

Effect of boundary condition on Kapitza resistance between superfluid $^3\text{He-B}$ and sintered metal

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Understanding the temperature dependence of thermal boundary resistance, or Kapitza resistance, between liquid helium and sintered metal has posed a problem in low temperature physics for decades. In the ballistic regime of superfluid $^3\text{He-B}$, we find the Kapitza resistance can be described via scattering of thermal excitations (quasiparticles) with a macroscopic geometric area, rather than the sintered metal's microscopic area. We estimate that a quasiparticle needs on the order of 1000 collisions to successfully thermalize with the sinter. Finally, we find that the Kapitza resistance is approximately doubled with the addition of two mono-layers of solid ^4He on the sinter surface, which we attribute to an extra magnetic channel of heat transfer being closed as the non-magnetic solid ^4He replaces the magnetic solid ^3He .

I. INTRODUCTION

The thermal boundary resistance, or Kapitza resistance, R_K between liquid helium and sintered metal is a common limiting factor in the pursuit of ultra-low temperatures. As temperature decreases the thermal boundary resistance R_K increases, reducing the cooling power attainable in dilution refrigerators. According to acoustic mismatch theory, phonon-phonon transfer should yield a boundary resistance proportional to inverse temperature cubed, $R_K \propto T^{-3}$ [1]. A common way of decreasing the Kapitza resistance between liquid helium and metal and increasing refrigerator performance is to increase the surface area using sintered metal powders. However, the problem of Kapitza resistance between sintered metal and liquid ^3He is still yet poorly understood despite the large scale use of dilution refrigerators, in part due to sintered metals' complicated geometry [1]. At very low temperatures, $T \leq 10\text{ mK}$, the boundary resistance deviates significantly from the prediction of acoustic mismatch theory. A lower than expected Kapitza resistance is observed in general, and with a temperature dependence of $R_K \propto T^{-1}$ [2]. In superfluid $^3\text{He-B}$ at ultra-low temperatures (about $0.3 T_c$ or 0.3 mK at zero pressure) the mean free path of the thermal excitations exceeds the cell dimensions and hydrodynamic picture becomes inadequate. In this ballistic regime previous measurements reported an exponential dependence [3, 4] as well as quadratic or cubic relationships [5] of Kapitza resistance with temperature.

It is important to also consider the possible surface

effects of solid helium at low temperatures as a few layers of solid helium will form on the surfaces due to van der Waal's forces [6, 7]. It is thought that the magnetic properties of ^3He could play a large role in the smaller than expected Kapitza resistance, by the creation of a magnetic channel of energy exchange with magnetic impurities in the sintered metal [8, 9].

Recently, it has become a popular technique in ultra-low temperature physics to pre-plate the surfaces of the experimental cell and objects with solid ^4He . ^4He preferentially adsorbs to surfaces over ^3He due to its lower zero-point energy. Control over the number of ^4He layers allows fine tuning of the surface scattering specularity. This technique has been used for the stabilization of the newly discovered polar phase in nematic aerogels [10] and the suppression of the B phase in thin slab geometries when the scattering at the slab surface becomes completely specular [6, 7]. Importantly, solid ^4He is also non-magnetic. In the ballistic regime of the B phase, heat transfer should be dominated by quasiparticle collisions with the surface. The difference in magnetic and non-magnetic quasiparticle scattering has been found to have a significant effect on the stabilisation of the A phase [11, 12] and of the polar phase [13] in anisotropic media. It is therefore likely that the magnetic properties of solid ^3He are an important factor in the Kapitza resistance. Hence pre-plating surfaces with non-magnetic ^4He should change the effective Kapitza resistance, a key consideration for future experiments at ultra-low temperatures.

In this work we demonstrate the difference in Kapitza resistance between superfluid $^3\text{He-B}$ and sintered silver with and without pre-plating of the surface with 2 layers of ^4He . We compare the measured Kapitza resistance to earlier work [3, 14] and find very good agreement with the reported exponential temperature dependence. Our observed difference in Kapitza resistance between solid

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^3He and solid ^4He coverage provides evidence for the role of the magnetic channel in decreasing the Kapitza resistance between metal and liquid ^3He . We use a simple model to calculate the increase in probability of a quasiparticle collision with sintered metal eventually resulting in quasiparticle recombination. We find that sinter covered with ^3He offers about double the probability of recombination.

We have analysed the results of three experiments and conclude that in the ballistic regime it is the geometric area of the sinters that needs to be considered in the calculation of the Kapitza resistance. We define the geometric area as the area of plates with direct contact to the liquid in the experimental volume which provides consistent results between measurements. The total (interfacial) area of all sintered plates or the area calculated from the sponge-like sinter geometry at the microscopic level do not provide consistent results between different measurements. Similar conclusions have been made about the sinter surface area in contact with a saturated ^3He - ^4He solution [15]. This makes intuitive sense, as a quasiparticle created in the volume has little chance of colliding with sintered plates that have other plates between them and the quasiparticle.

II. EXPERIMENTAL DETAILS

Our experimental apparatus is a Lancaster-style nested nuclear demagnetization cell attached to a custom-built dilution refrigerator (shown in Fig. 1). The inner cell contains 8 copper plates of thickness 1.1 mm and 80 copper plates of thickness 0.2 mm which are used as a refrigerant for nuclear demagnetization. A silver powder of 70 nm particle size is sintered to both sides of each copper plate with a filling factor of 0.5 and results in a microscopic surface area of 80 m^2 [16]. From the total surface area, which is more or less equal to the total microscopic sinter surface area, we can calculate the amount of gas needed to pre-plate all surfaces with 2 layers of solid ^4He [17]. This is accomplished by inserting a small amount of ^4He gas before filling the cell with ^3He to saturated vapour pressure. After demagnetizing to the required magnetic field (or temperature) the copper plates act as a thermal bath.

Inside the cell we have a set of mechanical probes: A relatively large moving wire with a diameter of $135\text{ }\mu\text{m}$, a small vibrating loop wire with a diameter of $4.5\text{ }\mu\text{m}$ and a small quartz tuning fork. The damping in ballistic ^3He -B measured via mechanical resonance widths Δf of the vibrating loop and tuning fork is determined by the number of quasiparticle collisions, and hence the number density of quasiparticles in the superfluid. In the ballistic regime the quasiparticle density is exponential with temperature, thus vibrating resonators can be very sensitive thermometers [18]. The large wire can be moved at constant velocity with a direct current in a magnetic field which generates a Laplace force, which we term a

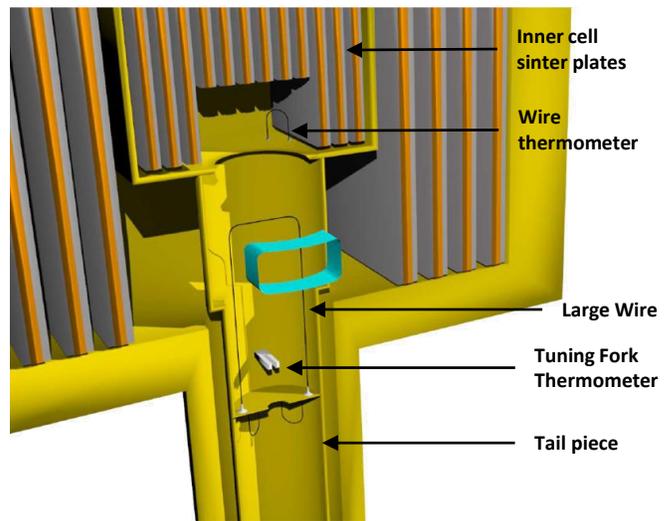


FIG. 1. The experimental cell. The inner cell contains eighty 0.2 mm thick and eight 1.1 mm thick copper plates with dimensions 49 mm by 28 mm. The plates are sintered with a silver powder, giving a total microscopic sinter area of 80 m^2 . A 2 cm by 2 cm by 1 cm geometric volume is formed by cutting the middle plates. The cuts from these plates are in an alternating pattern of a 1.9 cm by 1.1 cm rectangle followed by a 2.0 cm by 1.0 cm rectangle to create 1 mm protrusions that increase the surface area without changing the volume. The geometric volume contains the vibrating loop wire thermometer. A cylindrical volume containing the large wire and quartz tuning fork is connected via a circular cutout to the bottom of the geometric volume. The cylindrical volume also has a tail piece separated by a small hole.

DC pulse [19]. Moving the wire heats the experimental cell and increases the number of quasiparticles above the thermal equilibrium density [20]. Hence monitoring the width response of the vibrating loop and tuning fork during a DC pulse allows us to detect the heating and subsequent cooldown. Note, that the actual temperature change is small due to the exponential dependence of the resonance width on temperature.

III. RESULTS

Initially, the bulk quasiparticle population is in thermal equilibrium with the thermal bath and the thermometer is resonating with a base resonance width of Δf_{base} .

After a DC pulse is started, the released heat goes directly into the liquid and increases the bulk quasiparticle population, detected by a rapid increase in thermometer width up to a peak value. The quasiparticles excited begin colliding with surfaces where the area is dominated by the silver sinter. In the ballistic regime these collisions are either near-elastic or result in the quasiparticles losing enough energy to successfully recombine as a Cooper pair. We expect an exponential decay of the quasiparticle

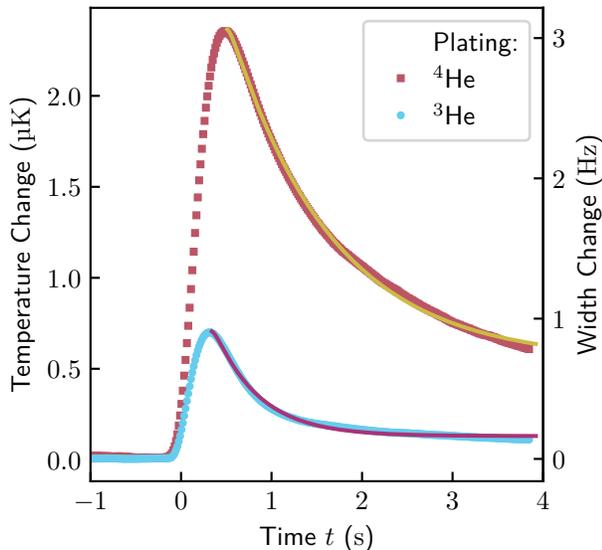


FIG. 2. Comparison of the response of the vibrating loop wire with diameter $4.5\ \mu\text{m}$ for pure ^3He and two layers of solid ^4He coverage on the cell surface at temperatures of $197\ \mu\text{K}$ ($\Delta f_{base} = 30.4\ \text{Hz}$) and $193\ \mu\text{K}$ ($\Delta f_{base} = 25.9\ \text{Hz}$), respectively. The resonance width is related to temperature by the equation $\Delta f = \Delta f_{vac} + \gamma \exp(-\Delta_B/k_B T)$, where $\Delta f_{vac} = 92\ \text{mHz}$ is the resonance width in vacuum and γ is a fitting constant [22]. The corresponding width change for the ^4He data is given by the right y axis. The ^3He data was measured at a slightly different temperature, and hence the width change is 5% larger for a given temperature change. Solid lines represent the fits from Eq. (1).

density until thermal equilibrium is reached with the surroundings, measured by the thermometer width reaching the base value. Figure 2 shows a typical response of a thermometer width to a DC pulse that we model as [21]

$$\Delta f = \Delta f_{base} + H \frac{\tau_b}{\tau_b + \tau_w} \left(e^{-t/\tau_b} - e^{-t/\tau_w} \right). \quad (1)$$

Here H is a constant describing the amplitude of the width response and τ_w is the response time of the thermometer, determined by the resonance width and is approximately equal to $1/(\pi\Delta f_{base})$. The decay time constant τ_b is governed by the effective boundary resistance R_K , area A and the heat capacity C_B of superfluid $^3\text{He-B}$ [4]

$$AR_K = \frac{\tau_b}{C_B}. \quad (2)$$

The heat capacity of $^3\text{He-B}$ in the ballistic regime is determined by the number of quasiparticles and exponentially depends on temperature $C_B \propto \exp(-\Delta_B/k_B T)$, where Δ_B is the superfluid energy gap of $^3\text{He-B}$ and k_B is the Boltzmann constant.

Figure 2 shows the different responses of the vibrating loop thermometer to identical pulses for pure ^3He and ^4He pre-plated cases. The decay constant τ_b extracted for ^4He pre-plated surfaces is $1.0 \pm 0.1\ \text{s}$ which is approximately double the $0.5 \pm 0.1\ \text{s}$ constant observed in pure ^3He . Similar results were obtained for the quartz tuning fork. Interestingly, the time constant was found to not vary with the wire velocity of the DC pulse. The time constant is thus independent of the energy released by the DC pulse at least when the energy released is varied from $5\ \text{pJ}$ to $100\ \text{pJ}$ (wire velocities of $2\ \text{mm s}^{-1}$ to $50\ \text{mm s}^{-1}$). Furthermore, the thermalization time constant τ_b is independent of temperature for both types of coverages, which is demonstrated in Fig 3. According to Eq. (2), this demonstrates an exponential temperature dependence on Kapitza resistance in both cases, and leads to the conclusion that pre-plating with solid ^4He doubles the Kapitza resistance.

In the above analysis we have assumed that only the bulk ^3He heat capacity is relevant. It is known that the solid ^3He layer in a magnetic field and at low temperatures can have a large contribution. Elbs *et al.* measured the surface contribution to the overall heat capacity for a $0.13\ \text{cm}^3$ container of ^3He and found that at higher temperatures around $0.16\ \text{mK}$ to $0.19\ \text{mK}$ in similar magnetic field to our measurements the heat capacity of solid and liquid helium were roughly equal [23]. For our much larger volume of $8.6\ \text{cm}^3$ the contribution to heat capacity from the superfluid $^3\text{He-B}$ is much more than the contribution to heat capacity from any solid layers, thus we neglect this heat capacity.

IV. DISCUSSION

The exponential temperature dependence is entirely consistent with previously reported by Parpia [4], Castelijns *et al.* and Carney *et al.* [3, 14]. Thermalization time τ_b reported by Castelijns *et al.*, is about ten times larger. In that work an electrical heater was used to create heating bursts, which likely created a bubble of normal fluid around the heater and altered the time constant [3]. The advantage of our method is the direct creation and relaxation of quasiparticles. The wire moving at supercritical velocities does not destroy the bulk superfluid state [20]. Therefore, we observe purely the dynamics of the quasiparticles, which in the ballistic regime governs the heat transport properties of the superfluid.

Consider a superfluid quasiparticle excited by the DC pulse. The quasiparticle travels with group velocity v_g which is approximately $20\ \text{ms}^{-1}$ at these temperatures and pressure. Due to the superfluid energy gap, when the quasiparticle scatters with a wall it has a chance to either scatter elastically or lose energy Δ_B and recombine into a Cooper pair. The recombination results in a reduction of the overall superfluid temperature. However, losing enough energy for recombination after scattering

Cell	Experimental Volume (cm ³)	Sinter Area			Sinter Mass (g)
		Interfacial (m ²)	Microscopic (m ²)	Geometric (cm ²)	
This work	8.6	0.21	80	36	96
Castelijns <i>et al.</i> [3]	1.0	0.011	22	3.0	28
Carney <i>et al.</i> [14]	1.0	0.17	41	3.0	49

TABLE I. Experimental cells for each measurement. The interfacial area is the area of all plate faces covered in sinter and microscopic area is the area of the sintered powder’s sponge-like surface. Geometric area is the sintered plate surfaces that face the experimental volume containing the large wire with no other sintered surfaces between it and the volume (see text). The experimental volume quoted for this work excludes the tail piece, in which a small hole limited heat flow into the tail piece volume. However, the tail piece volume is not large and its inclusion would not change the results significantly.

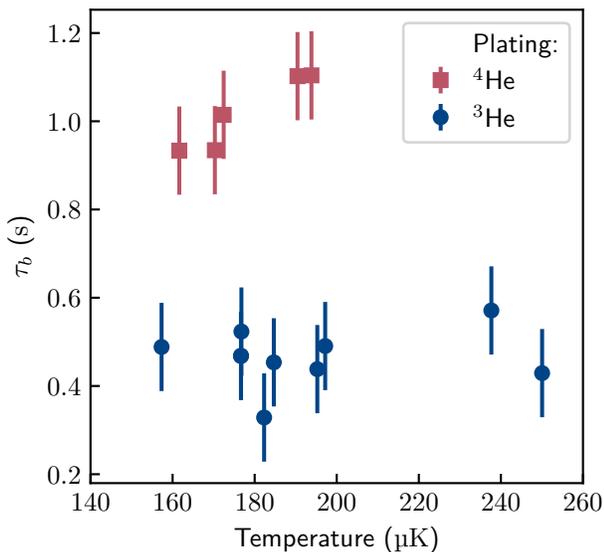


FIG. 3. Comparison of quasiparticle relaxation time constant τ_b as measured by the vibrating loop thermometer. The average τ_b is 0.5 ± 0.1 s and 1.0 ± 0.1 s for solid ^3He and solid ^4He coverage, respectively. Absence of discernible variation over temperature is consistent with an exponential dependence of R_K .

with cell walls is extremely unlikely and quasiparticle-quasiparticle interactions can be neglected in the ballistic regime, hence only scattering with sinter matters. The pore size in the sinter is roughly equal to the coherence length of the superfluid pairs which is around 80 nm at zero pressure [2, 24]. Hence, the sinter could appear as a wall of metal and high normal fluid density to any approaching quasiparticle [25].

We can estimate the number of collisions needed for a quasiparticle to eventually recombine by considering its motion in a cubic box of dimension d with only one thermally conductive wall due to the sintered copper plates. The time it takes to traverse from one wall to another is roughly $t_{col} = d/v_g$ and the average time taken for there to be no more collisions is approximately τ_b . Therefore

the probability of collision successfully leading to recombination is $P = \frac{t_{col}}{6\tau_b}$. This gives an estimate on the order of 1000 collisions needed for a quasiparticle to lose its energy with the sinter and recombine.

For ^4He coverage we also observed a similar magnetic field dependence as measured by Osheroff and Richardson [26] with pure ^3He . About a 20% increase was observed in τ_b as the field was doubled from 63 mT to 125 mT. This confirms the conclusion that magnetic impurities in the sinter also reduce the Kapitza resistance, and that this reduction is independent of the magnetic layers of solid ^3He that form on all surfaces in the absence of ^4He preplating.

The simple quasiparticle collision model described above assumes that the sinter is a flat surface in just one side of the cell. In contrast, our experimental cell has many plates of sinter and many of these plates are behind other plates. However, we may assume that a quasiparticle in the experimental volume has a significant chance of scattering only with sinter that is near the experimental volume and has no other plates or walls between it and the volume. We define a “geometric area” which consists of only the faces of the sintered plates that are in direct contact with this volume. We treat this area as if it has no gaps, meaning a quasiparticle cannot travel around the small gap between plates and the cell walls. This also means we assume the areas made of a collection of plates pushed together, such as the one just above the vibrating wire thermometer, as continuous. In reality there are small gaps. We can then test our assumption and the model by comparing our values of thermal boundary resistance to those obtained by Castelijns *et al.* and Carney *et al.* using the same silver powder and sintering technique as used in this work [16].

We fit zero pressure data from Castelijns *et al.* and Carney *et al.* with a function that uses the BCS gap $\Delta_B = 1.76k_B T_c$. We compare several different areas for use in Eq. (2): The geometric area described above; the microscopic area, the area of all the sinter when not treated as flat surface at the microscopic level; and the interfacial area, calculated by the area of all plates in the cell. Table I gives details of the volumes and different areas for each experiment.

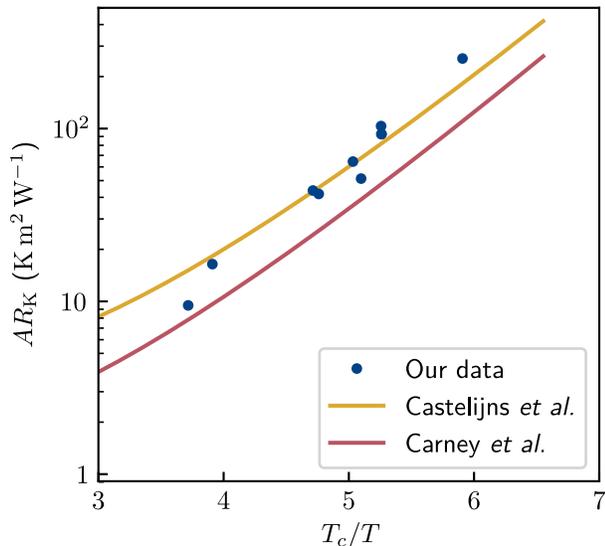


FIG. 4. The effective thermal boundary resistance R_K multiplied by the “geometric” sinter scattering area A for quasiparticles created by the wire as a function of inverse temperature. $T_c = 929 \mu\text{K}$ is the critical temperature of superfluid ^3He at zero pressure. The gold and red lines are fits for data from Refs. [3] and [14], respectively, and converted into thermal boundary resistance. For comparison, our data shown is only in pure ^3He . They lie mostly on the gold line, or between the two lines if the tailpiece volume is included.

We find that the geometric area gives good agreement with our results, shown in Fig. 4. Moreover, this is the only area that gives any agreement. Notably, in both experiments by Carney *et al.* and Castelijns *et al.* have the exact same cell geometry in terms of geometric area, but the ratio between the measured boundary resistances at the lowest temperatures was about 2.5. Our data points lie closer to the results of Castelijns *et al.*, or between the two lines if the tail piece volume is included in the calculation of the heat capacity in Eq. (2).

The difference between the results of Castelijns *et al.* and Carney *et al.* comes from the assumption that gaps between plates do not matter. In reality, a quasiparticle may go between the gaps and begin colliding within the plates. Since there is a much shorter distance between these two close plates, a quasiparticle has much less time between the collisions resulting in quicker recombination. Naturally, the chances of a quasiparticle going inside a gap will increase with the number of gaps. In Castelijns *et al.* the cell had twelve 1 mm thick plates, and a square was cut out of seven to form a 1 cm^3 box. In Carney *et al.*, ninety-two plates of 0.1 mm were used, resulting in many more gaps and the lower Kapitza resistance seen in Figure 4. In our cell, there is a combination of both thick and thin plates, and our values lie closer to those reported from Castelijns *et al.*. Therefore, the sinter plate layout is the likely explanation for the different outcomes obtained

by these three experiments.

The difference between the two types of coverage, we believe, is due to different magnetic properties of the two. It has long been thought that a magnetic channel for transfer of heat is key to explaining the observed difference in Kapitza resistance between experiment and theory [27]. Further evidence was added by König *et al.*, who saw a large difference in the performance of different brands of silver powder [8, 9, 28]. They concluded that Ulvac powder has a larger content of magnetic impurities and a lower Kapitza resistance at millikelvin temperatures. Incidentally, we, Osheroff and Richardson [26], Castelijns *et al.* [3] and Carney *et al.* [14] all used the 70 nm Ulvac powder, which has the highest magnetic impurity content of all brands and sizes measured by König *et al.*

V. CONCLUSIONS

We have demonstrated that in the ballistic regime the thermal boundary resistance between sintered metal and ^3He is dominated by the collisions of quasiparticles with sinter walls. The probability of an eventually recombining collision can be calculated using the thermal time constant. The probability is surprisingly very low, on the order of one in a thousand. By considering the geometric surface area quasiparticles have available to scatter with, we find good agreement of Kapitza resistance with previous measurements. To increase the thermal boundary conductivity it is therefore important to increase the frontal surface area the particles can collide with in the experimental volume.

When designing cells for ultra-low temperature experiments, increasing the geometric surface in contact with the ^3He is an important factor. Future designs should aim to increase the contact area, possibly by using ridge-like protrusions.

It is also important to consider the magnetic properties of the surface the quasiparticles scatter with. Covering the surfaces with two layers of non-magnetic solid ^4He doubles the thermal boundary resistance. This provides further evidence of a magnetic energy transfer channel between liquid ^3He and metals to explain deviations in Kapitza resistance from theory. A well-developed theory explaining the Kapitza resistance at ultra-low temperatures should include the magnetic properties and future sinter designs should aim at utilizing magnetic impurities.

It would be beneficial to extend the scope of the measurements by increasing the temperature range and probing different phases. Unfortunately, the described bolometry method can only be applied in the ballistic regime of the B phase and cannot be used in the A phase. Therefore, we were unable to make a similar measurement in the A phase. The method of heat transfer from superfluid ^3He -A to sinter at ultra-low temperatures is an interesting question for further work, since the propagation of

quasiparticles is significantly different [29]. One would assume it is unlikely that the result in the B phase would then apply, but earlier measurements of the A phase found an exponential dependence on temperature similar to that in the B phase between 230 μK and 450 μK at zero pressure [30].

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