

Analogue experiments on the rise of large bubbles through a solids-rich suspension: a “weak plug” model for Strombolian eruptions

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Abstract

Physical interactions between bubbles and crystals affect gas migration and may play a major role in eruption dynamics of crystal-rich magmas. Strombolian eruptions represent an end member for bubble-crystal interactions, in which large bubbles (significantly larger than the crystal size) rise through a crystal-rich near-surface magma. Indeed, volcanoes that produce Strombolian eruptions often generate ejecta with > 30 vol% (often > 45 vol%) average crystallinity. At Stromboli Volcano, Italy, average crystallinity can reach 55 vol%, which is approaching the eruptibility limit for magmas. At such high crystallinities the solids interact mechanically with each other and with bubbles. This complex rheology complicates the two-phase (liquid-gas) slug flow model often applied to Strombolian eruptions. To examine the effect of crystals on bubble rise, we performed analogue experiments in which large bubbles rise in a vertical tube filled with silicone oil and polypropylene particles. The particles have a slightly lower density than the oil, and therefore form a layer of oil + particles at the upper surface. We varied surface pressure, particle volume fraction, length of the particle-bearing cap, and bubble size to examine the ways in which these parameters influence Strombolian-type eruptions. We show that in experiments, suspended solids begin to affect bubble rise dynamics at particle volume fractions as low as 30 vol% (or, when divided by the random close packing value, a normalized particle fraction $\varphi = 0.64$). Bubbles in experiments with higher particle contents deform as they rise and burst through a small aperture, generating surface fountains that begin abruptly and decay slowly, and longer-lasting acoustic signals of lower amplitude than in crystal-poor experiments. In the experiments, particle fractions > 37 vol% ($\varphi > 0.80$) generated strong deformations on fast-expanding bubbles that applied a high stress on the cap, but they trapped bubbles that were less overpressured. Qualitatively, the gas release behavior observed in particle-rich experiments is consistent with observations of Strombolian eruptions. Moreover, we estimate that the observed crystallinity of pyroclasts at Stromboli volcano represents $\varphi > 0.8$. From this we suggest a “weak plug” model for Strombolian eruptions that evolves towards a low-viscosity

35 equivalent of Vulcanian-style plug failure with a more crystalline, stronger, and less permeable plug.
36 Importantly, this model allows the rise of several bubbles in the conduit at the same time and
37 suggests that longer-lasting, more pulsatory and complex eruptions may reveal an increase in near-
38 surface crystallinity, shedding some light on changing conduit conditions that could help determine
39 the different gas rise regimes involved in passive degassing, puffing, and different expressions of
40 Strombolian explosions.

41 **Keywords:** Eruption dynamics; Stromboli; Source mechanism; three-phase magma; Conduit
42 processes; Analogue experiments

43 1. Introduction

44 Strombolian eruptions are generally small and frequent, but can be associated with dangerous
45 paroxysms, as demonstrated by recent explosions at Stromboli volcano, Italy (2019), and Fuego,
46 Guatemala (2018). In this way, Strombolian eruptions provide direct (and often long-term) insight
47 into changes in conduit conditions that precede and follow hazardous activity. Nevertheless, while
48 Strombolian eruptions are intensively studied (primarily at Stromboli volcano), our interpretation of
49 their source dynamics is hindered by a major flaw: the traditional two-phase model for Strombolian
50 eruptions neglects the effect of crystals on bubble rise, despite the crystal-rich nature of pyroclasts
51 associated with this activity.

52 Most models for Strombolian eruptions consider Taylor bubbles (slugs) ascending in a Newtonian
53 liquid (e.g. Seyfried and Freundt, 2000; Blackburn et al., 1976; Vergnolle, 1998; Del Bello et al.,
54 2012; Hasan et al., 2019). As slugs expand during ascent, their internal pressure exceeds that in the
55 magma column above; this self-sustained bubble expansion accelerates the overlying liquid to
56 accommodate the gas volume change and increases bubble overpressure at burst (James et al.,
57 2008, 2009; Del Bello et al., 2012; Lane et al., 2013).

58 However, pyroclasts ejected by many Strombolian eruptions have moderate to high crystallinities.
59 For example, pyroclasts contain >55 vol% crystals at Etna, Italy (Polacci et al., 2006; Giordano et al.,
60 2010; Edwards et al., 2018); 30-40 vol% at Yasur, Vanuatu (Metrich et al., 2011); 45 – 55 vol% at

61 Stromboli, Italy (Metrich et al., 2010; Landi et al. 2011). This evidence has motivated models
 62 involving more complex near-surface processes including magma mingling (Lautze and Houghton,
 63 2005), conduit convection (Landi et al., 2004, 2011; Beckett et al., 2014), and near-surface
 64 rheological changes (e.g. Gurioli et al., 2014; Del Bello et al., 2015; Gaudin et al., 2017).

65 Scaled analogue experiments with gas slugs ascending from a low to high viscosity Newtonian liquid
 66 have explored the effects of a near-surface viscous transition on slug flow in a cylindrical conduit
 67 (Del Bello et al., 2015; Capponi et al., 2016, 2017). These investigations proposed three geometrical
 68 configurations of the slug-cap interactions based on the viscosity of the upper layer (the viscous
 69 “cap”) and the size of the cap relative to the bubble volume (Figure 1). Longer and more viscous caps
 70 impede bubble expansion (hence compress bubbles) below the cap, which affects pressure signals
 71 recorded at the base of the experiment, burst processes, and acoustic signals at the surface.

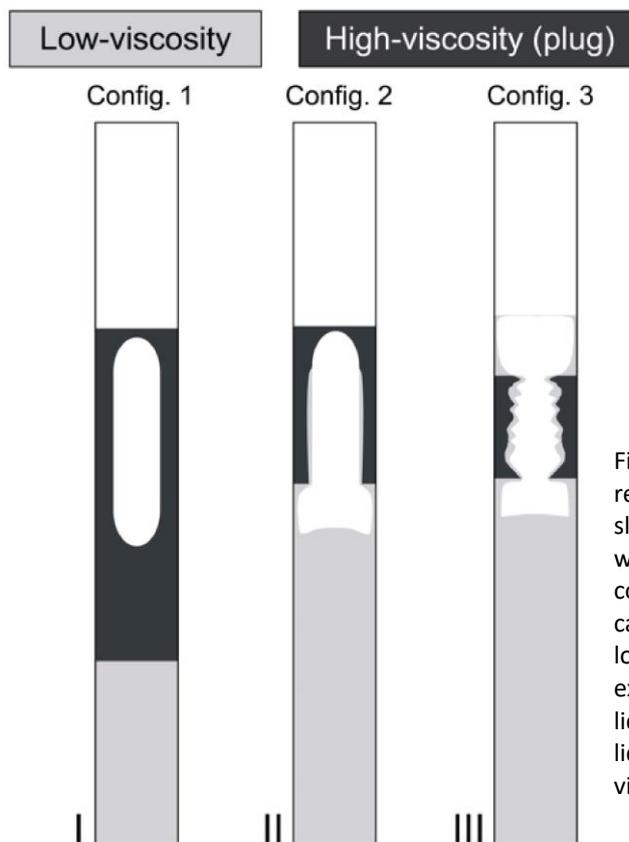


Figure 1: Flow configurations in Capponi et al. (2016, reprinted with permission). In configuration 1 (I), the slug is small enough to be fully accommodated within the cap and bursts at the cap surface. In configuration 2 (II), the bubble nose bursts from the cap into the air above while its tail is still in the lower liquid. In configuration 3 (III), bubble expansion during rise causes the lower viscosity liquid to intrude through the upper more viscous liquid, such that bubble burst occurs in the low-viscosity liquid that is replaced above the cap.

73 High magma crystallinity will not only increase viscosity but also create a non-Newtonian rheology.
74 Rheometry of synthetic and analogue magmas demonstrates that high crystallinities (> ~20-40 vol%
75 in basalts) produce both yield strengths and shear-thinning behavior (e.g. Hoover et al., 2001; Jerram
76 et al., 2003; Caricchi et al., 2007; Mueller et al., 2010; Picard et al., 2013; Moitra and Gonnermann,
77 2015). Consequently, the slug model has been modified to include both shear-thinning rheology and
78 an increasing viscosity towards the surface, which affect bubble overpressures at burst (Von der
79 Lieth and Hort, 2016). In contrast, Suckale et al. (2016) depart from the slug model, suggesting that
80 Strombolian eruptions occur by tensile failure of a porous, rigid plug, generated by bubble
81 overpressure below the plug and aided by regional tectonic stress.

82 Solid particles also directly affect bubbles by trapping, deforming, and/or splitting them (Belien et
83 al., 2010; Tran et al., 2015; Oppenheimer et al., 2015; Lindoo et al., 2017; Barth et al., 2019).
84 Migration regimes of growing bubbles depend primarily on particle concentrations (Oppenheimer et
85 al., 2015). At low particle fractions, the liquid-particle suspension is approximately Newtonian and
86 growing bubbles are round. At random loose packing (RLP, “the loosest possible random packing
87 that is mechanically stable”; Onoda and Liniger, 1990), the bubbles deform as they grow. At random
88 close packing (RCP, the maximum random packing), gas propagates in a fracture-like pattern.
89 Therefore, interaction with solids in a crystal-rich upper magma must also affect bubble morphology
90 and rise dynamics during Strombolian eruptions. In this context, we will refer to Taylor bubbles in
91 Newtonian liquids as “slugs” but use the term “bubble” for all geometries of bubbles in non-
92 Newtonian suspensions.

93 Here, we use analogue experiments to model gas bubbles rising below and into a particle-laden
94 layer, investigating how particles in suspension affect the slug rise model for Strombolian eruptions.
95 We show that particle-rich suspensions affect bubble morphology and bubble rise and generate
96 burst dynamics consistent with observations at Stromboli Volcano, Italy. Our data suggest a weak

97 plug model as a source mechanism for Strombolian eruptions at hydrous open-system mafic
98 volcanoes.

99 2. Activity at Stromboli Volcano, Italy

100 Stromboli Volcano is persistently active with eruption recurrence times of $10 - 10^3$ seconds (e.g.
101 Barberi et al., 1993; Rosi et al., 2013). Eruptions during “normal activity” last up to tens of seconds
102 and include several pulses with durations of 0.05 - 2 seconds (Patrick et al., 2007; Taddeucci et al.,
103 2013; Gaudin et al., 2014). The frequency and intensity of normal activity at Stromboli varies with
104 time, sometimes within days (Harris and Ripepe, 2007a). Strombolian eruptions are classified into
105 four sub-categories: type 0 emit very few small particles at high velocity; type 1 eject mainly coarse
106 ballistics; type 2 generate ash-rich plumes with (2a) or without (2b) ballistics (Patrick et al., 2007;
107 Harris et al., 2013; Leduc et al., 2015). Eruptions derive from the North-East (NE), central, and South-
108 West (SW) vents, with shorter, louder explosions in the NE (typically type 1), and longer, pulsatory
109 events in the SW (typically type 2; Ripepe and Marchetti, 2002; Chouet et al., 2003; Harris and
110 Ripepe, 2007a).

111 These eruptions produce pyroclasts with an average of 45 – 55 vol% phenocrysts during normal
112 activity (Landi et al., 2004; Metrich et al., 2010). Plagioclase begins to crystallize at 2 – 4 km depth
113 (Métrich et al., 2010), but plagioclase crystallinity rapidly increases ~800 m below the crater (Landi
114 et al., 2004; Agostini et al., 2013). Crystal-poor basalt resides at depths > 7 km and only erupts
115 during paroxysms (Metrich et al., 2010; LaFelice and Landi, 2011). This volatile-rich lower magma
116 provides the gas source for normal Strombolian eruptions. Therefore, a rheological transition from a
117 crystal-poor basalt to a crystal-rich cap begins at 2 – 4 km depth and accelerates at ~0.8 km depth.
118 These depths correspond to estimated slug source depths of 0.8 and 2.7 km (Burton et al., 2007),
119 estimates which assume, however, that bubbles form at chemical equilibrium and ascend quickly
120 without substantial exchange of volatiles with the melt.

121 Estimates of gas flux, however, show that Strombolian eruptions account for less than 10% of the
122 total mass of gas erupted; most outgassing occurs via puffing or quiescent degassing (Francis et al.,
123 1993; Allard et al., 1994; Harris and Ripepe, 2007b). Gas compositions indicate that non-explosive
124 outgassing has a shallow source (Burton et al., 2007). Pyroclasts ejected during puffing are less
125 crystalline than in normal explosions (Landi et al., 2011). Puffing generates lower amplitude acoustic
126 signals than Strombolian eruptions, and is generally active in one vent at a time, but migrates
127 between vents, and is therefore interpreted as a train of small weakly overpressured bubbles of
128 shallower origin than those that generate Strombolian eruptions (Ripepe et al., 2007; Landi et al.,
129 2011; Lane et al., 2013).

130 3. Methods

131 3.1. Experimental set-up

132 We performed experiments using the same apparatus as Del Bello et al. (2015) and Capponi et al.
133 (2016), although with a modified bubble injection system (Figure 2), and same low-viscosity liquid as
134 Capponi et al. (2016). A vertical 3-m-high tube of internal diameter $D = 0.0257 \pm 0.0001$ m was
135 connected to a bubble trap at its base and to a vacuum pump at the top to reduce ambient pressure
136 ($P_{\text{surf}} = 0.3 \pm 0.1$ kPa, 1 ± 0.2 kPa, 50 ± 1 kPa, and 101 ± 1 kPa) and scale for near-surface gas
137 expansion at Stromboli (James et al., 2008; Lane et al., 2013). The tube was filled to 1.43 ± 0.01 m
138 above the bubble trap with silicone oil (Wacker Chemie AG – AS 100; viscosity 0.1 ± 0.05 Pa s;
139 surface tension 0.021 N/m) and polypropylene particles (A. Schulman – Icorene N4420-1200, sieved
140 by hand). Microscope analysis of 200 particles revealed angular morphologies with an average
141 equivalent sphere diameter of 0.8 mm (standard deviation of 0.48 mm; Supplementary Material).
142 The particle density (900 kg/m^3) was slightly lower than the silicone oil (990 kg/m^3); therefore, the
143 particles rose to the top of the column and, at the start of each experiment, formed a layer of oil +
144 particles (the “cap”) above the pure oil. The caps contained particle masses of 5.4, 14, 23, 46, and 92

145 grams ($\pm 10\%$), which correspond to “packed” cap lengths of approximately 3.5, 8, 13, 25.4, and
146 53.5 cm respectively (Table 1).

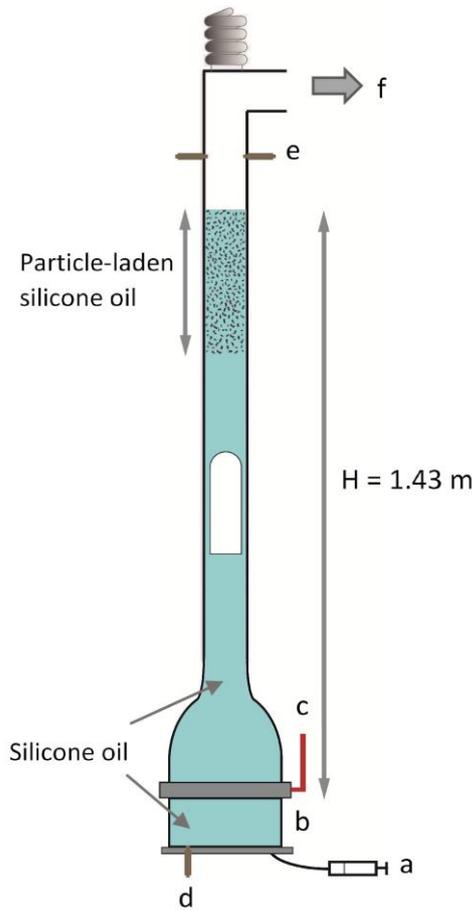


Figure 2: Experimental set-up. Gas slugs were injected through a syringe (a) into a bubble trap (b) and released using a butterfly valve (c). Measurements were made of base liquid pressure (d), gas pressure at the surface (e), along with high speed videos. Pressure at the liquid surface was controlled with a vacuum chamber (f).

147 To avoid pre-formed pathways within the cap, it was disrupted between each experiment with large
148 gas slugs that generated turbulence. This introduced small bubbles that foamed when ambient
149 pressure was reduced to experiment pressure, and dispersed particles throughout the tube. Particle
150 concentrations were then controlled by allowing the particles to rise until the cap reached the
151 desired length, so that for the same mass of particles, longer caps had lower particle concentrations.
152 For each experiment a bubble of volume 4, 10, 17, 32 or 49 ml ($\pm 10\%$) was injected into the bubble
153 trap and prevented from rising by a closed butterfly valve. When released from the trap, the bubble
154 rose as a gas slug in the tube. Cap lengths were non-dimensionalized as a function of internal tube
155 diameter (D). Particle fractions were divided by RCP to generate a normalized particle fraction, ϕ , for
156 comparison with other work involving particle-rich suspensions. RCP was measured as 47 ± 2 vol% by

157 pouring dry particles in a graduated cylinder ($D = 28$ mm) and tapping/shaking the container for
 158 minutes until the bulk volume was constant. We estimated ϕ by dividing the calculated cap length at
 159 RCP by the measured cap length in each experiment. Particle fractions were overestimated when
 160 particle-bearing clusters ejected during experiments remained attached to the tube walls. This error
 161 was larger for shorter caps because a small loss of particles caused a larger relative change in cap
 162 length. Additionally, as particle contents could vary within the cap, all reported particle fractions
 163 were averages of the full cap.

164 Simply allowing the particles to rise should have created a random *loose* packing because of the
 165 small density difference between particles and liquid (Onoda and Liniger, 1990). However, closer
 166 packings occurred ($\phi < 0.92$) because residual small bubbles shook the suspension as they ascended
 167 through the particle layer during compaction. For our particles, RLP was likely near the median value
 168 for packed caps (~ 40 vol% particles). RCP was not achieved in experiments.

169 Two differential pressure transducers (Honeywell 163PC01D36; sampling frequency 5 kHz) recorded
 170 pressure changes in the air above the liquid surface with respect to the pressure in the vacuum
 171 chamber (Lane et al., 2013). Two cameras recorded the experiments: a Basler acA2000-340km
 172 filmed the entire column at 300 ± 0.1 fps, and a Canon Powershot G15 recorded only the particle

Number of expts.	Initial bubble size (mL)	Surface pressure (kPa)	γ (plug-free)	Mass of particles (g)	Cap length (cm)	Dimensionless cap length (D)	Particle content (vol%)	ϕ
9	4, 10, 17, 32	0.3	8.8 - 70	0	0	0	0	0
15	4, 10, 17, 32, 49	1	0.83 - 10	0	0	0	0	0
8	4, 10, 32, 49	1	0.83 - 10	5.4	3 - 10	1.1 - 4.0	11 - 39	0.24 - 0.84
10	4, 10, 32, 49	50	$(1.4 - 17) \times 10^{-3}$	5.4	3 - 6	1.2 - 2.5	18 - 36	0.39 - 0.77
4	10, 49	100	$(1.6 - 7.8) \times 10^{-3}$	5.4	3 - 6	1.3 - 2.2	20 - 35	0.43 - 0.75
8	4, 10, 32, 49	1	0.83 - 10	14	7 - 12	2.8 - 4.8	24 - 42	0.52 - 0.90
12	4, 10, 32, 49	50	$(1.4 - 17) \times 10^{-3}$	14	8 - 14	3.2 - 5.6	21 - 37	0.45 - 0.79
8	10, 17, 32, 49	100	$(1.6 - 7.8) \times 10^{-3}$	14	7 - 13	2.8 - 5.1	23 - 42	0.49 - 0.90
4	10, 32	0.3	22 - 70	22 - 23.5	11 - 13	4.4 - 5.1	38 - 42	0.82 - 0.90
15	4, 10, 32, 49	1	0.83 - 10	22 - 23.5	12 - 28	4.6 - 11.0	17 - 42	0.37 - 0.90
10	4, 10, 32, 49	50	$(1.4 - 17) \times 10^{-3}$	23	13 - 20	4.9 - 7.9	24 - 39	0.52 - 0.84
12	2, 4, 10, 32, 49	100	$(0.32 - 7.8) \times 10^{-3}$	23	12 - 14	4.5 - 5.4	36 - 43	0.76 - 0.92
4	17	1	3.5	37.2	20 - 53	8.0 - 20.7	15 - 39	0.32 - 0.84
4	4, 10, 32	0.3	8.8 - 70	46	25	9.6 - 9.9	39 - 40	0.83 - 0.86
4	4, 10, 32, 49	1	0.83 - 10	46	25 - 27	9.6 - 10.5	37 - 40	0.79 - 0.85
1	32	0.3	70	92	53	20.7	38	0.8
2	10, 32	1	2.1 - 6.6	92	52 - 55	20.2 - 21.5	36 - 38	0.77 - 0.81
Total:	130	2 - 49	0.00032 - 70	0 - 92	0 - 55	0 - 21.5	0 - 43	0 - 0.92

Table 1: Summary of experimental conditions. A more detailed list is available in Supplementary Material.

173 layer at 120 ± 1 fps. The images allowed estimates of surface rise velocities, bubble shapes, and
 174 whether fragments were ejected during burst. Transducer data and the Basler videos were
 175 synchronised through LabVIEW 2014 software.

176 3.2. Suspension rheology

177 We measured suspension rheology at 20°C using a HAAKE RheoStress1 with a modified concentric
 178 cylinder geometry and gap of 11.7 ± 0.1 mm. We ran the rheometer in controlled stress mode at 10
 179 – 50 Pa with increments of 10 Pa, and for 15 – 50 seconds until the strain rate response to the

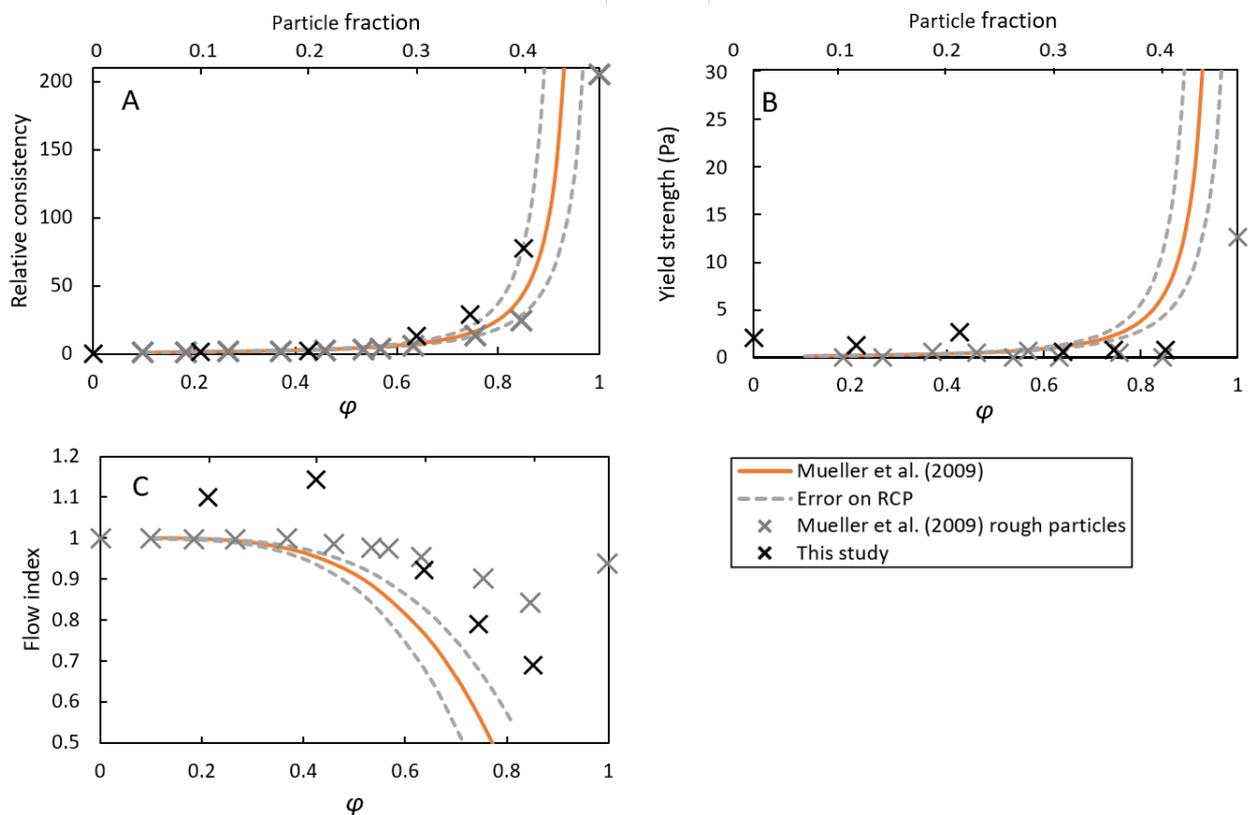


Figure 3: Rheology of the particle-bearing suspensions. Solid lines are calculated from the empirical model by Mueller et al. (2009, 2011), and dashed lines show how the error on RCP (of ± 2) modify the model. Black crosses are rheology measurements with a concentric cylinder (this study), and grey crosses are measurements by Mueller (2009) for crushed particles. Together, these three datasets give an overall idea of cap rheology. A: The relative consistency is the consistency (K) divided by the viscosity of the Newtonian liquid (0.1 Pa s here). K has the dimensions Pa s^n and is equivalent to viscosity when $n = 1$. B: Yield strength. Experiment yield strengths determined through curve fitting were relatively consistent with the experimental data for crushed particles in Mueller et al. (2009). Our first experimentally measured yield strength occurred at 40 vol% particles (Supplementary Material). C: Flow index indicates whether the suspension is shear-thinning ($n < 1$), shear-thickening ($n > 1$), or Newtonian ($n = 1$). Here, our data falls between the crushed particles and model in Mueller et al. (2009), possibly indicating large errors. The apparent shear-thickening in experiments with low ϕ may also have been caused by particle rise.

180 induced stress equalized; we recorded the strain rate over the last three seconds. Instrumental
181 errors on viscosity are ± 0.02 Pa s, although greater errors were caused by bubbles in suspension
182 and particle rise. We fitted our measurements to a Herschel-Bulkley (1926) model:

$$183 \quad \tau = \tau_y + K\dot{\gamma}^n, \quad (1)$$

184 where τ is applied stress, τ_y is yield strength, n is flow index, and K is consistency.

185 Due to the possibility of large experimental errors, we compared our data to models by Mueller et
186 al. (2009, 2011) by determining K_r (relative consistency), τ_y , and n using equations 2.4, 4.1, and 5.2
187 from Mueller et al. (2009), which requires a fitting parameter, φ_m , that represents the particle
188 fraction at which suspensions can no longer be sheared. We use our measured RCP as a best
189 approximation of φ_m . Indeed, although sheared suspensions typically generate $\varphi_m > \text{RCP}$, Mueller et
190 al. (2009) generate values close to RCP. The aspect ratio used to determine n was also generated
191 from RCP, using equation 4 in Mueller et al. (2011). Additional details are available in Supplementary
192 Material.

193 3.3. Scaling considerations

194 We modelled our experiments assuming that rapid (non-equilibrium) bubble expansion near the
195 surface at the volcano scale can be approximated at laboratory scale by varying surface pressure
196 (P_{surf} ; James et al., 2008). James et al. (2009) and Del Bello et al. (2012) define a dimensionless
197 expansion index (γ) for slug flow in a Newtonian liquid as

$$198 \quad \gamma = \frac{\rho_l g A' V_a}{P_{surf} \pi r^2 (1 - A')}, \quad (2)$$

199 with ρ_l the liquid density, g the gravitational acceleration, A' the dimensionless cross-sectional area
200 of the falling liquid film (equation (28) in Del Bello et al., 2012), V_a the slug volume at P_{surf} if it were at
201 equilibrium, and r the tube radius. Rapid bubble expansion occurs when $\gamma > 1$. Therefore, γ provides
202 an estimate of bubble expansion conditions in the Newtonian liquid below the cap, but ignores the

203 viscous resistance from the cap. Our range of P_{surf} covers the full range of slow (equilibrium) and
204 rapid (non-equilibrium) bubble expansion.

205 The density and viscosity of the lower liquid allowed bubble rise parameters, such as falling film
206 thickness, to be scaled to bubble rise in the lower (basaltic and crystal-free) magma at Stromboli
207 (Supplementary Table 1; Capponi et al., 2016). To account for uncertainty on cap thickness and
208 crystallinity at Stromboli, we covered a range of thicknesses and particle contents in experiments.
209 We did not attempt to scale particle sizes to crystal sizes at Stromboli. Instead, particle sizes were
210 chosen to avoid wall effects and preserve flow properties. We chose a conservative particle size that
211 fit >30 particles in the inner tube diameter to allow for the counter-flow of liquid + particles during
212 bubble rise in the suspension to approach a 10-particle thickness. Smaller particles could have
213 introduced non-negligible capillary and cohesion forces and increased the particle rise (cap “reset”)
214 time between experiments.

215 Other simplifications included: smooth, cylindrical walls, no density-driven convection, no bubbles in
216 the solids-rich cap, little variation in particle shape/size, a single liquid phase, no diffusion between
217 phases, and an abrupt change from a particle-absent to particle-rich suspension. We therefore
218 ignored the effects of near-surface crystallization, vesiculation, and outgassing on magma
219 convection (Palma et al., 2011; Beckett et al., 2014; Gurioli et al., 2014) and melt viscosity, and did
220 not account for the decrease in overpressure from non-adiabatic bubble expansion (Bagdassarov,
221 1994). Furthermore, we neglected the effect of crystal-scale bubbles and variations in crystal shape
222 and size on cap rheology. Additional details are available in Supplementary Material.

223 4. Results

224 After injection, gas slugs rose through the column of silicone oil until they reached the layer of oil +
225 particles (the cap). Subsequent gas migration behaviors depended on both the particle fraction in
226 the cap and the ratio of bubble size to cap length.

227 4.1. Slug rise in the particle-free liquid

228 In a tube filled with a Newtonian liquid, the slug base rises at a constant velocity, while the slug nose
229 accelerates until it bursts at the surface (e.g. Seyfried and Freundt, 2000; James et al., 2008, 2013;
230 Lane et al., 2013; Del Bello et al., 2015). In our experiments, the rise velocity of the slug base in the
231 Newtonian liquid below the particle-bearing cap was constant, regardless of cap parameters and
232 surface pressure. On average, slug base velocity $U_s = 0.149$ m/s (standard deviation 0.005 m/s). This
233 velocity is within error of the calculated velocity of 0.157 ± 0.009 m/s following Wallis (1969;
234 Supplementary Material).

235 4.2. Geometrical flow configurations

236 Slug flow in a liquid overlain by a higher viscosity liquid can be categorized by flow configurations
237 that depend on the relative sizes of the bubble and the cap (Del Bello et al., 2015; Capponi et al.,
238 2016): (1) the bubble is fully encased in the cap at burst, (2) the bubble base is still in the lower liquid
239 at burst, and (3) bubble expansion is such that the lower liquid breaks through the cap (Figure 1). To
240 compare with previous work with Newtonian caps, this section focuses on experiments with surface
241 pressures of 1 kPa because they complement data from Capponi et al. (2016).

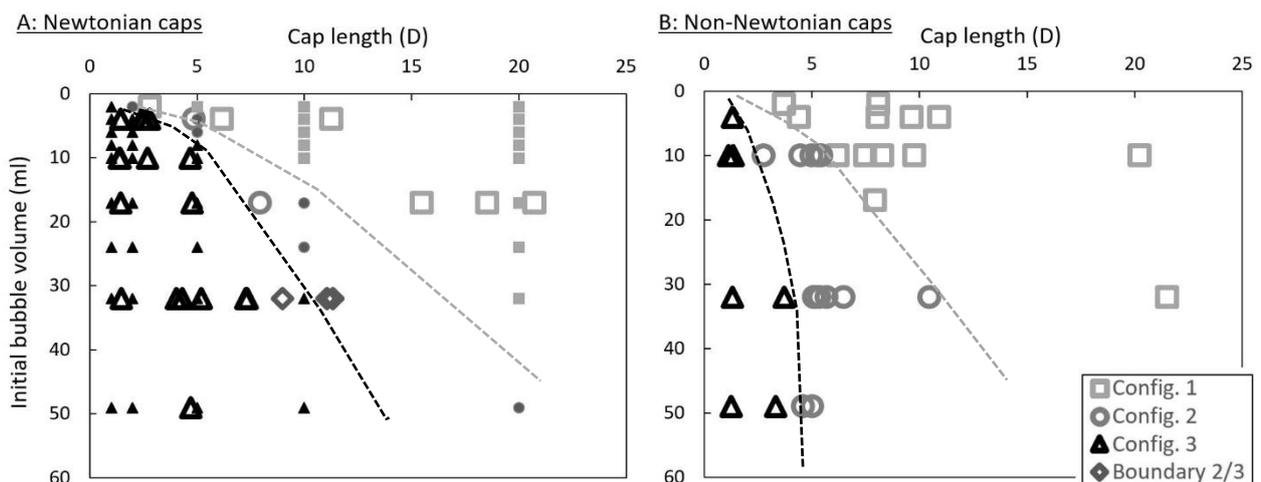


Figure 4: A: Flow configurations in Capponi et al. (2016; smaller filled symbols) and in experiments with Newtonian caps in this study ($< \sim 30$ vol% particles; large empty symbols). The “boundary 2/3” category describes experiments that were difficult to categorize due to the opacity of the particle layer: the lower liquid may or may not have reached the surface shortly ahead of the bubble. B: Flow configurations in experiments with non-Newtonian caps ($> \sim 30$ vol% particles). Since all experiments with $> \sim 30$ vol% particles are shown here, viscosities vary over ~ 1 order of magnitude. The dashed lines guide the eye to the transitions between regimes. All experiments in this figure have surface pressure = 1 kPa.

242 Our rheology measurements suggested that caps with < 30 vol% particles behaved as a Newtonian
243 fluid ($n \approx 1$; Fig. 3) with effective viscosities between 0.1 Pa s (particle-free) and ~ 0.8 Pa s (30 vol%
244 particles), which approached those used by Capponi et al. (2016; 1 Pa s). The presence of particles in
245 these experiments did not significantly affect flow configurations (Figure 4A).

246 At particle contents > 30 vol%, the cap rheology was non-Newtonian ($n < 1$ with a low yield strength,
247 Figure 3). Under these conditions, transitions between configurations occurred at shorter cap
248 lengths (Figure 4B) compared to experiments with particle-poor caps, consistent with the effect of a
249 greater cap viscosity (Capponi et al., 2016). The experiments shown in Figure 4B contained 30 – 43
250 vol% particles, corresponding to a variation in consistency of slightly over one order of magnitude
251 (Figure 3).

252 4.3. Rheological flow regimes

253 Bubble morphology and rise dynamics in the cap depended on cap rheology. Flow regimes were
254 determined through visual characteristics of bubble rise (Figures 5 and 6). In some cases, gradients in
255 particle fraction caused “hybrid” regimes, such that bubbles behaved differently at the bottom and
256 top of the cap.

257 When the cap comprised a dilute particle suspension, bubble expansion in the lower liquid caused
258 the particle-free oil to intrude into the center of the cap ahead of the bubble (Figure 7A). In the cap,
259 the bubble remained axisymmetric but its diameter decreased and it developed a rounded base. This
260 sequence matches observations of slug flow into a Newtonian liquid of higher viscosity (Del Bello et
261 al., 2015; Capponi et al., 2016), and thus we classify this regime as a **slug flow regime** (Figure 5A). At
262 low P_{surf} , the film at the bubble nose broke in several places and discharged a few liquid-particle
263 fragments, in contrast to the particle-free scenario, where bubble burst generated one accelerated
264 droplet.

265 The **side flow regime** occurred with higher particle fractions. Here, bubble expansion in the lower
266 liquid caused a finger of liquid to intrude the side of the cap and, although the lower portion of the

267 cap was diluted by the intruded liquid, most of the cap rose upwards. When it reached the cap, the
 268 bubble nose filled the finger and then slowed as it pushed the cap upwards, while the tail of the
 269 bubble continued rising as liquid drained from the falling film at the bubble walls. The bubble thus
 270 became shorter and wider, and slowly migrated upwards. The duration of coupled rise of the bubble
 271 and cap was greater for smaller bubbles and for longer caps with higher particle concentrations. In
 272 the cap, the bubble flowed against the tube wall, usually as a linear continuation of the original
 273 finger although in some cases it also spiraled slightly (Figure 5B & 7B). The particle suspension
 274 remained in one piece, deforming around the bubble. Bubble burst occurred at the side of the tube
 275 and was often accompanied by ejection of clasts that fountained above the suspension surface.

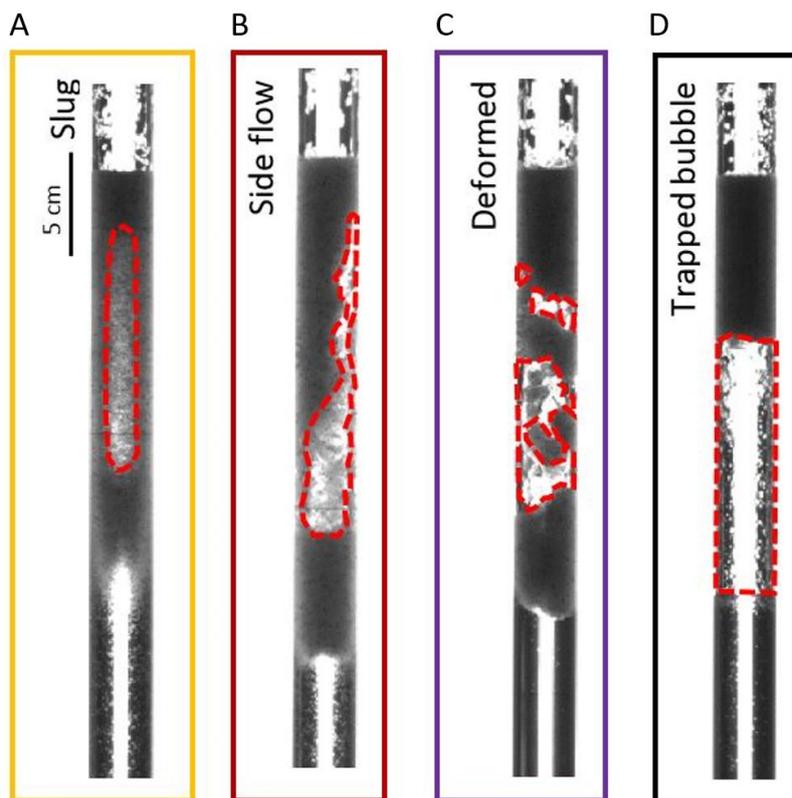


Figure 5: Comparison of the different regimes discussed in this research. These illustrative examples were produced by different experimental conditions.

276 A further increase in particle fraction induced a transition to the **deformed regime**. Here, bubble
 277 expansion in the lower liquid caused the cap to slide upwards as a plug, presumably with a film of oil
 278 at the wall; we did not explore whether the dynamics would be significantly different with a rough
 279 wall. Again, the bubble paused before entering the cap; the duration of this pause increased with
 280 particle fraction. In the cap, the bubble advanced intermittently, the particle suspension often

281 separated into several pieces, and clusters of liquid + particles slid down the side of the tube as the
 282 bubble made its way through the cap (Figure 5C & 7B,C). Accelerations and decelerations of the cap
 283 surface reflected variations in bubble expansion rate. The bubble burst at the side of the tube and
 284 generated a fountain of small clasts (supplementary video 2).

285 At high particle fractions and low bubble expansion, some bubbles remained trapped indefinitely
 286 below (Figure 5D) or within the cap, thus defining the **trapped bubble regime**. Bubbles trapped
 287 within the cap initially rose in the side flow or deformed regime, then decelerated and stopped. The
 288 trapped bubbles could often be mobilized by injecting another slug at the base of the apparatus,
 289 when the sudden displacement of the entire column caused by slug injection and expansion was
 290 sufficient to push the trapped bubble upwards and break the cap. This process sometimes had to be
 291 repeated several times before the trapped gas was mobilized sufficiently to escape.

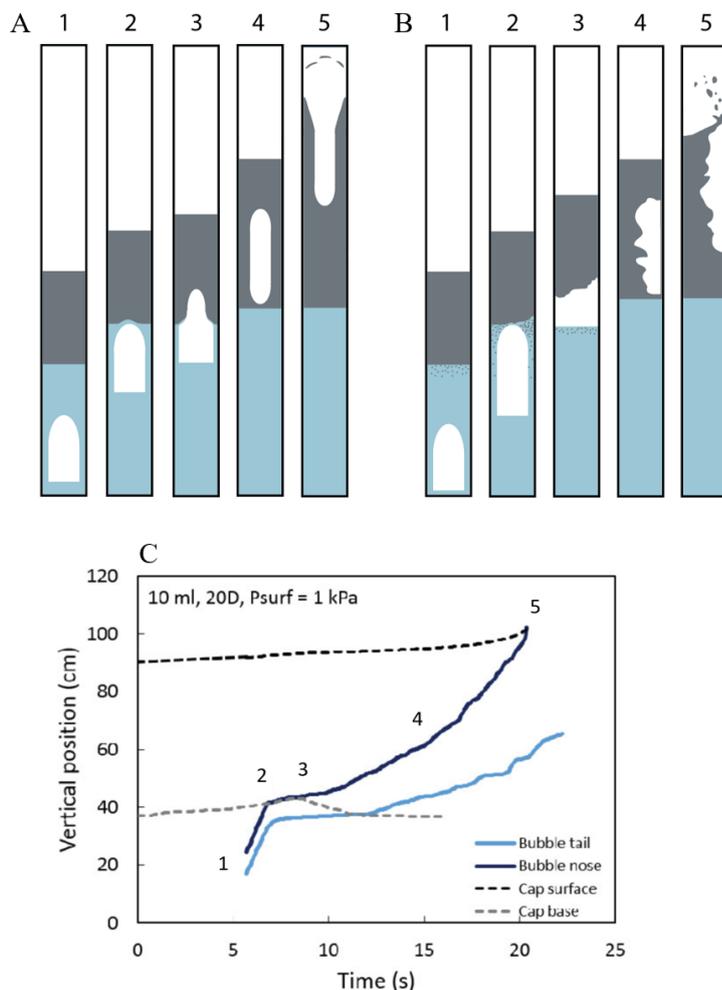


Figure 7: Bubble rise in the rheologically layered experiments can be subdivided into stages of ascent, as shown in (A) for a Newtonian cap and (B) for a non-Newtonian cap. (C) Shows tracks of the bubble, the cap, and the surface of an experiment in the deformed regime, for a bubble of initial volume 10 ml and $\gamma > 1$. First, the slug rose in the lower liquid (1). When the slug reached the cap (2), bubble behavior depended on flow regime. In the slug flow regime, bubbles flowed seamlessly from the lower liquid into the upper liquid. In the side and deformed regimes, bubbles were temporarily trapped below the cap. As the bubble pierced the cap (3), a portion of the liquid + particle suspension flowed down the side of the tube, forming a thick bubble film that is viscously supported by the tube wall. In stage (4), the bubble was fully encased in the cap, and in (5) the bubble burst at the surface. Note that in stage (4) the shear-thinning rheology is visible in the overall curvature of the bubble base position in (C). Base velocities of conduit-filling bubbles are constant in Newtonian liquids (White and Beardmore, 1962; Viana et al., 2003). Here, the bubble base accelerates upward with time as its increasing overpressure interacts with the shear-thinning cap.

292

293 4.4. Regime diagrams

294 Of the four parameters varied in our experiments (particle fraction, initial bubble volume, surface
295 pressure, and cap length), particle fraction provided the dominant control on regime transitions.
296 Bubble expansion, controlled mainly by surface pressure but also by initial bubble size, had a
297 moderate effect. Cap length, while affecting other flow characteristics, did not affect regimes (Figure
298 6).

299 Slug flow occurred only at particle fractions <30 vol%, or $\varphi < 0.64$, regardless of other parameters
300 (Figure 6, orange dashed line). The departure from the slug flow regime at $\varphi \approx 0.64$ corresponds
301 approximately to the departure from Newtonian rheology (Figure 3C). Immediately above $\varphi \approx 0.64$,
302 bubbles travelled through the cap in either the side flow or deformed regime. The transition
303 between these regimes depended on both the expansion index γ (an indicator of stress on the cap)
304 and particle fraction. In experiments with $\gamma < 1$ (low bubble expansion), the deformed bubble regime
305 was observed in experiments with particle contents >35 vol% ($\varphi > 0.75$). At $\gamma > 1$, the deformed
306 regime began at ~ 37 vol% particles ($\varphi \approx 0.80$; Figure 6A).

307 Bubbles were trapped at $\gamma < 1$ and high particle volume fractions. Notably, all bubbles with $\gamma < 1$ that
308 interacted with a cap containing >37 vol% particles ($\varphi > 0.80$) were trapped, even for thin caps
309 (Figure 6A,B). Bubble entrapment below, rather than within, the cap (Figure 5D) also occurred
310 primarily at $\varphi > 0.80$, although bubble entrapment within the cap occurred at $\varphi > 0.7$, plausibly
311 recording a hybrid regime between trapped bubbles and bubbles that break the surface. All trapped
312 bubbles applied buoyancy forces < 0.6 N on the cap (Figure 6C).

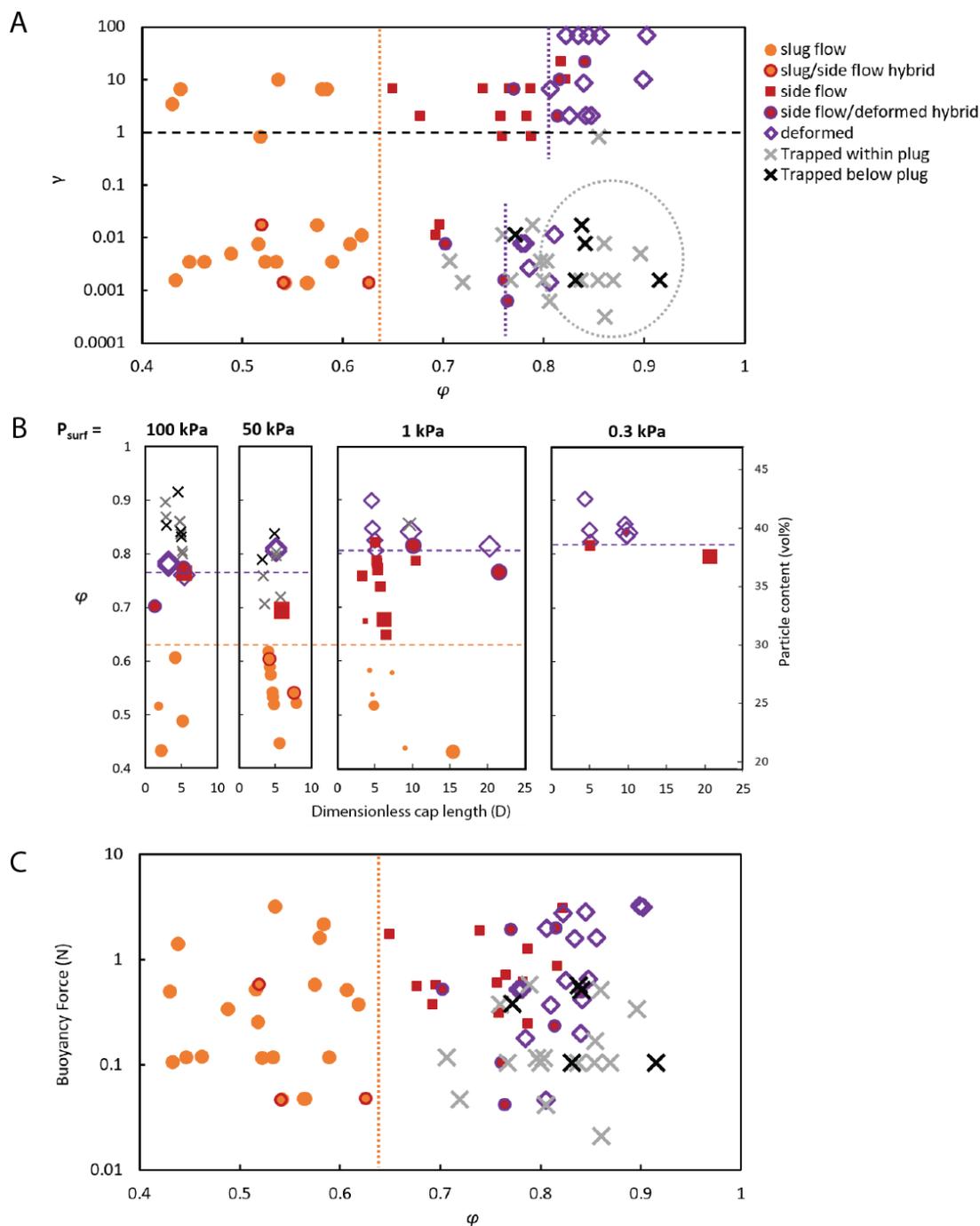


Figure 6: Diagrams of rheological regimes. (A) The dimensionless expansion index γ (James et al., 2009; Del Bello et al., 2012), indicates whether the bubbles could theoretically expand to equilibrium pressure ($\gamma < 1$) or not ($\gamma > 1$) in the absence of a cap. γ gives an indication of stress on the cap from bubble overpressure and expansion for given initial bubble volumes and surface pressures. Dotted lines represent approximate regime transitions, while the dotted grey circle represents an overall area occupied by the trapped regimes. (B) Deconstruction of the effect of cap length and surface pressure on regime transitions. Each box contains experiments at a different surface pressure. Cap length does not affect regime transitions, but surface pressure does have a minor role. Symbols and dotted lines as in (A), with symbol size indicating configurations: large symbols are configuration 1; medium symbols are configuration 2; smallest are configuration 3 and were only observed at $P_{surf} = 1$ kPa due to experimental conditions. (C) Bubble buoyancy force applied on the cap when the bubble reaches the bottom of the cap. (Therefore, values depend on both bubble size and cap length.)

314 4.5. Flow regimes affect surface processes

315 The particle-rich caps also affected surface level rise, bubble burst dynamics, and acoustic signals
 316 emitted during burst. Figure 8 compares maximum surface height variations in experiments
 317 containing the same mass of particles (with varying cap lengths) for experiment suites with a given
 318 bubble size. An increasing surface height indicates bubble expansion. In the particle-free scenario,
 319 rapid bubble expansion accelerated the liquid ahead of the bubble, so that surface height increased
 320 substantially. At $\phi < 0.64$ (Newtonian cap), the total surface rise was only slightly reduced, as
 321 exemplified by experiments with 17 ml bubbles. Maximum heights in experiments in the side flow
 322 and deformed regimes were significantly reduced (by about half) compared to the particle-free
 323 scenarios, indicating that the gas was more compressed when it reached the surface.

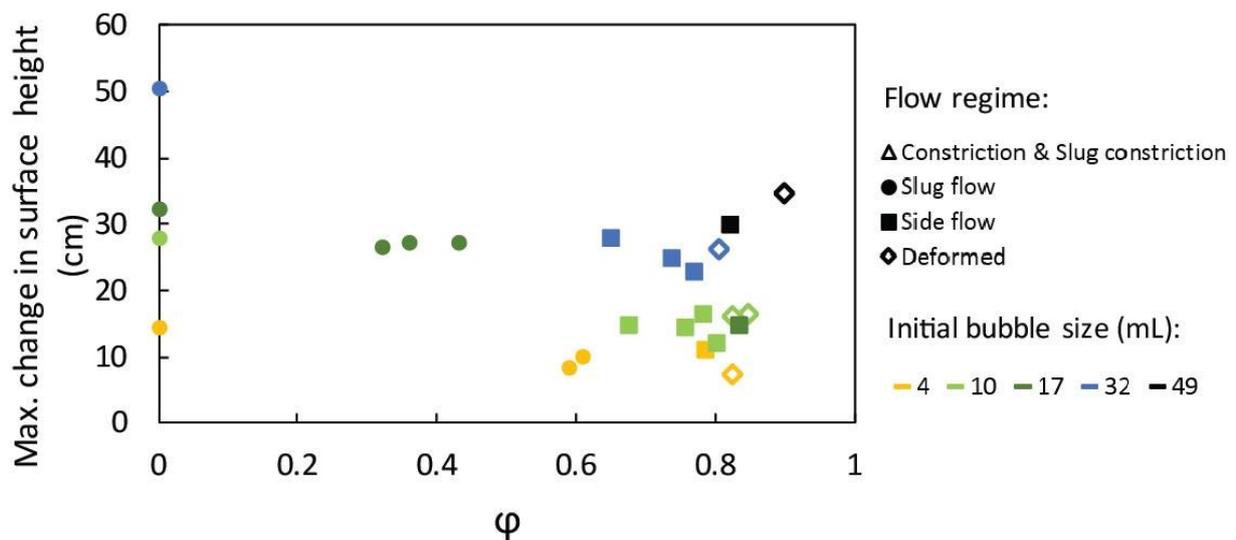


Figure 8: Total surface rise for experiments containing 23 g particles (and 37 g for the 17 mL bubble series) and at $P_{surf} = 1$ kPa. A surface height of 0 indicates the position at t_0 , which is 1.43 m above the bubble trap. Since particle mass is constant within each series, an increase in particle fraction causes a decrease in cap length. Colors indicate initial bubble size, and shapes indicate flow regime.

324 Figure 9 shows examples of acoustic signals for bubble burst in a particle-free (single viscosity)
 325 experiment and in two experiments with particle-rich caps. In the side flow and deformed regimes,
 326 the acoustic signals were more complex and smaller in amplitude than in the slug flow regime. The
 327 decrease in amplitude was complemented by longer signal duration, and thus an increase in the
 328 time during which expanding gas was emitted from the ruptured surface. Experiments within the

329 deformed regime that had bigger bubbles and longer caps were more likely to generate several
330 acoustic pulses, further increasing the total signal duration. This pulsatory style was occasionally
331 captured in the camera images as impulsive variations in clast ejection velocities.

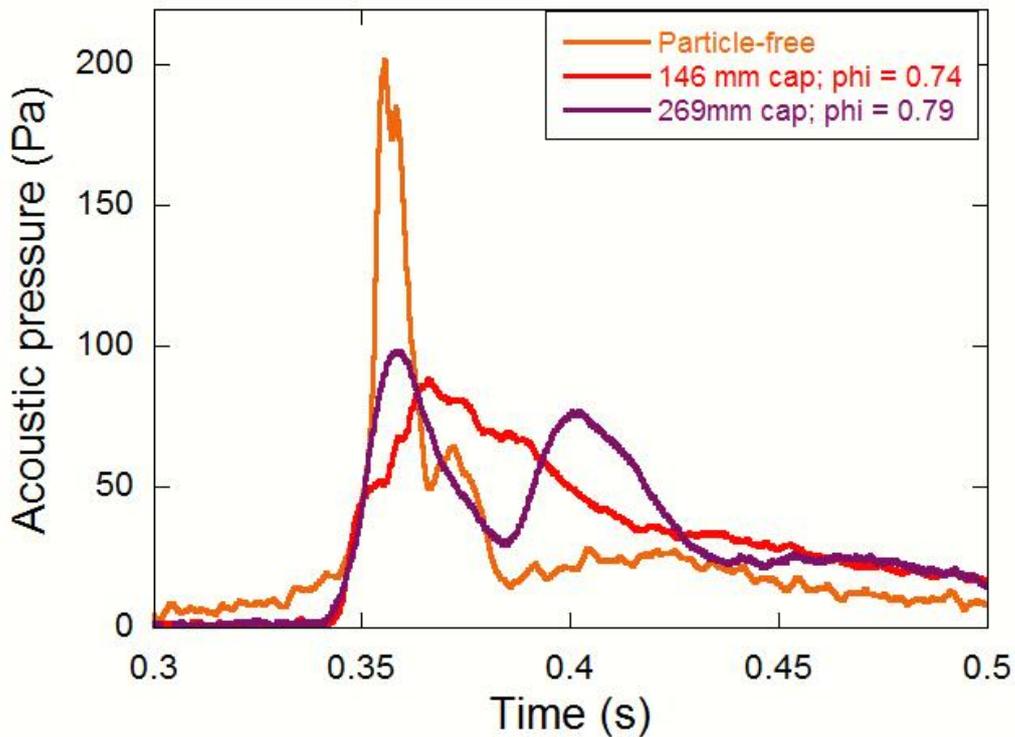


Figure 9: Example acoustic signals for bubbles of initial volume 32 mL, and at surface pressures of 1 kPa. The signal generated by a particle-free experiment (orange) is significantly louder and shorter than the particle-rich examples, which are in the side flow regime (red), and a side/deformed hybrid regime (purple).

332 5. Discussion

333 5.1. Flow configurations: comparison with Newtonian experiments

334 Flow configurations (Fig. 1) are a geometrical consequence of varying bubble and cap sizes; in
335 Newtonian experiments, they control bubble rise beneath the cap, particularly bubble overpressure
336 (Del Bello et al., 2015; Capponi et al., 2017). In our experiments with sufficiently low particle
337 fractions for the cap to be Newtonian ($\varphi < 0.64$), flow configurations were not affected by particles
338 (Fig. 4). In fact, the low φ experiments differed from those of Del Bello et al. (2015) and Capponi et

339 al. (2016) only in the style of slug burst in configurations 1 and 2, where the particle-bearing film
340 above the slug nose broke in several places; the result was emission of several particle-liquid clots
341 rather than one accelerated drop. This multi-source rupture was likely caused by particle-generated
342 discontinuities in the rapidly thinning film. For non-Newtonian caps ($\varphi > 0.64$), our experiments
343 showed that transitions in flow configurations shifted toward shorter caps, consistent with the
344 effects of increased viscosity (Capponi et al., 2016). These observations suggest that flow
345 configurations can be estimated using simplified rheological descriptions of the cap, regardless of
346 bubble behavior within that cap.

347 5.2. Rheological flow regimes

348 Particle fraction in the cap exerted a major control on regime transitions between slug flow, side
349 flow, deformed bubbles, and trapped bubbles, consistent with Oppenheimer et al. (2015). We
350 compare these transitions to the effects of particles on cap rheology (Figure 3).

351 The first regime transition, from slug flow to side flow, occurred at ~ 30 vol% particles ($\varphi \approx 0.64$; Fig.
352 6). At this value, shear-thinning and consistency increased dramatically, indicating the onset of non-
353 Newtonian rheology and weak interactions between particles. The occurrence of particle clusters
354 with a weak yield strength may have contributed to the irregular shape of the bubble as it rose
355 through a heterogeneous cap. Inefficient packing near the tube walls, where particle concentrations
356 and suspension consistency were lower than in the middle of the tube, may have aided bubble rise,
357 while a small yield strength may have suppressed thin falling films, such that a larger physical
358 dimension was required for the exchange down-flow to overcome yield strength.

359 The next regime transition, from side flow to deformed bubbles, depended weakly upon stress on
360 the cap (generated through bubble expansion, overpressure, and buoyancy; Fig. 6). γ is an imperfect
361 measure of bubble expansion regimes since it ignores the cap, but it approximates stress on the cap
362 from bubble expansion and overpressure. At low stress ($\gamma < 1$), the transition occurred at $\varphi \approx 0.75$. At
363 higher stress ($\gamma > 1$) the transition occurred at $\varphi \approx 0.80$, a value that corresponds with a significant

364 increase in yield strength in particle-bearing suspensions (e.g. Mueller et al., 2009; Brown et al.,
365 2011; Moitra and Gonnermann, 2015). Yield strength is generally associated with pervasive networks
366 of interacting particles (Caricchi et al., 2007; Mueller et al., 2009; Picard et al., 2013).

367 The transition to deformed bubbles at $\varphi \approx 0.75 - 0.80$ occurs at slightly lower φ than the random
368 loose packing (RLP) for spheres at $\varphi = 0.86$ (Jerkins et al., 2008). RLP is also associated with pervasive
369 particle networks (Onoda and Liniger, 1990) and deformed bubbles (Oppenheimer et al., 2015). Our
370 experiments show an added constraint of applied stress, however, with the regime transition
371 increasing from $\varphi \approx 0.75$ to 0.80 with increased γ . The high bubble overpressure (≤ 100 kPa) in
372 Oppenheimer et al. (2015) further suggests that RLP may provide the upper bound for transition to
373 deformed bubbles at high stress. Since bubble deformation is controlled primarily by networks of
374 interacting particles, this stress-dependence may suggest that particle networks begin at moderate
375 φ (≈ 0.75) before becoming pervasive at $\varphi \approx 0.86$. However, other factors may affect regime
376 transitions, such as variable particle shape and size, whether the suspension is static or pre-sheared,
377 and experimental uncertainties.

378 5.3. Bubble trapping mechanism

379 Bubble rise through the cap requires shearing of the liquid-particle mixture because surface tension
380 prevents bubble rise in the liquid network between particles. As surface tension is negligible on the
381 tube (slug) scale ($Bo \gg 1$), the indefinite trapping of bubbles in or below the cap indicates that
382 buoyancy was insufficient to overcome the strength of the cap in those experiments. Figure 6C
383 shows that buoyancy force and cap rheology (φ) alone do not determine whether a bubble is
384 trapped, and that stresses from bubble overpressure and bubble nose acceleration (reflected in γ ;
385 Fig. 6A) are also important. Trapped bubbles occurred exclusively for $\gamma < 1$ and $\varphi > 0.7$ (Fig. 6A); at φ
386 > 0.8 , strong particle networks gave the suspension sufficient strength to arrest all bubbles with $\gamma <$
387 1 . Therefore, bubble trapping may have been enhanced by the smooth experiment walls, which
388 allowed bubble expansion to be accommodated by the cap sliding upwards. However, bubble

389 buoyancy force (< 0.6 N, Fig. 6C) generated a stress on the base of the cap of up to 1200 Pa, which
390 was much greater than the suspension yield strengths ($\ll 100$ Pa based on rotational rheometry;
391 e.g. Mueller et al., 2009, 2011; Tran et al. 2015; Fig. 3), suggesting that bubbles should not have
392 been trapped. The lateral spreading of the bubble may explain this discrepancy. Lateral spreading
393 was driven by deceleration of the bubble nose as it reached the more resistant (and slightly less
394 dense) cap while its base continued to rise in the less viscous pure liquid below. The resulting
395 thinning of the down-flowing annulus of fluid around the bubble reduces the yield stress (relative to
396 the buoyancy stress) required to trap a bubble indefinitely (Dubash and Frigaard, 2004).
397 Furthermore, complete spreading of the bubble to fill the tube below the cap generated horizontal
398 layers; thus gas ascent through the denser cap requires a Rayleigh-Taylor instability of a wavelength
399 limited by the tube diameter (Seropian et al, 2018). Therefore, bubble rise may depend more on the
400 deformation of the cap under its own weight.

401 Yield strength, consistency, and shear-thinning increase with φ (Figure 3). In some experiments, a
402 vertical increase in particle fraction within the cap caused rising bubbles to decelerate and change
403 regime; we classified these as hybrid regimes. Bubble entrapment *within* the cap occurred over a
404 wide range of average φ (Figure 6), which suggests that either (1) the top of these caps achieved $\varphi >$
405 0.8 whereupon bubbles became trapped regardless of cap thickness, or (2) the feedback between
406 energy loss during bubble rise and increase in φ was sufficient to trap bubbles even if $\varphi < 0.8$. In this
407 scenario, bubble expansion was insufficient to maintain stress on the cap, such that the apparent
408 viscosity increased and bubbles decelerated until the stress applied by the bubbles fell below the
409 cap's yield strength and/or the bubbles spread laterally to fill the tube. Therefore, the coupled effect
410 of a shear-dependent viscous response and increasing φ near the surface may be an effective
411 mechanism to trap bubbles in the cap.

412 6. Significance for Stromboli

413 6.1. Flow regimes in near-surface magma

414 The near-surface basaltic magma at Stromboli contains 45-55 vol% phenocrysts (Landi et al., 2004;
415 Metrich et al., 2010). Rheological investigations of synthetic basalts observe the onset of yield
416 strength at 20-40 vol% crystals (e.g. Philpotts et al., 1999; Jerram et al., 2003; Picard et al., 2013);
417 experiments on andesites show that bubbles begin to deform and connect at ~20 vol% crystallinity
418 (Lindoo et al., 2017). These values suggest that Strombolian magma is likely within or above the
419 crystallinity range for the deformed bubble regime.

420 Our experiments in the deformed regime had pulsatory bubble burst events that lasted longer and
421 decayed more slowly than in the slug regime (Figure 9) and produced small clasts that fountained
422 above the surface (supplementary video 2). These characteristics may reflect smaller burst apertures
423 that vibrate as gas is released. With increasing ϕ , bubble deformation increases (Oppenheimer et al.,
424 2015), hence the bubble aperture is likely to decrease and generate bubble bursts with higher
425 frequency and more gradual gas release (Fig. 9). By comparison, eruptions during normal activity at
426 Stromboli are pulsatory (Taddeucci et al., 2013; Gaudin et al., 2014), last up to tens of seconds
427 (Houghton et al., 2016), have an abrupt start and slow decay (Gaudin et al., 2014), and are
428 accompanied by pyroclast fountains hundreds of meters high. These characteristics are consistent
429 with a highly deformed bubble regime.

430 6.2. Variability of normal activity

431 The experimental regime transitions occur over a small range of particle fractions (~17 vol% from
432 the onset of side flow to RCP). Hence small variations in solid fraction may cause significant
433 transitions in gas migration regimes. At Stromboli, the NE vent typically has short, loud and ballistic-
434 generating eruptions (type 1 events) relative to the long, pulsatory, complex ash-generating
435 eruptions from the SW vent (type 2 events; Ripepe and Marchetti, 2002; Harris and Ripepe, 2007a).
436 In our experiments, increasing the particle fraction produced longer burst durations and more

437 complex pulsatory acoustic signals of lower amplitude (Figure 9). This resembles the description for
438 eruptions from the SW vent, consistent with observations that magma in the SW vent is more
439 crystalline (Landi et al., 2011). In contrast, puffing occurs at hotter (lower crystallinity) vents (Landi
440 et al., 2011). We therefore suggest that variations in crystallinity may cause spatial and temporal
441 variations in activity.

442 6.3. Slug model vs Plug model

443 There is growing evidence that the slug model for Strombolian eruptions requires modification to
444 account for crystal-rich near-surface magma. Alternative models suggest rupture of a crystal-rich
445 plug as a source mechanism (Gurioli et al., 2014; Suckale et al., 2016). Here bubbles accumulate
446 under the plug until (1) the bubble pressure causes the plug to rupture or (2) the plug becomes
447 gravitationally unstable, and the bubble pressure is suddenly released to the surface.

448 The near-surface crystal-bearing magma at Stromboli is likely deeper (0.8 km and 2-4 km depth;
449 Landi et al., 2004; Metrich et al., 2010; Agostini et al., 2013) than the onset of rapid (non-
450 equilibrium) bubble expansion ($\gamma > 1$; James et al., 2008; Del Bello et al., 2012), which is estimated to
451 begin at ≤ 100 m below the crater (Del Bello et al., 2012). In such a case, bubbles reach the cap with γ
452 < 1 , and rapid expansion begins when the bubble is already in the crystal-rich layer. This condition
453 means that bubble rise occurs in a deformed (or other crystal-rich) regime and models predicting
454 overpressure must consider irregular bubble rise in non-Newtonian suspensions. Additionally, if $\gamma < 1$
455 when the bubble reaches the crystal-rich layer, bubble entrapment may occur either beneath or
456 within that layer. In our experiments with $\gamma < 1$, bubble entrapment is related to yield strength. Since
457 basalts can develop yield strengths at 20 – 40 vol% crystals (e.g. Philpotts et al., 1999; Picard et al.,
458 2013), even moderate crystallinities at depth can trap bubbles. Therefore, breaching the cap may
459 require external modifiers such as tectonic stresses and/or modified rheology and compressibility
460 caused by a reservoir of small bubbles in the cap (Suckale et al., 2016).

461 The crystal-rich layer can also enable the accumulation and coalescence of smaller bubbles into
462 conduit-sized bubbles that eventually rise through the plug (Belien et al., 2010; Suckale et al., 2016;
463 Barth et al., 2019). Furthermore, trapped bubbles can occur at any level in the crystal-rich magma.
464 Therefore, while the slug model depends on slow slug formation and rapid slug rise such that only
465 one slug can rise in the conduit at any time, a model where bubbles can be trapped or delayed no
466 longer precludes simultaneous rise from depth of several bubbles. Indeed, magma levels in the
467 conduit appear to increase with gas flux (Ripepe et al., 2002), which may indicate increased bubble
468 entrapment.

469 When analyzed from an equilibrium perspective, gas compositions from normal Strombolian activity
470 suggest source depths of 0.8 and 2.7 km below the craters (Burton et al., 2007). While both source
471 depths may be within crystal-bearing (“high porphyritic”) magma, the shallower source corresponds
472 to the estimated depth of the crystal-rich cap (Landi et al., 2004; Agostini et al., 2013), and is
473 associated with weaker eruptions (Burton et al., 2007). Our data suggest that these bubbles could
474 have been trapped or delayed in a crystal-rich plug. Importantly, bubbles change chemistry by
475 volatile exchange with the surrounding melt. Estimates of bubble source depths (e.g., Burton et al.,
476 2007) assume equilibrium degassing at depth followed by sufficiently fast ascent to preserve the
477 deep gas signature. This leads to erroneous depth estimates if gas chemistry changed without
478 equilibrating during bubble entrapment or hindered ascent (Pichavant et al., 2013).

479 The likelihood of bubble entrapment in the Stromboli conduit suggests that a weak plug model is
480 reasonable. Importantly, many volcanoes that have Strombolian activity also have moderate-to-high
481 crystallinities. Investigating eruption behavior at other volcanoes alongside crystal textures may help
482 to constrain the role of crystals in Strombolian eruptions. For example, the 2000 eruption at Etna
483 volcano, Italy, alternated between lava fountains (~35 vol% crystals) and Strombolian eruptions (> 55
484 vol%; Polacci et al., 2006; Giordano et al., 2010), as did activity during the 1943-1952 eruption of
485 Paricutin (with 40-50% crystals; Erlund et al., 2010). At Tungurahua Volcano, Ecuador, which has

486 intermediate magma composition, Strombolian eruptions have lower crystallinity than (and
487 alternate with) Vulcanian eruptions (Wright et al., 2012). Cashman and Sparks (2013) show that
488 Strombolian and Vulcanian eruptions have similar ranges in crystallinity but differ mainly in melt
489 viscosity. These data support the soft plug model for Strombolian eruptions where near-surface
490 magmas have sufficiently high crystallinity to temporarily impede bubble rise, with stronger, more
491 crystalline, less permeable plugs leading to a low-melt-viscosity equivalent of Vulcanian-style plug
492 failure. At the other extreme are Strombolian eruptions formed by rise of individual large bubbles in
493 crystal-poor lava lakes, such as Kilauea and Erebus (e.g. Gerst et al. 2013; Qin et al. 2018).

494 7. Conclusions

495 Most models for Strombolian eruptions ignore the effect of crystals on bubble rise. Here, we show
496 that particles modulate the rise of conduit-filling bubbles, generating flow characteristics that
497 depend on particle fraction and stress applied by the bubble on the cap.

498 If the gas bubbles expand slowly (low stress on the cap), particle-rich suspensions can efficiently trap
499 large bubbles, allowing gas to accumulate below or within the cap before rising through the cap. This
500 is essentially a “weak plug” model. At Stromboli volcano, the crystal-bearing magma is deeper or of
501 similar depth to the onset of rapid (high stress) gas expansion. Therefore, Stromboli may have a
502 weak plug.

503 During rapid gas expansion in a particle-rich suspension, bubbles are highly deformed, and therefore
504 burst at the surface through a small aperture. Gradual gas release through a vibrating aperture leads
505 to pulsatory fountains of clasts and longer acoustic signals of lower amplitude, which start abruptly
506 and decay slowly. Since burst aperture decreases at higher particle fraction, these features likely
507 become more pronounced as particle fraction increases. These observations fit with observations at
508 Stromboli volcano, suggesting that variations in explosion duration, pulsations, and fountaining may
509 provide insight into near-surface magma crystallinity. This research suggests that Strombolian

510 eruptions are linked to near-surface crystallization, and that local/temporal variations in crystallinity
511 or crystal-bubble interactions may explain variations in degassing style.

512 8. Acknowledgements

513 This research was funded by the People Programme (Marie Curie Actions) of the European Union's
514 Seventh Framework Programme (FP7/2007-2013) under the project NEMOH, REA grant agreement
515 number 289976. We would like to thank Einat Lev, Jon Blundy, Bettina Scheu, Marie Edmonds, and
516 Mike Kendall for helpful comments and insights, as well as Heidi Mader and Paul Jarvis for their help
517 with rheology concepts and measurements. We would also like to express our warm appreciation of
518 insightful edits and reviews by Tamsin Mather, Lucia Gurioli, and an anonymous reviewer;
519 unfortunately, due to length constraints we were unable to include all suggested additions.

520 9. Supplementary videos

521 **Supplementary video 1** shows bubble rise and burst in an experiment in the slug flow regime ($\varphi =$
522 0.36; initial bubble volume = 17 mL). The video is slowed 5x. The start of the video corresponds with
523 bubble injection in the experiment.

524 **Supplementary video 2a** shows bubble rise in an experiment in the side flow regime, where bubble
525 burst at the surface was more complex ($\varphi = 0.82$; initial bubble volume = 49 mL). The video is slowed
526 5x and starts at bubble injection. **Supplementary video 2b** shows a close-up of the surface at burst.
527 Video is slowed 10x.

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