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# Introduction to the Physics of Ionic Conduction in Narrow Biological and Artificial Channels

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Version May 14, 2021 submitted to Entropy

**Abstract:** The permeation of ions through narrow water-filled channels is essential to life and of rapidly-growing importance in technology. Reaching an understanding of the mechanisms underlying the permeation process requires an interdisciplinary approach, where ideas drawn from physics are of particular importance and have brought encouraging progress in recent years. This Introduction sets into context the several ground-breaking papers presented in the *Entropy* Special Issue on “The Physics of Ionic Conduction in Narrow Biological and Artificial Channels”.

**Keywords:** ion channel; nanopore; ionic selectivity; Coulomb blockade; hydration energy; molecular dynamics; Brownian dynamics; nonlinear dynamics; stochastic process.

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“There is plenty of room at the bottom”

Richard Feynman

Understanding, predicting and optimising the ionic selective transport properties of nanopores remains a critical challenge, both to nanotechnology and to biophysics. The last few decades have witnessed substantial progress in the analysis of such transport based on the use of a variety of experimental, numerical, and theoretical methods. Indeed, it would require several books to do full justice to the current state of the art in the field.

In some cases, the crystal structures, e.g. those of potassium, sodium, and calcium voltage-gated channels, have been discovered. This has provided invaluable insight but has also thrown into sharp relief the structure-function problem: how to predict the conduction/selectivity properties of a known structure; or conversely how to design a structure with required properties. A reliable solution to the problem offers to open new horizons in terms of pharmaceutical applications and in improved fabrication of solid-state nanopores for the sensing of molecules, desalination, DNA sequencing and the other developments that together are marking a new era in nanotechnology.

Novel numerical methods and computer hardware nowadays enable microsecond-long simulations of systems with hundreds thousands of atoms and the exploration of polarizable and quantum mechanical force fields. They provide unprecedented capabilities for reaching an understanding of experimental data and for the development of novel devices and techniques. Theoretical advances not only underlie many developments in molecular dynamics, including enhanced sampling and advanced force fields, but are also opening up new research frontiers and shedding fresh light on a number of longstanding problems such as binding probabilities, knock-on mechanisms of conduction, gating, electric double-layers, and local dielectric permittivity, just to mention a few.

32 It is now appreciated that selective conduction in biological ion channels has a great deal in  
33 common with that in artificial nanopores. In each case, there are intriguing analogies with the physics  
34 of quantum dots leading to the development of the theory of ionic Coulomb blockade. We dedicate  
35 this issue to the memory of our late colleague, Dr Igor Kh. Kaufman, who developed an elegant  
36 theory of ionic Coulomb blockade in biological ion channels and suggested a simple classification of  
37 voltage-gated channels based on the charge of the selectivity filter.

38 At the same time it is known that specific features of ionic conduction – such as dehydration,  
39 ion-specific binding affinities, protonation, the multicomponent and competitive nature of ion  
40 dynamics, the complex and adaptive structure of the ionic pathway, long range interaction, local  
41 variation of the effective dielectric constant, highly correlated motion of more than one ion within a  
42 narrow channel, electric double layers, and water layering at the channel entrances – add many layers  
43 of complexity to the fundamental physics analogies.

44 This Special Issue brings together original high-quality papers on ionic permeation through  
45 narrow water-filled channels, both biological and artificial, from some of the best researchers in the  
46 field. It includes papers on the statistical physics of the process, on molecular dynamics and Brownian  
47 dynamics simulations, and on relevant experiments. Although any selection of papers can only be  
48 a narrow slice of the field, our aim is to emphasize the complexity and mutual interdependence of  
49 recent multifaceted progress in understanding the physics of ion channels and nanopores. The time is  
50 ripe for bringing together these complementary approaches, and we anticipate that they will facilitate  
51 major breakthroughs, enabling the design of nanopores to meet particular technological requirements  
52 as well as improvements in drug design and perhaps in personalised medicine.

53 Importantly, the Poisson-Nernst-Planck (PNP) and kinetic models remain among the principal  
54 tools for predicting current through nanopores both in biology and nanotechnology. An example of  
55 the classical application of the PNP model to the analysis of reversal potentials and zero-current fluxes,  
56 in a system with a fixed profile of permanent charges and two mobile ion species, is provided by the  
57 paper by Mofidi et al [1]. Rigorous analytic and numerical results establish the dependence of the  
58 electric and chemical potential profiles on voltage and permanent charge.

59 At the same time it is well known that classical Poisson-Boltzmann (PB) and PNP theories do  
60 not take account of short-range ion-ion, ion-wall, or ion-water interactions in ion channels. Efforts to  
61 eliminate, or ameliorate the effects of, this deficiency of the continuum models have a long history. This  
62 stream of research is represented by the interesting paper of J.-L. Liu and R.S. Eisenberg [2] featuring  
63 the development of a molecular mean-field theory – a fourth-order Poisson–Nernst–Planck–Bikerman  
64 theory for modeling ionic and water flows in biological ion channels. The theory treats ions and  
65 water molecules, in channels of any volume or shape, with interstitial voids, polarization of water,  
66 and ion-ion and ion-water correlations. It can be applied to electrolyte solutions in the nanopores of  
67 batteries and fuel cells.

68 Modelling ionic currents with reduced models is extensively analysed by Boda et al [3]. They  
69 show that channels are especially amenable to reduced modelling because their functions and  
70 the relationships between input parameters (e.g. applied voltage, bath concentrations) and output  
71 parameters (e.g. current, rectification, selectivity) are well-defined, allowing one to focus on the physics  
72 of input-output relationships rather than on the atomic-scale physics inside the pore. Based on decades  
73 of research, the authors propose four rules of thumb for constructing good reduced models of ion  
74 channels and nanopores, focusing on the physics of input-output relationships rather than on atomic  
75 structure. The proposed rules relate to the importance (1) of the axial concentration profiles, (2) of  
76 the pore charges, (3) of choosing the right explicit degrees of freedom, and (4) of creating the proper  
77 response functions. Examples demonstrating the application of these rules are provided. Further  
78 improvements in predicting the capabilities of reduced models can be achieved by incorporating  
79 into the solution of the one-dimensional electro-diffusion model the potential of the mean force  
80 obtained from MD simulations. The performance of two such methods is examined by A. Pohorille  
81 and M. A. Wilson1 [4] using stochastic simulations. These methods require neither knowledge of

82 the diffusivity nor simulations at multiple voltages, which greatly reduces the computational effort  
83 needed to probe the electrophysiology of ion channels. They can be used to determine the free energy  
84 profiles from either forward or backward one-sided properties of ions in the channel, such as ion fluxes,  
85 density profiles, committor probabilities, or from their two-sided combination. In this work large  
86 sets of stochastic trajectories were generated individually designed to mimic the molecular dynamics  
87 crossing statistics of models for channels of trichotoxin, p7 from hepatitis C and a bacterial homolog of  
88 pentameric ligand-gated ion channel, GLIC. The authors found that the free energy profiles and the  
89 current–voltage curves obtained from the generated trajectories reproduce with good accuracy results  
90 obtained in molecular dynamics simulations.

91 The charged particles of which matter is composed move when an external electric field is  
92 applied, and their changed distribution is traditionally described in terms of a polarisation field. For  
93 insulators, it is usually possible to define a relative permittivity (dielectric constant) to quantify the  
94 material’s responsiveness to the electric field. In ion channels, for example, the protein walls and  
95 the water are usually treated as dielectric continua with relative permittivities of around 2 and 80  
96 respectively. This approach can be very helpful and revealing, but it involves greater approximation  
97 than just that of spatial averaging because, as R.S. Eisenberg points out [5], the material’s response  
98 to the electric field may be both nonlinear and time-dependent. In order to accommodate such  
99 phenomena – simultaneously challenging physicists to review their knowledge of electromagnetism  
100 in biological dielectrics – he proposes and discusses an apparently minor change in Maxwell’s first  
101 equation. It produces a major consequence when joined with Maxwell’s second equation in that  
102 conservation of total current (including the displacement current) then emerges as a general principle.  
103 In one dimensional systems, like ion channels or electronic circuit components, the consequences are  
104 profound: there, total currents are equal at all locations at any given time, so the space variable does  
105 not appear in the description of total current.

106 There follow two papers reporting MD simulations of ion currents in biological and artificial  
107 channels. First, S.M. Cosseddu et al [6] present an extended MD-based analysis of ion motion within  
108 the KcsA channel. They reveal complicated patterns of potassium currents that are governed by  
109 the structural variability of the selectivity filter. They show that ion motion involves the complex  
110 dynamics of a strongly-correlated network of residues and water molecules. Intriguing features of  
111 self-organisation and readjustment of the network are analysed statistically and discussed in detail.

112 Secondly, we note that ionic transport in nano- to subnano-scale pores is highly dependent on  
113 translocation barriers and potential wells. These features in the free-energy landscape are primarily  
114 the result of ion dehydration and electrostatic interactions. For pores in atomically thin membranes,  
115 the ionic dynamics both inside and outside the geometrical volume of the pore can be critical in  
116 determining its transport properties. S. Sahu and M. Zwolak [7] examine regimes of transport that are  
117 highly sensitive to pore size due to the interplay of dehydration and interaction with pore charge, where  
118 picometer changes in the size, e.g. due to a minute strain, can lead to a large change in conductance.

119 We have already remarked upon the crucial importance of water, the electric double-layer,  
120 water-layering, polarisation, and the resultant changes of local dielectric permittivity at the entrances  
121 of nanopores. Another approach to this problem is illustrated in the paper by T.-L. Horng [8]. Starting  
122 from the classical Helmholtz free energy functional for an electrolyte, including the solvation energies  
123 for anions and cations, the author follows the Bikerman modification by adding an entropy term to the  
124 functional, and he then extends the Bikerman approach by introducing ion-size-specific corrections to  
125 the theory.

126 The approach based on density functional theory (DFT), which works well near charged walls  
127 and in bulk electrolytes, can be extended to the analysis of the orientational ordering of water dipoles  
128 in membrane nanotubes. M. Drab et al [9] analyse water ordering in nanotubes by minimizing the  
129 corresponding Helmholtz free energy functional, also including the orientational entropy contribution  
130 of water dipoles, and deriving the modified Langevin Poisson-Boltzmann (MLPB) model of the  
131 electric double-layer. The MLPB equation is solved in cylindrical coordinates to determine the spatial

132 dependences of the electric potential, relative permittivity and average orientations of water dipoles  
133 within charged tubes of different radii. Results show that, for tubes of a large radii, the macroscopic  
134 (net) volume charge density of cations and counterions is zero on the geometrical axis. This is attributed  
135 to effective electrolyte charge screening in the vicinity of the charged inner surface of the tube. For  
136 tubes of small radii, the screening region extends into the whole inner space of the tube, leading to  
137 non-zero net volume charge density and non-zero orientational ordering of water dipoles near the axis.

138 The DFT results mentioned above are examples of statistical physics yielding insight into the  
139 function of ion channels and nanopores. This theme is continued and extended, first by Gibby et  
140 al [10] who apply their recent derivation of an effective grand canonical ensemble and linear response  
141 theory of ion channels to analyse the conduction of the bacterial NaChBac selectivity filter. The authors  
142 compare their theory to experimental current-voltage and current-concentration dependences for  
143 a single channel and for a whole cell. They find that the statistical theory in the linear response  
144 regime predicts correctly many important properties of the NaChBac filter including the concentration  
145 dependence of the reversal potential and the current-voltage relations. They also show that the  
146 theoretical results are consistent with MD simulations of the filter population at each binding site.

147 Secondly, analysis of quantum mechanical effects in ion channels is another important direction,  
148 supported by the extended capabilities of modern quantum mechanics/molecular mechanics  
149 simulations. In this respect, interesting perspectives are opened by mapping the statistical mechanics  
150 of ion channels onto an effective quantum mechanics. Such investigations are reviewed by T. Gulden  
151 and A. Kamenev [11], who study the dynamics and thermodynamics of ion channels, considered as  
152 effective 1D Coulomb systems whose statistical mechanics is dominated by entropic effects that may  
153 be taken accurately into account by mapping onto an effective quantum mechanics. The corresponding  
154 semiclassical calculations for non-Hermitian Hamiltonians are conducted by applying tools from  
155 algebraic topology. The relationship of the solutions to the thermodynamics and correlation functions  
156 of multivalent solutions within long water-filled channels is discussed.

157 The actual properties of real nanopores are, of course, discovered by experiment, which has been  
158 leading the research in this area especially since the discovery of the structure of the KcsA channel. In  
159 our Special Issue, experimental insight is provided by two of the leading research groups in the field.

160 O. Fedorenko et al [12] discuss the properties of voltage-gated sodium channels (Navs).  
161 These channels play fundamental roles in eukaryotes but lack structural resolution, which renders  
162 understanding their structure-function relationships a challenging problem. Bacterial Navs,  
163 representing simplified homologues of their eukaryotic counterparts, have enabled both structural  
164 resolution and electrophysiological characterization. However, their homotetrameric structure leads to  
165 an EEEE locus in the SF that is at odds with the DEKA locus of eukaryotic Navs. Indeed, prokaryotic  
166 Navs have long been considered more similar to eukaryotic calcium channels (Cavs) than to Navs,  
167 leading to the formulation of the "EEEE paradox". This was arguably solved by Kaufman et al by the  
168 realisation that there is a critical D residue close to the EEEE ring of eukaryotic Cavs generating an  
169 effective EEEED locus of charge  $-5e$ . Fedorenko et al. present a follow-up of a previous study, aimed  
170 at mimicking the SF of eukaryotic Navs by engineering radial asymmetry into the SFs of bacterial  
171 channels. This goal was pursued with two approaches: co-expression of different monomers of the  
172 NaChBac bacterial channel in mammalian cells, to induce the random assembly of heterotetramers;  
173 and the concatenation of four bacterial monomers to form a concatemer that can be targeted by  
174 mutagenesis on specific strands of the SF, thereby introducing asymmetry. Patch-clamp measurements  
175 and MD simulations showed that an additional gating charge in the SF leads to a significant increase  
176 of  $\text{Na}^+$  and a modest increase in  $\text{Ca}^{2+}$  conductance in the NavMs concatemer in agreement with  
177 the behaviour of the population of random heterotetramers with the highest proportion of channels  
178 with charge  $-5e$ . This study confirms that, although the charge at the SF is important, it is not the  
179 only factor affecting conduction and selectivity. It also offers new tools extending the use of bacterial  
180 channels as models of eukaryotic ones.

181 The work by A. Chernev et al [13] reviews the most promising approaches to the fabrication of  
182 artificial nanofluidic devices capable of reproducing properties of single ion channels. It is shown that  
183 modern technologies have great potential in allowing one to test various theoretical models of ion  
184 channels. The review aims to highlight ionic Coulomb blockade — the phenomenon which (see above)  
185 can often be key player in ion channel selectivity. The authors discuss the most critical obstacles  
186 associated with these studies and suggest possible solutions to further advance the field.

187 The rapid interdisciplinary advances in nanotechnology can be characterised as the beginning of  
188 a new industrial revolution, where novel devices and materials are fabricated and controlled on the  
189 atomic level. Ion- and water-selective nanopores represent an important frontier in these advances.

190 The selected papers in this Special Issue provide both a snapshot of the present and strong  
191 indications of how the subject is likely to evolve over the coming years. We may, for example, anticipate:  
192 major developments in the theory at a fundamental level, based on statistical mechanics and quantum  
193 mechanics; substantial improvements in “intermediate level” theories like PNP, modified CKE and  
194 DFT which promise quantitative predictions of the properties of real channels; together with much  
195 faster and more capacious MD modelling of larger ensembles of atoms on longer timescales, more  
196 accurate due to use of polarizable force field and QM/MM, encompassing gating and permeation  
197 events at a statistically useful level. This progress is expected to lead to the first-principles design  
198 and fabrication of structures optimised for many important applications including ion pumps, energy  
199 harvesting, and field effect ionic transistors as well as those mentioned above at the beginning. Many  
200 of these will require theory and experiment on small scales where disciplinary distinctions have mostly  
201 faded away, but where physics predominates.

202 An additional impulse propelling these developments forwards is expected due to the fusion of  
203 physics-based approaches with artificial intelligence. The latter has already been proven to be a very  
204 useful for accelerated learning of the force fields in MD, as well as for reconstruction of the potentials  
205 of the mean force and neural-network-based discovery of partial differential equations. Remarkably, it  
206 also underlies a recent breakthrough in the solution of the protein-folding problem.

207 **Funding:** This research was funded by the Leverhulme Trust (UK) grant number RPG-2017-134.

208 **Acknowledgments:** We are very grateful for numerous valuable discussions with Aneta Stefanovska, Bob  
209 Eisenberg and other authors of the papers in this Special Issue.

210 **Conflicts of Interest:** The authors declare no conflict of interest.”

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