

Autonomous Learning Multiple-Model Zero-Order Classifier for Heart Sound Classification

Eduardo Soares^a, Plamen Angelov^a, Xiaowei Gu^a

^a*School of Computing and Communications, Lancaster University, Lancaster, LA1 4WA, UK*

E-mail: e.almeidasoares@lancaster.ac.uk; p.angelov@lancaster.ac.uk; x.gu3@lancaster.ac.uk

Abstract

1 This paper proposes a new extended zero-order Autonomous Learning Multiple-
2 Model (ALMMo-0*) neuro-fuzzy approach in order to classify different heart
3 disorders through sounds. ALMMo-0* is build upon the recently introduced
4 ALMMo-0. In this paper ALMMo-0 is extended by adding a pre-processing
5 structure which improves the the performance of the proposed method. ALMMo-
6 0* has as a learning engine composed of hierarchical a massively parallel set of
7 0-order fuzzy rules, which are able to self-adapt and provide transparent and
8 human understandable *IF ... THEN* representation. The heart sound record-
9 ings considered in the analysis were sourced from several contributors around
10 the world. Data were collected from both clinical and nonclinical environment,
11 and from healthy and pathological patients. Differently from mainstream ma-
12 chine learning approaches, ALMMo-0* is able to learn from unseen data. The
13 main goal of the proposed method is to provide highly accurate models with
14 high transparency, interpretability, and explainability for heart disorder diagno-
15 sis. Experiments demonstrated that the proposed neuro-fuzzy-based modeling
16 is an efficient framework for these challenging classification tasks surpassing its
17 state-of-the-art competitors in terms of classification accuracy. Additionally,
18 ALMMo-0* produced transparent AnYa type fuzzy rules, which are human in-
19 terpretable, and may help specialists to provide more accurate diagnosis. Med-
20 ical doctors can easily identify abnormal heart sounds by comparing a patient's
21 sample with the identified prototypes from abnormal samples by ALMMo-0*.

Keywords:

Autonomous Learning, Data Clouds, Evolving Fuzzy Systems, Heart Sound Classification, Rule-Based System.

22 **1. Introduction**

23 The development of models able to efficiently classify values is a hard and
24 of great importance task in a variety of knowledge domains [1]. In the case of
25 heart sound classification it is of vital importance as most of the heart valve
26 disorders are reflected to heart sounds [2]. Heart sounds are characterized by
27 low frequency signals produced by heart valves [3]. However, disorders caused
28 by turbulence in the blood circulation through contracted heart valves or reflow
29 through the valves between atria and ventricles cause high frequency sounds.
30 Such abnormal sound is known as murmur [4].

31 According to [5], cardiovascular disease is one of the leading cause of mor-
32 bidity and mortality worldwide with an estimated 17.9 million, or 31.0% of the
33 global population, have died from cardiovascular diseases related conditions in
34 2017. In low to middle income countries, this situation is particularly alarming,
35 as high quality diagnostics can be often difficult to obtain, due to its high costs in
36 these regions [6]. As stated in [7], heart sounds may include indicators of disor-
37 der, or warnings about future disorders. These indicators may be present during
38 at all time occurring throughout the whole signal, or can occur randomly. Ac-
39 curate heart sound classification allows more time for emergency management,
40 preparation and mobilization of resources for recovery, and may save many lives
41 [8]. Additionally, better classification results improve the predictions of other
42 metrics such as blood pressure [9].

43 As the quality of monitoring data has improved over the years [6], data
44 become indispensable in operational heart sound classification models. However,
45 uncertainty contained in numerical models vary substantially as heart sounds
46 change their pattern due to complex and highly nonstationary nature of heart
47 sound signals, with negative effects on the quality of the classification task [10].

48 Advanced classifiers have been proposed specifically for heart sound classi-
49 fication, such as neural-network-based [3], and support vector machine [11, 12]
50 classifiers. However, if they are not equipped with evolving algorithms capable
51 of adapting their parameters and structure, then they are not able to capture
52 certain time-varying properties of nonstationary heart sound conditions and fea-
53 tures of a rich variety of vibrations of the heart and blood flow [6]. Although,
54 several studies have been conducted the digital recording of heart sounds, named
55 as phonocardiogram (PGC). There is a lack of studies using transparent rule-
56 based approaches that provide explainable and interpretable results for special-
57 ists [13, 14, 15]. Most of the existing studies are with ‘black box’ approaches or
58 very complex models [16, 17, 18].

59 Moreover, as the volume of the data collected continuously with a fast rate
60 has increased due to the advent of the Internet of Things (IoT), automation
61 of complex systems, and proliferation of small-scale computing devices, data
62 stream processing has become an issue of primary importance [19, 20]. A way
63 to deal with such large volumes of data is through the use of a class of compu-
64 tational methods known as evolving intelligent systems [21, 22, 23, 24, 25, 26].
65 The evolving approach is an effective and efficient way of handling data streams
66 due to its ability to adapt models to different situations and provide quick re-
67 sponse to changes [27, 28]. Evolving systems have demonstrated great ability
68 to deal with medical applications as one can see in [29, 30, 31, 32].

69 A granular neural network framework for evolving fuzzy system is introduced
70 by [29] and it demonstrated great ability to deal with Parkinson’s symptom
71 prediction surpassing its competitors in terms of accuracy due to its ability to
72 adapt itself on a non-stationary environment. According to [30] spiking neural
73 networks have revealed themselves as one of the most successful approaches to
74 model the behavior and learning potential of the brain, and exploit them to
75 undertake practical online learning tasks due to its evolving ability. Moreover,
76 [31] has shown that eClass can effectively be applied to the classification of
77 diabetes and dermatological diseases from discrete numerical samples.

78 This paper we propose a new a new method to autonomously classify ab-

79 normal heart disorders through sounds. It builds upon the recently introduced
80 zero-order Autonomous Learning Multiple-Model (ALMMo-0) classifier [33, 34].
81 The ALMMo-0 classifier is significantly extended as we add a standardization
82 and normalization pre-processing structure. The pre-processing block helps to
83 improve the accuracy of the classifier as it creates more stable models [35]. The
84 proposed approach has a learning mechanism composed of a massively parallel
85 set of 0-order fuzzy rules, which are able to self-adapt and provide transparent
86 and human understandable *IF ... THEN* representation [36]. It is also able
87 to self-evolve its structure and self-update its meta-parameters as newly ob-
88 served training images arrive from the data stream, which makes the classifier
89 applicable for real-time applications [37, 38]. Due to its evolving structure, the
90 proposed method is able to deal with large volumes of data, avoiding the curse
91 of dimensionality.

92 A ‘PhysioNet’ dataset was considered in the analysis. The ‘Phisionet’ dataset
93 is composed of eight independent heart sound databases sourced from several
94 contributors around the world. Data were collected from either clinical and
95 nonclinical environment, and from healthy and pathological patients. Both
96 healthy and pathological patients include children and adults [39]. The dataset
97 is provided by [39], and it was used in the ‘Computing in Cardiology Challenge’,
98 which is the major challenge involving computing and cardiology.

99 In brief, the main contributions of this paper are:

- 100 • It offers a new method to automatically classify heart disorders through
101 sounds.
- 102 • An extended version of the recently zero-order Autonomous Learning
103 Multiple-Model (ALMMo-0) classifier with a improved pre-processing block.
- 104 • A human-interpretable, computationally efficient classifier outperforming
105 the competitors.

106 The remainder of this paper is structured as follows. Section II presents the
107 proposed extended Zero-order Autonomous Learning Multiple-Model (ALMMo-

108 0*) system classification approach. Section III describes the methodology em-
109 ployed in the analyses, and the performance indexes used for comparison. Re-
110 sults and discussions are shown in Section IV. Conclusion and future research
111 directions are given in Section V.

112 2. ALMMo-0* Neuro-Fuzzy System

113 Traditionally the pipeline of learning from data has the following steps:

114 1)Pre-processing, which includes different substeps like normalization, stan-
115 dardization, dealing with missing data, and feature selection [40]. Specifically
116 for image processing there are often other stages, such as rotation, augmenta-
117 tion, scaling, elastic deformation, etc [41]. Even deep learning methods which
118 claims to avoid handcrafting applies some of the cited steps.

119 2)Learning phase, which can be offline, when the complete dataset is avail-
120 able; or it can be done online, when the data arrives in the form of data streams
121 (sample-by-sample). Evolving learning, ability of the algorithms to adapt their
122 parameters and structure according to data streams, is non sophisticated form
123 of online learning [42, 28].

124 3)Generating outputs for new unseen data, which is the validation phase.
125 Different algorithms use different strategies in order to validate the model gen-
126 erated in the learning phase.

127 The proposed method also starts with a pre-processing step which involves
128 mostly the same steps depending on the specific problem, for example, for image
129 processing we may also apply scaling, augmentation, rotation. Practically for
130 all problems normalization and standardization is required. The technique we
131 use is as follows:

132 First of all, let $\{x_1, x_2, \dots, x_N, \dots\}$ ($x_i = [x_{i,1}, x_{i,2}, \dots, x_{i,M}]^T$) be a particular
133 data stream in a M dimensional real space, s^M . The subscript i denotes the
134 time instance at which x_i arrives. It is assumed that the data stream is com-
135 posed of samples of C different categories/classes, and, thus, the stream can be
136 divided into C sub-data streams in accordance to the categories that the data

137 samples belong to (one sub-stream per category). At the N^{th} time instance,
 138 the c^{th} sub data-stream is denoted as $\{x_{c,1}, x_{c,2}, \dots, x_{c,N_c}\}$, where $c = 1, 2, \dots, C$
 139 and $\sum_{c=1}^C N_c = N$. Unless specifically declared otherwise, all the mathemat-
 140 ical derivations in the remainder of this paper are conducted at the N^{th} time
 141 instance by default.

142

143 2.1. Architecture

144 The ALMMo-0* is build upon on the ALMMo-0 neuro-fuzzy system [33]
 145 which based on the zero-order parallel IF...THEN rules of AnYa type [43]. The
 146 general architecture of the ALMMo-0* is given in Figure 1. Figure 1(a) presents
 147 the architecture of the neuro-fuzzy system during the system identification stage;
 148 Figure 1(b) gives the system architecture during the validation stage; Figure 1(c)
 149 is the zoomed-in architecture of the c^{th} parallel IF...THEN rule ($c = 1, 2, \dots, C$).

150

The ALMMo-0* neuro-fuzzy system, as illustrated in Figure 1, is composed
 of C parallel IF...THEN rules, each of which corresponds to one of the C cate-
 gories and has the following form ($c = 1, 2, \dots, C$)[33]:

$$\begin{aligned}
 &IF (x \sim p_c^1) OR (x \sim p_c^2) OR \dots OR (x \sim p_c^{P_c}) \\
 &THEN (category \ c)
 \end{aligned} \tag{1}$$

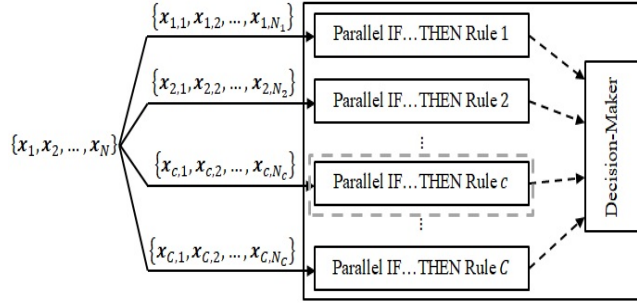
151 where $p_{c,j}$ ($j = 1, 2, \dots, P_c$) is the j^{th} prototype of the c^{th} category; P_c is the
 152 number of the identified prototypes in total from the observed data samples of
 153 the c^{th} category.

154

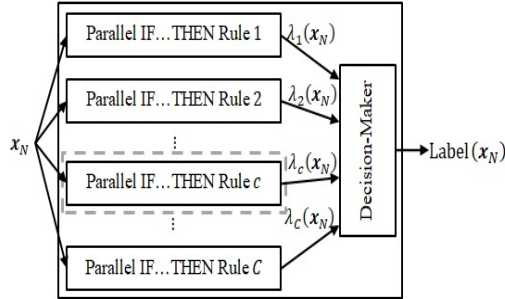
155 As one can see from equation (1) and Figure 1, each parallel IF...THEN
 156 rule is built upon a number of prototypes that are identified from data samples
 157 of the corresponding sub-data stream through a nonparametric, self-organizing,
 158 self-evolving, online learning process in parallel. The prototypes are connected
 159 by the local decision-maker, which decides the output of the IF...THEN rule

160 during the validation process using the “winner takes all” principle. There-
 161 fore, the IF...THEN rule can be also viewed as a series of simpler fuzzy rules of
 162 AnYa type [43] with singleton consequences connected by logic “OR” operator.
 163 Thanks to the prototype-based nature, the ALMMo-0 neuro-fuzzy system sup-
 164 ports collaborative learning as well [44].

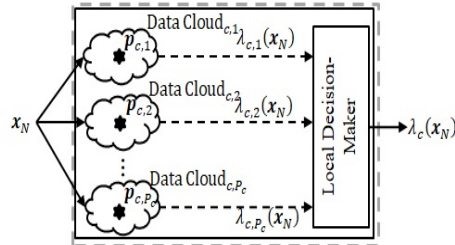
165



(a) The architecture for identification



(b) The architecture for validation



(c) Zoom-in structure of the c^{th} parallel IF...THEN rule

Figure 1: The general architecture of ALMMo-0*.

166 In the following two subsections, we will summarize the main steps of the
 167 system identification and validation processes. For the detailed algorithmic
 168 procedures, please refer to [33, 44].

169 2.2. Identification Process

170 As each parallel IF...THEN rule is identified through a independent pro-
 171 cess from others, we present the identification process of the c^{th} rule as follows
 172 ($c = 1, 2, \dots, C$). One can apply the same principle to all IF...THEN rules of the
 173 rule base.

174

175 The same principle to all IF...THEN rules of the rule base may be applied.

176

177 **Step 1.** Standardize the newly observed data sample, $x_{c,k}$

$$x_{c,k} = \frac{x_{c,k} - \min_{\forall k}(x_{c,k})}{std(x_{c,k})} \quad (2)$$

178 Then, the data are rescaled within the range $[0, 1]$ to consider variables in
 179 the same proportion. Unity-based normalization of the c -th element of the k -th
 180 sample is given by:

$$x_{c,k} = \frac{x_{c,k} - \min_{\forall k}(x_{c,k})}{\max_{\forall k}(x_{c,k}) - \min_{\forall k}(x_{c,k})} \quad (3)$$

181 If $k = 1$, go to **Step 2**; otherwise, go to **Step 3**.

182

Step 2. Initialize the global meta-parameters with the first data sample,
 $x_{c,1}$ observed:

$$P_c \leftarrow 1; \quad \mu_c \leftarrow x_{c,1}; \quad (4)$$

183 where μ_c denotes the global mean of data samples of the c^{th} category.

184

Secondly, initialize the first data cloud, $C_{c,1}$:

$$\begin{aligned} C_{c,1} &\leftarrow \{x_{c,1}\}; & p_{c,1} &\leftarrow x_{c,1}; \\ S_{c,1} &\leftarrow 1; & r_{c,1} &\leftarrow r_o; \end{aligned} \quad (5)$$

185 where, $p_{c,1}$ is the prototype of $C_{c,1}$; $S_{c,1}$ is the corresponding support (num-
 186 ber of members); $r_{c,1}$ is the corresponding radius of area of influence of $C_{c,1}$;
 187 r_o is a constant for stabilizing the new data cloud. In this paper, we use
 188 $r_o = \sqrt{2 - 2\cos(30^\circ)}$, which is the same as [33].

189

Finally, initialize the IF...THEN rule:

$$R_c : \quad IF (x \sim p_{c,1}) \quad THEN (category \ c) \quad (6)$$

Step 3. Calculate the data density at $x_{c,k}$ and $p_{c,j}$ ($j = 1, 2, \dots, P_c$) [44]:

$$D_{c,k}(z) = \frac{1}{1 + \frac{\|z - \mu_c\|^2}{1 - \|\mu_c\|^2}}; \quad (7)$$

190 where, $z = x_{c,k}, p_{c,1}, p_{c,2}, \dots, p_{c,P_c}$.

191

Then, identify the nearest prototype p_{c,n^*} to $x_{c,k}$:

$$n^* = \underset{j=1,2,\dots,P_c}{\operatorname{argmin}} (\|x_{c,k} - p_{c,j}\|) \quad (8)$$

If the following condition (equation (9)) [33] is met, go to **Step 4**; otherwise,
 go to **Step 5**.

$$\begin{aligned} &IF (D_{c,k}(x_{c,k}) > \max_{j=1,2,\dots,P_c} (D_{c,k}(p_{c,j}))) \\ &OR (D_{c,k}(x_{c,k}) < \min_{j=1,2,\dots,P_c} (D_{c,k}(p_{c,j}))) \\ &OR (\|p_{c,n^*} - x_{c,k}\| > r_{c,n^*}) \\ &THEN (add a new data cloud) \end{aligned} \quad (9)$$

Step 4. Add a new data cloud:

$$\begin{aligned} P_c &\leftarrow P_c + 1; & C_{c,P_c} &\leftarrow \{x_{c,k}\}; \\ p_{c,P_c} &\leftarrow x_{c,k}; & S_{c,P_c} &\leftarrow 1; \\ & & r_{c,P_c} &\leftarrow r_o; \end{aligned} \quad (10)$$

192 Then, go to **Step 6**.

Step 5. Update the meta-parameters of the nearest data cloud:

$$\begin{aligned} C_{c,n^*} &\leftarrow C_{c,n^*} + \{x_{c,k}\}; \\ p_{c,n^*} &\leftarrow \frac{S_{c,n^*}}{S_{c,n^*} + 1} p_{c,n^*} + \frac{S_{c,n^*}}{S_{c,n^*} + 1} x_{c,k}; \\ S_{c,n^*} &\leftarrow S_{c,n^*} + 1; \\ r_{c,n^*} &\leftarrow \sqrt{\frac{r_{c,n^*} + (1 - \|p_{c,n^*}\|^2)^2}{2}}; \end{aligned} \tag{11}$$

193 Then, go to **Step 6**.

194 **Step 6.** Update the IF...THEN rule, R_c with the identified prototypes:

$$\begin{aligned} R_c : \quad &IF (x \sim p_{c,1}) OR \dots OR (x \sim p_{c,P_c}) \\ &THEN (category \ c) \end{aligned} \tag{12}$$

195 The ALMMo-0* Predict learning and estimation algorithm is summarized
196 below.

197

ALMMo-0*: Learning Procedure

199 1: While the new data sample of the the c -th class $x_{c,k}$ available

200 2: Standardize and Normalize $x_{c,k}$ according to equations 2 and 3

201 3: **IF** $k = 1$

202 4: $P_c \leftarrow 1$;

203 5: $\mu_c \leftarrow x_{c,1}$;

204 6: $C_{c,1} \leftarrow x_{c,1}$;

205 7: $p_{c,1} \leftarrow x_{c,1}$;

206 8: $S_{c,1} \leftarrow 1$;

207 9: $r_{c,1} \leftarrow r_o$;

208 10: **ELSE**

209 11: Calculate $D_{c,k}$ using equation 7;

210 12: Update $p_{c,j}$ ($j = 1, 2, \dots, P_c$) using equation 7;

211 13: **IF** Condition (eq. 9) is satisfied **THEN**

212 14: Add a new data cloud using equation 10;
 213 15: **ELSE**
 214 16: Updated nearest data cloud using equation 11;
 215 17: **END**
 216 18: **END**

217 2.3. Validation Process

218 Each available validation data sample is sent to all AnYa FRB sub-classifiers
 219 corresponding to the C classes of the dataset. As each class may have several
 220 AnYa type of fuzzy rules, the output, namely, the score of confidence λ of each
 221 AnYa FRB rule is given as follows:

$$R_c : \text{ IF } (x \sim p_{c,1}) \text{ THEN } (\lambda_j = \exp(-\frac{1}{2} \|x - p_{c,1}\|^2)) \quad (13)$$

222 The “winner takes all” operator is used to select the most confident rule and
 223 assign the validation data sample the corresponding label. In other words, each
 224 validation data sample is compared to all prototypes identified in the training
 225 phase, and a label is attached to his validation data sample according to the
 226 label of the nearest identified prototype as illustrated in Figure 2.

$$Label = \underset{j=1,2,\dots,P}{\operatorname{argmax}} (\lambda_j) \quad (14)$$

227 3. Numerical Results

228 The ‘PhysioNet’ dataset contains a total of 13015 samples of heart sound
 229 recordings, lasting from 5 seconds to just over 120 seconds. Recordings were
 230 collected from different locations on the body, including aortic area, pulmonic
 231 area, tricuspid area and mitral area. The collected heart sound recordings were
 232 divided into two types: normal and abnormal heart sound recordings. The
 233 normal recordings were from healthy subjects and the abnormal ones were from

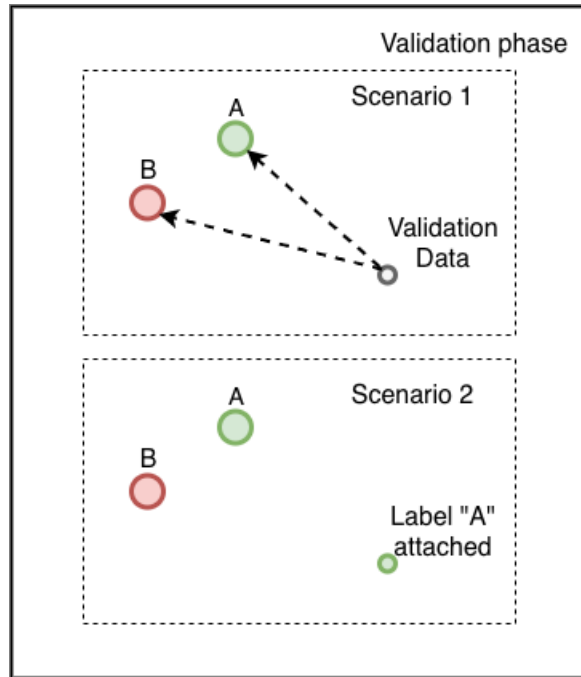


Figure 2: Validation phase illustration.

234 patients with a confirmed cardiac diagnosis. Figure 3 illustrates the normal and
 235 abnormal heart sound over time, while Figure 4 shows the power spectrum over
 236 the normalized frequency for both normal and abnormal heart sound conditions
 237 [39, 45].

238 3.1. Pre-Processing

239 The ‘PhisoNet’ dataset was divided into 70% for training and 30% for val-
 240 idation purposes. It is important to highlight that the ‘PhisoNet’ dataset is
 241 imbalanced as it contains 3158 samples of normal condition heart sounds and
 242 9857 samples of abnormal sounds.

243 The following types of features were extracted from the heart sound record-
 244 ings:

- 245 • Statistical features: mean, median, and standard deviation.

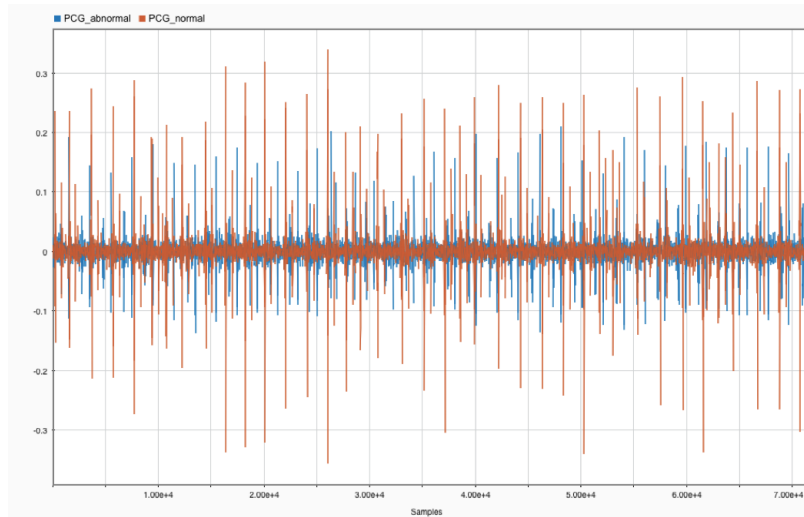


Figure 3: Normal and abnormal heart sound over time

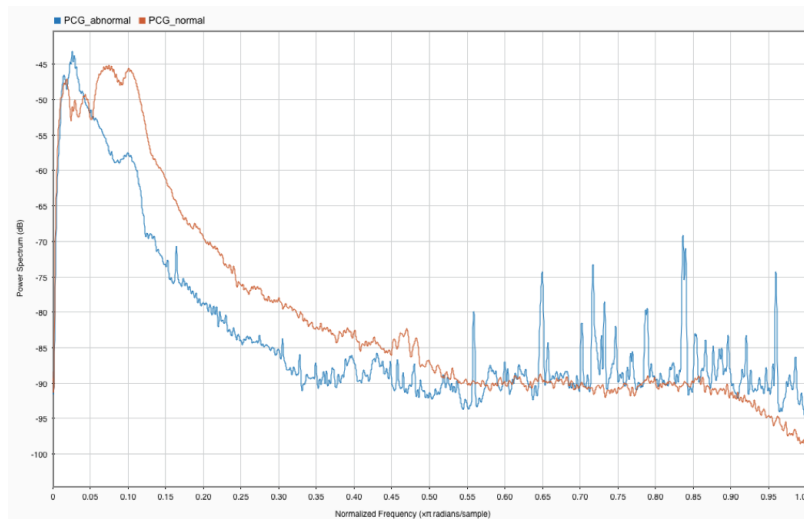


Figure 4: Power spectrum over the normalized frequency

- 246 • Signal processing features: dominant frequency, spectrum entropy, and
- 247 Mel Frequency Cepstral Coefficients (MFCC).

248 Dominant frequency refers to the most relevant frequency in the sound spec-

249 trum [46]. Spectrum entropy is defined as a measure of its spectral power
250 distribution, and it is based on the Shannon entropy [47]. Spectrum entropy
251 treats as a probability distribution the signal's normalized power distribution
252 in the frequency domain. Then, it calculates the Shannon entropy of it, see [48]
253 for detailed proof for spectrum entropy.

254 Mel Frequency Cepstral Coefficients is a representation of the short-term
255 power spectrum of a sound, based on a linear cosine transform of a log power
256 spectrum on a nonlinear mel scale of frequency [49].

257 MFCCs are commonly derived as follows [49]:

- 258 • Divide the signals into frames
- 259 • Take the Fourier transform of each signal.
- 260 • Take the logs of the amplitude spectrum.
- 261 • Take the discrete cosine transform of the list of logs generated in the
262 previous step.
- 263 • The MFCCs features are the amplitudes of the resulting spectrum.

264 Therefore, 27 features extracted from the audio recordings signals are de-
265 scribed in Table 1.

Table 1: Features Summary

Features	Quantity	Type
Mean	1	Statistical
Median	1	Statistical
Standard Deviation	1	Statistical
Mean Absolute Deviation	1	Statistical
Quantile 25	1	Statistical
Quantile 75	1	Statistical
Signal IQR	1	Signal Processing
Sample Skewness	1	Statistical
Sample Kurtosis	1	Statistical
Signal Entropy	1	Signal Processing
Spectral Entropy	1	Signal Processing
Dominant Frequency Value	1	Signal Processing
Dominant Frequency Magnitude	1	Signal Processing
Dominant Frequency Ratio	1	Signal Processing
MFCC	13	Signal Processing

266 *3.2. Performance Evaluation*

267 In order to evaluate the performance of the considered methods the follow-
 268 ing indexes are considered: sensitivity (Se), specificity (Sp), and overall score
 269 (MAcc). These indexes are calculated as:

$$Se = \frac{TP}{TP + FN}, \quad (15)$$

$$Sp = \frac{TN}{TN + FP}, \quad (16)$$

$$MAcc = \frac{Se + Sp}{2}. \quad (17)$$

270 where TP, FP, TN, FN denote true and false, negative and positive respectively.

271 Sensitivity is considered as an indicator of the classifier’s ability to discover
272 the true class. Specificity is considered as a index of the classifier’s ability to
273 define other classes. The overall score (MAcc) is given by the mean of sensitivity
274 and specificity indexes.

275 The receiver operating characteristic (ROC) method is also considered in the
276 analysis. As the ROC method is insensitive to both changes in class distribution
277 and proportion of samples per class it provides a convenient way to evaluate the
278 quality of evolving classifiers in nonstationary environment [50].

$$TP_{ratio} = \frac{TP}{TP + FN} \quad (18)$$

$$FP_{ratio} = \frac{FP}{FP + TN} \quad (19)$$

279 Each cut-off threshold in the ROC approach corresponds to a point (sensi-
280 tivity/specificity pair) in the ROC space [50]. The closer the ROC curve is to
281 the upper left corner, the better is the classification rate.

282 All the experiments were conducted with MATLAB 2018a using a personal
283 computer with a 1.8 GHz Intel Core i5 processor, 8-GB RAM, and MacOS oper-
284 ating system. The classification experiments were executed using 10-fold cross
285 validation under the same ratio of training-to-testing sample sets. The proposed
286 approach is compared with results obtained by Computing in Cardiology Chal-
287 lenge winners in order to determine the efficiency of the proposed model. Data
288 and methods used in this research are available upon request.

289 3.3. Classification Results

290 In this section we will demonstrate the results obtained for heart sounds clas-
291 sification. Computational simulations were performed to assess the accuracy of
292 the classification methods considering heart sounds recordings. Table ?? sum-
293 marizes the results obtained by the proposed ALMMo-0* and its competitors

294 considering the ‘Classification of Normal/Abnormal Heart Sound Recordings’
 295 dataset provided by Phisionet. Were considered 27 features inputs in the data
 296 space in order to determine if the patient heart sound is classified as normal or
 297 abnormal. Initial parameters were set in order that the final structure of the
 298 ALMMo-0*, and ALMMo-0 contained a reasonable amount of identified proto-
 299 types, improving interpretability of the final model. The following parameter
 300 was chosen: $r_o = \sqrt{2 - 2\cos(30^\circ)}$ for the ALMMo-0*, and ALMMo-0 neuro-
 301 fuzzy classifiers.

Table 2: Performance Comparasion: Heart sound classification

Method	<i>Sensitivity(Se)</i>	<i>Specificity(Sp)</i>	<i>MAcc</i>
ALMMo-0*	0.9082	0.9526	0.9304
ALMMo-0	0.7930	0.9430	0.8680
AdaBoost & CNN [6]	0.9424	0.7781	0.8602
Ensemble of SVMs [6]	0.8691	0.8490	0.8590
Regularized Neural Network [6]	0.8743	0.8297	0.8520
MFCCs, Wavelets, Tensors & KNN [6]	0.8639	0.8269	0.8454
Random Forest + LogitBoost [6]	0.8848	0.8048	0.8448
Ensemble of neural networks [51]	0.8982	0.9253	0.9117
Deep Structured Features [10]	0.8450	0.8690	8380
Matrix norm sparse coding + 20 time-domain features [52]	0.8867	0.8816	0.8841

302 Table 2 shows that the ALMMo-0* approach has the higher accuracy per-
 303 formance. ALMMo-0* could obtain better results in terms of *Sp* and *MAcc*
 304 than its competitors, including ALMMo-0. The AdaBoost & CNN could ob-
 305 tain a better performance in terms of sensitivity, in other words, it had a better
 306 ability to discover the true class. However, ALMMo-0* showed a better perfor-
 307 mance in terms of specificity (classifier’s ability to define other classes), due to
 308 its prototype-based nature. Moreover, it had the second best result in terms
 309 of sensitivity. Therefore, the proposed approach could obtain the best result in

310 terms of overall score ($MAcc$). Figure 5 illustrates the overall accuracy perfor-
311 mance of the best considered approaches.

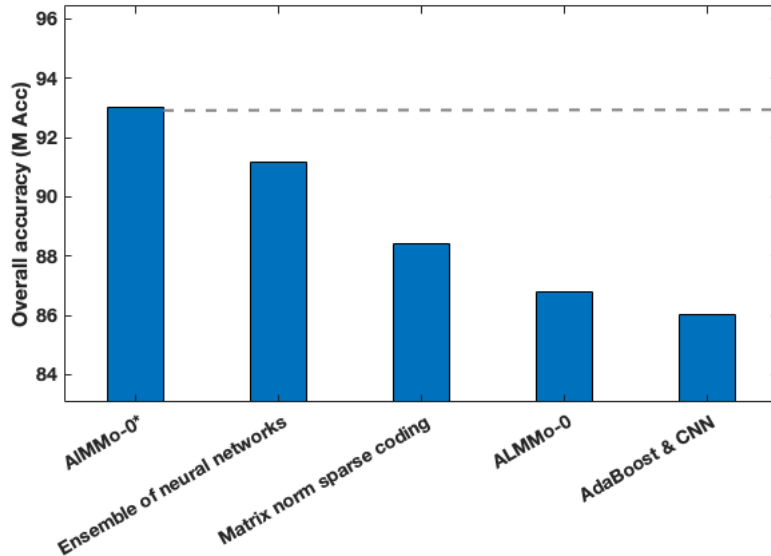


Figure 5: Overall accuracy performance of the best considered approaches

312 The area under the ROC curves confirms that ALMMo-0 is able to work
313 efficiently in this classification problem, no matter if the distribution is changed
314 to any other distribution or if the dataset is imbalanced. The area above the
315 ALMMo-0 ROC curve refers in part to 5.81% of classification error with different
316 assigned labels.

317 The prototypes identified by ALMMo-0* are visualized in Figure 7, where
318 the first two principal components are used for visual clarity. Voronoi tessel-
319 lations are created by using these prototypes to attract nearby data samples
320 forming data clouds. Thanks to its prototype-based nature, medical doctors
321 can easily identify abnormal heart sounds by comparing a patient’s sample with
322 the identified prototypes from abnormal samples by ALMMo-0* (also see Figure
323 7).

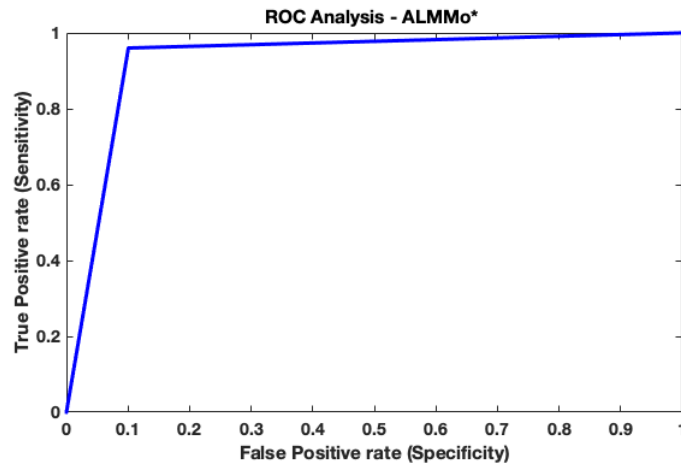


Figure 6: ROC analysis for heart sound classification using ALMMo-0*

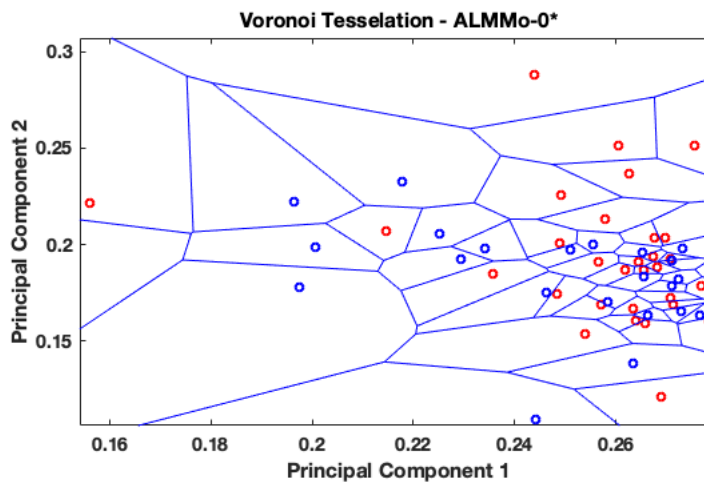


Figure 7: Voronoi Tessellation of the identified prototypes - ALMMo-0*

324 AnYa type fuzzy rules generated by the ALMMo-0* model provide a very
 325 intuitive representation for specialists. Moreover, each of the AnYa type fuzzy
 326 rules can be interpreted as a number of simpler fuzzy rules with single prototype
 327 connected by ‘OR’ operators. As a result, a massive parallelization is possible.
 328 The transparent process provided by the ALMMo-0* model supports under-

standability of the system, differing from other machine learning approaches, which are called ‘black box’, since they hide (due to its nature) from users all the insights used to generate the final resulting structure.

AnYa fuzzy rule for the Normal class in ALMMo-0* top layer can be written as following:

IF $(x \sim \{p_1^1\})$ OR $(x \sim \{p_1^2\})$ OR $(x \sim \{p_1^3\})$ OR ... OR $(x \sim \{p_1^{20}\})$
THEN ‘Normal heart sound’

The prototypes identified for the ‘Normal heart sound’ rule are demonstrated on Table 3.

In short, experiments have shown that the proposed deep neuro-fuzzy modeling is an efficient framework for heart sound classification tasks. Classification accuracies were higher than those produced by state-of-the-art approaches considered for this problem. The proposed ALMMo-0* could also achieve better results than achieve better results than ALMMo-0. Differently from the state-of-the-art approaches which are ‘black box’, the proposed method produced transparent linguistic fuzzy rules, which are human interpretable, and helpful for specialists to make a full diagnosis about the patient situation.

Generally, time to process data and adapt a fuzzy model is not a constraint for the classification problems. However, it may be an issue in higher-frequency data streams applications in real-time, as heart sound classification. ALMMo-0* adaptation deals with nonstationarities very efficiently and fast. Therefore, ALMMo-0 becomes interesting for real-time sound classification scenarios.

4. Conclusion

In this paper, we propose an extended version of the zero-order Autonomous Learning Multiple-Model neuro-fuzzy classifier in order to classify heart sounds recordings. The proposed method extends the recently introduced ALMMo-0 classifier by adding a standardization and normalization pre-processing structure, which improves the accuracy of the method as illustrated in the analysis.

355 The proposed method could obtain better results in terms of classification
356 accuracy than the state-of-the-art methods for this type of problem. Moreover,
357 the proposed autonomous learning neuro-fuzzy classifier has demonstrated to be
358 able to self-adapt its structure and provide human-understandable *IF ... THEN*
359 fuzzy rule-based system structure. Rules generated may support specialists in
360 order to make a deeper diagnosis of the patient situation. Due to its prototype-
361 based the proposed method showed a better performance in terms of specificity
362 (classifier's ability to define other classes), and also a better overall score result.
363 ALMMo-0* is able to deal with the data without making any prior assumptions
364 or training any parameters, differently from its competitors as the Convolutional
365 Neural Network approach.

366 Future research will concentrate on the development of hierarchical struc-
367 tures, in order to favor the human interpretability of the results obtained. Fur-
368 thermore, a density-based feature will be proposed to select the best features
369 that explains the problem, and also provide more interpretable results for spe-
370 cialists.

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Table 3: Identified Prototypes for the ‘Normal heart sound’ rule

Features	p_1^1	p_1^2	p_1^3	p_1^{20}
f_1	-2.7121e-05	1.5511e-04	-8.0804e-05	-5.4135e-05
f_2	1.5259e-04	0.0013	0	-1.2207e-04
f_3	0.0203	0.0795	0.0167	0.0096
f_4	0.0123	0.0441	0.0099	0.0057
f_5	-0.0084	-0.0220	-0.0067	-0.0034
f_6	0.0082	0.0237	0.0063	0.0030
f_7	0.0166	0.0457	0.0130	0.0064
f_8	1.4484	-0.4713	0.0276	0.2136
f_9	21.1471	15.7475	22.7916	15.4637
f_{10}	-2.7659	-1.5085	-2.9793	-3.5261
f_{11}	0.2868	0.3124	0.4749	0.3184
f_{12}	17.0982	41.0357	35.6619	21.0064
f_{13}	0.0669	0.0439	0.0278	0.0633
f_{14}	0.2244	0.2951	0.1133	0.2680
f_{15}	88.1961	100.0686	92.9163	87.5767
f_{16}	7.3405	2.4487	4.5780	5.2651
f_{17}	6.4674	7.0189	-2.6415	-4.2657
f_{18}	-0.0512	1.3058	-1.1482	6.2212
f_{19}	-2.5149	-2.9223	-3.8693	4.6041
f_{20}	-3.1430	-2.3074	-6.2024	-4.0199
f_{21}	-1.9638	0.8658	-6.2406	-7.7832
f_{22}	-0.1132	-4.5618	-3.1221	-3.3297
f_{23}	-0.2849	-5.7582	0.8459	-0.3391
f_{24}	1.6218	0.9306	-0.6360	-0.1036
f_{25}	-0.5334	-3.0779	-0.6840	-2.0954
f_{26}	-1.6926	-2.3390	1.9931	-3.0208
f_{27}	-2.0239	-0.8391	0.6190	-0.9700