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# Understanding the fluid-structure interaction from wave diffraction forces on CALM buoys: numerical and analytical solutions

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9

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# ABSTRACT

This research fills the gap in understanding fluid-structure interaction (FSI) from wave diffraction forces on CALM buoys and cylindrical structures, based on the hydrodynamics with connections. Recently, there is an increased application of (un)loading marine hoses for Catenary Anchor Leg Moorings (CALM) buoy systems in the offshore industry due to the need for more flexible marine structures that are cost-saving, easier to install, and service. However, different operational issues challenge these hoses, like during hose disconnection. Also, the fluid behaviour was investigated based on the analytical and numerical models. The numerical modelling involves the boundary element method (BEM) and Orcaflex line theory. Hydrodynamic analysis is conducted on the disconnection-induced load response of marine bonded hoses during normal operation and accidental operation under irregular waves. A comparative study on hose performance during normal operation and accidental operation is also presented. Results of statistical analysis on CALM buoy system shows good motion characteristics.

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#### **KEYWORDS**

Wave diffraction forces; marine bonded hose; ocean waves hydrodynamics; disconnection-induced load; Catenary Anchor Leg Mooring (CALM) buoy; fluid– structure interaction

# **Highlights**

- Analytical solution on wave diffraction forces on CALM buoy systems.
- Understanding the fluid-structure interaction from wave diffraction forces.
- Wave load and flow angle analysis as hydrodynamic loads on hose profiles under irregular waves.
- Novelty in hydrodynamics on Lazy-S and Chinese-lantern configurations under normal and accidental operations.
- Wave diffraction analysis, and validation using statistical analysis in ocean environment.

### 1. Introduction

In recent times, there has been an increasing trend in the application of marine bonded hoses in the ocean engineering and marine industry. This has resulted from the need for more flexible marine structures, easier to install, easier to service, and more cost-effective structures. Oil prospecting companies lost revenue due to the recent crash in oil price in 2016, which was similar to the one that occurred during the Gulf war in 1991 and following the recent COVID-19 pandemic in 2020. As such, the oil/offshore operators need to adapt more exploration activities with less cost. This adaptation subsequently influenced the increase in the application of these marine bonded hoses. These marine hoses have a short service life of about 25 years, although they are pretty reliable and, therefore, highly utilized. Some studies on the stiffness behaviour of hoses and CALM buoy motion are presented in the literature (Amaechi, Wang, Hou, et al. 2019; Amaechi, Ye, Hou, et al. 2019; Amaechi 2021a, 2021b, 2021c, 2021d; Amaechi, Wang, et al. 2021a, 2021b). Also, buoy attachments can induce load response, such as the marine bonded hoses and mooring lines. These marine bonded hoses are designed for high-pressure ratings of 9 and 21 bar capacities. They have applications for loading and offloading purposes (Amaechi 2021e; Amaechi, Chesterton, Butler, et al. 2021a, 2021b; Amaechi, Wang, et al. 2021c). The material development of marine tubular structures includes composite materials on composite risers (Amaechi and Ye 2017; Amaechi, Gillet, Hon, et al. 2019; Amaechi, Gillett, Odijie, et al. 2019; Amaechi, Odijie, Etim, et al. 2019; Amaechi, Odijie, Sotavo, et al. 2019; Amaechi 2021f, 2021g, 2021h; Ye et al. 2021), and on marine hoses (EMSTEC 2016; Trelleborg 2016, 2018; Yokohama 2016; Continental 2020). Marine hoses are classified as single carcass and double carcass (Amaechi 2021e, 2021i, 2021j, 2021k, 2021l; Amaechi, Chesterton, Butler, et al. 2021a, 2021b). The primary function of marine hoses includes loading, transporting, transporting, discharging or offloading operations in the oil field (Bai and Bai 2005; Guo et al. 2005; Palmer and King 2008; Amaechi, Wang, Hou, et al. 2019). A typical CALM buoy hose system is shown in Figure 1.

Generally, CALM buoys are offshore structures that display six degrees of freedom (6DoF) motions (Berteaux 1976; Duggal and Ryu 2005; Ryu 2006; Bluewater 2009, 2011; Wang and Sun 2015) and are usually restrained using mooring lines (Ricbourg 2006; Wichers 2013; Amaechi, Wang, Hou, et al. 2019; Amaechi, Ye, Hou, et al. 2019). They are also used in ocean environments, and their motions could be induced by water waves (Chakrabarti 1972, 1975, 2001, 2005; Hirdaris et al. 2014; Sarpkaya 2014; Chandrasekaran 2015). Wave forces on offshore structures such as semi-submersibles (Zou et al. 2008, 2013, 2014; Bhosale 2017; Odijie, Quayle, Ye, et al. 2017; Odijie, Wang, Ye, et al. 2017; Amaechi,

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Figure 1. An operational floating CALM Buoy showing attached hawsers and floating hoses (Courtesy: CultofSea). (This figure is available in colour online.)

Odijie, Wang, et al. 2021; Amaechi, Wang, Ye, et al. 2021d, 2021e, 2021f) and Wave Energy Converters (WEC) structures (Pecher et al. 2014; Gu et al. 2018; Doyle and Aggidis 2019, 2021) are computed by considering both the inertial component and the drag component of the body as represented in Morison's equation (Morison 1950; Zhang et al. 2015; Odijie 2016; Amaechi, Wang, Hou, et al. 2019). The complexities associated with the incident, scattered and diffusion wave potentials have been a subject of discussion in the offshore industry for quite some time. Useful applicable theories have been postulated to resolve some of these problems in these works (Odijie 2016; Amaechi 2021i) and journal articles (Amaechi, Wang, Hou, et al. 2019; Amaechi 2021a; Amaechi, Wang, Ye, et al. 2021a, 2021b). These forces direct some stress effects and lead to some motion instabilities due to complex potentials on the material (Brown 1985a, 1985b; Brown and Elliott 1987, 1988; Esmailzadeh and Goodarzi 2001). Some comparative studies have also been conducted based on configurations (Pecher et al. 2014; Amaechi, Ye, Hou, et al. 2019; Amaechi 2021a; Hasanvand and Edalat 2021). Hasanvand and Edalat (2021) presented a comparative investigation on CALM and SALM terminals for operational and non-operational systems using the Persian Gulf Sea, by combining the techniques in the WEC model by Pecher et al. (2014) and CALM buoy model by (Amaechi, Wang, Hou, et al. 2019; Amaechi, Ye, Hou, et al. 2019). Hasanvand and Edalat (2020, 2021) observed that the tensions generated at the PLEM of the SALM were less than the tension for the CALM terminal, and that for both cases, the connection point should be one critical consideration. Stability and wave forces are also important as they could also direct some bending forces on hoses, and deformations on these offshore structures. As such, the need to investigate the motion characteristics of the floating structure, the hydrodynamic performance, and the structural component comes up based on earlier studies (MacCarny and Fuchs 1954; Garrison 1974, 1975, 1979, 1984; Isaacson 1977, 1979; Lighthill 1979; Molin 1979; Rahman 1984, 1997). There are recent investigations on the hydrodynamic performance and wave-structure interaction (WSI) of offshore structures (Kannah and Natarajan 2006; Konovessis et al. 2013; Gao et al. 2015; Nallayarasu and Senthil Kumar 2017; Jiang et al. 2020; Poguluri and Cho 2020). Poguluri and Cho (2020) presented a numerical and analytical investigation on wave interaction for a vertical slotted barrier based on computational fluid dynamics (CFD) using turbulent Reynolds-averaged Navier-Stokes (RANS) model, as a complementary approach to computing the hydrodynamic performance. Konovessis et al. (2013) presented an investigation on the stability of offshore floating offshore structure generally while Esmailzadeh and Goodarzi (2001) focused on CALM systems by presenting an analytical investigation on the stability of CALM floating offshore structures. The latter considered the governing equations for the motion of floating structures based on nonlinear parametric ordinary differential equations of secondorder and obtained conditions by applying Schauder's fixed-point theorem. Huseby and Grue (2000) conducted an experiment on higher-harmonic wave forces acting on a vertical cylinder for periodic Stokes waves on wave slope up to 0.24. Wang and Sun (2013). presented an analytical investigation on the wave exciting forces acting on CALM buoy having skirts with experimental validation and found that the skirts affect it, particularly the exciting wave forces (Newman 1967, 1996; Vugts 1968; Milgram and Halkyard 1971; Mavrakos and Grigoropoulos 1994). The model was developed using earlier experiments on truncated cylinders (Faltisen et al. 1995; Hai-tao et al. 2003; Zheng and Zhang 2016; Li and Liu 2019) and vertical cylinders (Jacobsen 1949; Chakrabarti 1972; Raman and Venkatanarasaiah 1976; Raman et al. 1977; Chau and Taylor 1992; Feng et al. 2020), similar to other studies on hydrodynamic loadings (Sabuncu and Calisal 1981; Yeung 1981; Bhatta and Rahman 1995, 2003; Bhatta 2007; Venugopal et al. 2008; Zhou et al. 2014) and wave diffraction (Mei 1978; Wu 1991; Bhatta 2007; Liu et al. 2016). Bhatta and Rahman (1995) studied the wave diffraction and radiation by a floating vertical truncated cylinder and investigated the wave forces and moment. Malenica and Molin (1995) presented on third-harmonic wave diffraction acting on a vertical cylinder, by using Green's function. Huang and Taylor (1996) presented some analytical modelling on second-order wave diffraction acting on a truncated cylinder that is circular and under monochromatic waves and predicted locations for maximum elevation from the free surface based on linear wave theory and the nonlinear theories. Newman (1963, 1967) presented the wave forces on large structures, drift force and moments on ships in waves, before later presenting an investigation on the second-order wave forces acting on a vertical cylinder (Newman 1996) and considered the finite depth formulation of MacCarny and Fuchs (1954) by using Bessel and Hankel functions. Different forces and loads act on offshore buoys. Zhou et al. (2014) investigated on the wave and current induced seabed response on submarine pipelines. Sagrilo et al. (2002) presented a coupled dynamic technique on CALM systems based on diffraction equation and diffraction/radiation theory, and the study presented some profiles on assessment of the tension for the connections. Culla et al. (2007) presented a statistical moment prediction for a moored floating body that oscillated under irregular waves as a reference on CALM systems, using CPSP and SLSP perturbation methods. Generally, these studies are needed for accessing the strength and stability of various offshore structures, hull designs and components. Slender body connections mostly consider Morison's theory, such as composite marine risers (Wang and Sun 2015; Pham et al. 2016; Amaechi and Ye 2017; Amaechi, Gillet, Hou, et al. 2019; Toh et al. 2018), bundled hybrid offset riser (BHOR) systems (Bai and Bai 2005; Webster et al. 2011; Dareing 2012, 2019; Sparks 2018) and marine bonded hoses (Amaechi and Ye 2017; Amaechi, Gillet, Hou, et al. 2019; Amaechi, Wang, Hou, et al. 2019; Amaechi, Ye, Hou, et al. 2019; Gao et al. 2016, 2017, 2018, 2021). Generally, marine hoses are also layered structures, that are well bonded and have a helix reinforcement which is usually made of steel. Different types of marine bonded hoses include floating hoses, submarine hoses, reeling hoses and water hoses. These marine hoses are dependent on the support of an existing marine structure, such as the Single Anchor Leg Mooring (SALM) buoy, Catenary Anchor Leg Mooring (CALM) buoy, Floating Production Storage and Offloading (FPSO) or FSO tanker. However, these marine hose structures are connected using different configurations on single point moorings (SPM) terminals. Currently, there are different configurations, such as the Lazy-S, Steep-S, Chinese lantern, Conventional Multi-Buoy Mooring (CMBM) and the tandem

mooring. Due to these different configurations and applications of these marine hoses, there are usually different operations and factors that result in hose failures and thus reduce the service life of the marine hoses. These include the impact of harsh waves and weather (environmental conditions), the hose-line clashing with another hose, the impact from an FPSO or a tug boat, the fail-safe failure during hose disconnection, the impact of marine hose on the mooring lines, the damage on the liner of the marine hoses, the disconnection-induced load creating large hose pressure, failure of the hose end valve (HEV), and failure of the marine breakaway coupling (MBC). There is a gap in the effect of disconnection on marine bonded hoses but this has also been an issue, as reported in the CALM buoy incidents (ABCNews 2005; Jean et al. 2005). An example is the Girassol buoy whereby there was premature rupture of Girassol buoy's mooring chains encountered an early fatal fracture despite being in operation for about 6 months which was attributed to the first free link of the mooring chain been out of plane thereby resulting to bending fatigue while still positioned in the fairlead of the chain support (Jean et al. 2005; Edward and Kr. Dev 2021), and this affected the system as an integrity check had to be carried out on the entire CALM buoy hoses. In another study by O'Sullivan (2002, 2003), some challenges on the prediction of different loads and responses that can interact thereby influencing the motion of offloading systems and particularly deep water CALM buoys were presented but the hose disconnection was not studied. Several researchers have investigated the mathematical, numerical and experimental model tests on marine bonded hoses. Some studies on the performance behaviour of marine bonded hoses conducted theoretically show that hoses respond to different loadings such as vertical bending forces (Quash and Burgess 1979; Brown 1984; Brown and Elliott 1988; O'Donoghue 1988; O'Donoghue and Halliwell 1990; Zhou et al. 2018; Gao et al. 2021). Some earlier investigations include small-scale model tests (Pinkster & Remery 1975; Quash & Burgess 1979) and large scale tests (Brady et al. 1974; Brady et al. 1974; Saito et al. 1980; Young et al. 1980; Tschoepe and Wolfe 1981; Lebon and Remery 2002). More recent investigations have involved more numerically investigations (Roveri et al. 2002; Lassen et al. 2014; Amaechi, Wang, Hou, et al. 2019; Edward and Kr. Dev 2021) and experimental validations (Cozijn and Bunnik 2004; Cozijn, Uittenbogaard, Brake, et al. 2005; Duggal and Ryu 2005; Le Cunff et al. 2007, 2008). Gao et al. (2021) and Zhou et al. (2018) presented theoretical analysis on the reinforcement layers of marine bonded hoses with spiral stiffeners subjected to internal pressure. Gao et al. (2018) presented an experimental and numerical analysis on marine composite rubber hoses that are ring-stiffened under internal pressure. Some other works include parametric studies on marine bonded hoses under internal pressure, multiscale modelling, progressive damage and compressive-tensile fatigue of the cords

(Tonatto, Forte, et al. 2017; Tonatto, Tita, et al. 2017; Tonatto et al. 2016, 2018; Tonatto et al. 2019; Tonatto et al. 2020). Based on the load response, Lassen et al. (2014) presented numerical modelling of marine bonded hoses with experimental tests on the helix and load-induced response. Amaechi et al. (2019) presented a submarine hose model using the finite element model in Orcaflex and the hydrodynamic model in ANSYS AQWA and validated the model analytically. However, these studies did not also consider any accidental operation. Thus, this present study contributes to the knowledge by investigating the disconnection of these marine hoses and their load response effect under different wave loadings, configurations, and environmental conditions.

In this article, numerical and analytical solutions to wave diffraction forces on CALM buoy hose system with disconnection-induced load response during different operations have been conducted. The hydrodynamic analysis is carried out on the disconnection-induced load response of marine bonded hoses during normal operation and accidental operation under irregular waves. The marine hoses investigation is conducted on the CALM buoy system carried out on Chinese Lantern and Lazy-S configurations. In Section 2, some mathematical theories and governing equations include wave theory, boundary element method (BEM) and catenary equations. In Section 3, numerical modelling carried out is presented including the materials and methodology applied. In Section 4, the results and discussion are presented on this study. This study also investigates the loads' response on marine bonded hoses attached to a CALM buoy, under disconnection-induced loads. A comparative study on normal operation and accidental operation is also presented, with details on the hose performance, and some statistical analysis on hose parameters for the CALM buoy hose system.

# 2. Theoretical modelling

In this section, some theory and the governing equations in this study are presented.

## 2.1. Theory and governing equations

# 2.1.1. Wave theory

The governing equations used in the Orcaflex algorithm are based on applying Newton's 2nd law of motion, Morison's equation, JONSWAP spectrum equation, hydrodynamic equations, Navier-Stokes, and buoy stability equations. For irregular waves, the flow considered is turbulent, therefore neglecting the forces due to elasticity and the surface tension.

JONSWAP wave spectrum accounts for any imbalance in the energy flow within the wave system. Equations (50) is from Pierson–Moskowitz spectrum (Pierson and Moskowitz 1964), which is then applied as the JONSWAP spectrum (Hasselmann 1973). It was modified to take care of regions with geographical boundaries to limit the fetch regarding wave generation. The JONSWAP relationship is given as follows:

$$S_{\eta}(\omega) = \frac{\alpha g^2}{\omega^5} \exp\left[-\frac{5}{4} \left(\frac{\omega_p^4}{\omega^4}\right)\right] \gamma^a \tag{1}$$

where  $\omega$  denotes the angular frequency,  $\omega_p$  denotes the peak angular frequency,  $\eta$  denotes the incident wave amplitude, gdenotes gravitational constant,  $\gamma$  denotes the peak enhancement factor, while the other parameters  $\sigma$ ,  $\sigma_1$ ,  $\sigma_2$  are data items used by the solver. These are also dependent on the significant wave height,  $H_s$  and the period at zero-crossing,  $T_z$ .

Based on the forces on the risers, Morison's equation was used, as it considers the wave forces moving onto a cylinder due to the body's relative motion when immersed in the fluid (Morison 1950). This is represented as the summation of the Froude–Kyrov force  $\mathbf{F}_{\text{FK}}$ , the hydrodynamic force of the fluid,  $F_{\text{H}}$ , and the drag force,  $F_{\text{D}}$ . Morison's equation is expressed in the following equation:

$$F = \rho V \dot{u}^{\dagger} \rho C_{a} V (\dot{u} - \dot{v}) + \frac{1}{2} \rho C_{d} A (u - v) |u - v|$$
(2)

where V is the volume of the body,  $V_r$  is the relative velocity of fluid particles, A is the area of the body,  $C_a$  is the added mass coefficient,  $C_d$  is the drag coefficient,  $C_m$  is the inertial force coefficient and D is the diameter of the body. The equation can be simplified, as the fluid force is equal to the sum of the drag force and the force of 4 😉 C. V. AMAECHI ET AL.

inertia, thus Equation (3);

$$F = (\Delta a_w + \rho C_a \Delta a_r + \frac{1}{2} + \rho C_d A V_r |V_r|$$
(3)

The global design conducted in this investigation was carried out under irregular waves, and the damping was calculated as presented in the revised Morison Equation (Morison 1950).

$$F = \rho V \overset{\downarrow}{u} \rho C_a DA(V_r) + \frac{1}{2} \rho C_d A(V_r) |V_r|$$
(4)

#### 2.1.2. Boundary element method

Two sets of numerical models were utilized in the present research; a finite element model (FEM) cum a hydrodynamic model based on the BEM which was formulated using potential flow theory, developed in ANSYS AQWA (ANSYS 2017a, 2017b). While the FEM uses differential equations in its solutions, BEM uses integral equations in its solutions. BEM is used because of the integral functions and source potentials, thus it reduces the integral equations. Secondly, the BEM considers only the surface of the body during meshing, and reduces the dimensions by first-order. This reduces the size of the problem and is convenient for solving finite elements occupied within infinite space, as such far distances are not considered. The motion responses and force parameters for this CALM buoy were calculated using this model. The body's motion is relative to the submerged volume of the CALM buoy, which is the wetted surface, sw. As the CALM buoy hull oscillates, there are changes in the surface area, and it experiences some deformation (Odijie and Ye 2015a, 2015b; Odijie 2016; Amaechi, Wang, Hou, et al. 2019; Amaechi 2021a). However, to explain the dynamic effect of fluid-structure interactions on the stability (balance) and strength (deformation) of floating bodies like CALM buoys, a complete overview of diffracted and radiation wave conditions is needed. In this analysis, hydrodynamic relationships were used to evaluate flow pressure and force quantities and to correlate different variables and correlations. These are founded on the fluid's source potential resolution of a free-floating body having 6DoF. When considering an impermeable CALM buoy hull having an incompressible, irrotational and inviscid fluid, the velocity field of the fluid flow domain satisfies the Laplace definition expressed in Equation (5); where  $\emptyset$  denotes the velocity potential and  $\nabla$  demotes the Laplace operator.

$$\nabla^2 \emptyset = 0 \tag{5}$$

Considering the rectangular coordinate system (x.y,z), the Laplace identity in Equation (5) becomes:

$$\nabla^2 \emptyset = \frac{\partial^2 \emptyset}{\partial x^2} + \frac{\partial^2 \emptyset}{\partial y^2} + \frac{\partial^2 \emptyset}{\partial z^2} = 0$$
(6)

While, in a cylindrical or polar coordinate system  $(r,\theta,z)$ , the Laplace identity in

$$\nabla^2 \emptyset = \frac{\partial^2 \emptyset}{\partial z^2} + \frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial \emptyset}{\partial \theta} \right) + \frac{1}{r^2} \frac{\partial^2 \emptyset}{\partial \theta^2} = 0 \tag{7}$$

Based on the application of the boundary conditions at the seafloor, at any submerged surface of the buoy's hull, and the free surface, then Equation (8) can be obtained as computed (for instance, choosing the seafloor).

$$\frac{\partial \emptyset}{\partial z} = 0 \tag{8}$$

Bernoulli's equation correlates the fluid's velocity potential of a flowing stream to the hydrodynamic pressure  $(P_{hyd})$  given in the

relationship in Equation (9);

$$P_{hyd} = -\rho \left( \frac{\partial \phi}{\partial t} + \frac{1}{2} |\nabla \phi|^2 + gh \right)$$
(9)

where *h* denotes the draft height (that is the height of the buoy's hull from its submerged area), *t* denotes time and  $\rho$  denotes the seawater density.

The complexities associated with resolving velocity potential around the boundaries described in the equations above can be resolved using various wave theories. The total wave potential is expressed as a sum of the incident, diffraction, and radiation wave potentials in linear normal wave theory (Airy wave), as given in Equation (10);

$$\varphi = \varphi_I \, \varphi_S + \, \varphi_R \tag{10}$$

where  $\phi_R$  denotes the radiation potential,  $\phi_S$  denotes the scattered wave potential and  $\phi_I$  denotes the incident wave potential.

On the *XY* plane, both the regular wave and the irregular wave have an elevation that forms an angle. The 'wave direction' is the term used to describe this angle, as illustrated in Figure 2.

#### 2.1.3. Hydrodynamic equations

Along the horizontal plane, the hydrodynamic force that acts on a body is represented in Equation (11), can be mathematically written as;

$$\{F_{hyd}\} = [M]\{\ddot{x}\} + [C]\{\dot{x}\}\} + [K]\{x\}$$
(11)

where {x} denotes the motion vector, [K] denotes the stiffness matrix, [C] denotes the structural damping matrix, [M] denotes mass matrix of the hull while { $F_{hyd}$ } denotes the hydrodynamic force vector (Odijie and Ye 2015a; Odijie 2016; Amaechi, Wang, Hou, et al. 2019).

Since the hydrodynamic exciting forces are a product of the wave potential, which is a function of incident waves for each unit amplitude, they were derived from the wave exciting force.

$$\{F_i^w\} - \rho \iint (if_w - \{W\} \cdot \nabla)(u_i + u_d) e^{(-if_w t)} n_i \, ds \tag{12}$$

The expression for the wave exciting forces is represented in Equation (12), where{W} denotes the velocity field vector of the steady flow;  $f_w$  denotes the wave oscillating frequency,  $u_i$  denotes the incident diffraction wave potentials per unit amplitude;  $u_i$  denotes the diffraction wave potentials per unit amplitude;  $\rho$  denotes the density of sea water; and *i* denotes DoF.

#### 2.1.4. CALM Catenary equations

The governing equation used in the calculation of the statics for the mooring lines is the Catenary equation. It is also applied in other applications like Steel Catenary Risers (SCR) and cable structures (Irvine 1981; Bai and Bai 2005; Amaechi, Wang, Hou, et al. 2019). In the case of mooring lines, which suspends from the PC Semi to the anchor on the seabed, and thus take up a catenary shape that is approximate, and is defined by the following Equation (13), where w denotes weight per unit length and H denotes the tension along the horizontal component.

$$y = \frac{H}{w} \left[ \cosh\left(w\frac{x}{H}\right) - 1 \right]$$
(13)

$$T_H = \omega \left[ \frac{s^2 - h^2}{2.h} \right] \tag{14}$$

$$T_{\nu} = \omega.s \tag{15}$$

$$T = T_H + h.\omega \tag{16}$$





The catenary equations for CALM systems is presented in Equations (13)–(19), where h (or z) denotes the height above seabed, s denotes the arc length, x denotes the section length of the mooring cable,  $w_s$  denotes the submerged weight,  $T_H$  denotes the tension along the horizontal component,  $T_v$  denotes the tension along the vertical component, T denotes the tension component along the plane, V denotes the body's volume and W denotes the body's weight. The schematic of the catenary mooring system of

the CALM Buoy is illustrated in Figure 3.

$$T_H = \omega \left[ \frac{s^2 - h^2}{2.h} \right] \tag{17}$$

$$x = \frac{T_H}{\omega} \cdot \ln \left[ \frac{T}{T_H} + \sqrt{\left[ \left( \frac{T}{T_H} \right) \right]^2 - 1} \right]$$
(18)

$$X = h + X_0 - s + x \tag{19}$$



Figure 3. Schematic of Catenary Mooring system of CALM Buoy under static state. (This figure is available in colour online.)

## 2.1.5. Marine hose and riser equations

Considering the motion of the hose to be in the direction perpendicular to the Mean Water Level (MWL), then the equation of motion in Equation (20) exists, as presented by Bishop & Johnson (2011), where the load, Q depends on the weight of the hose, w and the radius of the hose, r located on the sea of sea depth, h and  $\text{EI}_z$  is the bending stiffness of a general section of hose.

$$EI_z \frac{\partial^4 y}{\partial x^4} + m \frac{\partial^2 y}{\partial t^2} = Q$$
(20)

Considering a short segment of the hose-string, as given in Figure 4, it can be easily deduced from the governing differential equations (Sparks 2007; Dareing 2012). The resultant force,  $T_0$  is located at point A on the arc length, s. The horizontal force,  $H_0$  is from the origin, O of the Cartesian Coordinate system and the



Figure 4. Schematic of short segment of riser hose string. (This figure is available in colour online.)

vertical force is  $V_0$ . The external pressure  $P_0$ , acts on the body of the hose whilst the external force,  $F_0$  acts at the top section of the hose string. Due to the motion of the hose string being different for each time duration, thus it will make different angles between the axis of the hose string and horizon,  $\theta_{(i=1,2,3,..n)}$ . The amount of times it uses for a full wave cycle is given by *n*. Betwixt the horizontal and the resultant force's direction makes an angle given by  $\theta_0$ . The submarine hose being modelled is considered as a beam under tension, as shown Figure 5.

Hose curvature is given by the inverse of the minimum bending radius (MBR), as

$$Curvature = \frac{1}{MBR}$$
(21)

The limit of permission for the bending radius is subject to the stiffness, EI, becomes

Minimum Bending Moment, 
$$M_o = \frac{\text{EI}}{\text{MBR}}$$
 (22)

Based on the hose content or marine riser content, the pressure field acting on the internal fluid column is closed and in equilibrium with the weight of the internal fluid. The lateral pressures acting on the pipe wall are equal and opposite to those acting on the internal fluid. Hence, by superposition and *addition* of the two force systems, those lateral pressures are eliminated. However, the supposedly axial tension in the fluid column denoted as  $-p_iA_i$ remains; where  $p_i$  is the internal pressure and  $A_i$  is the internal cross-sectional area of the pipe (Sparks 2007, 2018). This leads to the equations for the effective tension  $T_e$  and apparent weight  $w_a$ of the equivalent system.

When external pressure  $p_e$  is also present, it can be approached in a similar fashion. Both lateral pressure effects are removed by adding the force systems acting on the pipe section and the internal fluid, then subtracting the force system operating on the displaced fluid. When external pressure  $p_e$  is also present, it is approached similarly, as depicted in Figures 6 and 7.

The force systems operating on the pipe section and the internal fluid are added together, and then the force systems are subtracted. In Figures 6 and 7, and  $w_t$  denotes the equivalent system's weight,  $w_e$  denotes the weight of the displaced fluid column,  $w_a$  denotes the weight of the internal fluid column while  $w_i$  denotes the weight per unit length of the tube.

The effective tension,  $T_e$  denotes the axial tension calculated at any point of the riser by considering only the top tension and the apparent weight of the intervening riser segment (Sparks 2007, 2018; Dareing 2012, 2019; Amaechi et al. 2019). The equations for the effective tension  $T_e$  can be expressed as in Equations (23) and (24).

$$T_e = T_{tw} - (-p_i A_i) - (-p_i A_e)$$
(23)

$$T_e = T_{tw} - p_i A_i + p_i A_e \tag{24}$$



Figure 5. Submarine hose segment showing spline line and nodes. (This figure is available in colour online.)



Figure 6. The equivalent force system of Marine Risers/Hoses for internal fluid and external fluid flows. (This figure is available in colour online.)

For the apparent weight  $w_a$  that can then be represented by Equation (74)

$$w_a = w_t + w_i - w_e \tag{25}$$

The resolution of forces along the axial direction of an element of length *ds*, can be represented as:

$$\frac{dT_e}{ds} = w_a \cos \varphi \tag{26}$$

Considering the resolution of forces along the vertical plane of an element of length *ds* at small angles to the vertical, yields:

$$\frac{dT_e}{ds} = \frac{dT_e}{dx} = w_a \tag{27}$$

#### 2.1.6. Orcaflex line theory

The Line theory as depicted in the line theory model in Figure 8 was applied for the Finite Element Model (FEM) in Orcaflex 11.0f. It was modelled by utilising the nodes on the hoses and mooring lines, as shown in Figure 11. It applies some discretization for the CALM buoy, to ensure less computational time and resources (Orcina 2014, 2020, 2021; Amaechi, Wang, Hou, et al. 2019; Amaechi, Ye, Hou, et al. 2019).

# 2.2 Analytical model

The analytical model for the CALM buoy having skirt is depicted in Figure 9. Based on the problem formulation, the floating buoy of mass m is considered having a draft denoted as T, radius of the buoy denoted as  $a_1$  and radius of the buoy's skirt is  $a_2$ .



Figure 7. Schematic of force loads and pressures acting along a hose-string segment or a long riser segment. (This figure is available in colour online.)



Figure 8. Orcaflex line model (Adapted with permission, Courtesy: Orcina 2014, 2020). (This figure is available in colour online.)



Figure 9. Illustration of CALM buoy with skirt and wave diffraction. (This figure is available in colour online.)

The water depth is denoted as d, and is assumed to be constant. The skirt has a thickness that is equal to  $S_2$ - $S_1$ , where  $S_2$  denotes the distance between the top of the skirt and the seabed, while  $S_1$  denotes the distance between the bottom of the skirt and the seabed.

Some assumptions that were considered include that the fluid is inviscid, incompressible and irrotational flow. For the model, two reference frames acting from the origin locus at the seabed, were considered. These are the cylindrical polar coordinates  $(r,\theta,x)$  and the cylindrical cartesian coordinates (x,y,z), acting along the vertical axis in z-direction and the horizontal axis in x-direction. To appreciate the force field induced on the buoy by considering a regular wave having a wave height *H*, and propagates along the horizontal plane in the *x*-axis with wave frequency  $\omega$ . Thus, the total velocity potential can be represented using cylindrical polar coordinates (r, $\theta$ ,x), for the diffracted waves and the incident waves, as:

$$\varphi(r,\,\theta,\,z) = \operatorname{Re}\left\{\frac{-igH}{2\omega\cosh\left(kd\right)}\emptyset(r,\,\theta,\,z)e^{-i\omega t}\right\}$$
(28)

However, the wave frequency is related by dispersion with the wave number k as in:

$$\frac{\omega^2}{g} = k \tanh(kd) \tag{29}$$

Where the value of  $i = (-1)^{1/2}$  or  $i = \sqrt{-1}$ , k denotes the wave number and g denotes the acceleration due to gravity.

The velocity potential can be represented from solving the Laplace equation and obtaining the solution for the entire fluid domain which will satisfy the following boundary domains:

$$\frac{\partial \emptyset(r,\,\theta,\,z)}{\partial z} = \frac{\omega^2}{g} \emptyset(r,\,\theta,\,z), \qquad r \ge a_1, \ z = d \tag{30}$$

$$\frac{\partial \emptyset(r,\,\theta,\,z)}{\partial z} = 0, \qquad z = 0 \tag{31}$$

$$\frac{\partial \mathcal{Y}(r, \theta, z)}{\partial r} = 0,$$

$$r = a_2, \ S_1 \le z \le S_2; \ r = a_1, \ S_2 \le z \le d$$
(32)

$$\frac{\partial \emptyset(r,\,\theta,\,z)}{\partial z} = 0, \qquad a_1 \le r \le a_2, \, z = S_2; \ r \le a_2; \ z = S_1 \qquad (33)$$



Figure 10. Schematic chart for the numerical analysis. (This figure is available in colour online.)



Figure 11. Hydrodynamic Panel Model of CALM buoy (in ANSYS AQWA R2 2020). (This figure is available in colour online.)

An additional boundary condition considered is the radiation written as condition for the outgoing waves on the CALM buoy system, thus:

$$\lim_{r \to \infty} \sqrt{r} \left\{ \frac{\partial \emptyset}{\partial r} - ik\emptyset \right\} = 0 \tag{34}$$

To linearize the problem, the fluid pressure  $p(r,\theta,z,t)$  can be obtained by applying the unsteady linearized Bernoulli's Equation, where  $\rho$  denotes the seawater density and t is the time for the wave oscillation in the polar coordinate.

$$p(r, \theta, z, t) = -\rho \frac{\partial \varphi(r, \theta, z, t)}{\partial t}$$
(35)

The resultant wave excitation moment and the resultant wave excitation forces that acts upon the floating CALM buoy can be

$$F_x = \iint_{S_B} -p(r, \theta, z, t)n_x ds = f_{x^0} e^{-i\omega t}$$
(361)

$$F_z = \iint_{S_B} -p(r, \theta, z, t)n_z ds = f_{z^0} e^{-i\omega t}$$
(37)

$$M_{y} = \iint_{S_{B}} -p(r, \theta, z, t)[(z - z_{g})n_{x} - xn_{z}]ds = m_{y^{0}}e^{-i\omega t}$$
(38)

Herewith, the CALM buoy's mean wetted surface denoted by  $S_B$ , the vertical position of the Centre of Gravity (CoG) is denoted by  $z_g$ , the x- component of the outward unit normal vector is denoted by  $n_x$  while the z-component of the outward unit normal vector is denoted by  $n_z$ .

As depicted in Figure 9, the fluid domain has been subdivided into three fluid regions represented by  $\Omega_1$ , l=1, 2, 3, as depicted in Figure 9. The relationship for the velocity potential  $\varphi_1$ , that satisfies the Laplace Equation and Equations (30), (31), and (34) 10 👄 C. V. AMAECHI ET AL.

can be written to be:

$$\varphi(r, \theta, z) = \sum_{m=0}^{\infty} \varepsilon_m i^m \cos m\theta. \varphi_l^m(r, z),$$
  

$$\varepsilon_0 = 1; \ \varepsilon_m = 2(m \ge 1)$$
(39)

Within the exterior fluid region  $\Omega_1$ , the velocity potential around can be written as:

$$\varphi_{1}^{m}(r,z) = J_{m}(i\mu_{0}r)\cos(\mu_{0}r) + A_{m0}\frac{H_{m}^{(1)}(i\mu r)}{H_{m}^{(1)'}(i\mu_{0}a_{2})}\cos(\mu_{0}r) + \sum_{n=1}^{\infty}A_{mn}\frac{K_{m}(\mu_{n}r)}{K_{m}'(\mu_{n}a_{2})}\cos(\mu_{0}r)$$
(40)

whereby  $J_m(i\mu_0 r)$  represents the Bessel function of first kind and order m;  $K_m(\mu_0 r)$  represents the modified Bessel function of the second kind of order m, while  $K'_m(\mu_0 r)$  represents its first derivative;  $H_m^{(1)}(i\mu_0 r)$  represents the Hankel function of first kind of order m, while  $H_m^{(1)'}(i\mu_0 r)$  represents its first derivative.

It is noteworthy to state that  $\mu_0 = -ik$ , whereby  $\mu_n$  satisfies the expression in Equation (41):

$$\frac{\omega^2}{g} = \mu_n \tan{(\mu_n d)}, \quad n \ge 1$$
(41)

Within the interior fluid region  $\Omega_2$ , the solution for the velocity potential can be written as

$$\varphi_2^m(r,z) = B_{m_0} \left(\frac{r}{a_2}\right)^m \cos\left(\lambda_0 r\right) + \frac{B}{a_{n-1}} mn \frac{I_m(\lambda_n r)}{I'_m(\lambda_n a_2)} \cos\left(\lambda_n z\right) \quad (42)$$

$$\lambda_n = \frac{n\pi}{S_1}, \quad n \ge 0 \tag{43}$$

where  $I_m(\lambda_n r)$  denotes the modified Bessel function of first kind and order *m*.

Thus, within the fluid region  $\Omega_3$ , the velocity potential can be written as

$$\varphi_{3}^{m}(r, z) = C_{m0} \frac{H_{m}^{(1)}(i\mu_{0}r)}{H_{m}^{(1)'}(i\mu_{0}a_{1})} \cos\left(\mu_{0}[z - S_{2}]\right) + \sum_{n=1}^{\infty} C_{mn} \frac{K_{m}(\mu_{n}r)}{K'_{m}(\mu_{n}a_{1})} \cos\left(\mu_{n}[z - S_{2}]\right) + D_{m0} \frac{H_{m}^{(2)}(i\mu_{0}r)}{H_{m}^{(2)'}(i\mu_{0}a_{2})} \cos\left(\mu_{0}[z - S_{2}]\right) + \sum_{n=1}^{\infty} D_{mn} \frac{I_{m}(\mu_{n}r)}{I'_{m}(\mu_{n}a_{2})} \cos\left(\mu_{n}[z - S_{2}]\right) \frac{\omega^{2}}{g} = -\mu_{n} \tan\left(\mu_{n}[d - S_{2}]\right), \quad n \ge 0$$
(45)

Whereby  $H_m^{(2)}(i\mu_0 r)$  represents the Hankel function of second kind of order m, and  $H_m^{(2)'}(i\mu_0 a_2)$  represents its derivative.

The boundary conditions for continuity of the potential function at  $r = a_2$ , are given as

$$\varphi_1^m(a_2, z) = \varphi_2^m(a_2, z), \qquad 0 \le z \le S_1 \tag{46}$$

$$\varphi_1^m(a_2, z) = \varphi_3^m(a_2, z), \quad S_2 \le z \le d$$
(47)

Considering the both the conditions that are needed for the continuity of the velocity in addition to the kinematical boundary conditions at  $r = a_2$ , these boundary conditions can be written as

$$\frac{\partial \mathscr{Q}_{1}^{m}(r,z)}{\partial r}\Big|_{r=a_{2}} = \begin{cases} \frac{\partial \mathscr{Q}_{1}^{m}(r,z)}{\partial r}\Big|_{r=a_{2}}, & 0 \le z \le S_{1} \\ 0, & S_{1} \le z \le S_{2} \\ \frac{\partial \mathscr{Q}_{1}^{m}(r,z)}{\partial r}\Big|_{r=a_{2}}, & S_{2} \le z \le d \end{cases}$$
(48)

The body boundary conditions at  $r = a_1$ , can be expressed as

$$\frac{\partial \partial m_1^m(r,z)}{\partial r}|_{r=a_2}=0 , \qquad S_2 \le z \le d$$

$$\tag{49}$$

Using the method by Wang and Sun (2013), both sides of Equation (46) are multiplied by  $\cos(\lambda_j z)$ , Equations (47 and 49) by  $\cos(\mu_j [z - S_2])$  and Equation (48) by  $\cos(\mu_j z)$ , and next integrating the resultant equations all through each of the regions of validity. Based on logistics on the numerical implementation of the method, some truncation of series to limit it is necessary. The infinite series are truncated after N<sub>1</sub>+1 terms within region  $\Omega_1$ , N<sub>2</sub>+1 terms within region  $\Omega_2$ , N<sub>3</sub>+1 terms within region  $\Omega_3$ , respectively. By utilising the trigonometric functions' orthogonal characteristics, the solution can be obtained for the unknown coefficients of  $A_{mn}B_{mn}$ .

#### 3. Numerical modelling

#### 3.1 Model description

CALM buoys are offshore structures that display 6DoF, as depicted in Figures 12 and 13. CALM buoys are designed as an application of single point mooring (SPM), by considering industry specifications. For mooring of the floating structures, the design considerations used are from industry specifications API RP 2SK (API 2005), ABS (ABS 2021) and DNVGL-OS-E301 (DNV 2015a, 2015b, 2016). They are also used in ocean environments and their motions could be induced by water waves. The global loads are based on DNVGL (2017). Wave forces on marine structures are computed by considering both the inertial component and the drag component of the body as represented in Morison's equation. This is detailed in subsequent sections herein.

#### 3.2 Methodology

The methodology applied is a coupled dynamic modelling of ANSYS AQWA and Orcaflex, as presented. A schematic sketch of this numerical procedure is depicted in Figure 10. The methodology for the analysis was performing the hydrodynamic analysis of the floating buoy using ANSYS AQWA R2 2020. The amplitude values for the motion called RAOs are then loaded into Orcaflex 11.0f. The method of analysis is based on the effect of disconnection-induced loads on the marine hoses, as such the motion of the buoy was also investigated. The numerical procedure was conducted in two stages. The first stage was the hydrodynamic analysis or diffraction analysis, and the second stage was the finite element analysis (FEA), as shown in Figure 10. The model involves the generation of the RAOs and then using the fluid hydrodynamic pressure to input the RAOs. These RAOs are computed at a variation of phase angles and can be exported in two ways: either by using ANSYS AQWA beta mode or loading the generated RAOs in a text file that is scripted using FOTRAN language in ANSYS APDL. This is then loaded into the finite element analysis as a load mapping processing.

#### 3.3 Panel hydrodynamic model

The modelling of hydrodynamic aspects includes the development of the panel hydrodynamic model for the CALM buoy. This has



Figure 12. FEM of CALM Buoy system in Lazy-S showing nodal axes in Orcaflex. (This figure is available in colour online.)



Figure 13. Motion components showing coordinates and six degrees of freedom of a floating buoy. (This figure is available in colour online.)

been presented in the sea environment as in Figure 11. It was utilised in the hydrodynamic investigation in ANSYS AQWA R2 2020. The RAO values obtained were from a free-floating CALM buoy without any mooring lines or marine bonded hoses attached to the CALM buoy.

#### 3.4 Finite element model

As illustrated in the line theory model in Figure 8, the Line theory was applied for the Finite Element Model (FEM) in Orcaflex 11.0f. It was modelled by utilising the nodes on the hoses and mooring lines, as shown in Figure 12. It applies some discretization for the CALM buoy, to ensure less computational time and resources (Orcina 2014, 2020, 2021). The submarine hose model was configured as Lazy-S. The statics calculation for the submarine hose was done by B-splines as presented in Figure 5. The model setup for a similar study has been given in the literature (Amaechi, Wang, Hou, et al. 2019; Amaechi, Ye, Hou, et al. 2019).

# 3.5 Materials

The materials applied in this numerical model are presented in this sub-section.

# 3.5.1 Buoy

The cartesian coordinate system of the floating buoy is presented in Figure 13. The buoy's body was 10m in diameter, and a draft line was considered in the modelling. The model was developed by fitting the floating characteristics of the buoy in the FEM, as shown in Figure 14. The details on the buoy parameters are presented in Table 1.

# 3.5.2 FPSO tanker

The FPSO applied in this model is an FPSO tanker that can be used for offloading and discharging operations, as presented in the Orcaflex model shown in Figure 15. The length of the FPSO is 103 m, and it is designed with attachments couplings for the floating hose and hawsers. Details of the FPSO parameters are presented in Table 2. The calculations on the FPSO are the primary motion for



Figure 14. FEM in Orcaflex showing floating buoy model with details on moorings and marine bonded submarine hoses. (This figure is available in colour online.)

Table 1. Parameters for the Buoy.

Particulars	Value	Unit
Height	4.40	m
Draft size	2.40	m
Main body diameter	10.00	m
Skirt diameter	13.87	m
Buoy mass	198,762.00	kg
Water depth: Lazy-S	100.00	m
Water depth: Chinese-Lantern	26.00	m



Figure 15. The 6DoF motions for the FPSO. (This figure is available in colour online.)

the 6DoFs, wind load, current load, 1<sup>st</sup> order wave loads, 2nd order wave drift load, wave drift damping, damping, and added mass. The hydrodynamics of the floating FPSO was designed using vessel theory (Orcina 2020). The ship-shaped FPSO has six degrees of freedom (6DOFs), as presented in Figure 13.

Table	2.	Parameters	for the	FPSO.
-------	----	------------	---------	-------

Parameters	Value	Unit
Length	103.00	m
Draft	6.70	m
Height	13.40	m
Width	16	m

#### Table 3. Parameters for the Float.

Particulars	Value	Unit
Inner diameter	0.799	m
Outer diameter	1.23	m
Metal part material	Stainless Steel	-
Net buoyancy	280	kg
Type of float	Standard bolted-type float	_
Weight in air	102	kg
Shell material	Polyethylene	_
Pitch of float	2.00 (depends on section)	m
Filling material	Polyurethane foam	-
Number of floats	Depends on configuration	-
Length of float	0.60	m

## 3.5.3 Floats

The floats are made from materials that can help them to float and ensure good buoyancy. The floats were designed differently depending on the application. The float on the submarine hoses and the floating hoses were slightly different sizes but the same materials, as given in Table 3. An illustration of buoyancy floats is shown in Figure 16.

#### 3.5.4 Marine breakaway coupling (MBC)

The MBC was modelled to have three sections and was attached to the floating hose. The outer diameter (OD) of the MBC is 0.735m while the inner diameter (ID) of the MBC is 0.5 m. It was made of steel material with a material density of 7850kg/m<sup>3</sup>. MBC can be connected between two hose sections at strategic locations close to the hose end nearer to the service tanker or where needed on the marine hose, such as on reeling hoses and floating hoses (EMSTEC 2016; Yokohama 2016; GallThomson 2018; MarineBreakawayCouplings 2018; TechFlowMarine 2021). Typical MBC is shown in Figure 17.

### 3.5.5 Floating hose

The floating hose modelled in this investigation is connected to a manifold, as illustrated in Figure 18. The hose has an outer diameter of 0.64 m and an inner diameter of 0.5 m, and a mass per unit length of 182.1 kg/m. It was designed using GMPHOM OCIMF (OCIMF



Figure 16. illustration of floats on a marine bonded hose. (This figure is available in colour online.)



Figure 17. Typical: (a) Marine Breakaway Coupling on a floating hose and (b) a Petal Valve MBC (Courtesy: Gall Thomson). (This figure is available in colour online.)

2009) and API 17K (API 2017) industry standards with a limit consideration on the minimum bending radius of 2.0 m. A typical floating hose is shown in Figure 17(a).

#### 3.5.6 Submarine hose

The submarine hoses were designed using Lazy-S configuration as depicted in Figures 19. The submarine hose's inner diameter (or bore) is 0.49 m, while the outer diameter is 0.65m, as detailed in Table 4. The length of the submarine hose was 162.63 m, and connected from the Pipeline End Manifold (PLEM) to the underneath manifold of the CALM buoy, as illustrated in Figures 18. The hoses were designed for fully filled conditions and tested with both seawater and oil. The seawater and the oil densities are 1025 and 825 kg/m<sup>3</sup>, respectively.

# 3.5.7 Hawser

Two hawser cables were designed that connect the floating buoy to the FPSO tanker, shown in Figure 20. The outer diameter 0.0765 m, with mass per unit length of 5.25 kg/m. The hawser is a thick cable because the principle behind its manufacture is with three-rope

strands twisted together left-handed in three ways to have nine strands. The hawser is designed with polyamide materials. It is a thick rope with flexible properties. The weight was considered in setting up the model for the single point mooring (SPM).

## 3.5.8 Mooring lines

The CALM buoy model was moored using six (6) mooring lines, arranged as shown in Figures 20 and 21. The materials for the mooring lines were a composite arrangement of steel chain and polyester rope, as detailed in Table 5.

## 3.6 Design parameters

The design parameters applied in this investigation are presented in this sub-section.

#### 3.6.1 Ocean and seabed

The numerical model was designed using some ocean and seabed considerations for the model. The seabed profile is modelled as 3D flat seabed, and it is determined by using the top surface of the seabed



Figure 18. Illustration showing loadings on the floating hose and submarine hose attached to the floating buoy. (This figure is available in colour online.)



Figure 19. Hose segment of 12m in length, showing descriptions with markings. (This figure is available in colour online.)

Parameters	Arrangement	Value
Hose division 1	Analysinen	Vulue
Itom dotail	First off Puov with Float collars	
Ronding stiffnoss (kN m <sup>2</sup> )	C1 (fitting)	10.000
bending sumess (kiv m)	S1 (ming) S1 (reinforce and)	10,000
	ST (Terriforce end)	70
	SI (DOUY)	70
lless inner dienseter (m)	ST (Itting)	10,000
Mass (kg/m)		0.490
Mass (kg/m)		239
Length (m)		8.49
1. I. I.	Hose division 2	
Item detail	Mainline without Float collars	
Bending stiffness (kN m <sup>2</sup> )	S2 (fitting)	10,000
	S2 (end)	98
	S2 (body)	78
	S2 (end)	98
	S2 (fitting)	10,000
Hose inner diameter (m)		0.490
Mass (kg/m)		495
Length (m)		9.02
	Hose division 3	
ltem detail	First-off PLEM with Float collars	
Bending stiffness (kN m <sup>2</sup> )	S3 (fitting)	10,000
-	S3 (end)	98
	S3 (body)	78
	S3 (reinforce end)	120
	S3 (fitting)	10,000
Hose inner diameter (m)	(	0.490
Mass (kg/m)		239
Length (m)		8.49

 Table 4. Array of the submarine hose-string for 3 divisions (or sections).

in regards to its position with the surface of the sea called the Mean Sea Level (MSL), as shown in Figures 11, 13 and 20. The seabed is a function of hydraulic pressure that influences its stability, such as pore water pressure, as detailed in literature (Eshiet 2012; Li et al. 2016; Odijie 2016). The parameters for the seabed and the ocean in the study are given in Table 6. This method of wave computation coupled with oceanic and seabed parameters has been validated in some technical studies on different offshore structures (Odijie and Ye 2015a, 2015b; Odijie 2016; Amaechi, Wang, Hou, et al. 2019; Amaechi 2021; Amaechi, Wang, et al. 2021a).

#### 3.6.2 Waves and wave spectrum

The numerical model was designed using some environmental considerations for the weather. The wave angles considered in this investigation were at an interval of 0°, and are as follows: 0°, 30°, 60°, 90°, 120°, 150°, 180°, as detailed in the wave parameters given in Table 7. An illustration showing the direction of waves and FPSO across the sea is presented in Figure 22. The lowest frequency applied for the hydrodynamic design analysis in ANSYS AQWA was 0.06048 Hz. For the waves, the value for the peak factor was 3.3, and the wave spectrum considered was the JONSWAP spectrum, as plotted in Figure 23.

#### 3.6.3 Wind and current

The present researched models were set up using some parameters in the modelling. For the wind and current, the speed of the wind was 22 m/s, while the speed of the surface current was 0.5 m/s. For



Figure 20. The FPSO tanker attached to the CALM buoy offloading system showing hose disconnect (in Orcaflex 11.0f). (This figure is available in colour online.)



Figure 21. The arrangement of the mooring chains around the CALM buoy showing top plan view with global load linearity. (This figure is available in colour online.)

Table 5. Parameters for the Moorings.

Particulars	Value	Unit
Type of mooring configuration	Catenary Mooring	-
Contact diameter	0.229	m
Nominal diameter	0.120	m
Drag coefficient, C <sub>d</sub>	1.00	_
Mass coefficient, Cm	1.00	_
Axial stiffness, EA	407,257.00	kN
Bending stiffness	0.00	kN
Mass per unit length	0.088	kN/m
Ratio of section lengths	150:195	-
Poisson ratio	0.50	-
Angles apart for each moorings	60	0

Table 6. Parameters for the Ocean and Seabed.

Value	Unit
0	0
3D Profile	-
Nonlinear Soil Model	-
10	°C
1.35 ×10 <sup>-6</sup>	m²/s
0	%
0.5	-
7.5	kN/m m <sup>2</sup>
0.145	m
1,025	kg/m <sup>3</sup>
	Value 0 3D Profile Nonlinear Soil Model 10 1.35 ×10 <sup>-6</sup> 0 0.5 7.5 0.145 1,025

the air, an air kinematic viscosity of  $15.0 \times 10^{-6} \text{ m}^2 \text{s}^{-1}$  under an air density of 1.225 kg m<sup>3</sup> (0.00123 g cm<sup>-3</sup>), as detailed in Table 8. A uniform profile for the current as presented in Figure 24 is utilised on the marine hose models on each of the cases investigated. Figure 25(a) presents the wind load coefficient, while the current load coefficient is presented in Figure 25(b).

#### 3.7. Validation

The validation of the theory applied on this study is based on existing validated studies by the author (Amaechi, Wang, Hou, et al. 2019; Amaechi, Ye, Hou, et al. 2019; Amaechi, Wang, et al. 2021a). The dynamic models from Orcaflex are expected to be able to perform dynamic analysis on the hose in centennial configuration. The dynamic effects offered by Orcina's Orcaflex Table 7. Wave Parameters.

Cases	Hs	Tz	T <sub>P</sub>	Wave Angle
1st Case	1.87m	4.10s	5.27s	0°, 30°, 60°, ,180°
2nd Case	2.20m	5.60s	7.20s	0°, 30°, 60°, ,180°
3rd Case	4.10m	7.00s	9.00s	0°, 30°, 60°, ,180°

were examined on catenary S-lay pipeline through recently completed sea testing in field trials (Wang et al. 2017) and experimentally in Lancaster University wave tank (Amaechi 2021c, 2021d, 2021i). It was also validated numerically using confirmed static models on Lazy-S configuration (Amaechi, Wang, et al. 2021a), as well as on Chinese-lantern Configuration (Amaechi, Wang, Hou, et al. 2019). To evaluate the numerical model, a comparative analysis of a load case from the experimental test was used to validate the model and analytical model (Amaechi 2021c, 2021d).

The second validation was carried out by comparing result of experiment against the analytical model in Section 2.2. To achieve this, values for  $N_1,N_2$  and  $N_3$  were assumed for a finite depth d1 of 1.0m, deeper depth of 100m, and cylinder draft D of 0.3m, and the same radius of cylinder a1 of 0.13m. Figure 26(a) is for the wave exciting force, while Figure 26(b) is for the wave exciting moment. The analytical solution was obtain using the analytical solutions presented in Section 2. Comparing the results against experimental results (Hintao et al. 2003), the analytical results (Wang and Sun 2013) and the numerical results (present study) shows good agreement as observed in Figure 26(a,b). Other validation methods considered are using coupled models and the parameters like effective tension and bending moment in other related studies.

#### 4. Results and discussion

The results of this investigation and the discussion are put forward in this part of the article.

#### 4.1 Buoy motion study

# 4.1.1 Statistical analysis on buoy motion response

The result of the environmental conditions given in Table 7 was applied to investigate the buoy motion responses. It was conducted using the hydrodynamic RAOs generated from ANSYS AQWA, then inputted into the Orcaflex model by coupling. It can be observed that the buoy motion is dependent on the environmental conditions, as the three cases had different motion behaviour. It can be observed that the CALM buoy motion increased more in the surge motion than in the heave. Therefore, the tension magnitude of the mooring cables attached to the CALM buoy needs to be improved. However, the *case3* values were generally the highest, followed by the *case2* values and then the *case1* values. Thus, this shows that some perturbations from the buoy motion can induce some response on the hoses, as will be shown in results in subsequent sections.

For the statistical method, two methods were applied to validate the model. They are the Pearson Correlation Coefficient and the Weibull statistical method. The application of the Pearson Correlation Coefficient to study the data from the buoy responses was possible when loaded with wave RAO loads. Pearson Correlation Coefficient is an important technique used in data mining in Ocean Engineering analysis (Mahjoobi et al. 2008; Moon et al. 2008; Gao et al. 2010; Wang et al. 2016; Ali and Prasad 2019). Correlation analysis is a technique used to investigate and analyse some relativity correlation of data variables, their dependence on the other, and the correlation of the direction of one variable with respect to others. Pearson correlation coefficient helps to obtain



Figure 22. Illustration showing the direction of waves and FPSO with respect to the sea, showing (a) the wave heading with various types of seas defined, and (b) waves on ship-shaped FPSO. (This figure is available in colour online.)



Figure 23. The sea states for the JONSWAP wave spectrum. (This figure is available in colour online.)

the strength, magnitude and direction correlation between the variables. This coefficient varies from -1 to 1, and values that approach close to 1 are positive correlations while the values close to -1 are the negative correlation.

The Correlation Coefficient of the buoy motions for surge, heave, roll and pitch motions are obtained for the 3 environmental conditions being investigated win the 42 cases. It was used to obtain the relationship when the buoy is loaded with wave load RAOs and when it is without wave load RAOs. Pearson Correlation Coefficient was obtained for each of the environmental conditions as presented

#### Table 8. Wind and Current Parameters.

Particulars	Value
Wind type	Constant
Density of air (g/cm <sup>3</sup> )	0.00123
Kinematic viscosity of air (m <sup>2</sup> /s)	0.000015
Power law exponent	7.0
Current method	Power Law
Current direction (°)	180
Surface current (ms <sup>-1</sup> )	0.50
Seabed current (ms <sup>-1</sup> )	0.45
Speed of wind (ms <sup>-1</sup> )	22.0

in the literature (Amaechi, Wang, Hou, et al. 2019; Amaechi, Ye, Hou, et al. 2019). These coefficients are obtained by using the equation for Pearson correlation coefficient, given in Equation (50).

$$r_{pearson} = \frac{\left[\sum_{i=1}^{n} (x - \bar{x})(y - \bar{y})\right]}{\sqrt{\left(\sum_{i=1}^{n} (x - \bar{x})^{2}\right)\left(\sum_{i=1}^{n} (y - \bar{y})^{2}\right)}}$$
(50)

Where *n* denotes the sample size,  $\bar{x}$  denotes the average of the buoy motion without wave load RAOs,  $\bar{y}$  denotes the average of the buoy motion with wave load RAOs, and r denotes the Pearson Correlation Coefficient. From Table 9, it can be seen that there is positive correlation between the buoy motions for the surge, roll and pitch while a negative correlation exists for the heave motion. This means that the motion of the buoy being predicted by the analysis will affect the hoses, despite the shallow water depth. However, the hoses need to be redesigned to cushion the heave effect from the heave motion of the buoy.

For the Weibull statistical method, 95% confidence values of 21.8825 and 26.4572 were obtained. The 3-hour return level for the upper tail of the pitch motion (RY) is 23.4187° from the Weibull distribution. A threshold of 41 data points above the threshold of



Figure 24. The vertical profile of the Current at seabed origin. (This figure is available in colour online.)

17° with decluttering based on mean up-crossings is used. The fitted Weibull parameters obtained are presented in Table 10. The Weibull distribution tool has been used to validate the reliability of these motion results. The expression for the Weibull distribution is given by Equation (51):

$$F(x, \alpha, \beta) = 1 - e^{-\left(\frac{x}{\beta}\right)^{a}}$$
(51)

where x,  $\alpha$  and  $\beta$  are numeric values; x is the value that is required to evaluate the function. From the results, it shows that the roll had the highest data points, followed by the surge motion. It was least in the heave, which means it had good stability in the heave motion.

## 4.1.2. Surge RAO & radiation damping on buoy

An investigation on the surge RAO and radiation damping has been carried out on three buoy models of varying skirt geometries. The skirts on the buoy presented in Table 11 and Figure 27 were investigated for effect on the hydrodynamic behaviour using surge RAO. As shown in Figure 28(a), *BuoySkirt1*(13.90m diameter) had the least surge RAO while *BuoySkirt3* (11.90m diameter) had the highest surge RAO. Thus, the higher the skirt diameter, the lesser the surge RAO. Figure 28(b) shows that *BuoySkirt1*was maximum at 215,191 N/(m/s). Thus, the diameter of the buoy skirt affects the surge RAO and the radiation damping. However, a detailed study on the motion response is recommended.

# 4.2. Load response study

# 4.2.1. Floating hose load response in normal configuration

The investigation on the disconnection-induced load on the floating hose was investigated and the results are presented in Figures 29–31. The hose bending moment in the normal operation shown in Figure 29(a,b) shows a lower profile than the hose bending moment in accidental operation in Figure 29(c,d). It was recorded that Case



Figure 25. CALM buoy system loads showing (a) Wind load coefficient and (b) current load coefficients. (This figure is available in colour online.)



Figure 26. Validation of wave diffraction on buoy showing (a) wave exciting force and (b) wave exciting moment. (This figure is available in colour online.)

Table 9. Pearson Correlation Coefficients for the Buoy Motions.

	Motions			
Environmental Conditions	Surge, X	Heave, Z	Roll, RX	Pitch, RY
Case 1	0.985649	-0.30552	0.451008	0.764914
Case 2	0.981876	-0.21852	0.51911	0.938082
Case 3	0.924578	-0.36845	0.906697	0.920569

Table 10. Weibull Analysis Distribution of the CALM buoy motions.

Parameters	Data Points	Threshold
Surge	59	3.22 m
Heave	16	—1.083 m
Roll	89	0.00037°
Pitch	41	17°

Table 11. Table showing CALM buoy skirt diameters considered.

CALM buoy Skirt Cases	Skirt Diameter, D <sub>s</sub> (m)	Buoy Diameter, D <sub>b</sub> (m)	Diameter Ratio, D = D <sub>s</sub> /D <sub>b</sub>
Skirt 1	13.90	10.0	1.39
Skirt 2	12.90	10.0	1.29
Skirt 3	11.90	10.0	1.19

3 has higher bending moment profile than that of Case 2, and the least bending moment is Case 1. The hose curvature in the normal operation shown in Figure 30(a,b) shows a lower profile than the hose curvature in accidental operation in Figure 30(c,d). It was recorded that Case3 has higher curvature profile than of Case 2, and the least curvature is Case 1. However, the curvatures obtained are still within the safe limit of less than 2.0 m as recommended in OCIMF (2009) industry standard. In a similar manner, the hose effective tension in the normal operation shown in Figure 31(a,b) shows a lower profile than the hose effective tension in accidental operation in Figure 31 (c,d). It was recorded that Case 3 has a higher effective tension profile than that of Case2, and the least effective tension is the Case1. Thus, it can be deduced that the hose performance is affected by disconnection-induced loads, however a fatigue study and local design are recommended on this to evaluate the extent of damage on the hose. It can be also be observed that the effective tension profiles at the ends are higher than at midpoints of the floating hoses, and at disconnection, the profile increases and has a transfer of tension in the opposite direction, which is typically represented as given in Section 2.5. Thus, it would be necessary to ensure that reliable and welltested marine breakaway couplings are used during disconnection.

# 4.2.2. Submarine hose load response in Chinese-lantern configuration

The investigation on the disconnection-induced load on the submarine hoses in Chinese lantern configuration was investigated and the results are presented in Figure 32. This was also investigated by considering the  $DAF_{hose}$ , as proposed by Amaechi, Wang, Hou, et al. 2019. The hose curvature for the accidental operation has higher curvature than the normal operation in Figure 32(a). It was also observed in Figure 32 (b) that the curvature  $DAF_{hose}$  for the normal operation is also lower than that of the accidental operation. In a similar manner, the hose effective tension for the accidental operation



Figure 27. CALM buoy of skirt diameter (a) Ds<sub>1</sub>=13.90m (b) Ds<sub>2</sub>=12.90m and (c) Ds<sub>3</sub>=11.90m. (This figure is available in colour online.)



(a) Effect of buoy skirt diameters on Surge RAO

(b) Effect of buoy skirt diameters on Radiation Damping

Figure 28. Influence of buoy skirt diameters. (This figure is available in colour online.)



Figure 29. Result of the hose bending moment during (a-b) normal operation and (c-d) accidental operation. (This figure is available in colour online.)



Figure 30. Result of the hose curvature during (a-b) normal operation and (c-d) accidental operation. (This figure is available in colour online.)

has higher effective tension than the normal operation in Figure 32(c). It was also observed in Figure 32(d) that the effective tension  $DAF_{hose}$  for the normal operation is also lower than that of the accidental operation. Also, the hose bending moment for the

accidental operation has a higher bending moment than the normal operation in Figure 32(c). It was also observed in Figure 32 (d) that the bending moment  $DAF_{hose}$  for the accidental operation is also higher than that of the normal operation. As such, it is



Figure 31. Result of the hose effective tension during (a-b) normal operation and (c-d) accidental operation. (This figure is available in colour online.)



Figure 32. Effect of hydrodynamic loads on the submarine hose in Lazy-S config. (This figure is available in colour online.)



Figure 33. Effect of hydrodynamic loads on the submarine hose in Chinese-lantern config. (This figure is available in colour online.)

necessary that a good integrity check is carried out on the submarine hoses after any accidental operation, no matter how minimal it may appear, unless it is assessed to be within safe limits. In the profiles, the Chinese-lantern configuration for the bending moment and the curvature have a slightly similar profile but different magnitudes. However, this does not ascertain the configuration that is more affected by the disconnection-induced load effect, but it indicates the presence of some load response from the marine bonded hoses. This requires further investigation on fatigue study which is recommended and investigated in another study.

### 4.2.3. Submarine hose load response in Lazy-S configuration

The investigation on the disconnection-induced load on the submarine hoses in lazy-S configuration was investigated and the results are presented in Figure 33. This was also investigated by considering the  $DAF_{hose}$ , as proposed by Amaechi, Wang, Hou, et al. 2019. The hose curvature for the accidental operation has higher curvature than the normal operation in Figure 33(a). It was also observed in Figure 30(b) that the curvature  $DAF_{hose}$ for the normal operation is also lower than that of the accidental operation. In a similar manner, the hose effective tension for the accidental operation has higher effective tension than the normal operation in Figure 33(c). It was also observed in Figure 33(d) that the effective tension  $DAF_{hose}$  for the normal operation is also lower than that of the accidental operation. Also, the hose bending moment for the accidental operation has a higher bending moment than the normal operation in Figure 33(c). It was also observed in Figure 33(d) that the bending moment  $DAF_{hose}$  for the accidental operation is also higher than that of the normal operation. As such, it is necessary that a good integrity check is carried out on the submarine hoses after any accidental operation, no matter the magnitude unless it is



Figure 34. Curvature of submarine hose in Chinese-lantern configuration. (This figure is available in colour online.)

assessed to be within safe limits. In the profiles, the bending moment and the curvature have similar profiles under the lazy-S configuration but have different magnitudes (and units). However, this is different from the Chinese-lantern configuration in Section 4.2.2, where the bending moment and the curvature have inversely similar profiles and with different magnitudes and units. Although, it does not ascertain the configuration that is more affected by the disconnection-induced load effect, it indicates the presence of load response on the marine bonded hoses.

# 4.2.4. Wave load and flow angle analysis on bending moment

The effect of hydrodynamic loads was investigated for the submarine hoses under a water depth of 26 m, under Chinese-lantern configuration as it does not require much length in the investigation. The results presented in Figure 35(a-d) show the details on the configuration, and the profiles for the bending moment at two ends – End A and End B. The maximum bending moment was recorded at the hose ends. Also, the curvature is within the limit as recommended in the industry standard by OCIMF (2009). Thus, it shows that the designed submarine hose is fit for



Figure 35. Influence of RAO load on bending moment of submarine hose in Chinese-lantern configuration. (This figure is available in colour online.)



Figure 36. Tension region of submarine hose in Chines-lantern configuration. (This figure is available in colour online.)

the designed application. As can be observed in Figure 34, the curvature of the hose from the bending moment is within the design limit as specified in OCIMF (2009). The hose curvature has been induced by the wave and current loads as well as other hydrodynamic loads. As recorded in Figure 35, it can be observed that the SeaState3 reflected the highest bending moment magnitudes over the SeaState2 and SeaState1. This is due to the higher frequency of the SeaState3 and the significant wave height being of higher value than the others. A comparative study on the model by including RAOs as given in Figure 35 shows that the hydrodynamic load affects the performance of the marine bonded hoses. In addition, it was recorded that across the varying flow angles investigated, that the case of flow angle 180° was the highest. However, it is also relatively dependent on the RAO loads as seen too. Thus, the RAO loads and the wave angles are key parameters that influence the load response of the marine bonded hoses. As observed in the tabulated hose bending characteristics, it can be observed that the bending moment profiles shows that the hydrodynamic loads influence the motion behaviour of the submarine hoses. It is evidently clear too that the SeaState3 reflected the highest bending moment magnitudes over the SeaState2 and SeaState1. This is due to the higher frequency of the SeaState3 and the significant wave height being of higher value than the others. Based on the statistical analysis, the 90° flow angle gave the least deviation in bending moment in all the three sea states. This is due to the flow being in line with the wave direction. But for perpendicular flows in 0° and 180°, the bending moments have higher deviations. Thus, the study is highly indicative of high bending moment across the different flow angles investigated, especially along the hose arc lengths that have maximum curvatures. Thus, it is recommended to dampen the hose sections around those regions that recorded high bending moments, such as increasing the damping coefficients.

#### 4.2.5. Wave load and flow angle analysis on effective tension

The effect of hydrodynamic loads was investigated for the submarine hoses under a water depth of 26m, under Chinese-lantern configuration as it does not require much length in the investigation. The results presented in Figure 37(a-d) shows the details on the configuration, and the profiles for the effective tension at two ends – End A and End B. The maximum effective tensions were recorded at the hose ends. Also, the tension recorded is within the limit as recommended in the industry standard by OCIMF (2009). Thus, it shows that the designed submarine hose is fit for the designed application. As can be observed in Figure 36, the region of the hose-string that is most susceptible to high tension is close to the manifolds, as depicted. As recorded in Figure 37, it was recorded that the SeaState3 reflected the highest bending moment magnitudes over the SeaState2 and SeaState1. This is due to the higher frequency of the SeaState3 and the significant wave height being of higher value than the others. Furthermore, it was recorded that across the varying flow angles investigated, that the case of flow angle 180° was the highest. However, it is also relatively dependent on the RAO loads as seen too. Thus, the RAO loads and the wave angles are key parameters that influence the load response of the marine bonded hoses. In conclusion, the effective tension plots in Figure 37 shows that the tension profiles reflect that the hydrodynamic loads have an effect on the submarine hoses. It is evidently clear too that the SeaState3 reflected the highest bending moment magnitudes over the SeaState2 and SeaState1. This is due to the higher frequency of the SeaState3 and the significant wave height being of higher value than the others. The hose tension has been induced by the wave and current loads as well as other hydrodynamic loads. In addition, when such happens, the hoses twist or experience some torsion which in turn induces high tension. In that light, the hoses begin to experience high fatigue from the induced loadings. Another scenario for the induced loadings is during the disconnection, where the disconnectioninduced loads induce some fatigue on the marine hoses. In summary, the study is highly indicative of high tensions across the different flow angles investigated. Thus, it is recommended to reinforce those regions with reinforced ends to offset the high tensions recorded.

#### 4.3. Discussion

The investigation on the hydrodynamic analysis has shown the existence of disconnection-induced load response on the CALM buoy hose system and presented some comparative profiles for two different hoses- the floating hoses and the submarine hoses. It was observed that there is the presence of disconnection-induced loading from the comparative study between normal operation and accidental operation. There was also a comparison in the influence of the designs using Lazy-S and Chinese-lantern configurations on submarine hoses. It was also observed that there had different profiles that were inversely similar. Also, the magnitudes of the bending moment, curvature, and effective tensions were not the



Figure 37. Influence of RAO load on effective tension of submarine hose in Chinese-lantern configuration. (This figure is available in colour online.)

same. On the aspect of investigating the most affected configuation, it was concluded that further research on the fatigue study of the marine hoses is conducted. On the part of the statistical analysis on the submarine hoses and the buoy motion, there were good findings that suggest that the hoses were fit for use as they passed the recommendations of the industry standard (OCIMF 2009). In addition, the profiles presented on the wave loads and the flow angles showed that the hydrodynamic analysis on the marine bonded hoses had good correlations for the parameters investigated.

# 5. Conclusion

The hydrodynamic analysis on disconnection-induced load response of marine bonded hoses during normal operation and accidental operation under irregular waves has been presented in this paper. The study involves numerical investigation on the CALM buoy and the marine bonded hoses attached to it. Two hoses were applied in the model: the floating hoses and the submarine hoses. Some presentations made on the mathematical formulations include the wave theory, the BEM, hydrodynamics equations, catenary equations, and the equations on marine hoses and marine risers. Detailed numerical investigation on CALM buoys with submarine hoses in two configurations: Lazy-S and Chinese-lantern, were conducted. The hydrodynamic panel was developed in ANSYS AQWA and computed using diffraction theory and JONSWAP Wave Spectrum for the three (3) environmental conditions used (). The boundary conditions considered for the submarine hoses were attached on the PLEM and hose manifold underneath the CALM buoy. The RAOs calculated were then coupled into the Orcaflex FEM model developed based on Orcaflex Line theory. This proposed line theory uses the nodes on the hoses and mooring lines, but applies some discretization for the CALM buoy, to ensure less computational time and resources, and has been validated in an earlier study (Amaechi, Wang, Hou, et al. 2019).

The model highlights the following: firstly, novelty in disconnection-induced load response on marine bonded hoses under different ocean conditions and normal and accidental operations. Secondly, wave load and flow angle analysis on bending moment and effective tensions under irregular waves. Thirdly, a novelty in hydrodynamic studies on the hose disconnection studies for Lazy-S and Chinese-lantern configurations using water waves. Fourthly, the effect of different hose parameters hydrodynamic loads on hose profiles for bending moment, curvature, deflection, and effective tension on hose behaviour. Lastly, the effect of wave loads on buoy motion response from the diffraction analysis, and validation using statistical analysis. This study is important in enabling designers to design appropriately based on the hose behaviour, buoy geometry and environmental data.

The study presented a detailed investigation on the effect of disconnection-induced loads on the marine bonded hoses, and presented profiles for the normal operation and accidental operation for floating hoses and submarine hoses in Lazy-S, and for submarine hoses in Chinese-lantern configurations. It was observed that the accidental operation which was the case during disconnection of hose from the CALM buoy and the FPSO tanker showed good results as predicted. Thus, extra checks must be taken to ensure that the hoses have reliable marine breakaway couplings (MBCs) and hose end valves (HEVs). Also, it is recommended to reinforce the hoses towards ends that record very high tensions. On the buoy study, the motion was a function of the wave loads, such as in the surge RAO magnitudes. It would be recommended to have some floats around the buoy to reduce the vortex effect around it, and to reduce its damping or use strakes, and pneumatic fenders. However, further investigation using CFD is recommended. On the aspect of investigating the most affected configuration, it was concluded that further research on the fatigue study of the marine hoses is conducted. On the aspect of the statistical analysis on the submarine hoses and the buoy motion, the findings suggest that the hoses were fit for use as they passed the recommendations of the industry standard (OCIMF 2009). In addition, the profiles presented on the wave loads and the flow angles showed that the hydrodynamic analysis on the marine bonded hoses had good correlations for the parameters investigated. Further investigation on model tests in large scale can be conducted for the disconnection-induced load effect on a CALM buoy hose system. In addition, a detailed study on the motion response of the CALM buoy is recommended.

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## Data availability statement

The raw/processed data required to reproduce these findings cannot be shared at this time as the data also forms part of an ongoing study.

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