A Compressive Sensing Assisted Massive 
SM-VBLAST System: Error Probability and 
Capacity Analysis

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Abstract—The concept of massive spatial modulation 
(SM) assisted vertical bell labs space-time (V-BLAST) 
(SM-VBLAST) system [1] is proposed, where SM sym-
bols (instead of conventional constellation symbols) are 
mapped onto the VBLAST structure. We show that the 
proposed SM-VBLAST is a promising massive multiple 
input multiple output (MIMO) candidate owing to its 
high throughput and low number of radio frequency 
(RF) chains used at the transmitter. For the gen-
eralized massive SM-VBLAST systems, we first derive 
both the upper bounds of the average bit error prob-
ability (ABEP) and the lower bounds of the ergodic 
capacity. Then, we develop an efficient error correction 
mechanism (ECM) assisted compressive sensing (CS) 
detector whose performance tends to achieve that of 
the maximum likelihood (ML) detector. Our simula-
tions indicate that the proposed ECM-CS detector is 
suitable both for massive SM-MIMO based point-to-
point and for uplink communications at the cost of a 
slightly higher complexity than that of the compressive 
sampling matching pursuit (CoSaMP) based detector 
in the high SNR region.

Index Terms—Spatial modulation (SM), Multiple-
Input Multiple-Output (MIMO), Vertical Bell Labs 
Space-Time (VBLAST), Compressive Sensing (CS), 
Average Bit Error Probability (ABEP), Capacity anal-
ysis.

I. INTRODUCTION

A. Background

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The massive multiple-input multiple-output (MIMO) 
transmission technique [2]-[3], which employs a mul-
tiplicity transmit/receive antennas has been considered to 
be one of the key techniques for future wireless communica-
tions. Three popular classes of massive MIMO commu-
nication scenarios have attracted attention [2]: point-to-
point (P2P) communication, where both the transmitter 
and receiver employ numerous antennas, as well as uplink 
(UL) and downlink (DL) communications, where many 
more antennas are employed by the base station (BS) than 
by the individual users. Conventional MIMO solutions, 
e.g., VBLAST and space-time block codes (STBC) [4] [6], 
tend to require a large number of radio frequency (RF) 
chains, hence imposing a substantial implementation cost 
and signal processing complexity in massive MIMO chan-
nels. In contrast, spatial modulation (SM) based MIMO 
systems [6]-[9], which employs the indices of the activated 
antennas as an additional means of implicitly conveying 
information, is a promising low-cost massive MIMO can-
didate for next generation wireless communications [10]-
[35].

The existing state-of-the-art of massive SM-MIMO sys-
tems is mainly focused on UL communications [11]-[25], 
where each user invokes SM to convey information and the 
BS employs multi-user detection to recover the transmit 
messages. Specifically, in [11]-[16], the advantages of mas-
sive SM-MIMO systems have been demonstrated in terms 
of their spectral-, energy- and cost-efficiencies. Message 
passing (MP) algorithms based multiuser detectors have 
been conceived [17]-[20] for massive SM-MIMO system-
s communicating both over narrowband and broadband 
channels. Furthermore, low-complexity compressive sensing 
(CS) detectors have been developed in [21]-[22], which 
exhibited a modest performance erosion. Recently, the 
performance of massive SM-MIMO systems have also been 
studied in the context of visible light [23], non-orthogonal 
multiple access (NOMA) [24] and physical layer encryption 
communication scenarios [25].

Massive SM-MIMO systems designed both for DL and 
P2P communication scenarios have been studied in [26]-
[35]. However, these systems are mainly designed for ac-
tivating only a few antennas. Naturally, the number of 
transmit antenna combinations (TACs) is determined by 
the number of antennas $N_u$ activated during each symbol 
slot. When both $N_u$ and the number of transmit antennas
(TA) \( N_t \) increases, finding an efficient bit-to-symbol mapping and demapping may not be easy for a high number of TACs [36]. To circumvent this issue, antenna group based massive SM-MIMO schemes have been developed independently in [1] and [35], where the TAs are divided into multiple small groups and SM is employed in each group. In this treatise we refer to the scheme of [1] as SM-VBLAST. In an SM-VBLAST system, the information bits are conveyed by \( N_u \) sub-indices (instead of a single activated index), hence the complexity of mapping and demapping is comparable to that of the conventional SM scheme. It has been shown in [1] that SM-VBLAST is capable of providing substantial performance gains over both the conventional generalized SM (GSM) [8] and the VBLAST systems at an identical number of RF chains. This compelling benefit equips the SM-VBLAST system with the unique ability to support massive MIMO based P2P, UL and DL communications.

B. Motivations and Contributions of This Work

Theoretical analysis of Average Bit Error Probability (ABEP) for massive SM-VBLAST is more complex than that for its small-scale counterpart. The ABEP upper bound of massive SM-VBLAST for \( M = 1 \), where \( \log_2(M) \) refers to the number of information bits sent by each SM symbol (in addition to that conveyed by the indices of the activated TAs), has been derived in [1]. In this case, each SM-VBLAST symbol is consisted of \( N_u \) Space Shift Keying (SSK) symbols. When \( M > 1 \), however, the derivation approach in [1] for the ABEP upper bound may not be applicable. The upper bound of the ABEP for small-scale GSM associated with \( M > 1 \) has been derived in [7], but the complexity of the ABEP calculation is in the order of \( 2^B \), where \( B \) denotes the transmit rate of the GSM system. For massive SM-VBLAST, for example, the value of \( B \) may be as high as 320 bits per channel use (bpcu) for the settings of \( N_t = 320, N_u = 80, M = 4 \), which makes the ABEP calculation prohibitively challenging.

To the best of our knowledge, the closed-forms of the Average Bit Error Probability (ABEP) expressions and the capacity of UL massive MIMOs relying on a large number of users have not been investigated. Although the ABEP of massive SM-MIMO supporting a low number of users has been studied in [17], it may not be straightforward to extend it to a large number of users and/or receiver antennas (RAs). In conventional GSM systems, the ergodic capacity performances have been studied in [37]-[38] for small-scale SM-MIMO only, but these approaches may not be suitable for the capacity analysis of massive SM-VBLAST.

Additionally, designing low-complexity CS capable of approaching the optimal performance at an acceptable complexity is still a challenging open issue [39]. It is worth pointing out that massive SM-VBLAST transmit signals exhibit inherent sparsity, which can be efficiently exploited by CS algorithms. The existing CS algorithms designed for massive SM-MIMO, such as Orthogonal Matching Pursuit (OMP) [40], Compressive Sampling Matching Pursuit (CoSaMP) [21] and MP [17]-[20] fail to strike an attractive performance vs. complexity trade-off. This motivates us to design an enhanced CS algorithm for massive SM-VBLAST systems.

Against the above background, the contributions of this paper are summarized as follows:

1) We analyze the ABEP of a massive SM-VBLAST system for generalized amplitude phase modulation (APM) schemes and derive a closed form ABEP upper bound for SM-VBLAST using low-order APM schemes, such as BPSK and QPSK.

2) We derive a lower bound of the ergodic capacity of massive SM-VBLAST systems and validate it through Monte Carlo simulations. Both our theoretical and simulation results indicate that the capacity of the massive SM-VBLAST system is significantly higher than that of the conventional VBLAST systems with an identical number of RF chains.

3) We develop an efficient Error Correction Mechanism (ECM) assisted CS detector for massive SM-VBLAST systems having large \( N_t \) and \( N_u \). Our proposed ECM assisted CS detectors are capable of approaching the error rate performance of the maximum likelihood (ML) detector by efficiently identifying and correcting the errors of the transmit indices encountered in the conventional CS detector at a low complexity.

4) We show that the closed-form ABEP expression derived and the ergodic capacity, as well as the ECM-CS detector are also applicable for UL massive SM-MIMO systems. We present the ABEPs of massive UL SM-MIMO systems having \( N_u = 40, N_r = 128 \) and \( N_u = 80, N_r = 256 \), where \( N_u \) and \( N_r \) are the number of users and the number of antennas in the BS, respectively. It is shown that the performance of our proposed ECM assisted CS detector approach that of the ML detector in these UL setups, despite only imposing a slightly higher complexity than that of the CoSaMP based detector.

5) We reveal that for a P2P communication system, the throughput of ECM-assisted massive SM-VBLAST can be hundreds or thousands bpcu but at a reduced number RF chains and a reduced complexity.

Notations: \(|\cdot|^2\) denotes the Frobenious norms of a matrix, while \(|\cdot|\) represents the magnitude of a complex quantity; \((\cdot)^T\) and \((\cdot)^H\) stand for the transpose and the Hermitian transpose of a vector/matrix, respectively. \(A \setminus B\) denotes removing the set \( B \) from the set \( A \) and \( A \cup B \) denotes adding the set \( B \) into the set \( A \).

II. MASSIVE SM-VBLAST SYSTEM

A. System model of P2P communication

The system model of the P2P SM-VBLAST system is shown in Fig. 1 (a). According to [1], the information bits of \( B = \sum_{l=1}^{N_u} B_l \) are partitioned into \( N_u \) (\( 1 \leq N_u \leq N_t/2 \)) groups. The \( l \)-th block of information bits \( B_l = \)
log₂(N_{l,s}^1) + log₂(M_l) can be mapped into a SM symbol having M_l-PSK symbols and N_{l,s}^1 TAs as
\[ x_l = \begin{bmatrix} 0, \ldots, 0, s_l, 0, \ldots, 0 \end{bmatrix}^T, \]
where q_l is the antenna index of the l-th SM symbol. Then, the transmitted signal can be expressed as
\[ x = [x_l^T, x_2^T, \ldots, x_{N_u}^T]^T = [0, \ldots, 0, s_1, 0, \ldots, 0, \ldots, 0, s_{N_u}, 0, \ldots, 0]^T. \]

The relationship between the l-th activated index k_l in x and q_l is expressed as
\[ k_l = \sum_{j=1}^{l-1} N_{s,m}^j + q_l. \]

Let H ∈ C^{N_r × N_t} and n ∈ C^{N_r × 1} be the MIMO channel matrix and noise matrix, whose entries have complex-valued Gaussian distributions of \( \mathcal{CN}(0, 1) \) and \( \mathcal{CN}(0, \sigma^2) \), respectively. The received signal y ∈ C^{N_r × 1} is written as
\[ y = Hx + n = H_A s + n, \]
where \( H_A = (h_{k_1}, h_{k_2}, \ldots, h_{k_{N_u}}) \) is the sub-matrix of H with \( N_u \) columns, and s = \( (s_1, \ldots, s_{N_u})^T \) is the transmit symbol vector corresponding to the TAC \( A = (k_1, \ldots, k_{N_u}) \).

According to [1], the optimal ML detector is formulated as
\[ (\hat{l}, \hat{s})_{ML} = \arg\min_{A \in \mathcal{A}, s \in \mathcal{S}} \| y - H_A s \|^2, \]
where \( \mathcal{A} \) is a TAC set having a size of \( N = \prod_{i=1}^{N_u} N_{s,m}^i \), and \( \mathcal{S} \) is the set of \( N_u \)-element symbol vectors.

### B. System model of UL communication

The system model of the UL SM-VBLAST system is shown in Fig. 1 (b). In UL communication, \( N_u \) denotes the number of users and \( N_{s,m}^l \) represents the number of TAs of the l-th user. Each user employs SM transmission using \( N_{s,m}^l \) TAs and \( M_l \)-PSK modulation. At the base station, the signal received by r-th (\( r = 1, \ldots, N_r \)) RA is expressed as
\[ y_r = \sum_{i=1}^{N_u} h_{r,i} x_l + n_r, \]

where \( h_{r,i} \in \mathbb{C}^{1 × N_{s,m}^l} \) can be considered as a subset of H of (4). The received signal of the base station in UL communication is \( \mathbf{Y} = [y_1, \ldots, y_{N_r}] \), which is the same as (4). Therefore, the ABEP analysis and signal detection in this paper are suitable for both P2P and UL communication. In order to make the system models more explicit, the notations of P2P and UL communication are concluded in Table I.

### III. GENERALIZED ABEP ANALYSIS OF MASSIVE SM-VBLAST SYSTEMS

In this section, the ABEP of massive SM-VBLAST associated with \( M_l > 1 \) is formulated as
\[ P_b = \frac{1}{2^{2B}} \sum_{i=1}^{2^B} \sum_{j \neq i}^{2^B} d(x^i, x^j) P(x^i \rightarrow x^j) \]
\[ \approx \frac{1}{2^B} \sum_{j=2}^{2^B} d(x^1, x^j) P(x^1 \rightarrow x^j), \]
where \( P(x^1 \rightarrow x^j) \) denotes the Pairwise Error Probability (PEP), \( d(x^i, x^j) \) is the Hamming Distance (HD) associated with the corresponding PEP event. Specifically, we have \( x^1 = [(x_{0,1}^1)^T, \ldots, (x_{N_u}^1)^T]^T \) and \( x^j = [(x_{0,1}^j)^T, \ldots, (x_{N_u}^j)^T]^T, j = (1, \ldots, 2^B) \), which are associated with information bits

\[ 1 \] Eq. (7) holds for BPSK, QPSK, as well as for gray coding aided \( M_l \)-PSK modulation. Hence, the ABEP analysis of this paper mainly aims for characterizing \( M_l \)-APM satisfying Eq. (7).
Table I
Notations for P2P and UL communication.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>P2P communication</th>
<th>UL communication</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_t$</td>
<td>The number of TAs</td>
<td>The number of TAs of all the users</td>
</tr>
<tr>
<td>$N_u$</td>
<td>The number of RF chains</td>
<td>The number of users</td>
</tr>
<tr>
<td>$N_{\text{TA}}^l$</td>
<td>The number of TAs of l-th level</td>
<td>The number of TAs of the l-th user</td>
</tr>
<tr>
<td>$k_l$</td>
<td>The index of the l-th activated TA</td>
<td>The activated TA index of the l-th user</td>
</tr>
<tr>
<td>$x_l$</td>
<td>The SM symbol of the l-th level</td>
<td>The transmit SM symbol of the l-th user</td>
</tr>
<tr>
<td>$N_r$</td>
<td>The number of RAs</td>
<td></td>
</tr>
</tbody>
</table>

as

$$b^1 = [0, 0, 0, 0, 0] \rightarrow x^1,$$

$$b^j = [c_1^j, c_2^j, \ldots, c_{N_u}^j] \rightarrow x^j. \quad (8)$$

According to [1], the PEP event can be defined as

$$P(x^1 \rightarrow x^j) = F(\tilde{\zeta}) = \gamma(\tilde{\zeta}) N_u \sum_{k=0}^{N_u-1} \left( \frac{N_r - 1 + k}{k} \right) [1 - \gamma(\tilde{\zeta})]^k, \quad (9)$$

where $\gamma(\tilde{\zeta}) = \frac{1}{2} \left( 1 - \sqrt{1 + \frac{2}{\tilde{\zeta}}} \right)$, and $\tilde{\zeta}$ is the mean value of $\zeta = ||Hx^1 - x^j||^2/2\sigma^2$ associated with $N_u = 1$ as

$$\tilde{\zeta} = E(\|H(x^1 - x^j)^2/2\sigma^2 | N_u = 1) = \|x^1 - x^j\|^2/2\sigma^2. \quad (10)$$

According to (8), there is only $T$ different values of $\tilde{\zeta}$ in (10) which are named as $\tilde{\zeta}_1, \ldots, \tilde{\zeta}_T$. Hence, Eq. (7) can be simplified to

$$P_b = D(\tilde{\zeta}_1)F(\tilde{\zeta}_1) + D(\tilde{\zeta}_2)F(\tilde{\zeta}_2) + \cdots + D(\tilde{\zeta}_T)F(\tilde{\zeta}_T), \quad (11)$$

where $D(\tilde{\zeta})$ denotes the Average HD (AHD) associated with $\tilde{\zeta}$. Since the values of $F(\tilde{\zeta}_1), \ldots, F(\tilde{\zeta}_T)$ are easy to calculate from (9), the calculation of $D(\tilde{\zeta}_1), \ldots, D(\tilde{\zeta}_T)$ is the key issue in the ABEP evaluation.

A. Generalized ABEP Analysis

According to (8), The HD between $x^l$ and $x^l$ $l = (1, \ldots, N_u)$ can be expressed as

$$d_{pq}^l = \text{setdiff}(b^l \setminus b^l) \in \{0, 1, \ldots, B_l\}, \quad (12)$$

where setdiff(x, y) is a function returning the difference between x and y, while $p_l = ||x^l - x^l||^2$ is expressed as

$$p_l = \begin{cases} \phi_{M_l}, & \text{if } q^l = q^j, \quad l = 1, \ldots, N_u, \\ 2, & \text{else} \end{cases}, \quad (13)$$

where $\phi_{M_l}$ denotes the Euclidean Distance (ED) between any two $M_l$-APM symbols. Upon considering BPSK and QPSK for example, $\phi_{M_l}$ is expressed as

$$\phi_{M_l} = \begin{cases} (0, 4), & \text{BPSK}, \\ (0, 2, 4), & \text{QPSK} \end{cases}, \quad (14)$$

Then the mean value of $\zeta$ and AHD are formulated as

$$\tilde{\zeta} = \|x^1 - x^j\|^2/(2\sigma^2) = \sum_{l=1}^{N_u} p_l/(2\sigma^2) = t/\sigma^2,$$

$$D(\tilde{\zeta}) = \frac{1}{\pi^2} \sum_{\forall(p_1, \ldots, p_{N_u} = 2l)} (d_{11}^p + d_{22}^p + \cdots + d_{N_u}^p). \quad (15)$$

Hence, how to find the common values of $\tilde{\zeta}$ and their corresponding HDs become the key issue in the calculation of $D(\tilde{\zeta})$. According to (14) and (15), there are some common values of $p_l$ in each level. Assuming that $N_{p_l}^l$ is the number of common values $p_l$, $l = 1, 2, \ldots, N_u$, (15) can be represented as

$$D_l(\tilde{\zeta}_l) = \sum_{i_l=1}^{N_{p_l}} \sum_{i_{N_u}=1}^{N_{p_N}} \sum_{i_l=1}^{N_{p_l}} \left( d_{p_l,i_l}^l + \cdots + d_{p_{N_u},i_{N_u}}^l \right) \frac{1}{B}, \quad (16)$$

with

$$N_{p_l} \sum_{i_l=1}^{N_{p_l}} \sum_{i_{N_u}=1}^{N_{p_N}} \left( d_{p_l,i_l}^l + \cdots + d_{p_{N_u},i_{N_u}}^l \right) = \prod_{l=2}^{N_u} N_{p_l} \sum_{i_l=1}^{N_{p_l}} d_{p_l,i_l}^l = \prod_{l=2}^{N_u} N_{p_l} \sum_{i_l=1}^{N_{p_l}} d_{p_l,i_l}^l,$$

$$= \prod_{l=2}^{N_u} N_{p_l} D_{p_l} + \prod_{l=1}^{N_u} D_{p_l}^{l+1} + \cdots + \prod_{l=1}^{N_u} D_{p_l}^{N_u} + \prod_{l=1}^{N_u} D_{p_l}^{N_u}, \quad (17)$$

where $D_{p_l}^l$ denotes the total HDs associated with $p_l$ as

$$D_{p_l}^l = \sum_{i_l=1}^{N_{p_l}} d_{p_l,i_l}^l. \quad (18)$$

As a result, the values of $N_{p_l}^l$ and $D_{p_l}^l$ become important for calculating (16), which are associated with specific antenna configurations. Considering BPSK and QPSK for example, we have $p_l = [0, 2, 4]$. The values of $N_{p_l}^l$ and $D_{p_l}^l$ can be obtained by

BPSK $\rightarrow \begin{cases} N_0^1 = 1, & D_0^1 = 0, \\ N_0^2 = 2(N_{17}^1 - 1), & D_0^2 = \sum_{b=1}^{B_1} bC_B^b - 1, \\ N_0^3 = 1, & D_0^3 = 1, \\ N_0^4 = 1, & D_0^4 = 0, \end{cases}$

QPSK $\rightarrow \begin{cases} N_0^2 = 4(N_{17}^1 - 1) + 2, & D_0^2 = \sum_{b=1}^{B_1} bC_B^b - 2 \\ N_0^4 = 1, & D_0^4 = 2. \end{cases}$

Based on the values of $N_{p_l}^l$ and $D_{p_l}^l$, the ABEP of the massive SM-VBLAST system using $M_l > 1$ is presented in Algorithm 1, where unique(-), find(-) and length(-) are the standard MATLAB functions.

In summary, for any $M_l$-APM symbol based massive SM-VBLAST system, the value of $N_{p_l}^l$ and $D_{p_l}^l$ can be obtained by (18). According to (9), (11), (16) and (17),...
the generalized ABEP of any \( M_0 \)-APM symbols can be calculated by Algorithm 1. Based on Algorithm 1, assuming that \( N_{\phi M_t} = \# \phi M_t \), the complexity order of the ABEP calculation is \( O(N_{\phi M_t}^4) \), which is independent of \( N_t \). As \( N_{\phi M_t} \) and \( N_u \) increase, the complexity of ABEP calculation still becomes excessive. Next, a closed form of the ABEP of massive SM-VBLAST associated with low-order APM symbols is derived.

B. Low-Complexity ABEP Analysis

In this section, the closed form of the ABEP upper bound is derived for massive SM-VBLAST using \( M_t = 2 \) and \( M_t = 4 \). For the cases of \( M_t > 4 \), the closed form of the upper bound becomes more complex and will be considered as our future work. Since \( \phi M_t = \{0, 2, 4\} \) holds true for \( M_t = 2 \) and \( M_t = 4 \), the value of \( t \in [1, \ldots, 2N_u] \) in (15) is dominated by the number of 0, 2, 4 in \( \{p_1, p_2, \ldots, p_{N_u}\} \). Assuming that \( \kappa_0, \kappa_2 \) and \( \kappa_4 \) are the total number of 0, 2, 4 in \( \{p_1, p_2, \ldots, p_{N_u}\} \), the relationship among them can be presented by

\[
2t = \sum_{i=1}^{N_u} p_i = 0 \times \kappa_0 + 2 \times \kappa_2 + 4 \times \kappa_4, \kappa_0 + \kappa_2 + \kappa_4 = N_u, \tag{19}
\]

hence we have \( \kappa_2 = t - 2\kappa_4, \kappa_0 = N_u - t + \kappa_4 \). For a certain combination of \( \kappa_2 \) and \( \kappa_4 \), there is a total of \( C_{N_u}^{\kappa_2} C_{N_u - \kappa_2}^{\kappa_4} C_{\kappa_0}^{\kappa_0} \) scenarios that satisfy (19). Considering \( N_u = 4, \kappa_2 = 2 \) and \( \kappa_4 = 1 \) for example, there are 12 scenarios having \( p_1 + p_2 + p_3 + p_4 = 8 \), which are...

Assuming that \( p_1 = \cdots = p_{N_u} \) = \( 2, p_{N_u+1} = \cdots = p_{N_u+k_4} = 4 \), according to (16)-(17), the HDs of one of the cases are expressed as

\[
H(\kappa_2, \kappa_4) = \sum_{i=1}^{N_u} \sum_{i_1=1}^{N_u} \sum_{i_2=1}^{N_u} \ldots \sum_{i_{\kappa_2+k_4}=1}^{N_u} \left( d_{i_1}^2 + \ldots + d_{i_{\kappa_2+k_4}}^2 \right) \cdot \prod_{u=2}^{N_u} N_{\kappa_2+k_4} D_{i_{u-1}} \cdot \prod_{u=\kappa_2+1}^{N_u} \prod_{i_{\kappa_2+k_4}+1}^{4} \prod_{i_{u}=1}^{N_u} \prod_{i_{u}=\kappa_2+1}^{4} N_{\kappa_2+k_4} D_{i_{u}} \cdot \ldots + \prod_{u=\kappa_2+1}^{N_u} N_{\kappa_2+k_4} D_{i_{u}}, \tag{21}
\]

Since there are \( C_{N_u}^{\kappa_2} C_{N_u - \kappa_2}^{\kappa_4} \) scenarios for this case, the total HDs associated with \( \sum_{i=1}^{N_u} p_i = 2\kappa_2 + 4\kappa_4 \) can be expressed as

\[
H^{\text{all}}(\kappa_2, \kappa_4) = \sum_{(i_1, \ldots, i_{\kappa_2+k_4})} \sum_{(i_{\kappa_2+k_4+1}, \ldots, i_{\kappa_2+k_4+1})} H(\kappa_2, \kappa_4), \tag{22}
\]

where \( I_{\kappa_2}^u \) denotes the Index Combination Set (ICS) that consists of choosing \( \kappa_2 \) indices from \( \{1, 2, \ldots, N_u\} \), while \( I_{\kappa_2+k_4}^u \) represents the ICS consisting of choosing \( \kappa_4 \) indices from \( \{1, 2, \ldots, N_u\} \setminus I_{\kappa_2}^u \). Taking \( N_u = 4, \kappa_2 = 2 \) and \( \kappa_4 = 1 \) for example, the sets \( I_{\kappa_2}^4 \) and \( I_{\kappa_2+k_4}^4 \) are expressed as

\[
I_{\kappa_2}^4 = \{ (1, 2), (1, 3), (1, 4), (2, 3), (2, 4), (3, 4) \}. \tag{23}
\]

The above HD analysis is based on a certain combination of \( \kappa_2 \) and \( \kappa_4 \). However, according to (19), different values of \( \kappa_2 \) and \( \kappa_4 \) can result in a common value of \( t \). Hence, the calculation of AHD \( D(\tilde{\kappa}) \) associated with the event \( \sum_{l=1}^{N_u} p_l = 2t \) will be determined by all the different combinations of \( \kappa_2 \) and \( \kappa_4 \). Next, how to obtain the combinations of \( \kappa_2 \) and \( \kappa_4 \) for different values of \( t \) will be discussed in four cases: 1) \( t \) is even with \( t \leq N_u; 2) \) \( t \) is odd with \( t \leq N_u; 3) \) \( t \) is even with \( t > N_u \) and 4) \( t \) is odd with \( t > N_u \).

**Case 1** - \( t \) is even with \( t \leq N_u \): For this case, the values of \( \left( p_{l_1}, \ldots, p_{l_{N_u}} \right) \) satisfying \( \sum_{l=1}^{N_u} p_l = 2t \) are given by

\[
\begin{align*}
&\left\{ p_{l_1}, \ldots, p_{l_{N_u}} \right\} : \quad \begin{cases}
2 \to \kappa_2 = t, & 0 \to \kappa_0 = N_u - t \\
4 \to \kappa_2 = (t+2), & 0 \to \kappa_0 = N_u - (t+2)
\end{cases}, \\
&\vdots \\
&\left\{ p_{l_1}, \ldots, p_{l_{N_u}} \right\} : \quad \begin{cases}
2 \to \kappa_2 = t, & 0 \to \kappa_0 = N_u - t \\
4 \to \kappa_2 = (t+2), & 0 \to \kappa_0 = N_u - (t+2)
\end{cases}.
\end{align*}
\tag{24}
\]

where \( l_1, \ldots, l_{N_u} \in \{1, N_u\} \). Observe from (24) that the
value of $\kappa_4$ ranges from zero to $t/2$. According to (19), (21), (22), the AHD of Case 1 is calculated by

$$D(\xi \leq N_u) = \frac{1}{B} \sum_{\kappa_4=0}^{t/2} H_{(\kappa_2,\kappa_4)}.$$

**Case 2 - t is odd with $t \leq N_u$**. For this case, the values of $(p_1, ..., p_{N_u})$ satisfying $\sum p_i = 2t$ are given by

$$\left\{ \begin{array}{l}
\{p_1, \ldots, p_{t/2}, p_{t+1}, \ldots, p_{N_u}\}, \\
2 \rightarrow \kappa_4 = t/2 \quad 0 \rightarrow \kappa_0 = N_u - t/2
\end{array} \right.$$

(26)

Observe from (26) that the value of $\kappa_4$ ranges from zero to $(t - 1)/2$. According to (19), (21), (22), the AHD of Case 2 is calculated by

$$D(\xi < N_u) = \frac{1}{B} \sum_{\kappa_4=0}^{(t-1)/2} H_{(\kappa_2,\kappa_4)}.$$

**Case 3 - t is even with $t > N_u$**. For this case, the values of $(p_1, ..., p_{N_u})$ satisfying $\sum p_i = 2t$ are given by

$$\left\{ \begin{array}{l}
\{p_{t/2}, \ldots, p_{t/2}, p_{t+1}, \ldots, p_{N_u}\}, \\
4 \rightarrow \kappa_4 = t/2 \quad 0 \rightarrow \kappa_0 = N_u - t/2
\end{array} \right.$$

(28)

Observe from (28) that the value of $\kappa_4$ ranges from $t - N_u$ to $t/2$. According to (19), (21), (22), the AHD of Case 3 is calculated by

$$D(\xi > N_u) = \frac{1}{B} \sum_{\kappa_4=t-N_u}^{t/2} H_{(\kappa_2,\kappa_4)}.$$

**Case 4 - t is odd with $t > N_u$**. For this case, the values of $(p_1, ..., p_{N_u})$ satisfying $\sum p_i = 2t$ are given by

$$\left\{ \begin{array}{l}
\{p_{(t-1)/2}, \ldots, p_{(t-1)/2}, p_{(t+1)/2}, \ldots, p_{N_u}\}, \\
4 \rightarrow \kappa_4 = (t-1)/2 \quad 2 \rightarrow \kappa_0 = N_u - (t+1)/2
\end{array} \right.$$

(30)

Observe from (30) that the value of $\kappa_4$ ranges from $t - N_u$ to $(t - 1)/2$. According to (19), (21), (22), the AHD of Case 4 is calculated by

$$D(\xi > N_u) = \frac{1}{B} \sum_{\kappa_4=t-N_u}^{(t-1)/2} H_{(\kappa_2,\kappa_4)}.$$

Furthermore, assuming that $N_{sm}^1 = N_{sm}^2 = \cdots = N_{sm}^{N_u}$ and $M_1 = M_2 = \cdots = M_{N_u}$, (25), (27), (29) and (31) can be further simplified as (32). According to (32), the closed form of the ABEP upper bound is given by (11).

**IV. CAPACITY ANALYSIS OF MASSIVE SM-VBLAST SYSTEM**

**A. Capacity analysis of conventional VBLAST system**

The receiver signal $Y_v \in N_{r} \times 1$ of a VBLAST system having $N_t$ TAs and $N_r$ RAs can be expressed as

$$Y_v = Hx_n + n,$$

where $x_n \in C_{N_t \times 1}$ denotes the transmit signal, while $H$ and $n$ have the same definition in (4). The capacity of VBLAST can be formulated as

$$C = I(x_v, y_v) = E \left\{ \log_2 [\det(I_{N_t} + \frac{\rho}{N_t}HH^H)] \right\},$$

where $\rho = 10^{SNR/10}$. According to [47], the lower bound of $C$ is expressed as

$$C \geq \frac{\mu \log_2}{N_t} \left[ 1 + \frac{\rho}{N_t} \exp \left( \frac{1}{\mu} \sum_{j=1}^{K-j} \frac{1}{j} - \gamma \right) \right],$$

(35)

where we have $\mu = \min(N_t, N_c)$, $K = \max(N_t, N_c)$ and $\gamma \approx 0.5772$.

**B. Capacity analysis of proposed massive SM-VBLAST system**

In this section, the capacity of the massive SM-VBLAST system is analyzed. According to [37]-[38], the Mutual Information (MI) between the input and output signal spaces can be expressed as

$$I(x, A, y) = E \left\{ \log_2 [\det(I_{N_t} + \frac{\rho}{N_t}H_AH_A^H)] \right\} +$$

$$\frac{1}{N} \sum_{i=1}^{N} E_y \left[ \log_2 \left( \frac{p(y|A)}{p(y)} \right) \right],$$

(36)

with

$$p(y|A) = \frac{1}{(\pi N_0)^{N_t}} \exp \left( -\frac{\|y - H_As\|^2}{N_0} \right)$$

(37)
According to (15), the value of symbols $\mathbf{x}$ and $\mathbf{F}$ The number of each value of $t$ expressed as $(P + \zeta)x_i \geq 2$, where $\mathbf{x}$ and $\mathbf{F}$ with $M = 1$, which can be computed by (9) also relying on [1]. As a result, the lower bound is expressed as $I[\mathbf{x}; \mathbf{y}|A] \geq \log_2 \left| \text{det} (I_{N_A} + \gamma \mathbf{H}_A \mathbf{H}_A^H) \right|$, + \frac{1}{N} \sum_{i=1}^{N} \sum_{k=1}^{N} P(\mathbf{x}^i \to \mathbf{x}^k|M = 1) \log_2 \frac{P(\mathbf{x}^i \to \mathbf{x}^k|M = 1)}{\sum_{m=1}^{N} P(\mathbf{x}^m \to \mathbf{x}^k|M = 1)}$,

where $P(\mathbf{x}^i \to \mathbf{x}^k|M = 1)$ denotes the PEP between $\mathbf{x}^i$ and $\mathbf{x}^k$ with $M = 1$, which can be computed by (9) also relying on [1]. As a result, the lower bound is expressed as $I[\mathbf{x}; \mathbf{y}|A] \geq \log_2 \left| \text{det} (I_{N_A} + \gamma \mathbf{H}_A \mathbf{H}_A^H) \right|$.

For a massive SM-VBLAST system, the value of $N$ is extremely large, hence the computational complexity of Eq. (41) becomes impractical. According to [1], there are some common values of $P(\mathbf{x}^m \to \mathbf{x}^k|M = 1)$ for different $n$ and $k$, so that (41) can be further simplified, which is introduced as follows.

For the case of $M = 1$, the activated TAC transmits all symbols '1', so that we have

$$\| \mathbf{x}_l^m - \mathbf{x}_l^k \|^2 = p_l = \begin{cases} 0, & \text{if } \mathbf{x}_l^m = \mathbf{x}_l^k, \ l = 1, \ldots, N_u, \\ 2, & \text{if } \mathbf{x}_l^m \neq \mathbf{x}_l^k, \ l = 1, \ldots, N_u. \end{cases}$$

(44)

The number of $p_l = 0$ and $p_l = 2$ can be expressed as $N_l^0 = 1, N_l^2 = 2^{B_l} - 1, l = 1, \ldots, N_u$. (45)

According to (15), the value of $\tilde{\zeta}_{(\mathbf{t}, M = 1)}$ is expressed as

$$\tilde{\zeta}_{(\mathbf{t}, M = 1)} = \frac{\| \mathbf{x}_l^m - \mathbf{x}_l^k \|^2}{2 \sigma^2} = \frac{t}{\sigma^2},$$

(46)

where $t$ is the number of nonzero elements in $(p_1, p_2, p_3, \ldots, p_{N_u})$ for this case. As a result, there are a total of $N_u^0$ different values of $F(\tilde{\zeta}_{M = 1})$ as $F(\tilde{\zeta}_{1, M = 1}), F(\tilde{\zeta}_{2, M = 1}), \ldots, F(\tilde{\zeta}_{N_u, M = 1})$. For each value of $F(\tilde{\zeta}_{(\mathbf{t}, M = 1)})$, the $t$ nonzero values can be expressed as $(p_{t_1} = \ldots = p_{t_t} = 2)$. More specifically, we have $(l_1, l_2, \ldots, l_t) \in I_{N_u}^t$, which indicates that the ICS consists of $t$ indices selected from $(1, 2, \ldots, N_u)$. For a certain combination of $(l_1, l_2, \ldots, l_t)$, there are a total of $\prod_{i=1}^{t} N_{l_i}^2$ cases to satisfy $(p_{t_1} = \ldots = p_{t_t} = 2)$. As a result, for a given value of $\mathbf{x}^n$, the total number $\varphi_t$ of $\mathbf{x}^n$ having the value of $\tilde{\zeta}_{(\mathbf{t}, M = 1)}$ is expressed as

$$\varphi_t = \begin{cases} C_{N_u}^t (2^{B_1} - 1)^t, & \text{if } B_1 = \ldots = B_{N_u}, \\ \sum_{(l_1, \ldots, l_t) \in I_{N_u}^t} \prod_{i=1}^{t} (2^{B_{l_i}} - 1), & \text{else.} \end{cases}$$

(47)

Since (47) satisfies

$$\sum_{t=1}^{N_u} \varphi_t = \sum_{t=1}^{N_u} \sum_{(l_1, \ldots, l_t) \in I_{N_u}^t} \prod_{i=1}^{t} (2^{B_{l_i}} - 1) = N - 1,$$

which is proved in Appendix, the value of

$$\sum_{t=1}^{N_u} \varphi_t = \sum_{t=1}^{N_u} \sum_{(l_1, \ldots, l_t) \in I_{N_u}^t} \prod_{i=1}^{t} (2^{B_{l_i}} - 1) = N - 1,$$

which is proved in Appendix, the value of

$$\sum_{t=1}^{N_u} \varphi_t = \sum_{t=1}^{N_u} \sum_{(l_1, \ldots, l_t) \in I_{N_u}^t} \prod_{i=1}^{t} (2^{B_{l_i}} - 1) = N - 1,$$

which is proved in Appendix, the value of

$$\sum_{t=1}^{N_u} \varphi_t = \sum_{t=1}^{N_u} \sum_{(l_1, \ldots, l_t) \in I_{N_u}^t} \prod_{i=1}^{t} (2^{B_{l_i}} - 1) = N - 1,$$

As a result, the lower bound of $I(A; \mathbf{y})$ is simplified as

$$\frac{1}{N} \sum_{i=1}^{N} \sum_{k=1}^{N} P(\mathbf{x}^i \to \mathbf{x}^k|M = 1) \log_2 \frac{P(\mathbf{x}^i \to \mathbf{x}^k|M = 1)}{\sum_{m=1}^{N} P(\mathbf{x}^m \to \mathbf{x}^k|M = 1)}$$

$$= \frac{1}{N} \sum_{i=1}^{N} \sum_{k=1}^{N} \left\{ \sum_{l \neq i} P(\mathbf{x}^i \to \mathbf{x}^k|M = 1) \log_2 \frac{P(\mathbf{x}^i \to \mathbf{x}^k|M = 1)}{\sum_{m=1}^{N} P(\mathbf{x}^m \to \mathbf{x}^k|M = 1)} \right\}$$

$$= \frac{1}{N} \sum_{i=1}^{N} \left\{ \sum_{l \neq i} \phi_l F(\frac{\zeta}{\sigma^2}) \log_2 \left[ NF(\frac{\zeta}{\sigma^2}) \right] \right\}$$

$$+ [1 - \sum_{l \neq i} \phi_l F(\frac{\zeta}{\sigma^2})] \log_2 \left[ NF(\frac{\zeta}{\sigma^2}) \right]$$

+ $[1 - \sum_{l \neq i} \phi_l F(\frac{\zeta}{\sigma^2})] \log_2 \left[ NF(\frac{\zeta}{\sigma^2}) \right]$.

(51)

According to (36), (39), (41) and (51), the closed form of the massive SM-VBLAST system capacity lower bound becomes

$$I[\mathbf{x}; \mathbf{y}|A] \geq \mu \log_2 \left[ 1 + \frac{\zeta}{\sigma^2} \exp \left( \frac{1}{\mu} \sum_{j=1}^{K-1} \frac{1}{\mu - \gamma} \right) \right]$$

$$+ [1 - \sum_{l \neq i} \phi_l F(\frac{\zeta}{\sigma^2})] \log_2 \left[ NF(\frac{\zeta}{\sigma^2}) \right]$$

$$+ \sum_{l \neq i} \phi_l F(\frac{\zeta}{\sigma^2}) \log_2 \left[ NF(\frac{\zeta}{\sigma^2}) \right].$$

(52)

V. EFFICIENT ECM ASSISTED COMPRESSIVE SENSING DETECTOR FOR MASSIVE SM-VBLAST SYSTEM

In this section, an efficient ECM assisted CS detector is designed for massive SM-VBLAST systems, which is shown in Fig. 2. A threshold is designed to judge whether
**Algorithm 2** The proposed ECM-CS detector for the Massive SM-VBLAST system

**Input:** $\hat{y}$, $\hat{H}$

**Output:** $x_o$

1. Obtain $\hat{x}^0$ by conventional CS algorithm and get the initial $R^0 = \|y - H\hat{x}^0\|^2$.
2. if $R^0 < V_{th}$ then
   3. $x_o = \hat{x}^0$, return;
4. else
   5. for $t \in (1, N_{iter})$ do
      6. $x_t = \hat{x}^{t-1}, R_t = R^{t-1}, \tilde{R}^t = \phi$;
     7. for $l \in (1, N_u)$ do
        8. Remove the $l$-th symbol from $\hat{x}^t$ as
           $\hat{x}_t^l = (\hat{x}_t^1, \cdots, \hat{x}_t^{l-1}, \hat{x}_t^{l+1}, \cdots, \hat{x}_t^{N_u})^T$;
        9. Get the residual vector $R^{l,t}$ by (54);
     10. $[L_o, v] = \arg\max_j (R^{l,t} \cdot \text{desender}^j)$;
     11. Get the first $m$ indices as $I_m = L_o(1 : m)$;
     12. Re-estimate the $l$-th symbol $\hat{x}_t^l$ as
          $\hat{x}_t^l = (\hat{x}_t^1, \cdots, \hat{x}_t^{l-1}, \hat{x}_t^l, \hat{x}_t^{l+1}, \cdots, \hat{x}_t^{N_u})^T$;
     13. Update the $l$-th residual vector as $\tilde{R}^{l,t} = y - H\hat{x}_t^l$;
     14. if $\|\tilde{R}^{l,t}\|^2 \leq V_{th}$ then
         15. $x_o = \hat{x}_t^l$, return;
     15. else
         16. $\tilde{R}^t = [\tilde{R}^t, \tilde{R}^{l,t}]$;
     17. end if
   18. end if
   19. $\|\tilde{R}_{min}^t\|^2 = \min(\|\tilde{R}_{min}^{l,t}\|^2)$ and get its corresponding estimated signal $\hat{x}_{min,t}$;
   20. if $\|\tilde{R}_{min}^t\|^2 = \|R_t\|^2$ then
     21. $x_o = \hat{x}_{min,t}$, return;
   22. else
     23. Update the signal residual vector as $x_t = \hat{x}_{min,t}$, $R_t = \tilde{R}_{min}$;
   24. end if
   25. end for
   26. end if
   27. $x_o = \hat{x}_{min,N_{iter}}$
   28. end if

the initial signal estimated by the conventional CS algorithm is reliable or unreliable. If it is judged to be unreliable, our ECM means is invoked to further test the estimated signal’s reliability. We will show that this ECM technique is also capable of correcting the erroneous indices.

### A. Proposed Detector

**Step 1:** As shown in Fig. 2(a), we first obtain the initial transmit signal $\hat{x}^0 = (\hat{x}_1^0, \cdots, \hat{x}_1^0, \cdots, \hat{x}_{N_u}^0)^T$ via the conventional CS algorithm.

**Step 2:** Determine whether the estimated signal is reliable or unreliable. If the ED of the estimated signal $(\Lambda, s)$ satisfies
\[
\|y - H\hat{x}^0\|^2 \leq V_{th},
\]

where $V_{th} = \beta N_u \sigma^2$, then $(\Lambda, s)$ is deemed to be the final detection result with $\beta$ being a constant. The choice of $\beta$ is analyzed in the threshold design part of Section V-B.

**Step 3:** Otherwise, the result $\hat{x}^0$ will be further judged to be either reliable or unreliable by our proposed ECM scheme. For the reliable result $\hat{x}^0$, it will be judged as the final result by calculating about $N_v m M$ EDs, where $m$ is a preset number to strike a performance vs. complexity trade-off. By contrast, for the unreliable result $\hat{x}^0$, it will be corrected by calculating about $n_e N_u m M$ EDs, where $n_e$ represents the number of errors that our ECM can correct.

### B. Proposed ECM Scheme

In the proposed ECM scheme, the $l$-th symbol $l = (1, \cdots, N_u)$ of the initial result $\hat{x}^0$ will be further judged to be either reliable or unreliable in the sequel. The total number of checking iterations is dominated by the value of $n_e$. Assuming that the $l$-th iteration result is $\hat{x}_t = (\hat{x}_1^t, \cdots, \hat{x}_1^t, \cdots, \hat{x}_{N_u}^t)^T$ associated with TAC index $\Lambda = (\hat{k}_1, \cdots, \hat{k}_{N_u})$ and symbol vector $\hat{s} = (\hat{s}_1, \cdots, \hat{s}_{N_u})$, the ECM operates as follows.

**Step 1:** As shown in Fig. 2(b), we first remove the $l$-th symbol $\hat{x}_l$ from $\hat{x}^t$ as
\[
\hat{x}^{t,l} = \hat{x}^t \setminus \hat{x}_l^t = (\hat{x}_1^t, \cdots, \hat{x}_t^{l-1}, \hat{x}_t^{l+1}, \cdots, \hat{x}_{N_u}^t)^T,
\]
where $O_{N_{iter}^{t,m}}$ de-
notes $N_s^l$ zeros. Assuming that $\Lambda = (k_1, ..., k_{N_a}), s = (s_1, ..., s_{N_c})$ are the accurate TAC index and symbol vector, two residual vectors in the $l$-th iteration are defined as

$$\mathbf{R}^l = y - \mathbf{Hx}^l = \mathbf{R}^l_1 + \cdots + \mathbf{R}^l_{l-1} + \mathbf{R}^l_{l+1} + \cdots + \mathbf{R}^l_{N_c},$$

$$\mathbf{R}^{l+1} = y - \mathbf{Hx}^{l+1} = \mathbf{R}^{l+1}_1 + \cdots + \mathbf{R}^{l+1}_{l-1} + \mathbf{R}^{l+1}_{l+1} + \cdots + \mathbf{R}^{l+1}_{N_c},$$

where $R^l_i = h_{k_i,s_i} - h_{k_i,s_i}$.  

**Step 2:** Re-estimate the $l$-th symbol as $\hat{x}^l_i$ based on the Multipath Matching Pursuit (MMP) algorithm [44]. Specifically, the new index $k_i$ and symbol $\hat{s}_i$ of the signal $\hat{x}^l_i$ can be estimated by

$$(k_i, \hat{s}_i) = \arg \min_{k_i \in I_m, \hat{s}_i \in S} \| \mathbf{R}^{l,t} - \mathbf{h}_k \hat{s}_j \|^2,$$  

where $S$ is the set of APM symbols and $I_m$ denotes the $m$-th possible candidates, which is obtained by

$$I_m = L_o(1 : m),$$

where $H^H_{[N_{n}]}$ denotes the $N_s^l$ rows of $H^H$ corresponding to the $l$-th symbol $\mathbf{x}$. 

**Step 3:** Update the estimated symbol as $\hat{x}^{l,t} = (\hat{x}^{l,t}_1, ..., \hat{x}^{l,t}_{l-1}, \hat{x}^{l,t}_l, \hat{x}^{l,t}_{l+1}, ..., \hat{x}^{l,t}_{N_c})^T$. 

**Step 4:** Update the residual vector based on the estimated result $\hat{x}^{l,t}$ as

$$\tilde{R}^{l,t} = y - \mathbf{H\hat{x}}^{l,t} = \mathbf{R}^{l,t} - \mathbf{h}_{k_i} \hat{s}_i.$$  

**Step 5:** Repeat Steps 1-4 and obtain $N_u$ residual vectors $\tilde{R}^t = [\tilde{R}^{1,t}, ..., \tilde{R}^{N_u,t}]$. Then find the minimum value of $\| \tilde{R}^t \|^2$ as $\| \tilde{R}^t \|^2$. 

**Step 6:** Judge the estimated result $\hat{x}^l$ to be reliable or unreliable using $\tilde{R}$. Specifically, if we have

$$\| \tilde{R}^t \|^2 < \mathbf{R}^t$$

it implies that there is no erroneous result in $\hat{x}^l$ and it will be considered as the final result. If we have

$$\| \tilde{R}^t \|^2 < \| \mathbf{R}^t \|^2$$

and $\| \tilde{R}^t \|^2 < V_{th}$, it means that there is only one erroneous result in $\hat{x}^l$ and it will be corrected in this step. Then the updated transmit signal $\hat{x}^{l+1,t}$ having the ED of $\| \tilde{R}^t \|^2$ is considered as the final result. Otherwise, there may be more than one erroneous result in $\hat{x}^l$ and the checking process will be continued. The updated transmit signal $\hat{x}^{l+1,t}$ will be considered as the initial result of the $(l+1)$-th iteration.

In conclusion, the proposed detector is summarized at a glance in Algorithm 2, where $N_{iter}$ means the number of iteration, which is usually smaller than $N_a$.

### C. Complexity Analysis

In this subsection, the complexity of the proposed detector designed for the massive SM-VBLAST system is analyzed in terms of the number of real-valued multiplications and additions [40]. For specific matrices $\mathbf{A} \in \mathbb{C}^{m \times n}$, $\mathbf{B} \in \mathbb{C}^{n \times p}$, $\mathbf{c} \in \mathbb{C}^{n \times 1}$ and $\mathbf{d} \in \mathbb{C}^{n \times 1}$, the operations of $\mathbf{AB}$, $\| \mathbf{c} \|^2_F$ and $\mathbf{c} \pm \mathbf{d}$ require $8mp - 2mp$, $4n - 1$, and $2n$ flops, respectively. According to (54)-(57), the complexity of the proposed detector can be expressed as

$$C_P = C_{CS} + 8N_u N_r(N_u - 1) N_{s}^{av} + N_{s}^{av} \sum_{l=1}^{N_u} 8N_t N_s^{l} + 10N_u N_r N_{s}^{av} + 10N_u N_r N_{s}^{av},$$

where $C_{CS}$ denotes the complexity of the conventional CS detector and $N_{s}^{av}$ denotes the average number of errors the ECM has corrected, which is smaller than $N_u$. In order to strike a performance vs. complexity trade-off, we opted for low complexity CS algorithms such as CoSaMP and OMP in the first step, whose complexity is expressed as:

$$C_{CoSaMP} = (12N_r - 1 + 8N_r N_t + 2N_t + 4K^3 + 12N_r K^2 + 7K^2 + 6N_r K) \omega_{C0},$$

$$C_{OMP} = N_u (2N_r N_t + 10N_r N_{s}^{sm} M),$$

where $K = 3N_u$ and $\omega_{C0}$ denote the average iterations in the CoSaMP algorithm.

### D. Performance Analysis for Our Proposed ECM assisted CS Detector

In this section, the performance of the proposed detector is analyzed. According to Algorithm 2, the BER performance of the proposed detector can be characterized as

$$P_e \approx 1 - \left(1 - P_r (\rho_e \leq V_{th})\right) \left(1 - P_{e ECM} \right) \left(1 - P_{e ML} \right),$$

where $P_{ML}$, $P(e \leq V_{th})$ and $P_{ECM}$ denote the error probability estimated by the ML detector of (59), by the threshold based decision of (53) and by the ECM detector of (55). For a given antenna configuration, the values of $P_{ML}$ are fixed. As a result, the performance of the proposed detector is mainly dominated by $P(e \leq V_{th})$ and $P_{ECM}$, which will be analyzed in detail as follows.

1) **Threshold Design**

According to [40], the ED between the estimated signal $\hat{x}$ and the receiver signal is expressed as

$$\rho = \| y - \mathbf{Hx} \|^2 = \| n \|^2,$$

$$\rho_e = \| y - \mathbf{Hx} \|^2 = \| \mathbf{H(x - \hat{x})} + n \|^2,$$

where $\hat{x}$ and $\hat{x}$ follow the Chi-square distribution with degree $2N_r$ as

$$\frac{2\rho}{\sigma^2} \sim \chi^2(2N_r), \quad \frac{2\rho_e}{\sigma^2 + \| x - \hat{x} \|^2} \sim \chi^2(2N_r),$$

whose Probability Density Function (PDF) is given by

$$f_{\chi^2(2N_r)}(x) = \left\{ \begin{array}{ll} \frac{1}{2^{N_r} \Gamma(N_r)} e^{-x/2} x^{N_r - 1}, & x > 0 \\ 0, & x \leq 0 \end{array} \right.$$ \hspace{1cm}(65)

As a result, the values of $P(e \leq V_{th})$ and $P(e \leq V_{th})$ can be obtained by

$$P(e \leq V_{th}) = \int_0^{2V_{th}} f_{\chi^2(2N_r)}(x) dx,$$

$$P(e \leq V_{th}) = \int_0^{2V_{th}} f_{\chi^2(2N_r)}(x) dx.$$
The value of $\rho$ and $\rho_e$ are encountered by (55), the new estimated index and symbol are $\hat{l}$ and $\hat{s}$, respectively. It is clear that the PDFs of $\hat{\rho}$ and $\rho_e$ are associated with different setups at 6 dB and 8 dB, respectively. It is clear that the PDFs of $\rho$ and $\rho_e$ are associated with specific setups and SNRs. If the threshold $V_{th}$ is set too small, even the most reliable signal will be judged to be unreliable, which may impose extra search complexity. By contrast, if the threshold $V_{th}$ is set too high, even an unreliable signal having one or two errors will also be judged to be reliable, which may result in erroneous detection. In this paper, the thresholds are set based on the ABEP, where the value of $\rho_e$ is close to the theoretical ML detector’s performance. Based on this design principle, the thresholds for the specific setups are presented in Table II.

### Table II

<table>
<thead>
<tr>
<th>$V_{th}$ design for specific setups.</th>
<th>$(N_t, N_u, N_r, M)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$(128, 16, 64, 4)$</td>
<td>$N_r \sigma_r^2$</td>
</tr>
<tr>
<td>$(128, 16, 128, 4)$</td>
<td>$0.925 N_r \sigma_r^2$</td>
</tr>
<tr>
<td>$(120, 30, 128, 4)$</td>
<td>$0.91 N_r \sigma_r^2$</td>
</tr>
<tr>
<td>$(160, 40, 128, 4)$</td>
<td>$0.91 N_r \sigma_r^2$</td>
</tr>
<tr>
<td>$(240, 60, 256, 4)$</td>
<td>$0.89 N_r \sigma_r^2$</td>
</tr>
<tr>
<td>$(320, 80, 256, 4)$</td>
<td>$0.89 N_r \sigma_r^2$</td>
</tr>
</tbody>
</table>

Assuming that $\rho_e^{n_e}$ represents the ED with $n_e$ errors in the estimated signal $\hat{x}_t$, Fig. 3 portrays the PDF of $\rho$ and $\rho_e$ associated with different setups at $6$ dB and $8$ dB, respectively. It is clear that the PDFs of $\rho$ and $\rho_e$ are associated with specific setups and SNRs. If the threshold $V_{th}$ is set too small, even the most reliable signal will be judged to be unreliable, which may impose extra search complexity. By contrast, if the threshold $V_{th}$ is set too high, even an unreliable signal having one or two errors will also be judged to be reliable, which may result in erroneous detection. In this paper, the thresholds are set based on the ABEP, where the value of $\rho_e$ is close to the theoretical ML detector’s performance. Based on this design principle, the thresholds for the specific setups are presented in Table II.

#### 2) Error Correction Mechanism

In this section, the performance of the ECM scheme has been analyzed.

**Case 1 - $n_e = 0$:** If the ED of the signal that was deemed reliable does not satisfy (53), then it will be judged to be reliable by the ECM of (58). Specifically, after removing the $l$-th symbol $\hat{s}_l$, the residual vector in (54) can be updated as $\hat{\mathbf{R}}^{l,t} = \mathbf{h}_{k_l} s_l + \mathbf{n}$. Assuming that no errors are encountered by (55), the new estimated index and symbol are $\hat{k}_l = k_l$ and $\hat{s}_l = s_l$. Then we will have $\hat{\mathbf{R}}^{l,t} = \mathbf{n} = \hat{\mathbf{R}}^{N_r,t}$. As a result, the estimated signal will ultimately be judged to be reliable by (58).

**Case 2 - $n_e = 1$:** Assuming that only the $l$-th index and symbol are estimated inaccurately as $\hat{k}_l$ and $\hat{s}_l$, according to (63), the ED $\rho_e^1$ is expressed as

$$\rho_e^1 = \| h_{k_l} s_{k_l} - h_{k_l} \hat{s}_l + \mathbf{n} \|^2 .$$

For the $l$-th step, after removing the $l$-th symbol $\hat{s}_l$, the residual vector is updated as $\hat{\mathbf{R}}^{l,t} = \mathbf{h}_{k_l} s_l + \mathbf{n}$. Assuming that no errors are encountered by (55), $k_l$ and $s_l$ can be estimated accurately and the ED is updated as $\| \hat{\mathbf{R}}^{l}_{\text{min}} \|^2 = \rho = \| \mathbf{n} \|^2$. If $\| \hat{\mathbf{R}}^{l}_{\text{min}} \|^2 < \rho_e^1$, this erroneous index can be corrected by this ECM. Otherwise, the error probability is the same as that of the ML detector.

**Case 3 - $n_e \geq 1$:** Assuming that the unreliable indices are $\hat{k}_{l_1}, \ldots, \hat{k}_{l_{n_e}}$, the ED between the estimated signal and the received signal is expressed as

$$\rho_e^2 = \| h_{k_{l_1}} s_{k_{l_1}} - h_{k_{l_1}} \hat{s}_{k_{l_1}} + h_{k_{l_2}} s_{k_{l_2}} - h_{k_{l_2}} \hat{s}_{k_{l_2}} \|^2 ,$$

$$\vdots$$

$$\rho_e^{n_e} = \| h_{k_{l_1}} s_{k_{l_1}} - h_{k_{l_1}} \hat{s}_{k_{l_1}} + \cdots + h_{k_{l_{n_e}}} s_{k_{l_{n_e}}} - h_{k_{l_{n_e}}} \hat{s}_{k_{l_{n_e}}} \|^2 .$$

If $\rho_e^{n_e-1} < \rho_e^{n_e}$ holds true, the ECM becomes capable of correcting the erroneous indices. Fig. 4 portrays the erroneous decision probabilities $P_e(\rho_e^{n_e-1} < \rho_e^{n_e})$ of $\rho_e^{n_e-1} < \rho_e^{n_e}$ in conjunction with $N_r = 128$ and 256 antennas. Fig. 4 shows that $P_e(\rho \leq \rho_e^1) < P_e(\rho \leq \rho_e^2) < P_e(\rho \leq \rho_e^3) < P_e(\rho \leq \rho_e^4)$ holds true for these setups. Moreover, these values monotonically decrease both with $N_r$ and the SNR. This implies that the proposed ECM works better for larger values of $N_r$ in the high SNR regions. However, when the MMP detector of (55) encounters estimation errors, the proposed ECM may suffer from error propagation.

### VI. Simulation Results

In this section, the capacity, the BER performance and complexity of the massive SM-VBLAST system are analyzed in conjunction with different antenna configurations. For P2P communication, the Largest Number First (LNF) principle of [1] is employed. For UL communication, the...
notations can be found in Table I.

A. Capacity Analysis Results

Figs. 5-6 portray the maximum achievable rate of the SM-VBLAST systems having different number of RAs. In order to achieve the maximum attainable rate, $N_u = N_t/2$ is employed in SM-VBLAST. The capacity of the classic VBLAST systems having the same number of RF chains and TAs are added as benchmarks. In order to evaluate our analytical lower bound, the capacity of SM-VBLAST is calculated by Monte-Carlo simulation and analytical result are compared using small-scale MIMO setups in Fig. 5. Specifically, $(N_t, N_u, N_r) = (8, 4, 4), (8, 4, 8)$ are employed for SM-VBLAST, while $(N_t, N_r) = (8, 4), (4, 8), (4, 8)$ are used for VBLAST system. Observe from Fig. 5 that the Monte-Carlo results closely approach the analytical lower bound upon increasing the SNR values.

Furthermore, in the massive setups of Fig. 6, the capacity calculation based on the Monte-Carlo simulation of (36) becomes impractical, hence only the analytical lower bound of (52) is included for comparison. Observe from Figs. 5-6 that since the antenna indices are activated for conveying extra information, the capacity of the SM-VBLAST system is always higher than that of the VBLAST systems having the same number of RF chains and RAs. When comparing it to the VBLAST system having the same values of $N_t, N_r$, the proposed SM-VBLAST is capable of approaching the MIMO capacity in the context of the under-determined antenna configuration, while it is still far from the MIMO capacity in the context of the over-determined antenna configuration. This implies that an enhanced SM-VBLAST system can be developed for approaching the MIMO capacity for the balanced antenna setup, which will be considered in our future work.

\begin{table}[h]
<table>
<thead>
<tr>
<th>Capacity (bpcu)</th>
<th>Capacity (bpcu)</th>
<th>Capacity (bpcu)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1000</td>
<td>200</td>
<td>600</td>
</tr>
<tr>
<td>400</td>
<td>600</td>
<td>700</td>
</tr>
<tr>
<td>800</td>
<td>100</td>
<td>0</td>
</tr>
<tr>
<td>10</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

**Fig. 5.** Comparison of the capacity for different antenna configurations. The simulated and analytical capacity of VBLAST is calculated by the Monte-Carlo simulation of (34) and from the analytical lower bound in (35), respectively. The simulated and analytical capacity of SM-VBLAST is calculated by the Monte-Carlo simulation of (36) and from the analytical lower bound in (52), respectively.

**Fig. 6.** Comparisons of the analytical capacity of the massive SM-VBLAST system and of the VBLAST system, which are calculated by (35) and (52), respectively.

**Fig. 7.** Performance comparison with different CS detectors for SM-VBLAST systems at 80 bpcu. a) $N_t = 128, N_u = 16, N_r = 64, M = 4$; b) $N_t = 128, N_u = 16, N_r = 128, M = 4$. These systems can also be considered as UL systems with 16 users. Each user is equipped with 8 antennas.

**Fig. 8.** Performance comparison with different CS detectors for SM-VBLAST systems. a) $N_t = 120, N_u = 30, N_r = 128, M = 4$ at 120 bpcu; b) $N_t = 160, N_u = 40, N_r = 128, M = 4$ at 160 bpcu. These systems can also be considered as UL systems with 30 and 40 users. Each user is equipped with 4 antennas.
TABLE III
COMPLEXITY COMPARISON OF THE PROPOSED ECM-OMP, ECM-CoSaMP AND MP DETECTORS.

<table>
<thead>
<tr>
<th>(N_t, N_u, N_r, M)</th>
<th>scheme</th>
<th>N_{eav}</th>
<th>Complexity normalized by the MP detector</th>
</tr>
</thead>
<tbody>
<tr>
<td>(128, 16, 64, 4)</td>
<td>Pro. ECM-OMP m = 4</td>
<td>11.8</td>
<td>3.1%</td>
</tr>
<tr>
<td>10 dB</td>
<td>Pro. ECM-CoSaMP m = 4</td>
<td>1.1</td>
<td>4.7%</td>
</tr>
<tr>
<td>(128, 16, 128, 4)</td>
<td>Pro. ECM-OMP m = 4</td>
<td>8.6</td>
<td>1.25%</td>
</tr>
<tr>
<td>6 dB</td>
<td>Pro. ECM-CoSaMP m = 4</td>
<td>1.02</td>
<td>2.44%</td>
</tr>
<tr>
<td>(120, 30, 128, 4)</td>
<td>Pro. ECM-OMP m = 4</td>
<td>18.7</td>
<td>4.55%</td>
</tr>
<tr>
<td>8 dB</td>
<td>Pro. ECM-CoSaMP m = 4</td>
<td>1.4</td>
<td>8.36%</td>
</tr>
<tr>
<td>(160, 40, 128, 4)</td>
<td>Pro. ECM-OMP m = 4</td>
<td>29.6</td>
<td>7.64%</td>
</tr>
<tr>
<td>10 dB</td>
<td>Pro. ECM-CoSaMP m = 4</td>
<td>1.94</td>
<td>10.85%</td>
</tr>
<tr>
<td>(240, 60, 256, 4)</td>
<td>Pro. ECM-OMP m = 4</td>
<td>36.5</td>
<td>6.54%</td>
</tr>
<tr>
<td>8 dB</td>
<td>Pro. ECM-CoSaMP m = 4</td>
<td>1.95</td>
<td>8.25%</td>
</tr>
<tr>
<td>(320, 80, 256, 4)</td>
<td>Pro. ECM-OMP m = 4</td>
<td>58.4</td>
<td>11.65%</td>
</tr>
<tr>
<td>8 dB</td>
<td>Pro. ECM-CoSaMP m = 4</td>
<td>8.84</td>
<td>11.92%</td>
</tr>
</tbody>
</table>

Fig. 9. Performance comparison with different CS detectors for SM-VBLAST systems. a) N_t = 240, N_u = 60, N_r = 256, M = 4 at 240 bpcu; b) N_t = 320, N_u = 80, N_r = 256, M = 4 at 320 bpcu. These systems can also be considered as UL systems with 60 and 80 users. Each user is equipped with 4 antennas.

B. BER Performance Results

In this section, the BERs of different CS SM-VBLAST detectors are compared for different antenna configurations. The optimal thresholds are selected based on Table II. The theoretical ABEPs of ML detectors are calculated by (32). Moreover, both the OMP and CoSaMP detectors have been employed in our proposed detector for comparison, called ECM-OMP and ECM-CoSaMP detectors, respectively. QPSK is employed for massive SM-VBLAST in these simulation results.

Fig. 7 compares the performances of different detectors for massive SM-VBLAST systems having (N_t, N_u, N_r) = (128,16,64) and (128,16,128), respectively. Observe from Fig. 7 that the performances of the proposed ECM-CoSaMP and ECM-OMP detectors are improved as \( m \) increases and they outperform the conventional OMP as well as CoSaMP and MMSE detectors. The proposed ECM-OMP detector exhibits an error-floor for the case of \( N_r = 64 \) in Fig. 7 (a). This is because when too many errors are encountered by the OMP detector, our ECM assisted OMP detector fails to correct all the erroneous messages for the case of \( N_r = 64 \). Fortunately, by increasing \( N_r \), the error correction capability of our ECM assisted CS detector is improved. Observe from Fig. 7 (b) that the performance of both the proposed ECM-OMP and ECM-CoSaMP detectors approach that of the MP detector and the theoretical ML limit at high SNRs \(^3\) for the case of \( N_u = 16, N_r = 128 \).

Next, Fig. 8 compares the performances of different detectors for massive SM-VBLAST systems having (N_t, N_u, N_r) = (120,30,64) and (160,40,128), respectively. The performances of the VBLAST systems having \( N_t = 30, N_u = 128, M = 16 \) and \( N_t = 40, N_r = 128, M = 16 \) are added as benchmarkers. Observe from Fig. 8 (a) that both the proposed ECM-OMP and ECM-CoSaMP detectors approach the MP and ML detectors for the case of \( N_u = 30, N_r = 128 \). However, for the case of \( N_u = 40, N_r = 128 \) we observe in Fig. 8 (b) that the proposed ECM-CoSaMP detector still approaches the ML detector’s performance and outperforms the conventional MP, CoSaMP, MMSE and OMP detectors. Since the \( N_u \) is very large, the proposed ECM-OMP detector exhibits an error-floor.

To provide further insights, Fig. 9 compares the performance of different detectors for the massive SM-VBLAST systems having (N_t, N_u, N_r) = (240,60,256) and (320,80,256), respectively. The performance of the VBLAST systems having \( N_t = 60, N_r = 256, M = 16 \) and \( N_t = 80, N_r = 256, M = 16 \) are added as benchmarkers. Observe from Fig. 9 that our ECM scheme works efficiently for the case of \( N_r = 256 \). Specifically, the performance of the proposed ECM-CoSaMP detector is always capable of approaching that of the MP and ML detectors. More importantly, the performance of the proposed ECM-OMP

\(^3\)According to Figs. 6-8, it becomes clear that the analytical upper bound of ABEP only becomes tight at high SNRs. This is because the value of PEP in (9) may be inaccurate at low SNRs, hence resulting in the value of \( \sum_{j=2}^{N} P(x^j \rightarrow x^j) \) being much higher than 1.
has only about 2 dB performance loss over the MP and ML detectors for the case of \( N_t = 80, N_r = 256 \).

Fig. 10 compares the performance of SM-VBLAST systems relying on the classic VBLAST systems relying on the MP based detector at different channel estimation errors. The setups are the same as that of Fig. 9. According to [28] of the revised manuscript, the estimated channel having errors can be modeled as

\[
\hat{\mathbf{H}} = \mathbf{H} + \mathbf{H}_e \quad (70)
\]

where \( \mathbf{H}_e \in \mathbb{C}^{N_x \times N_t} \) denotes the error matrices, whose elements follow the complex Gaussian distributions \( \mathcal{CN}(0, \sigma_e^2) \).

Fig. 10 compares the performance of SM-VBLAST systems based on the proposed detectors and the MP detector based classic VBLAST system at different channel estimation errors. The setups are identical to those of Fig. 9. According to [28] of the revised manuscript, the estimated channel having errors can be modeled as

\[
\hat{\mathbf{H}} = \mathbf{H} + \mathbf{H}_e \quad (70)
\]

where \( \mathbf{H}_e \in \mathbb{C}^{N_x \times N_t} \) denotes the error matrices, whose elements follow the complex Gaussian distributions \( \mathcal{CN}(0, \sigma_e^2) \).

VIII. Appendix

Proof of (47): \( \sum_{t=1}^{N_u} \varphi_t = N - 1 \) with \( N = 2^{\sum_{i=1}^{\log_2 N_u/2} B_i} \).

1) \( N_u = 1, N_t = 2^{B_1} \), we have \( \sum_{t=1}^{N_u} \varphi_t = 2^{B_1} - 1 = N_1 - 1 \);

2) If \( N_u = K, N_K = 2^{\sum_{i=1}^{\log_2 N_u/2} B_i} \), we have \( \sum_{t=1}^{K} \varphi_t = N_K - 1 \).

Then, for the case of \( N_u = K + 1 \), we have \( \sum_{t=1}^{K+1} \varphi_t = 2^{\sum_{i=1}^{\log_2 (N_u+1)/2} B_i} \), and the value of \( \sum_{t=1}^{K+1} \varphi_t \) is expressed as

\[
\sum_{t=1}^{K+1} \varphi_t = \sum_{t=1}^{K} \varphi_t + \varphi_{K+1}
\]

\[
= \sum_{t=1}^{K} \varphi_t + \sum_{t=1}^{K+1} N_{K+1}^2
\]

\[
= \sum_{t=1}^{K} \varphi_t + \sum_{t=1}^{K} N_t^2 + \sum_{t=1}^{K} \sum_{i=1}^{K+1} N_i^2
\]

\[
= \sum_{t=1}^{K} \varphi_t + \sum_{t=1}^{K} N_t^2 + \sum_{i=1}^{K+1} N_i^2
\]

\[
= 2^{B_1} - 1 + 2^{B_1} - 1
\]

(71)

3) Based on the analysis of 1) and 2), it is concluded that (47) holds true for any number of \( N_u \).
REFERENCES


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