A 0.35 THz Extended Interaction Oscillator based on Overmoded and Bi-Periodic Structure

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A 0.35 THz Extended Interaction Oscillator based on Overmoded and Bi-Periodic Structure

Che Xu, Lin Meng, Claudio Paoloni, Yu Qin, Liangjie Bi, Bin Wang, Hailong Li, and Yong Yin

Abstract—An improved topology of Extended interaction oscillators (EIO) is presented with enhanced efficiency at 0.35 THz. A bi-periodic ladder-type structure is used for optimizing the performance of the TM31-2π mode operation. The proposed topology is based on bi-periodic interaction gaps composed by staggered short and long slots. The bi-periodic interaction mechanism permits to operate the circuit with a standing-wave field between the π and 2π modes, thus providing the potential to combine the advantages of both π and 2π modes in terms both of coupling and output performance. The resulting transverse TM31 operating mechanism exhibits a good agreement with bi-periodic structure in terms of coupling performance, with the short slot length positively correlated with the value of effective characteristic impedance $M^e R/Q$. The optimization of $M^e R/Q$ and $Q_e$, the circuit demonstrates attractive coupling and output characteristics. A state-of-the-art value $M^e R/Q$ of 59.69 Ω and a moderate $Q_e$ of 2523.52 are achieved for the proposed ladder-type EIO. A RF power of 540 W is obtained with a 42.5 kV, 0.6 A sheet beam, with 2.1% electronic efficiency at 0.35 THz.

Index Terms—Extended interaction oscillator (EIO), terahertz sources, vacuum electronics, bi-periodic structure.

I. Introduction

TERAHERTZ vacuum electronic devices (VEDs) are highly potent radiation sources known, which promise to enable higher power and efficiency than laser or semiconductor sources [1-5]. Among such devices, compact and powerful extended interaction devices (EIDs) have shown great potential in plasma diagnostics, spectroscopy, and military applications due to their high gain per unit length [1, 6-12]. With the characteristics of both slow-wave structure (SWS) and coupled cavities, extended interaction oscillator and extended interaction klystron (EIO & EIK) combine the advantages of traveling wave tubes (TWTs) and conventional multi-cavity klystrons.

Modern EID technology is demonstrated from 17 to 280 GHz, with the capability to approaching 1THz [1]. On the basis of the conventional-transverse 2π operation mode, EIDs have also evolved into higher-order modes in longitudinal (π mode) and transversal (TM31 modes) directions. Generally, 2π mode EID is able to delivering high values of characteristic impedance $R/Q$, which compensate the ohmic loss at the increase of frequency. This is of importance for improving the electronic efficiency in THz band. For example, a 0.34 THz, TM31-2π mode EIK shows an electronic efficiency of 1.3% [13]; a 0.67 THz multi-cavity EIK has an efficiency goal of 0.5% [2]; and a 0.35 THz high-order-mode EIO has a predicted electronic efficiency of ~1% [3]. On the other hand, better coupling capabilities and mode isolation for the π-mode are major advantages. As a reference, a G-band bi-periodic EIK with a high value $M^e R/Q$ of 29.34 Ω [14] demonstrated an efficiency target of 7.9% for stable operation in π-mode. The term $M^e$ refers to coupling coefficient. The effective characteristic impedance $M^e R/Q$ is the key parameter of EID technology [10]. To note that the more established 2π-mode operation has stable output characteristics but suffers from a lower coupling coefficient, while the π-mode usually exhibits high values of $Q_e$, the ratio of cavity energy storage to external circuit losses, and is therefore difficult to output because of the reduced weighting for the external circuit losses. The term $Q_e$ is the external quality factor.

Based on the above-mentioned electronic performances of π and 2π mode devices, the paper proposes a bi-periodic RF circuit with overmoded structure utilizing both π and 2π mode operation mechanisms. The proposed structure will show the following advantages.

Firstly, the transversal higher-order-mode scheme with TM31 distribution is adopted. In THz region, non-Brillouin thermal beam has a scalloped amplitude on the order of sub-millimeter wavelengths and the expansion of the longitudinal electron velocity prevents effective modulation [1]. Thus, an over-dimensioned high-order-mode structure is employed in order to overcome the size limitation of micro-circuits and to meet the requirements of high filling factor (beam current). Secondly, a strongly coupled 2π mode is established with a field distribution intermediate between conventional π and 2π modes. This will allow a trade-off between the stable output performance for the 2π mode and the high coupling characteristics for the π mode. Thirdly, the combination of an overmoded structure and a bi-periodic structure demonstrates...
strong coupling ability with a relatively higher $M^2 R/Q$ value (59.69 Ω) compared to other reported ladder-type EIDs [14-19]. For reference, the $M^2 R/Q$ values of several EIDs are listed in Table I.

This paper will discuss on the electronic characteristics of the proposed circuit and its potential to powerful THz EIDs through numerical simulations.

### II. CIRCUIT DESCRIPTION AND STABILITY ANALYSIS

**Fig. 1.** (a) The cross-sectional schematic diagram of the EIO structure in x-z plane and (b) a schematic of its 3D model.

**Fig. 2.** The cross-sectional schematic diagrams of the EIO structure in (a) y-z plane, and (b) x-y plane. Their z-directional electric field components, $E_z$, are represented as color mapping.

![Cross-sectional schematic diagram of the EIO structure](image)

Table I: Basic Parameters of Several Typical Reported EIDs

<table>
<thead>
<tr>
<th>Reference</th>
<th>Device</th>
<th>Operation mode</th>
<th>Frequency (GHz)</th>
<th>$M^2 R/Q$ (Ω)</th>
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<tr>
<td>[14]</td>
<td>EIK</td>
<td>$\pi$</td>
<td>219</td>
<td>29.34</td>
</tr>
<tr>
<td>[15]</td>
<td>EIO</td>
<td>$2\pi$</td>
<td>34</td>
<td>21.01</td>
</tr>
<tr>
<td>[16]</td>
<td>EIK</td>
<td>$\pi$</td>
<td>220</td>
<td>$\sim$15</td>
</tr>
<tr>
<td>[17]</td>
<td>EIK</td>
<td>$\pi$</td>
<td>35</td>
<td>$\sim$6</td>
</tr>
<tr>
<td>[18]</td>
<td>EIK</td>
<td>$2\pi$</td>
<td>94</td>
<td>$&lt;51$</td>
</tr>
<tr>
<td>[19]</td>
<td>EIO</td>
<td>$2\pi$</td>
<td>94</td>
<td>$\sim$22</td>
</tr>
<tr>
<td>This paper</td>
<td>EIO</td>
<td>$2\pi$-like</td>
<td>352</td>
<td>59.69</td>
</tr>
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</table>

Typically, for a $2\pi$ mode operation, there is a $2\pi$ phase difference between the adjacent long slots which are also isolated from each other. In this case, the interaction gaps can be considered as rectangular waveguides that transmit TE$_{10}$ waves [19]. Therefore, the cutoff frequency for such TE$_{10}$ wave is determined by the long-side widths, for instance, $g x l$ and $g x 2$ (in Fig. 1). If the long-side width decreases, the cutoff frequency of this rectangular waveguide increases and will exceed 0.35 THz when $g x$ is less than 0.43 mm. At this point, we place short slots (less than 0.43 mm in width) between the long slots, and the $\pi$-phase electric field between adjacent $2\pi$-phase fields will be expected to show weak transmission characteristics. The simulated cavity $E_z$ distribution is consistent with the above analysis, as shown in Fig. 2(a), the introduction of such a bi-period topology allows for the existence and propagation of a weak $\pi$-phase electric field in the short slots. In addition, the introduction of the short slot mechanism only increases the number of gaps and does not increase the machining accuracy requirements.

Each part of the circuit is designed to meet machining requirements of the UV-LIGA technique and electric discharge machining (EDM) [21, 22]. The overall length of the SWS is maintained below 3 mm and common sets of magnets are used with magnetic fields of approximately 1 T.

Fig. 3 shows the dispersion diagram of the proposed circuit with/without short slot structure. The period length $p$ is set at 0.15 mm synchronised with a beam voltage of ~42 kV. From the diagram, the TM$_{31}$ mode of the bi-period circuit provides higher-frequency 354.25 GHz compared to the TM$_{11}$ mode at 307.65 GHz. Furthermore, with the specific bi-period design as described above, the dispersion characteristics of the circuit show a significant difference from the conventional single-period structure. Fig. 3 shows that the beamline relative to the synchronous condition crosses both $2\pi$ and $3\pi$ points in the case of single period, thus predisposing to parasitic mode competition. In contrast, the bi-period mechanism utilizes $\pi$-mode dispersion characteristics to keep the parasitic modes (such as $3\pi$ mode) away from beamline, and more difficult to be excited. This selective mode isolation ensures stable operation at low noise levels.

The designed bi-periodic cavity possesses a number of discrete frequencies provided by the number of half-wavelengths between the end walls of the cavity, where TM$_{31}$-($2\pi$-1) and TM$_{11}$-2$\pi$ points are adjacent to the beam line.
TABLE II

<table>
<thead>
<tr>
<th>Mode</th>
<th>Frequency (GHz)</th>
<th>R/Q (Ω)</th>
<th>Q_e</th>
<th>M'/R'Q/ (Ω)</th>
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<tr>
<td>TM_{11}-2π</td>
<td>354.25</td>
<td>139.39</td>
<td>980.29</td>
<td>59.69</td>
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<tr>
<td>TM_{11}-2π-1</td>
<td>358.22</td>
<td>111.36</td>
<td>999.20</td>
<td>44.38</td>
</tr>
<tr>
<td>TM_{11}-2π</td>
<td>307.65</td>
<td>184.57</td>
<td>949.35</td>
<td>21.01</td>
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![Normalized g_e as a function of beam voltage U_b for the TM_{31}-2π, TM_{31}-2π-1, and TM_{11}-2π modes in the bi-periodic structure.](image)

Fig. 4. Normalized $g_e$ as a function of beam voltage $U_b$ for the TM_{31}-2π, TM_{31}-2π-1, and TM_{11}-2π modes in the bi-periodic structure.

in Fig. 3. A distinguishing characteristic for an oscillation mode is the existence of an absolute resonance threshold, for instance a voltage range, above or below which the cavity will not oscillate. Once the resonance condition is satisfied, undesired mode-competitions caused by TM_{31}-2π-1 and TM_{11}-2π modes may occur. When considering the beam loading in the circuit, the normalized beam-loading conductance $g_e$ is a key factor in the discussion of oscillation or amplification. A negative value of $g_e$ can satisfy the oscillation state. In this case, the energy exchange between the electron beam and circuit is such that the net energy flows to the circuit, which would form an oscillating positive feedback loop unless it is sufficiently loaded or sufficiently lossy. The normalized beam-loading conductance $g_e$ can be obtained from [22, 23]

$$g_e = \frac{1}{8} \beta^2 \left[ \left| M^2(\beta_e - \beta_q) \right| - \left| M^2(\beta_e + \beta_q) \right| \right], \quad (1)$$

where $M$ can be expressed by [23, 24]

$$M(\beta_e \pm \beta_q) = \int_{-\infty}^{\infty} E(z)e^{i(\beta_e \pm \beta_q)z} dz. \quad (2)$$

$\beta_e$ and $\beta_q$ are the propagation constants for DC beam and reduced plasma, respectively. The variation of $g_e$, with voltage of the TM_{31}-2π, TM_{31}-2π-1, and TM_{11}-2π modes are shown in Fig. 4, with their characteristic parameters shown in Table II. When the beam voltage is in the range of 37.5 to 45.7 kV, the oscillation conditions for the TM_{31}-2π-1 and TM_{11}-2π modes will not be satisfied ($g_e$ is positive), as shown in Fig. 4. This will ensure stable single-mode operation of the TM_{31}-2π mode synchronized with ~42 kV. However, as shown in Fig. 4, once the voltage has shifted outside the above-mentioned voltage range, the undesired TM_{31}-2π-1 mode is also potentially excited, and thus, operations in Region I and II should be avoided.

III. SIMULATIONS AND ANALYSIS

Extensive 3-D simulations and calculations for the proposed structure have been performed by CST-Microwave Studio [25] to demonstrate its behaviour and establish the strong coupled 2π mode. Copper is used as lossy metal material. The characteristic parameters $Q_e$ and $M'/R'Q$ as a function of length factor $\alpha = gx2/gx1$ are shown in Fig. 5(a) and 5(b), $Q_e$ is the ratio of cavity energy storage to external circuit losses. $R/Q$ [11, 23, 24] can be expressed by

$$R/Q = \frac{\left( \int_{-\infty}^{\infty} |E_z| dz \right)^2}{2\nu W}, \quad (3)$$

where angular frequency $\nu$ and total energy storage $W$ are the measure of $E_z$ field.

Three structures based on different length factor $\alpha$ were analyzed (results in Fig. 5). Case A (single-period, $\alpha$ less than 0.24), B (staggered bi-period, $\alpha=0.8$), and C (uniformed bi-period, $\alpha=1$), respectively, with their corresponding axial field components are shown in Fig. 6. Accordingly, their field distributions shift gradually with $\alpha$ from $2\pi$ to $\pi$ modes. From the definition of $Q_e$, a relatively small value of $Q_e$ risks reducing the energy storage in the cavity (represented by Case A in Fig. 5), while a too large $Q_e$ is highly detrimental to the RF output.

![Variations of (a) $Q_e$ and (b) $M'/R'Q$ for the proposed RF circuit as a function of length factor $\alpha$. In this case, the length of long slot, $gx1$, remains the same.](image)

![Axial electric field components of the beam axis at $\alpha$ less than 0.24 (Case A), equal to 0.8 (Case B), and equal to 1.0 (Case C).](image)
(represented by Case C). Nevertheless, this still suggests that the $2\pi$ mode (Case A) with a lower $Q_c$ value is more favorable for the output to the external circuit. From the other perspective, $M^\prime R/Q$, which is the key parameter of EID technology [10], appears to have a positive correlation with $\alpha$ (Fig. 5(b)). Such correlation not only implies that the structure A has an $M^\prime R/Q$ value greater than 34.81 $\Omega$, but also that at the increases of $\alpha$ (when the field profile approaching $\pi$ mode) a $M^\prime R/Q$ value could reach 109 $\Omega$, as shown in Fig. 5(b). Not only that, but the used TM$_{31}$ mechanism appears to be more compatible with the bi-periodic topology, in contrast to the TM$_{11}$ mechanism which provides an $M^\prime R/Q$ value below 30.90 $\Omega$ in Fig. 5(b). Where the value of $M^\prime R/Q$ is merely 21.01 $\Omega$ when $\alpha$=0.8. Similarly, for TM$_{11}$ coupling pattern, two recently reported bi-periodic EIKs for $\pi$-mode operation achieved $M^\prime R/Q$ values of $\sim$29.34 $\Omega$ [14] and $\sim$15.07 $\Omega$ [16], respectively.

From the above discussion, trade-offs should be made in obtaining favorable values of $M^\prime R/Q$ and $Q_c$. In the case C corresponding to $\pi$-mode, the near-infinite $Q_c$ leads to complete suppression of the output coupling, while the case A, corresponding to conventional $2\pi$-mode, restricts the increase of $M^\prime R/Q$. As a result, $\alpha = 0.8$ is adopted, with $M^\prime R/Q = 59.69$ $\Omega$ (Case B) with a modest $Q_c$ of 2523.52. In terms of electric field distribution, the wave-troughs amplitudes of $2\pi$-like field component established in Case B (Fig. 6) can be tuned to near zero, which is the physical mechanism that provides a larger coupling coefficient $M$ to establish the more idealized strong-coupled $2\pi$ mode (This can be derived by Eq. (2)).

To demonstrate the validity of the strong coupled $2\pi$ mode established in TM$_{31}$ operation mechanism, the 3D distributions formed by z-directional electric field components (E$_z$) are analyzed in Fig. 7(a) and 7(b), with length factors of $\alpha$=0.8 and $\alpha$=1 respectively. The 3D E$_z$ components at $\alpha$=0.8 are shown in Fig. 7(a), with a sinusoidal-like eight wave-crests and seven wave-troughs profile for the electric field along the beam tunnel. In short slots corresponding to the positions of wave-troughs, the uniform weak-$\pi$-phase fields can be observed, with the normalized amplitude defined as $A_1$. In long slots corresponding to the wave-crest, the $2\pi$-phase fields with normalized amplitude as $A_2 = 6A_1$ can play a major role in the speed modulation process. Such a sinusoidal-like profile of the electric field distribution is similar to the conventional $2\pi$ mode case at $\alpha$ less than 0.24 (consistent with Fig. 6), but the waveform has moved closer to the $\pi$-mode and therefore provides a relatively high coupling coefficient. In this case, standing wave field in the region of both two coupling cavities needs to accommodate standing-wave field for $\lambda_d/2$ in y-axis to successfully establish the TM$_{31}$ mode [20], where the waveguide wavelength $\lambda_d$ can be obtained by

$$\lambda_d = \frac{\lambda}{\sqrt{1 - (\lambda/\lambda_0)^2}}. \quad (4)$$

$\lambda$ and $\lambda_d$ are the free-space wavelength and cut-off wavelength of the coupling cavities, respectively. Therefore, the coupling cavity height $c_y$ should be slightly larger than $\lambda_d/2$ to ensure that the TM$_{31}$ field resonance conditions can be satisfied. After a long simulation work, a $c_y = 0.69$ mm was adopted, which is consistent with a value slightly larger than the calculated value of 0.65 mm for $\lambda_d/2$. As shown in Fig. 7(a), a standing wave field of $\lambda_d/2$ is excited in the coupling cavity, which represents successful establishment of the transversal over-dimensional TM$_{31}$ mode, and provides the favorable coupling condition for the output structure.

On the other hand, for Fig. 7(b) at $\alpha$=1, there is no standing wave field exists in the coupling cavity in the case of uniformed interaction gaps. Since the output structure extracts energy from the coupling cavity, this case is not conducive to energy coupling, which is consistent with the analysis in Fig. 5. From above, the analysis of 3D $E_z$ field components proves the validity of establishing a strongly coupled TM$_{31}$-$2\pi$ mode for a staggered bi-periodic structure.

Extensive particle-in-cell (PIC) simulations of the EIO have been carried out to demonstrate the performance of the circuit and its tolerance to injection conditions. The output power is extracted from a standard WR-2.8 waveguide through the coupling aperture which is above the middle of coupling cavity (Fig. 1). The stable output signal and particle energy distribution are obtained with an electron beam of 42.5 kV and 0.6 A, as shown in Fig. 8(a) and 8(b). A stable output power of 540 W and an electronic efficiency of 2.1% is obtained at 351.92 GHz. We have also considered the effect of copper surface roughness on the output in our calculations, and by slightly increasing the injection current we can achieve an efficiency comparable to that in Fig. 8(a). Fig. 9 shows the circuit output tolerance-performance as a function of the beam voltage and energy spread of the electron beam. Promising
characteristics were analyzed, showing the advantage of stable beam voltage and demonstrates a moderate tolerance compared to conventional EIO and shows a moderate tolerance for a THz interaction klystron at 0.34 THz.

In summary, these characteristics, with an electronic efficiency of 2.1%, the circuit has a slight additional processing difficulty and enhancing beam-wave interaction performance of THz-EIDs, especially for high-order (TM_{11}) mode operation.

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