 when considering the behaviour of these parameters. We also find that depending on the 786 dataset used (e.g. D0 or D4), the trend and steepness of the curve varies due to obser-787 vational density of high CPCP for D0 being much lower than for D4. Furthermore, we 788 find that the spread in values is much higher than observed by Shepherd (2007), which 789 is due to a larger sample size (they only used equinox data for their study) and shorter 790 sampling (they used 10 minute cadence for their map files whereas we use 2 minutes). 791 We suggest that using the verb "saturate" to describe the behaviour of these parame-792 ters is misplaced, as even at high values of Φ_D the CPCP increases, whereas a satura-793 tion implies the gradient of the curve reaching 0. 794

⁷⁹⁵ Whilst n is high when AL, Sym-H and the HMB are enhanced, we are not suggest-⁷⁹⁶ ing that the correlation equates to a causal link. This was already discussed by Walach ⁷⁹⁷ and Grocott (2019), who showed that the number of backscatter echoes tends to increase

-32-

during geomagnetic storms (when Sym-H is enhanced), as dayside driving increases, the 798 polar cap grows and the HMB moves to lower latitudes. Currie et al. (2016) showed how-799 ever that during intense geomagnetic storms, a reduction of backscatter was observed 800 in the Bruny Island radar in the middle- to far-ranges, and an increase in the amount 801 of backscatter from close-ranges. Here we show statistically, that as Sym-H is enhanced, 802 the HMB moves to lower latitudes and the number of backscatter echoes increases for 803 mid-ranges (the far- and close- ranges were removed beyond D0 by range limits). We thus 804 find that the relationships found by Walach and Grocott (2019) hold statistically, though 805 a large amount of variation is observed. 806

Wild and Grocott (2008) conducted a study (before the availability of StormDARN 807 radars) of regions where backscatter is lost during isolated substorms, and the progres-808 sion through the phases of the substorm due to auroral absorption. They identify that 809 backscatter reduction is greatest at \sim 70-80° magnetic latitude region between \sim 19 to 810 03 MLT. However, Wild and Grocott (2008) also observe that the main backscatter re-811 gion shifts equatorward to lower latitudes (below $\sim 65^{\circ}$) across all local times. Our re-812 sults support this statistically, as we find that the StormDARN radars do on average ob-813 serve more backscatter, and that the backscatter moves to lower latitudes when AL is 814 enhanced (which is expected to be the case for substorms). We also find that this trend 815 differs slightly for D0 and D4: due to better coverage with the StormDARN radars, the 816 HMB for D4 moves to lower latitudes than for D0. The trend of decreasing HMB with 817 decreasing AL is a statistical one and thus breaks at a latitudes close to $\sim 40^{\circ}$ due to low 818 observational densities 819

820

4.8 Is χ^2/n an Adequate Measure of Map Quality?

The current most simple way to assess map quality is to look at the χ^2/n statistic. In this study we have explored χ^2/n as a way to measure the quality of the fitting to the line-of-sight data as defined in the Data and Methods section of this paper. If we sum χ^2 and divide by the sum of n for each dataset D0 to D4, we obtain the following average values: $\langle \chi^2/n \rangle_{D0}$: 1.70; $\langle \chi^2/n \rangle_{D1}$: 2.01; $\langle \chi^2/n \rangle_{D2}$: 2.16; $\langle \chi^2/n \rangle_{D3}$: 1.88; and $\langle \chi^2/n \rangle_{D4}$: 1.81.

From this, we might conclude that D0 has overall the highest quality maps and is closest to the "good match" criterion (1) identified by Ruohoniemi and Baker (1998), ⁸²⁹ but we have shown that whilst the map fitting may be better for D0, the missing data ⁸³⁰ also equates to a qualitative penalty. A map could have a χ^2/n close to 1 (i.e. a "good" ⁸³¹ fit), but only have 10 closely clustered vectors, in which case the map is unreliable. We ⁸³² find from the χ^2/n distributions that most of the impact on χ^2/n are provided by range ⁸³³ limits and the addition of the StormDARN radar data. This emphasizes the importance ⁸³⁴ of good spatial coverage. We also see from these statistics, that overall, the TS18 model ⁸³⁵ improves map fitting.

Furthermore, at high latitudes, in the auroral zone and polar cap, fluctuations in 836 the velocity can be greater due to increased turbulence. These velocities are more likely 837 to fit badly with low order spherical harmonic fits (~6) leading to larger increases in χ^2/n . 838 Hence, the removal of far-range scatter will obviously reduce the average χ^2/n . Conversely, 839 low velocity scatter measured in regions of lower turbulence at low latitudes fits better 840 to the spherical harmonic expansion and will have a smaller contribution to χ^2 per scat-841 ter point (regardless of order), and so the addition of more low-latitude low-velocity data 842 will again reduce the average χ^2/n . Consequently, an amount of low latitude scatter will 843 have a much smaller contribution to χ^2/n than the same amount of higher latitude scat-844 ter. But an increased goodness of fit does not always mean a "better" map. There are 845 many example maps (such as those provided in Fig. S1c and d) in which a low χ^2/n does 846 not always equate to a higher quality map. True quality is however difficult to appraise. 847 In order to achieve this, one would have to define quality first, which is beyond the scope 848 of this study. In order to truly establish map quality, we recommend the close inspec-849 tion of the individual maps and comparison with independent data, where available (e.g. 850 Walach et al., 2017). 851

852 5 Summary

We have investigated how the SuperDARN maps have changed historically by creating 5 different versions of the convection map files for a timespan of 6 years and comparing them statistically. By using different processing parameters and gradually introducing more data to the maps, we were able to investigate how the derived convection maps differ with the inclusion of

- 858
- backscatter range limits (as was used by Thomas and Shepherd (2018))
- the polar cap radars, PolarDARN

860	• the mid-latitude radars, StormDARN
861	• a different background model (we compare Thomas and Shepherd (2018) and Ruohoniemi
862	and Greenwald (1996))
863	We have shown that
864	• introducing range limits does not always decrease χ^2/n ,
865	• n is not a good predictor for how good the fit is once range limits have been ap-
866	plied
867	- once range limits have been applied the CPCP stays the same 30% of the time and
868	the HMB stays constant most of the time (54%)
869	• the addition of PolarDARN data tends to reduce the CPCP,
870	• PolarDARN radars add the most data to the dataset (on average), but the Stor-
871	mDARN radars are also important for constraining the maps,
872	- when introducing StormDARN radars to the maps, the χ^2/n values tend to de-
873	crease, the HMB becomes better constrained and the CPCP tends to increase
874	• when changing the background model to TS18, the CPCP tends to decrease for
875	lower values of the CPCP in RG96, but is more likely to increase for larger val-
876	ues of the CPCP in RG96. If n is however high (> 400), the CPCP is less likely
877	to differ (differences $\sim <20$ kV).
878	- as n , AL and Sym-H all increase, the HMB tends to go to lower latitudes, which
879	appears to be a linear trend, though a break is seen at HMB ${\sim}50$ degrees, where
880	the observational density drops off sharply.
881	• if n is high, the CPCP is less likely to differ and the HMB is more likely to be found
882	at lower latitudes and χ^2/n tends to differ by the least amount,
883	- there is no clear break, where \boldsymbol{n} universally produces good convection maps, but
884	we show that for $n > 400$, χ^2/n is unlikely to differ by much and thus the map
885	is well constrained.
886	Naturally, assessing map quality has to include a qualitative discussion and we have
887	found that there is currently no perfect quantitative method for this assessment.
888	SuperDARN provides a powerful tool for assessing solar wind-magnetosphere-ionosphere
889	coupling and studying responses to solar wind driving of the system. Due to observa-
890	tions being available almost all the time, and new radars having been constructed over

-35-

the years, the dataset now spans several decades and is well-understood. We have pre-891 sented a statistical analysis, which shows that the measured parameters (such as the CPCP 892 and HMB) differ little on average, though in some circumstances they can be highly sus-893 ceptible to which processing parameters are used, as well as which radars are used when 894 generating map files. We have shown that most of the time, parameters such as the CPCP 895 are unlikely to change by a large amount. However, when SuperDARN maps are used 896 for studies of specific conditions or small case studies, as a sampling bias can occur. As 807 a result, care has to be taken when processing the data. We have found that a high num-898 ber of SuperDARN backscatter echoes are particularly important when constraining maps, so it is important to include StormDARN data in the generation of SuperDARN con-900 vection maps. The variety of conditions that we see in our statistical comparison illus-901 trates how rich the SuperDARN dataset is. Furthermore, we have illustrated concepts 902 which can be improved. For example, we have also shown that χ^2/n is not an adequate 903 measure of map quality and whilst the HMB is largely well-defined, the method can still 904 be improved. Further work is thus necessary to evaluate convection map quality and gen-905 erate a robust HMB selection method, especially at lower latitudes. 906

⁹⁰⁷ Appendix A SuperDARN processing parameters

⁹⁰⁸ In the SuperDARN processing (see section 2), we use the following parameters and ⁹⁰⁹ functions from RST:

- For fitting the autocorrelation function to the raw data: 'make_fit' with the option '-fitacf-version 2.5'.
- To make the gridded map files, the options '-i 120 -tl 120 -chisham -c' were added to 'make_grid'
- To add the range limits to the gridded files, the same options as above were used but in addition, the options '-minsrng 800 -maxsrng 2000' were added.
- The function 'map_grd' was used with 'map_addhmb -vel 100 -cnt 3'. Adding these
 options to 'map_addhmb' chooses the Heppner-Maynard boundary to the lowest
 possible latitude for which a minimum of three LOS vectors with velocities greater
 than 100 m/s lie along its boundary.

920	• To make the convection maps, we also use 'map_addimf -if' with the text file con-
921	taining the IMF data and the option '-df' with the text file containing the IMF
922	delay times.
923	• We then use 'map_add model -o 6 ' for a sixth order expansion and use '-d' to spec-
924	ify a light doping level.
925	- Finally, we add the model option '-rg96' to D0-D3 and '-ts18' to D4 and use the
926	function 'map_fit' to make the convection map files.
927	• We also use the function 'cnvmaptomap' to convert the binary file to ASCII for-
928	mat and 'trim_map' with the options '-st', '-et', '-sd' and '-ed' to make two-hour
929	long map files for our archive, but this is not necessary to obtain the results for
930	this study.

931 Acknowledgments

All data used for this study are available opensource from nonprofit organizations. The

⁹³³ authors acknowledge the use of SuperDARN data. SuperDARN is a collection of radars

⁹³⁴ funded by national scientific funding agencies of Australia, Canada, China, France, Italy,

Japan, Norway, South Africa, United Kingdom, and United States of America, and we

thank the international PI team for providing the data. The authors acknowledge ac-

ess to the SuperDARN database via the British Antarctic Survey (https://www.bas.ac.uk/project/superdarn/#d

938 Other data mirrors are hosted by the Virginia Tech SuperDARN group (http://vt.superdarn.org/)

and the University of Saskatchewan (https://superdarn.ca/data-download). The Radar

₉₄₀ Software Toolkit (RST) to process the SuperDARN data can be downloaded from Zen-

odo (https://doi.org/10.5281/zenodo.1403226 and references). All solar wind data and

geomagnetic indices were downloaded from NASA's SPDF Coordinated Data Analysis

⁹⁴³ Web (https://cdaweb.gsfc.nasa.gov/index.html/). The AE data is also available from the

WDC for Geomagnetism, Kyoto (http://wdc.kugi.kyoto-u.ac.jp/wdc/Sec3.html) who pre-

⁹⁴⁵ pared this index. M.-T. W. and A. G. were supported by Natural Environments Research

⁹⁴⁶ Council (NERC), UK, grant nos. NE/P001556/1 and NE/T000937/1. F. S. was supported

⁹⁴⁷ by a Science and Technology Funding Council (STFC) studentship. E. G. T. thanks the

⁹⁴⁸ National Science Foundation (NSF) for support under grants AGS-1934997 and OPP-

⁹⁴⁹ 1836426. We gratefully acknowledge the use of Lancaster University's High End Com-

⁹⁵⁰ puting Cluster, which has facilitated the necessary dataprocessing for this study. M.-T.

⁹⁵¹ W. would like to thank LU's Women's Network Writing Group for providing a support-

-37-

⁹⁵² ive virtual writing space and mentorship, which helped to forge this paper. M.-T. W.

⁹⁵³ also thanks Gareth Chisham and Mark Lester for the discussions, which helped improve⁹⁵⁴ this paper.

955 **References**

- Chisham, G., Lester, M., Milan, S. E., Freeman, M. P., Bristow, W. A., Grocott, A.,
 Walker, D. M. (2007). A decade of the Super Dual Auroral Radar Network
 (SuperDARN): Scientific achievements, new techniques and future directions.
 Surveys in Geophysics, 28(1), 33–109. doi: 10.1007/s10712-007-9017-8
 Chisham, G., & Pinnock, M. (2002). Assessing the contamination of SuperDARN
- global convection maps by non-F-region backscatter. Annales Geophysi *cae*, 20(1), 13-28. Retrieved from https://hal.archives-ouvertes.fr/
 hal-00316917
- Chisham, G., Yeoman, T. K., & Sofko, G. J. (2008). Mapping ionospheric
 backscatter measured by the superdarn hf radars part 1: A new empirical virtual height model. Annales Geophysicae, 26(4), 823–841. doi:
 10.5194/angeo-26-823-2008
- Cousins, E. D. P., Matsuo, T., & Richmond, A. D. (2013). Superdarn assimila tive mapping. Journal of Geophysical Research: Space Physics, 118(12), 7954 7962. Retrieved from https://agupubs.onlinelibrary.wiley.com/doi/abs/
 10.1002/2013JA019321 doi: 10.1002/2013JA019321
- Cousins, E. D. P., & Shepherd, S. G. (2010). A dynamical model of high-latitude
 convection derived from superdarn plasma drift measurements. Journal of Geo physical Research: Space Physics, 115 (A12). Retrieved from https://agupubs
 .onlinelibrary.wiley.com/doi/abs/10.1029/2010JA016017 doi: 10.1029/
 2010JA016017
- Currie, J. L., Waters, C. L., Menk, F. W., Sciffer, M. D., & Bristow, W. A. (2016).
 Superdarn backscatter during intense geomagnetic storms. *Radio Science*,
 51(6), 814-825. Retrieved from https://agupubs.onlinelibrary.wiley
 .com/doi/abs/10.1002/2016RS005960 doi: 10.1002/2016RS005960
- Davis, T. N., & Sugiura, M. (1966). Auroral electrojet activity index ae and its
 universal time variations. Journal of Geophysical Research (1896-1977), 71(3),
 785-801. Retrieved from https://agupubs.onlinelibrary.wiley.com/

984	doi/abs/10.1029/JZ071i003p00785 doi: https://doi.org/10.1029/
985	JZ071i003p00785
986	Doyle, M. A., & Burke, W. J. (1983). S3-2 measurements of the polar cap po-
987	tential. Journal of Geophysical Research, 88 (A11), 9125. doi: 10.1029/
988	JA088iA11p09125
989	Fogg, A. R., Lester, M., Yeoman, T. K., Burrell, A. G., Imber, S. M., Milan,
990	S. E., Anderson, B. J. (2020). An improved estimation of superdarn
991	heppner-maynard boundaries using ampere data. Journal of Geophysical Re-
992	search: Space Physics, 125(5), e2019JA027218. Retrieved from https://
993	agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2019JA027218
994	(e2019JA027218 10.1029/2019JA027218) doi: https://doi.org/10.1029/
995	2019JA027218
996	Forsythe, V. V., & Makarevich, R. A. (2017). Global view of the e region irreg-
997	ularity and convection velocities in the high-latitude southern hemisphere.
998	Journal of Geophysical Research: Space Physics, 122(2), 2467-2483. Retrieved
999	from https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1002/
1000	2016JA023711 doi: https://doi.org/10.1002/2016JA023711
1001	Greenwald, R. A., Baker, K. B., Dudeney, J. R., Pinnock, M., Jones, T. B., Thomas,
1002	E. C., Yamagishi, H. (1995). Darn/superdarn. Space Science Reviews,
1003	71(1), 761-796. doi: 10.1007/BF00751350
1004	Heppner, J. P., & Maynard, N. C. (1987). Empirical high-latitude electric field
1005	models. Journal of Geophysical Research, 92(A5), 4467–4489. doi: 10.1029/
1006	JA092iA05p04467
1007	Hill, T. W., Dessler, A. J., & Wolf, R. A. (1976). Mercury and mars: The role
1008	of ionospheric conductivity in the acceleration of magnetospheric particles.
1009	Geophysical Research Letters, 3(8), 429-432. Retrieved from https://
1010	agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/GL003i008p00429
1011	doi: https://doi.org/10.1029/GL003i008p00429
1012	Imber, S. M., Milan, S. E., & Lester, M. (2013). The heppner-maynard bound-
1013	ary measured by superdarn as a proxy for the latitude of the auroral oval.
1014	Journal of Geophysical Research: Space Physics, 118(2), 685-697. doi:
1015	10.1029/2012JA018222
1016	Iyemori, T. (1990). Storm-time magnetospheric currents inferred from mid-latitude

1017	geomagnetic field variations. Journal of geomagnetism and geoelectricity,
1018	42(11), 1249-1265. doi: 10.5636/jgg.42.1249
1019	Khan, H., & Cowley, S. W. H. (1999, Sep 01). Observations of the response time
1020	of high-latitude ionospheric convection to variations in the interplanetary
1021	magnetic field using eiscat and imp-8 data. $Annales Geophysicae, 17(10),$
1022	1306–1335. doi: 10.1007/s00585-999-1306-8
1023	Kunduri, B. S. R., Baker, J. B. H., Ruohoniemi, J. M., Nishitani, N., Ok-
1024	savik, K., Erickson, P. J., Miller, E. S. (2018). A new empirical
1025	model of the subauroral polarization stream. Journal of Geophysical Re-
1026	search: Space Physics, 123(9), 7342-7357. Retrieved from https://
1027	agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2018JA025690 doi:
1028	https://doi.org/10.1029/2018JA025690
1029	Kunduri, B. S. R., Baker, J. B. H., Ruohoniemi, J. M., Thomas, E. G., Shepherd,
1030	S. G., & Sterne, K. T. (2017, June). Statistical characterization of the large-
1031	scale structure of the subauroral polarization stream. J. Geophys. Res-Space
1032	Phys., $122(6)$, 6035–6048. doi: 10.1002/2017JA024131
1033	Lockwood, M. (1991). On flow reversal boundaries and transpolar voltage in average
1034	models of high-latitude convection. Planetary and Space Science, $39(3)$, $397-$
1035	409. doi: 10.1016/0032-0633(91)90002-r
1036	Lockwood, M., & Cowley, S. W. H. (1992). Ionospheric convection and the substorm
1037	cycle. In International conference on substorms.
1038	Lockwood, M., & McWilliams, K. A. (2021). A survey of 25 years' transpolar volt-
1039	age data from the superdarn radar network and the expanding-contracting
1040	polar cap model. Journal of Geophysical Research: Space Physics, 126(9),
1041	e2021JA029554. Retrieved from https://agupubs.onlinelibrary.wiley
1042	.com/doi/abs/10.1029/2021JA029554 (e2021JA029554 2021JA029554) doi:
1043	https://doi.org/10.1029/2021JA029554
1044	Matzka, J., Stolle, C., Yamazaki, Y., Bronkalla, O., & Morschhauser, A. (2021).
1045	The geomagnetic kp index and derived indices of geomagnetic activ-
1046	ity. Space Weather, 19(5), e2020SW002641. Retrieved from https://
1047	agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2020SW002641 doi:
1048	https://doi.org/10.1029/2020SW002641
1049	Milan, S. E. (2015). Magnetospheric Plasma Physics: The Impact of Jim Dungey's

1050	Research. In D. Southwood, S. W. H. Cowley FRS, & S. Mitton (Eds.), Mag-
1051	netospheric plasma physics: The impact of jim dungey's research (pp. 1–271).
1052	doi: 10.1007/978-3-319-18359-6_2
1053	Milan, S. E., Gosling, J. S., & Hubert, B. (2012, mar). Relationship between inter-
1054	planetary parameters and the magnetopause reconnection rate quantified from
1055	observations of the expanding polar cap. Journal of Geophysical Research,
1056	117(A3), A03226. doi: 10.1029/2011JA017082
1057	Mori, D., & Koustov, A. (2013). Superdarn cross polar cap potential depen-
1058	dence on the solar wind conditions and comparisons with models. Ad -
1059	vances in Space Research, 52(6), 1155-1167. Retrieved from https://
1060	www.sciencedirect.com/science/article/pii/S0273117713003803 doi:
1061	https://doi.org/10.1016/j.asr.2013.06.019
1062	Mori, D., Koustov, A. V., Jayachandran, P. T., & Nishitani, N. (2012). Res-
1063	olute bay cadi ionosonde drifts, polardarn hf velocities, and cross po-
1064	lar cap potential. Radio Science, 47(3). Retrieved from https://
1065	agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2011RS004947 doi:
1066	https://doi.org/10.1029/2011RS004947
1067	Nishida, A. (1968). Coherence of geomagnetic dp 2 fluctuations with interplanetary
1068	magnetic variations. Journal of Geophysical Research (1896-1977), 73(17),
1069	5549-5559. Retrieved from https://agupubs.onlinelibrary.wiley.com/
1070	doi/abs/10.1029/JA073i017p05549 doi: https://doi.org/10.1029/
1071	JA073i017p05549
1072	Nishitani, N., Ruohoniemi, J. M., Lester, M., Baker, J. B. H., Koustov, A. V., Shep-
1073	herd, S. G., Kikuchi, T. (2019). Review of the accomplishments of mid-
1074	latitude super dual auroral radar network (superdarn) hf radars. $Progress in$
1075	Earth and Planetary Science, $6(1)$, 27. doi: 10.1186/s40645-019-0270-5
1076	Pettigrew, E. D., Shepherd, S. G., & Ruohoniemi, J. M. (2010). Climatologi-
1077	cal patterns of high-latitude convection in the northern and southern hemi-
1078	spheres: Dipole tilt dependencies and interhemispheric comparisons. Journal
1079	
	of Geophysical Research: Space Physics, 115(A7). Retrieved from https://
1080	of Geophysical Research: Space Physics, 115(A7). Retrieved from https:// agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2009JA014956 doi:

¹⁰⁸² Press, W. H. and Teukolsky, S. A. and Vetterling W. T. and Flannery B. P. (2007).

1083	Numerical recipes: The art of scientific computing. Cambridge University
1084	Press.
1085	Reiff, P. H., Spiro, R. W., & Hill, T. W. (1981). Dependence of polar cap potential
1086	drop on interplanetary parameters. Journal of Geophysical Research, $86(A9)$,
1087	7639–7648. doi: 10.1029/JA086iA09p07639
1088	Ribeiro, A. J., Ruohoniemi, J. M., Baker, J. B. H., Clausen, L. B. N., Green-
1089	wald, R. A., & Lester, M. (2012). A survey of plasma irregularities as
1090	seen by the midlatitude blackstone superdarn radar. Journal of Geo-
1091	physical Research: Space Physics, 117(A2). Retrieved from https://
1092	agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2011JA017207 doi:
1093	https://doi.org/10.1029/2011JA017207
1094	Ruohoniemi, J. M., & Baker, K. B. (1998). Large-scale imaging of high-latitude con-
1095	vection with Super Dual Auroral Radar Network HF radar observations. Jour-
1096	nal of Geophysical Research, 103(A9), 20797. doi: 10.1029/98JA01288
1097	Ruohoniemi, J. M., & Greenwald, R. A. (1996). Statistical patterns of high-latitude
1098	convection obtained from Goose Bay HF radar observations. Journal of Geo-
1099	physical Research, 101(A10), 21743. Retrieved from http://doi.wiley.com/
1100	10.1029/96JA01584 doi: 10.1029/96JA01584
1101	Ruohoniemi, J. M., & Greenwald, R. A. (2005). Dependencies of high-latitude
1102	plasma convection: Consideration of interplanetary magnetic field, seasonal,
1103	and universal time factors in statistical patterns. Journal of Geophysical Re-
1104	search: Space Physics, 110 (A09204). doi: 10.1029/2004JA010815
1105	Shepherd, S. G. (2007). Polar cap potential saturation: Observations, theory, and
1106	modeling. Journal of Atmospheric and Solar-Terrestrial Physics, 69(3), 234-
1107	248. Retrieved from https://www.sciencedirect.com/science/article/
1108	pii/S136468260600263X (Global Aspects of Magnetosphere-Ionosphere
1109	Coupling) doi: https://doi.org/10.1016/j.jastp.2006.07.022
1110	Shepherd, S. G. (2014). Altitude-adjusted corrected geomagnetic coordinates: Def-
1111	inition and functional approximations. Journal of Geophysical Research: Space
1112	Physics, 119(9), 7501-7521. doi: 10.1002/2014JA020264
1113	Shepherd, S. G., Greenwald, R. A., & Ruohoniemi, J. M. (2002). Cross polar cap
1114	potentials measured with super dual auroral radar network during quasi-steady
1115	solar wind and interplanetary magnetic field conditions. Journal of Geo-

1116	physical Research: Space Physics, 107(A7), SMP 5-1-SMP 5-11. Retrieved
1117	<pre>from https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/</pre>
1118	2001JA000152 doi: https://doi.org/10.1029/2001JA000152
1119	Shepherd, S. G., & Ruohoniemi, J. M. (2000). Electrostatic potential patterns in
1120	the high-latitude ionosphere constrained by superdarn measurements. $Journal$
1121	of Geophysical Research: Space Physics, 105(A10), 23005-23014. Retrieved
1122	<pre>from https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/</pre>
1123	2000JA000171 doi: 10.1029/2000JA000171
1124	Siscoe, G. L., & Huang, T. S. (1985). Polar cap inflation and deflation. Journal of
1125	Geophysical Research, $90(A1)$, 543–547.
1126	SuperDARN Data Analysis Working Group, P. m., Thomas, E. G., Ponomarenko,
1127	P. V., Billett, D. D., Bland, E. C., Burrell, A. G., Walach, MT. (2018,
1128	August). Superdarn radar software toolkit (rst) 4.2. Retrieved from
1129	https://doi.org/10.5281/zenodo.1403226 doi: 10.5281/zenodo.1403226
1130	SuperDARN Data Analysis Working Group, P. m., Thomas, E. G., Ponomarenko,
1131	P. V., Bland, E. C., Burrell, A. G., Kotyk, K., Walach, MT. (2018,
1132	January). Superdarn radar software toolkit (rst) 4.1. Retrieved from
1133	https://doi.org/10.5281/zenodo.1143675 doi: 10.5281/zenodo.1143675
1134	SuperDARN Data Analysis Working Group, P. m., Thomas, E. G., Sterne, K. T.,
1135	Shepherd, S. G., Kotyk, K., Schmidt, M. T., Billett, D. D. (2019, Septem-
1136	ber). Superdarn radar software toolkit (rst) 4.3. Zenodo. Retrieved from
1137	https://doi.org/10.5281/zenodo.3401622 doi: 10.5281/zenodo.3401622
1138	Thomas, E. G., & Shepherd, S. G. (2018, apr). Statistical Patterns of Ionospheric
1139	Convection Derived From Mid-latitude, High-Latitude, and Polar Super-
1140	DARN HF Radar Observations. Journal of Geophysical Research: Space
1141	<i>Physics</i> , 123(4), 3196-3216. Retrieved from http://doi.wiley.com/10.1002/
1142	2018JA025280 doi: $10.1002/2018JA025280$
1143	Walach, MT., & Grocott, A. (2019). Superdarn observations during geomagnetic
1144	storms, geomagnetically active times, and enhanced solar wind driving. $Jour$ -
1145	nal of Geophysical Research: Space Physics, 124(7), 5828-5847. Retrieved
1146	<pre>from https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/</pre>
1147	2019JA026816 doi: 10.1029/2019JA026816
1148	Walach, MT., Grocott, A., & Milan, S. E. (2021). Average ionospheric electric field

-43-

1149	morphologies during geomagnetic storm phases. Journal of Geophysical Re-
1150	search: Space Physics, 126(4), e2020JA028512. Retrieved from https://
1151	agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2020JA028512
1152	$(e2020JA028512\ 2020JA028512)$ doi: https://doi.org/10.1029/2020JA028512
1153	Walach, MT., Milan, S. E., Yeoman, T. K., Hubert, B. A., & Hairston, M. R.
1154	(2017). Testing nowcasts of the ionospheric convection from the expand-
1155	ing and contracting polar cap model. Space Weather, $15(4)$, $623-636$. doi:
1156	10.1002/2017SW001615
1157	Wild, J. A., & Grocott, A. (2008). The influence of magnetospheric substorms on
1158	superdarn radar backscatter. Journal of Geophysical Research: Space Physics,
1159	113(A4). Retrieved from https://agupubs.onlinelibrary.wiley.com/doi/
1160	abs/10.1029/2007JA012910 doi: 10.1029/2007JA012910
1161	World Data Center for Geomagnetism in Kyoto, Nose, M., Iyemori, T., Sugiura, M.,
1162	& Kamei, T. (2015). Geomagnetic ae index. doi: 10.17593/15031-54800
1163	Wygant, J. R., Torbert, R. B., & Mozer, F. S. (1983). Comparison of s3-3 po-
1164	lar cap potential drops with the interplanetary magnetic field and mod-
1165	els of magnetopause reconnection. Journal of Geophysical Research:
1166	Space Physics, 88(A7), 5727-5735. Retrieved from https://agupubs
1167	.onlinelibrary.wiley.com/doi/abs/10.1029/JA088iA07p05727 doi:
1168	https://doi.org/10.1029/JA088iA07p05727