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Title: Pricing the Permission of Pollution: Optimal Control-Based Simulation of Payments for the Initial Emission Allowance in China

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Keywords: pricing; payment; initial emission allowance; optimal control-based; chemical oxygen demand; ammoniacal nitrogen

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Abstract: China has modified its pollution control policy system with such price tools as the pollution charge (PC) policy and the payment for initial emission allowance (PIEA) policy. The aim of PC policy is to compensate for the environment damage caused by pollutants, while PIEA is in charge of the initial emission allowance (IEA) within the emission trading system (ETS). However, since the implementation of PIEA, it has been criticized as redundant because of the similar pricing scheme with the PC. In addition, the existing PIEA pricing approaches have ignored interactions with other policies, such as PC and total emission control (TEC) policies. In this research, we established an optimal control-based model with chemical oxygen demand (COD) and ammoniacal nitrogen (NH₃-N), two independent pollutants variables, to simulate the water pollutants' PIEA price. Simulation results indicated that emission quantity and optimal social benefit in the PC-PIEA combination scenario was equal to the situation in the PIEA scenario. Under this design, PC compensated for the emission damage, and PIEA paid for the scarcity rent, while PIEA does not duplicate the PC policy. In addition, the PIEA policy has a complex effect on pollutant emission. Because PIEA policy increases the enterprises' discharging cost, most regions' COD emissions are less than the baseline, excepting Beijing, Shanghai, Jiangsu, Zhejiang, Fujian, Shandong, and Guangdong, in which emission quantities are greater than the baseline. The NH₃-N emission shows an opposite trend. The simulation result is that excluding Inner Mongolia, Hubei, Hunan, Tibet, Gansu, Qinghai, Ningxia, and Xinjiang, the NH₃-N emissions in the rest of regions are increased. TEC policy has a significant effect on pollutant emissions and the PIEA price. The COD emission quantity with TEC is lower than that without the TEC policy, therefore, the TEC policy will be effective for pollutant emission control. The pollutant beyond the restricted target will be charged a payment for IEA at a higher price than without the TEC policy.

Dear editor and three anonymous reviewers,

We would like to thank for editor's hard work to find reviewers, and we would like to thank to reviewers who spend time reading our article carefully and presenting professional and detailed advices. We have revised the article according to reviewers' suggestions and response to questions one by one. The revised article is more readable by following the reviewers' advices. We would appreciate your help!

Yours sincerely,

Jin-Nan WANG

Reviewer #1:

1. Too little is described and defined social benefits.

A: The details of social benefit are described in P 11 Line 15.

2. No comparison of the method and model of the other.

A: Some comparisons are elaborate in P 9 Line 16 methodology part.

3. What are the penalties, ie. What value and what character.

A: The detail explanation of the penalty function in SI in the P S5 Line 23. The penalty function in this study is actually a method used in the algorithm to deal with constraints, rather than intuitive understanding of the environmental policy used to punish excessive means of discharge and its standards.

4. What is the practical aspect of the model and studies? Is it just the diagnosis or the use of theses and practical results-appropriate decisions / Case Study/.

A: The practical application of this study is the pricing method designed for China's implementation of the PIEA policy. The PIEA Policy is piloted in 12 regions, and each region choose pricing method by their own decision. The most of pilot regions take treatment cost as pricing method for convenience, but does not take into account the existing policies, so this study is promoted.

5. What about the computational complexity.

A: Computational process is complex indeed, since words limited, all details cannot be described excepting briefly calculated steps and algorithms listed in the article. In order to calculate coefficients and parameters required by pricing model, we also need to set up some auxiliary models. These calculations are listed in SI. After modeling, simulation and solution are also important parts of the work. Solution algorithm is shown in the article.

6. Is obtained optimal solution or sub-optimal / simulation /.

A: Due to various restrictions, the impact on the environment is temporarily only pollutant emissions; the health impact has not been included in the study. The reasons why health effects incorporating into the study are explained in research limitation section.

7. No information about the implementation of the model / environment, tools and solvers etc./

A: The calculation tool uses the MATLAB software, and the solution algorithm is listed in SI.

Reviewer #2:

The paper studies the design of payment for initial emission allowance pricing approach based on optimal control theory. It is an important and interesting piece of work, and is relevant to real word problems. Nevertheless, I do have some concerns:

1. The current introduction section does not pinpoint the theoretical problem of prior research, and fails to highlight the intended contribution of the study. I'd suggest the authors to clearly spell out why this study is important, what's the gap in this literature, also how this study intends to contribute to the literature.

A: We rewrote the introduction section in accordance with the reviewers ' recommendations, highlighting why the study was important, what the existing research was, and the contribution of this study.

2. This may be not easy without a meaningful comparison with similar research in the literature. The literature review should be extended. As far as my understanding, many relevant references are missing.

A: In previous version, the literature review focus on the topic of initial emission allowance pricing, and the content of the discussion was limited. Following the reviewers ' suggestions, we extended the topic literature review to relevant resource pricing. We try to modify the paper better, but do not know if follow the instruction of topic proposed by reviewers, if there is more detailed advice, please let us know.

3. In section 3 Case and data, the authors only outlining the data sources without much discussion of the case. More information about the case will useful here.

A: We added information in the data collection section.

4. The simulation results Section is also weak. The authors only describe the results. No clear insights are drawn. I haven't learned anything from this manuscript from the environmental policy research viewpoint.

A: This study focuses on to establish a pricing method that is applicable to the implementation of the PIEA policy with the existing complex policies background. The previously version does not show the policy recommendations legible. Following the reviewers' suggestions, we reorganized the narrative of results, and list the viewpoints.

5. No policy implications are discussed. The conclusion should focus more on the practical implications and policy implications of your article. Although the main findings are summarized, what are the implications of these findings to the industrial firms or government policy makers? It is not entirely clear to me how the theory developed can be applied and used for policy evaluation.

A: As reviewer's suggestion, we add theory information about pricing method in theoretical analysis section to help understand how the theory can be applied and used for policy evaluation. Then we elaborate the implications of the research findings in discussion section.

6. The authors need to more critically discuss the research limitations and how these limitations inform further research in the future.

A: More information about research limitation is listed in discussion section.

7. There are some problems with grammar and sentence structure through the paper. Attention should be paid to avoid grammatical errors.

A: We try our best to correct grammatical errors and polish the article.

Reviewer #3:

This manuscript creatively established an optimal control-based model with two independent pollutants variables, chemical oxygen demand(COD) and ammoniacal nitrogen(NH₃-N), to simulate water pollutants payment for initial emission allowance(PIEA). The model establishment is reasonable and feasible. The previous mistaken understanding of pollution charges(PC) and PIEA has been proposed and corrected, and the influence of other policies, PC and total emission control(TEC) for example, has been taken into consideration. Besides, the interaction between two pollutants index, COD and NH₃-N, has been discussed, according to the simulation result. The conclusion of this manuscript has a critical reference value for the PIEA price setting in china.

A few major revisions are listed as follow:

1) As it is mentioned in P8 Line 26, maximum social benefit is the object of PIEA optimal model. But in the Formula (7) and (9), they are about the enterprise profits in different scenarios. It is kind of difficult to obtain the stimulated results about optimal social benefit, best pollution emission quantity and PIEA price based on the Formula (7) and (9) directly.

A: Thank you for your attention to the details of the model. Due to length limitation of the article, some details are omitted. Here is a more detailed explanation. Formula (6) represents the social benefit, and the formulas (8) and (10) represent the individual business benefits of Scenario 1 and Scenario 2 respectively. In formula (8), τ_C and τ_N represent initial payment price for COD and NH₃-N, and $g_C^i(x^i, K^i)$ and $g_N^i(x^i, K^i)$ represent firm COD and NH₃-N emissions. (The process of establishing the function of enterprise's profit function and the social benefit function, including the details how to establish the pollutant emissions function is described in SI, instead

of describing in main text.) The section in P 10 Line 8 describes the process how to find the initial allowance price that achieves optimal social benefit. “In the **first stage**, the policy maker offers a series of PIEA prices according to an area with several enterprises. In the **second stage**, enterprises take countermeasures. Increasing costs will decrease the enterprises’ profits after the PIEA policy has been implemented. Supposing that the enterprise is an ‘economic man’ who chases the maximum benefit; thus, the enterprise will take measures if the profit decrease is beyond the acceptable range. Two types of strategies are available to adopt by the enterprise: adjust the production output or raise the pollution reduction investment. The enterprise chooses the best suitable measure in accordance with the maximum profit principle. In the **third stage**, the policy maker decides which price will be taken for the benefits. The policy maker will measure the social benefit aimed at every price and choose the price that will maximize the social benefit.” Following description is easier to understand, the optimal social benefit is the objective solution, the best pollution emission is the emission when achieving objective solution, and the initial allowance price is the condition when pollutants are controlled at the best emission.

Thus, the equations are available for obtaining the stimulated results about optimal social benefit, best pollution emission quantity and PIEA price.

2) It is noted that the Table 1 has not mentioned the information what is introduced in P11 Line 15-16.

A: It’s our mistake in labeling, and we correct the mistake: the information about initial allowance price mentioned in P19 Line 10 is introduced in Fig 7 and Fig 8.

3) The relationship between PC and PIEA has been discussed many times in the whole manuscript. It would be better to be discussed in two aspects, in optimal social benefit and in PIEA price setting, separately.

A: Following the reviewer's instruction, we make the paragraph clear organized.

4) The structure of the manuscript is not clearly. Results, discussions and conclusions part are not proper. Especially the conclusions, it is not listed by points, and it is not well matched what has mentioned in the abstract and introduction.

A: We arrange the narrative order by following the structure that results, discussions and conclusions. The results part shows the optimal social benefit, best pollution emission and initial allowance price. The discussions part includes policy implication and research limitation. The conclusion part summaries the results and lists them by points.

Amount of words : 9547

Pricing the Permission of Pollution: Optimal Control-Based Simulation of Payments for the Initial Emission Allowance in China

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Abstract

China has modified its pollution control policy system with such price tools as the pollution charge (PC) policy and the payment for initial emission allowance (PIEA) policy. The aim of PC policy is to compensate for the environment damage caused by pollutants, while PIEA is in charge of the initial emission allowance (IEA) within the emission trading system (ETS). However, since the implementation of PIEA, it has been criticized as redundant because of the similar pricing scheme with the PC. In addition, the existing PIEA pricing approaches have ignored interactions with other policies, such as PC and total emission control (TEC) policies. In this research, we established an optimal control-based model with chemical oxygen demand (COD) and ammoniacal nitrogen (NH₃-N), two independent pollutants variables, to simulate the water pollutants' PIEA price. Simulation results indicated that emission quantity and optimal social benefit in the PC-PIEA combination scenario was equal to the situation in the PIEA scenario. Under this design, PC compensated for the emission damage, and PIEA paid for the scarcity rent, while PIEA does not duplicate the PC policy. In addition, the PIEA policy has a complex effect on pollutant emission. Because PIEA policy increases the enterprises' discharging cost, most regions' COD emissions are less than the

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1 baseline, excepting Beijing, Shanghai, Jiangsu, Zhejiang, Fujian, Shandong, and Guangdong,
2 in which emission quantities are greater than the baseline. The NH₃-N emission shows an
3 opposite trend. The simulation result is that excluding Inner Mongolia, Hubei, Hunan, Tibet,
4 Gansu, Qinghai, Ningxia, and Xinjiang, the NH₃-N emissions in the rest of regions are
5 increased. TEC policy has a significant effect on pollutant emissions and the PIEA price. The
6 COD emission quantity with TEC is lower than that without the TEC policy, therefore, the
7 TEC policy will be effective for pollutant emission control. The pollutant beyond the
8 restricted target will be charged a payment for IEA at a higher price than without the TEC
9 policy.

10 **Keywords: pricing; payment; initial emission allowance; optimal control-based;**
11 **chemical oxygen demand; ammoniacal nitrogen**

12

13 **1. Introduction**

14 The natural environment not only provides human beings with a habitat for survival but is
15 also involved in manufacturing processes as a factor of production. In addition to providing
16 natural resources, the environment receives pollution produced by manufacturing processes.
17 It is well-known that environmental capacity to receive pollutant emissions is a type of
18 natural resource. Environmental capacity resources are limited, while the demand for it is
19 growing; therefore, people need to measure the cost and benefits to use resources efficiently.
20 The cost of using environmental capacity resources is primarily caused by its external
21 damage, but the government employs a methodology to internalize externalities to make the
22 beneficiaries undertake the real environmental costs. When calculating the benefits of
23 environmental resources, the scarcity rents are often overlooked. The Chinese government
24 implemented the payment for initial emission allowance (PIEA) policy to capture scarcity
25 rents for environmental capacity resources.

26 The PIEA policy arises from the actual demand of the emission trading policy. In the initial
27 stage of emission trading, the manager allocated the allowance to enterprises by some rules
28 for free. Free allocation causes a lot of problems. Unpaid emission allowances are for
29 existing enterprises, and new entrants are required to purchase allowances from the emissions
30 trading market. Compared to the new entrants that have to pay for the allowance, the
31 enterprises that receive the allowance for free are basically receiving a subsidy(Bovenberg et
32 al., 2005). In addition, with free allowances, the enterprises lack incentives and pressure to

1 reduce emissions(Goulder et al., 2010). Unpaid allowances make enterprises using
2 environmental capacity resources inefficient, and the enterprises tend to use more allowances
3 than they need. Furthermore, allocating allowances for free promotes manager power
4 rent-seeking, that is, enterprises will attempt to obtain special approval for allowances(Gu,
5 2007).

6 To avoid the free allowance as a subsidy for enterprises, to improve the efficiency of resource
7 allocation and to avoid rent-seeking behavior in allocating, the Chinese government launched
8 the PIEA policy in 2008. The policy stipulates that for chemical oxygen demand (COD),
9 ammoniacal nitrogen (NH₃-N), sulfur dioxide (SO₂) and nitrogen oxide (NO_x) four pollutants,
10 enterprises should pay for the emission allowance that they obtained(General Office of the
11 State Council, 2014).

12 The practical significance of the PIEA policy is to meet the needs for an initial allowance
13 allocation in the first stage of the emissions trading market, since managers gradually realized
14 that if the demands for allowances are adequate, unrestricted rights to use them will lead to an
15 overextension of resources, and the scarcity rents of resources are wasted. Therefore,
16 additional policies are needed to ensure the sustainable use of resources. Since charging
17 appropriate scarcity rents for depleted resources can keep resource consumption at a
18 sustainable level (Hartwick, 1977), the PIEA policy has been implemented.

19 The initial emission allowance price as results of this study could be in support of the policy
20 implementation. In addition, the price is not only for the initial emission allowance but also
21 actually shows the scarcity rents for environmental capacity resources, meaning that the price
22 calculation method in this study could be implemented in resource value accounting.

24 **2. Literature Review**

25 In the PIEA policy, the allowance price is the key factor; thus, how to price allowances is a
26 concern of researchers. Many researchers studied methods for pricing initial emission
27 allowances. The market price method is conveniently used in pricing allowance. Several
28 researchers employed an auction to pricing emission allowance, such as the CO₂ emission
29 allowance within the EU emissions trading system (EU ETS)(Watanabe and Robinson, 2005),
30 carbon monoxide (CO), volatile organic compounds (VOC), sulfur dioxide (SO₂)(Karl, 1992),
31 and nitrogen oxides (NO_x)(Napolitano et al., 2007) in the United States Clean Air Act
32 (CAA)(McCarthy et al., 2007) and COD, NH₃-N, SO₂ and NO_x in the China PIEA

1 policy(Xiao et al., 2001). The auction method has advantages for pricing allowance.
2 Compared to the free allocation method, the auction method will generate income, thereby
3 reducing the government's dependence on ordinary taxes (Andrew Muller et al., 2002; Parry,
4 1997). Auction revenue also leads to a revenue-recycling effect that reduces tax distortions
5 (Goulder et al., 1999; Muller et al., 2002; Parry, 1997). In the carbon emissions trading
6 market, the allocation of initial allowance has significant impacts on price and allocation
7 efficiency, and auctions tend to reduce price and marginal cost differences, while free
8 allocation tends to amplify the differences (Burtraw et al., 2001). The auctions will encourage
9 companies to implement effective technical innovations(Milliman and Prince, 1989; Popp,
10 2003). However, the auction method has several drawbacks. As a market-based mechanism,
11 an auction is considered to be able to allocate resources efficiency and generate income, but
12 when the auction is applied to negative externality products, the effect on consumer welfare
13 and social welfare is uncertain (Li, 2015). In addition, in the EPA's emissions trading market,
14 auction settings may cause both buyers and sellers to underestimate the allowance value,
15 leading to lower efficiency in the emission trading market (Cason, 1993), and when the seller
16 can set the bid price, it will distort the market efficiency (Dijkstra and Haan, 2001). Thus,
17 researchers seek pricing methods other than auctions.

18 PIEA is charging for the environmental capacity to collect scarcity rent, which means
19 “missing money”(Fullerton and Metcalf, 2001; Zöttl, 2011); therefore, several researchers
20 adopted a pricing approach for natural resources. In the US SO₂ emission trading, the shadow
21 price of the SO₂ emission reduction is estimated using the output distance function, which is
22 considered to be the allowance price (Coggins and Swinton, 1996; Fare et al., 2007). Several
23 researchers believe that the initial emission allowance price is related to the cost of using the
24 environmental capacity resources. The environmental self-purification capacity is regarded as
25 environmental capacity resource, and its price is equivalent to its marginal opportunity cost
26 (Zhang, 1996). The cost recovery method was used to assess the price of environmental
27 capacity and took the price as the reference for the initial emission allowance price (Bi et al.,
28 2007). Similarly, it is believed that the price paid for the initial emission allowance is based
29 on the value of the environmental capacity resources; therefore, pollution control costs could
30 be used as a reference for pricing (Ye et al., 2011).

31 Other researchers believe that the price of the initial emissions allowance from the costs and
32 benefits of using environmental capacity should be considered, especially the damage caused
33 by the pollution emitted to the environment. The costs and benefits were took as a

1 consideration for the initial emissions allowance price model (Huang and Wu, 2004). An
2 initial allowance pricing strategy was established based on the value of water environmental
3 capacity, and the pricing strategy considered the economic value and ecological value of
4 water environmental capacity, as well as the differences between regions and industries (Yu
5 et al., 2012).

6 In the abovementioned studies, only the manager participates in pricing. However, when
7 manager and enterprises are involved in the pricing process, the pricing process becomes a
8 game process. From the perspective of a dynamic game, the evolution of the strategy of the
9 manager and enterprises in the formulation of the allowance price were analyzed, which
10 provides a reference for the government to formulate a fair and effective pricing model of the
11 initial allowance (Xia et al., 2010). The cooperative game theory was employed to construct
12 the Nash-Bargaining pricing model for the initial allowance of the Tai lake industry based on
13 multi-stakeholder cooperation (Liu et al., 2012).

14 Researchers discussed varied kinds of pricing approaches, several methods have been applied
15 in practice, and others remained at the theoretical stage. Observing these approaches from an
16 independent perspective, each approach has different considerations. However, when the
17 Chinese environmental policy framework is taken into account, certain approaches ignore the
18 interaction with existing policies (del Río González, 2007).

19 Prior to the PIEA policy, China embarked on policies related to environmental capacity
20 resources such as the pollution charge (PC) policy and the total emission control (TEC)
21 policy. Next, we focus on the following questions: the pollution charges paid by enterprises
22 in the PC policy as compensation for environmental damage is a part of the value for
23 environmental capacity resources. The payment for the initial allowance is also for
24 environmental capacity resources. The interaction between the PIEA and PC was not
25 considered in the pricing approach mentioned above. Does the payment for compensation
26 affect the allowance price in the PIEA policy? In the PC policy, the industrial average
27 treatment cost was used in calculating the payment of pollution charge calculation(Wang,
28 2005). In the abovementioned initial allowance pricing approaches, some methods involved
29 using the average treatment cost, therefore the pricing approach had been criticized as being
30 redundant because the same pricing approach was adopted with the pollution charges
31 (PC)(Zhang et al., 2015).

32 The allowance price is relative to the allowance quantity, and the allowance quantity for one
33 region is determined by this region's total emission control (TEC) cap(Goulder, 2013). The

1 effect of the TEC policy on the PIEA price is ignored. Does this emission restriction affect
2 the allowance price?

3 The PIEA policy for water pollutants refer to chemical oxygen demand (COD) and
4 ammoniacal nitrogen (NH₃-N) pollutants, and the two pollutants have a synergistic effect in
5 the treatment process (Eddy et al., 2014; Loosdrecht et al., 2016).When the enterprise
6 attempts to reduce one pollutant, the other pollutant is also reduced accordingly(Patwardhan,
7 2008). In previous studies, all approaches calculated the COD and NH₃-N pollutant price
8 individually without considering the synergistic effect on the pollutant treatment process.
9 Therefore, when pricing the initial emission allowance, the synergistic effect should be
10 considered.

11 In addition to pricing, the policy maker pays close attention to the influence after policy is
12 implemented. There are few studies on effect of PIEA policy implementation and the changes
13 in pollutant emission quantity. Because it is difficult to separate the PIEA policy effect from
14 other policies such as TEC and PC, it is difficult to quantify the environmental benefit from
15 the PIEA policy(Ye et al., 2011).

16 This research design utilizes the PIEA pricing approach based on optimal control theory.
17 With this pricing approach, the PIEA policy avoids duplicating the PC policy and takes other
18 relative policy interactions into consideration. Additionally, we clarify the effect of PIEA
19 policy implementation and whether the PIEA price is affected by other relative policies. The
20 result shows the prices in different policy-assembled scenarios. The findings also suggest
21 similar best emission quantities in different PC–PIEA policy-assembled scenarios. Finally,
22 we summarize the study and provide subjects for future research.

23 24 **3. Theoretical Analysis**

25 The pollution discharge from humans and business will affect the environment or even harm
26 the environment, but the implementation of zero emissions is also irrational according to the
27 cost-benefit analysis. In fact, the natural environment can absorb a certain amount of
28 pollution, and managers should control the pollutant emissions to an acceptable limitation.
29 Therefore, the problem of how to measure the acceptable level of pollution needs to be
30 solved by policy designers.

31 There are two methods to set the acceptable pollutant emission level: one is setting the
32 environmental exposure concentration of pollutants corresponding to the degree of acceptable

1 risk that affects human health and calculating the regional environmental capacity based on
2 the environmental quality criteria for the region; the other is the "best pollutant emission"
3 after the cost-benefit analysis (Tietenberg and Lewis, 2016).

4 Pollution discharge is known to produce benefits and damages; the effective emission level is
5 to maximize the net benefit in a simple static pollutant model. The emission level when
6 achieving the max net benefit is equivalent to the emission level when the externalities are
7 fully internalized. According to the optimal condition, we can observe that the net benefit of
8 pollution can only be maximized when the marginal benefit of pollution is equal to the
9 marginal damage. As shown in Fig 1, when the pollution marginal damage curve and
10 pollution marginal cost curve intersect at point E, then the marginal cost of pollution at that
11 point is equal to the marginal damage. In an ideal state, the pollution marginal damage curve
12 and pollution marginal reduction curve will intersect at one point, and this point is the best
13 emission quantity and the best emission charge point, as illustrated in Figure 1(Tietenberg
14 and Lewis, 2016). Then, the corresponding amount of pollutant emissions is the best
15 pollutant emissions. With the best emission target, the managers need to choose the
16 appropriate method to keep the amount of emissions at the best emissions.

17 This research focus on the PIEA policy and takes the existing PC policy into account,
18 payment for initial emission allowance and pollution charge, both of which are costs that
19 enterprises need to pay for discharging pollutant. In the current total emission control policy,
20 the amount of emissions set by the government is based on the target quantity that is not
21 linked with the environmental capacity to date. Therefore, we believe that in this study, the
22 PIEA policy and PC policy keep pollution at the best emission and that the total emission
23 control policy exists as an additional condition for limiting pollutant emissions.

24 As shown in Fig 1, when the emission reaches the best emission point W, the polluter paid
25 price at t , total fee is $W \times t$, which is composed of areas B and C. Area B lies below the
26 marginal damage cost curve, meaning that the polluter pays compensation for the damage
27 caused by the emission. Area C lies over the marginal damage cost curve, so the polluter pays
28 scarcity rent for acquiring the environmental capacity property resource. Therefore, the
29 payment from the polluter includes two parts: compensation for pollution damage and
30 scarcity rent, corresponding to the PC policy and PIEA policy in reality.

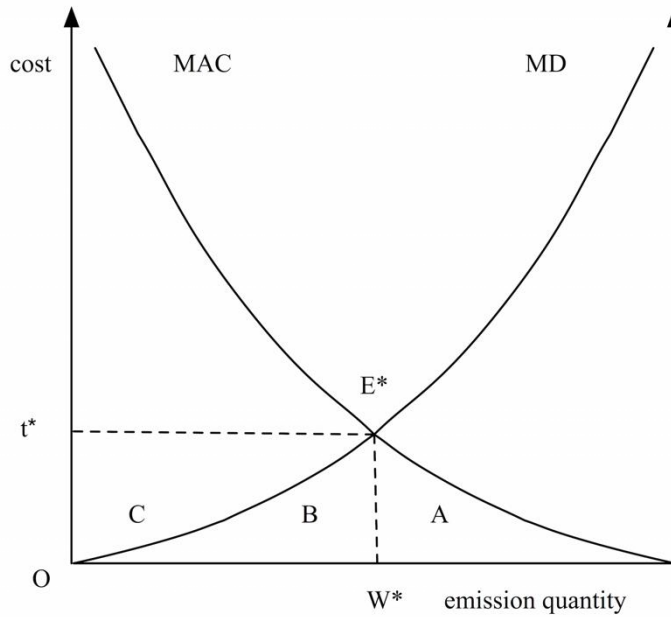


Fig 1 Emission charge for the best emission quantity

4. Methodology and Scenarios

4.1. Methodology

This research intends to solve the pricing problem of initial emission allowance and simulates what will occur when the policy is implemented. After identifying the best pollutant emission targets to achieve maximum net social benefits, it is necessary to build models to describe the best pollutant emission, the costs that polluters should pay, and the maximum net social benefits between these key variables relationships.

In the process of modeling, it is necessary to describe the relationships involved in the micro and macro levels individually: one of the relationships is each enterprise's response to the allowance price at the micro-level. The enterprise will account for changes in its earning after paying for the initial allowance. If the benefit decrease is unacceptable, the enterprise will adjust its strategy, including adjustment of their product amounts and additional pollution reduction investment. Another relationship is net social benefits after all enterprises implement response strategies. Instead of focusing on the benefits of individual enterprises, policy makers only focus on the net social benefits.

After receiving feedback that the net society benefits have changed, the policy makers will adjust the initial emission allowance price according to the feedback. This process "pricing

1 — strategy — feedback — price" is constantly cycling until it reaches the optimal goals set
2 by the policy makers, which is the maximum net social benefit.

3 According to the research idea, it is necessary to establish a model that describes the
4 individual enterprise behavior and link the enterprise model with the net social benefits
5 model. Additionally, the relationships need to be described in the model, including the micro
6 and macro levels, the long policy implementation time, and the many variables that change
7 during the execution since the socioeconomic and environmental systems are dynamic.
8 Therefore, the optimal goal at the beginning of the policy design may become non-optimal
9 goal in the implementation process. Therefore, the dynamic characteristics of economic
10 systems and environmental systems should be considered when formulating policy.

11 In this research, we employ the dynamic optimization model to find the optimal policy
12 according to the manager's objectives and realistic conditions, and analyze the impact on the
13 economy and environment. The dynamic optimal control is a given objective function and
14 constraint condition, which includes the state that must be achieved at a given time and to
15 select an optimal time path to achieve the optimal goal, which is actually a multi-stage
16 decision process in a discrete and continuous time. There are other ways to assess the policy
17 impact, such as the Input-Output (IO) model and Computable general equilibrium (CGE), but
18 those methods have limitations. IO can only address linear relationships, non-linear
19 relationships are not applicable (the relationship between pollutant emissions and amount of
20 products is not linear in this research); CGE is applicable to non-linearity, but it requires a
21 number of empirical parameters that are not easily obtained in this research. Finally, the two
22 methods cannot be applied at the enterprise-level but only in macro industries.

23 24 *4.2 Modeling process*

25 According to the efficient allocation of pollution theory, efficiency is achieved when the
26 marginal cost of control is equal to the marginal damage(Tietenberg and Lewis, 2016).
27 Corresponding to optimal emission quantity, the manager charges the polluter for fixing the
28 emission on the optimal quantity. The payments from polluters include two parts:
29 compensation for pollution damage and scarcity rent, corresponding to PC policy and PIEA
30 policy. For more details, see SI.

31 An optimal control-based model, has been widely applied in dynamic pollution regulation
32 (Biglaiser et al., 1995; Moledina et al., 2003). This method could account for the optimal
33 objective under a dynamic equilibrium situation. We consider the policy maker and

enterprises as two types of players in the modeling process. The policy maker focuses on the entire social benefit. In this study, the social benefit is the total benefit for the study area from producing goods plus the environmental value. The environment value shall cover damages caused by pollution and services provided by the environment(Tietenberg and Lewis, 2016). Enterprises only focus on their own profits and do not want to take the external cost caused by discharging pollution to the environment voluntarily. Thus, policy the maker must take action to internalize the externality caused by pollution damage to the environment.

The approach follows three-stage games of incomplete information. In the **first stage**, the policy maker offers a series of PIEA prices according to an area with several enterprises. In the **second stage**, enterprises take countermeasures. Increasing costs will decrease the enterprises' profits after the PIEA policy has been implemented. Supposing that the enterprise is an 'economic man' who chases the maximum benefit; thus, the enterprise will take measures if the profit decrease is beyond the acceptable range. Two types of strategies are available to adopt by the enterprise: adjust the production output or raise the pollution reduction investment. The enterprise chooses the best suitable measure in accordance with the maximum profit principle. In the **third stage**, the policy maker decides which price will be taken for the benefits. The policy maker will measure the social benefit aimed at every price and choose the price that will maximize the social benefit. The detailed process is shown in Fig 2.

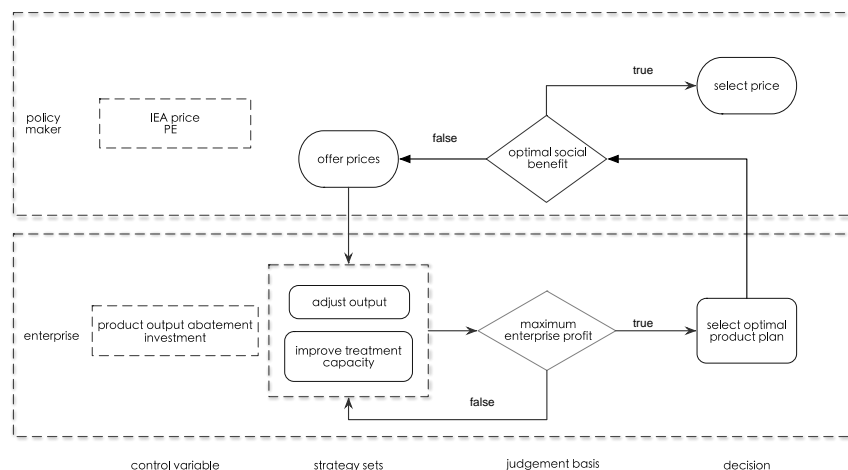


Fig 2 Modeling process of IEA pricing

The price model is based on the dynamic optimal control theory(Chiang, 2000). The modeling process refers to Biglaiser's research(Biglaiser et al., 1995) and modifies several of the items to be applicable to a realistic situation. The process can be expressed with an

1 enterprise with two control variables, which are the production output $x^i(t)$ and the
 2 pollution reduction investment I^i , and one state variable, which is the facility running fee
 3 $K^i(t)$. The enterprise's optimal objective is to maximum enterprise profit. The policy maker
 4 has one control variable, which is the PIEA price $\tau(t)$.

5 The enterprise profit is equal to sales income deducted by production cost, pollution
 6 treatment cost, and possible expenditure additional pollution reduction investment.

$$\text{enterprise profit} = \text{enterprise income} - \text{production cost} - \text{treatment } c - \text{investment} \quad (1)$$

7
 8 For the period from 0 to T , the discount rate is $\rho(\rho \geq 0)$. Assuming that the capital
 9 depreciation rate will not affect the result, the enterprise profit for a given time path is

$$\Pi^i = \int_0^T \{e^{-\rho t} [p^i x^i - w^i x^i - M g^i(x^i, K^i) - I^i] dt \quad (2)$$

10 $(i = 1, \dots, n)$

11 *St.* $x^i(t), I^i(t) \geq 0$.

12 In this equation, M is the PC price r , the PIEA price τ or $r + \tau$.

13 According to optimal control theory, the enterprise profit Hamiltonian function is

$$H^i = e^{-\rho t} [p^i x^i - w^i x^i - M g^i(x^i, K^i) - I^i] + \lambda I^i \quad (3)$$

14 The optimal objective is maximum social benefit. The existing study defines social benefits
 15 as the income minus damages caused by emissions (Perman et al., 2003). The social benefit
 16 function considers the following parts:

$$\begin{aligned} \text{social benefit} = & \text{social total income} - \text{total product cost} - \text{investment} \\ & - \text{pollution damage} \end{aligned} \quad (4)$$

17 Given a perfect competition market, social benefit can be presented as the sum of discounted
 18 enterprises' benefit minus the pollution damage, exclusive of emission taxes or profit from
 19 emission trading, since these represent only transfers between enterprises or between
 20 enterprises and the government (Biglaiser et al., 1995).

21 Under a perfectly competitive market, the social benefit could be presented as the sum of the
 22 enterprise discount profit subtracted by the pollution damage. The revenue from PIEA is not
 23 calculated because this part is the transfer payment from the enterprise and government. At
 24 the same time, the social benefit cost function is $D(\sum_i g^i(x^i, K^i))$. Assuming pollution
 25 damage to environment is linear:

$$D\left(\sum_i g^i(x^i, K^i)\right) = \delta \sum_i g^i(x^i, K^i) \quad (5)$$

1 In this equation, δ is the marginal emission damage coefficient.

2 For a period from 0 to T , the social benefit is

$$W = \int_0^T e^{-\rho t} \left\{ \sum_i [p^i x^i - w^i x^i - I^i] - \delta \sum_i g^i(x^i, K^i) \right\} dt \quad (6)$$

3 The social benefit Hamiltonian function is

$$H^w = e^{-\rho t} \{ p^i x^i - w^i x^i - I^i - \delta g^i(x^i, K^i) \} + \mu I^i \quad (7)$$

4 In this study, the COD and NH₃-N PIEA prices are set as two independent variables, which
5 are all calculated in the emission cost. We use a subscript to distinguish COD and NH₃-N.

6 The bivariate pollutant extended model and the details of multiple polluters extending the
7 model process are presented in SI. Further details are provided in SI.

8 *4.3 Scenarios*

9 In this study, we focus on three policies: the payment for initial emission allowance (PIEA)
10 policy, pollution charge (PC) policy and total emission control (TEC) policy. The previous
11 theory analysis has clarified the difference between PC and PIEA. PC means the polluter
12 pays to compensate for the damage caused by the emissions. PIEA means the polluter pays
13 scarcity rent for acquiring the environmental capacity property resource. For enterprises, both
14 PIEA and PC are expenditures that have no difference. Both costs are also calculated as
15 emission costs. The TEC policy is implemented as a penalty function(Weitzman, 1978), see
16 in SI.

17 We take a realistic situation as the baseline and set four scenarios. In scenario 1 (S1), only the
18 PIEA policy is implemented. The scenario 1 setting is used to compare with the scenarios
19 when PIEA is combined with PC. In scenario 2 (S2), PIEA and PC are implemented
20 simultaneously, which is the simulation mimicking reality. The previous theory analysis
21 discussed that PC requires compensation for the damage by emissions to the environment and
22 PIEA requires scarcity rent to be paid for acquiring environmental capacity property
23 resources. However, it is difficult to distinguish because it is an emission discharge cost

1 expenditure for the enterprise. The charge for the best emission amount is consistent with the
 2 compensation for emission damage and scarcity rent. The remaining part is the scarcity rent if
 3 the existing pollution charge is deducted. In scenarios 3 and 4 (S3, S4), the TEC policy is
 4 added based on scenarios 1 and 2 separately. The equations for the scenarios are as follows:

5 **Scenario 1: PIEA**

6 According to Equation (2), enterprise i profit is:

$$\Pi = \int_0^T \{e^{-\rho t} [p^i x^i - w^i x^i - \tau_C g_C^i(x^i, K^i) - \tau_N g_N^i(x^i, K^i) - I^i]\} dt \quad (8)$$

7 The Hamiltonian function is:

$$H^i = e^{-\rho t} [p^i x^i - w^i x^i - \tau_C g_C^i(x^i, K^i) - \tau_N g_N^i(x^i, K^i) - I^i] + \lambda I^i \quad (9)$$

8 **Scenario 2: PIEA+PC**

9 According to Equation (2), enterprise i profit is:

$$\Pi = \int_0^T \{e^{-\rho t} [p^i x^i - w^i x^i - r_C g_C^i(x^i, K^i) - r_N g_N^i(x^i, K^i) - \tau_C g_C^i(x^i, K^i) - \tau_N g_N^i(x^i, K^i) - I^i]\} dt \quad (10)$$

10 The Hamiltonian function is:

$$H^i = e^{-\rho t} [p^i x^i - w^i x^i - r_C g_C^i(x^i, K^i) - r_N g_N^i(x^i, K^i) - \tau_C g_C^i(x^i, K^i) - \tau_N g_N^i(x^i, K^i) - I^i] + \lambda I^i \quad (11)$$

11 **Scenario 3: PIEA+TEC**

12 The function is the same as in scenario 1, and the TEC policy is implemented as a penalty
 13 function.

14 **Scenario 4: PIEA+PC+TEC**

15 The function is similar to scenario 2, and the TEC policy is implemented as a penalty
 16 function.

17 *4.4 Implementation algorithm*

18 The preceding paragraph describes the process of establishing an initial emission allowance
 19 pricing model and to develop the theoretical general model into the model is applicable for
 20 two pollutants based on realistic needs. The maximum value principle is the first-order
 21 necessary condition in the optimal control theory to obtain the optimal value, which is used to
 22 solve a constrained pan-extremes problem. In the theoretical model, we determine the
 23 analytical solution based on the maximum principle.

24 According to formula A, the x^i value is determined by λ^i . The expression of λ^i is
 25 non-linear, therefore there is no analytical solution for x^i . This means that the maximum

value principle becomes no longer applicable to solve the partial differential equations. Although there is no analytical solution, we attempt to use software tools and algorithms to achieve its numerical solution.

In this research, we employed the BFGS-PSO[†] two-layer nestification algorithm to obtain the optimal object numerical solution (Møller, 1993; Poli et al., 2007) and take MATLAB software as the computational tool. We determine which PIEA price combination by τ_C and τ_N can achieve the optimal social benefit. We employed a two-layer nestification algorithm to solve the two optimal problems.

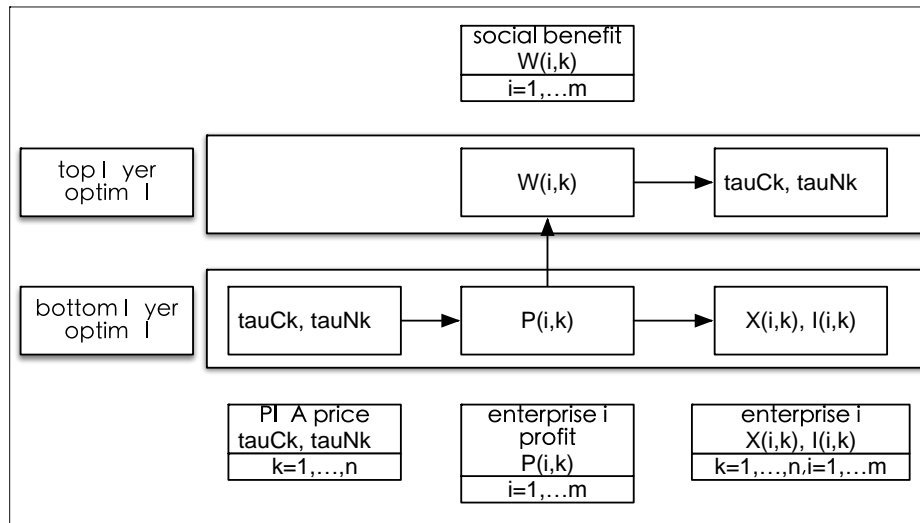


Fig 3 Two-layer nestification algorithm

As seen in Fig 3, the two-layer nestification algorithm is comprised of the optimal bottom layer and optimal top layer. We used the PIEA price τ_C and τ_N in the bottom layer to determine product quantity x^i and abatement investment I^i , which can achieve the enterprise optimal profit using the optimal pollutant discharging function. Next, we identified the top optimal PIEA price combination τ_C and τ_N , which can achieve the social benefit using the optimal bottom layer. The bottom layer uses the BFGS algorithm. The top layer uses the Particle Swarm Optimization algorithm.

5. Data Collection

[†] BFGS: Broyden, Fletcher, Goldfarb, Shanno; PSO: Particle Swarm Optimization.

1 5.1. Data source

2 The department implementing PIEA policy coincides with the administrative jurisdiction
3 range. Thus, the PC and TEC policy implementing areas additionally correspond to the
4 administrative jurisdiction range, dividing China to province and municipality level regions
5 as sample sets. This study involves 31 regions in the mainland of China (provinces,
6 municipalities, and autonomous regions). The data of the empirical simulation is based on the
7 China Environmental Statistics Database in 2013. The data contain 3 categories, 39 industries,
8 and 30,865 enterprises' information on energy and raw material consumption information,
9 production, and pollutant emission information. The study also employs the total pollutant
10 emissions for each region from the Ministry of Environmental Protection Total Emission
11 Reduction Database set in 2013, pollution charge standard for each region (latest standard),
12 emission standard for each industry (latest standard), and gross profit rate for each industry in
13 2013.

14
15 5.2. Data processing

16 The price model involves many other data, which cannot be obtained directly. Thus, the
17 following parameters and coefficients are calculated based on existing samples:

18 (1) Calculate the pollution discharge coefficients by establishing a model describing the
19 correlations among polluter emissions and product output and presents the value of
20 abatement investment(Biglaiser et al., 1995), then change it to a regression model with
21 regression samples from the China Environmental Statistics Database in 2013.

22 (2) The PIEA price model needs the treatment cost for each pollutant separately, but the
23 facility running fee from the environmental statistics data is for all pollutants. We adopted the
24 cost allocation approach to separate treatment costs for each pollutant(Wang, 2005).

25 (3) Calculate each enterprise's production cost, using the industrial average gross profit rate
26 to calculate the enterprise product cost(Helfert, 2001).

27 (4) After sample screening and trial calculation, we choose the function form and variables to
28 establish the regression equation according to past studies(Friedler and Pisanty, 2006;
29 Gonzalez-Serrano et al., 2005; Tsagarakis et al., 2003). Then, we obtain the marginal
30 pollution treatment cost through the marginal treatment cost function(Dasgupta et al., 1996).

31 (5) Calculate the marginal damage for the region.

32 (6) TEC constrains the pollution quantity to each region every year.

The data and coefficients involved are as follows: production cost, treatment cost, cost allocation, emission coefficients, region pollutant emission target, pollution charge standard, pollution control investment, pollution treatment cost function, marginal treatment cost, and region marginal damage, see in SI.

6. Results and Discussion

6.1. Optimal social benefits

The objective of the PIEA optimal model is to achieve maximum social benefit. Therefore, social benefit is the key point of focus in this study. The empirical simulation result shows the social benefit, as shown in Fig 4. The social benefit after charging the PIEA fee is approximately 50% of social benefit compared with baseline. The present model only considers pollutant emission damage to the environment and does not take into account the profit for pollutant emission reducing, such as ecological service function and effect on human health.

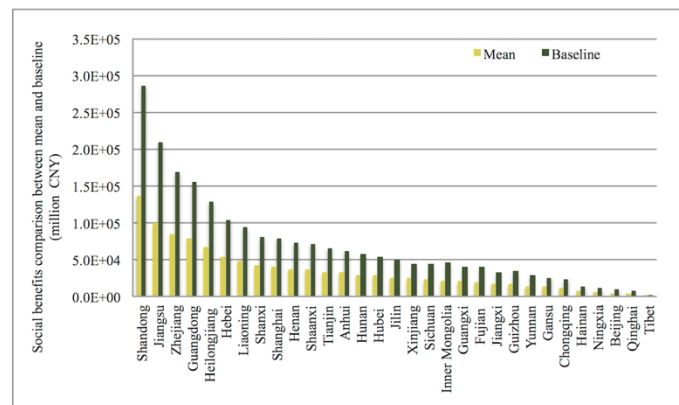


Fig 4 Social benefit comparison between mean and baseline

To clarify the difference in the social benefit in the four policy scenarios, we used the paired t-test to compare the results in Table 1. First, we tested S1–S2 and S3–S4 paired t-tests separately to determine whether the PIEA-only policy scenario and PIEA in combination with PC policy scenario can achieve equal social benefits. Table 1 shows the social benefit paired t-tests for the four scenarios. There is no significant difference observed for the social benefit in S1–S2 and S3–S4. Therefore, only the PIEA implemented and PIEA in combination with PC scenarios can achieve equal social benefit. Second, we performed

S1–S3 and S2–S4 paired t-tests to determine whether the TEC policy will affect the social benefit. When the TEC policy is implemented, there is a significant difference in social benefit with the scenario without the TEC policy. Looking back at the results in Fig 4, the social benefit in the scenario without the TEC policy is higher than the scenario with the TEC policy. This result indicates that the social benefit will decrease with the TEC policy.

Table 1 Social benefit paired t-test

Item	Variable	Obs	MeanDiff	t
Social benefit	S1–S2	31	3.258065	t = 0.3697
	S3–S4	31	20.09677	t = 0.1110
	S1–S3	31	130840.3	t = 2.0656**
	S2–S4	31	130857.2	t = 2.0663**

6.2. Best pollutant emission

Next, the best pollutant emission corresponding to the social benefit is shown. Fig 5 and Fig 6 display the simulated annual emissions of the two pollutants on average for the four scenarios compared to the baseline.

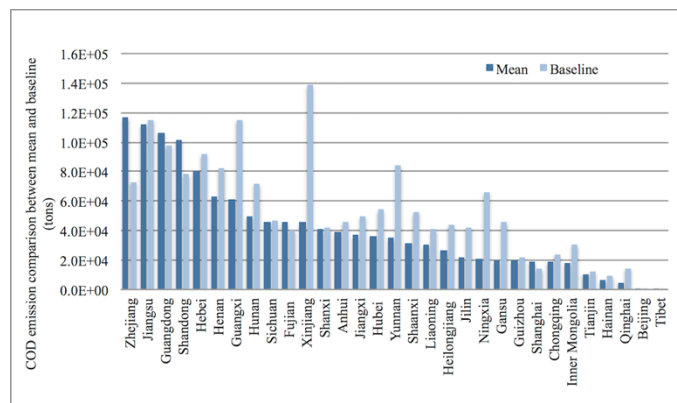


Fig 5 COD emission comparison between mean and baseline

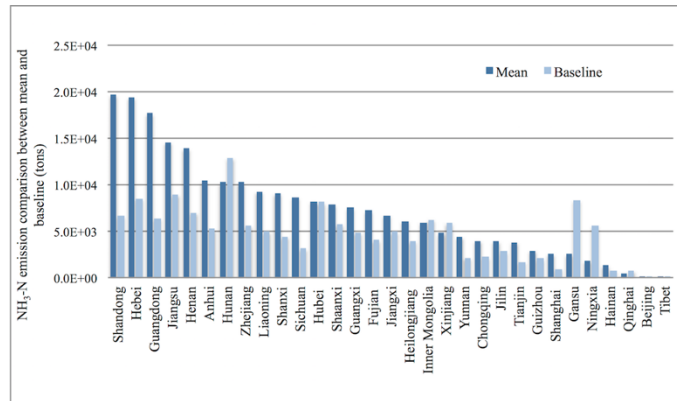


Fig 6 NH₃-N emission comparison between mean and baseline

From Fig 5, we know that most of the regions' emissions are decreased from the baseline, especially Yunnan, Gansu, Qinghai, Ningxia and Xinjiang, which are the top five regions in the emission depression percentage ranking. This result means that after being charged the payment for the initial emission allowance, the enterprises' discharge costs increased, so the pollution from the enterprises in most regions decreased. Unexpectedly, Beijing, Shanghai, Jiangsu, Zhejiang, Fujian, Shandong, and Guangdong, had emission quantities greater than the baseline. We inferred that for most of the enterprises in the regions whose emission are greater than the baseline, if their marginal profit caused by pollutant emissions per ton are higher than the PIEA expenditure, then the enterprises choose to increase pollutant emissions. Another interesting finding in Fig 6 is that excluding Inner Mongolia, Hubei, Hunan, Tibet, Gansu, Qinghai, Ningxia, and Xinjiang, the NH₃-N emissions after paying the PIEA fee show an increasing trend for the remaining regions. This result is probably due to the major pollution of enterprises in each region and the treatment facilities for major pollution. Some enterprises mainly emit COD, whereas the NH₃-N generation quantity is lower than that of COD. Thus, the pollution treatment facility is primarily for COD and the NH₃-N reduction is a synergistic effect (we can infer that the treatment facility is mainly aimed at allocating pollution treatment efficiency).

In Table 2, we also list the S1-S2, S3-S4, S1-S3, and S2-S4 paired t-tests for the best COD and NH₃-N emissions to discuss the differences between several scenarios. S1-S2 and S3-S4 paired t-tests are for testing if the PC policy will affect best emission quantity. S1-S3 and S2-S4 paired t-tests are for testing if the TEC policy will affect the best emission quantity. S1-S2 and S3-S4 paired t-tests show that the best emission quantities have no differences whether PC is implemented or not. In other words, the best emission quantities are equal

1 regardless of the PC policy implementation. This result means both PIEA policy strategy and
 2 PIEA plus PC policy strategy will achieve similar best emission quantities. S1-S3 and S2-S4
 3 paired t-tests show that the TEC policy has a significant effect on the best emission quantity.
 4 The COD emission quantity with TEC is lower than that without the TEC policy. However,
 5 the effect of NH₃-N emissions is not significant whether TEC is implemented.

6 Table 2 Best pollutant emission paired t-test

Item	Variable	Obs	MeanDiff	t
Best COD emission	S1-S2	31	10.15589	t = 0.9137
	S3-S4	31	49.16717	t = 1.3466
	S1-S3	31	3423.794	t = 2.0729**
	S2-S4	31	3462.806	t = 2.0980**
Best NH ₃ -N emission	S1-S2	31	4361.168	t = 1.0016
	S3-S4	31	-7.652266	t = -1.6471
	S1-S3	31	4480.461	t = 1.0222
	S2-S4	31	111.641	t = 0.9029

8 6.3. Initial emission allowance price

9 The price is the key point of the PIEA policy. Fig 7 displays the price of the initial emission
 10 allowance in the four scenarios for each region. Comparing the price of the four scenarios, S1
 11 is higher than S2 and S3 is higher than S4. The result is related to the scenario setting. S1 and
 12 S3 only included the PIEA policy, while S2 and S4 included the PC policy in addition to
 13 PIEA. Reviewing previous discussion shows that the charge for the best emission quantity is
 14 constituted by damage compensation and scarcity rent. If the charge is deducted by the
 15 existing PC price, then the remaining part is the PIEA price. Next, the portion of the S1 price
 16 that is higher than S2 is the pollution charge. S3 is higher than S4 for the same reason.

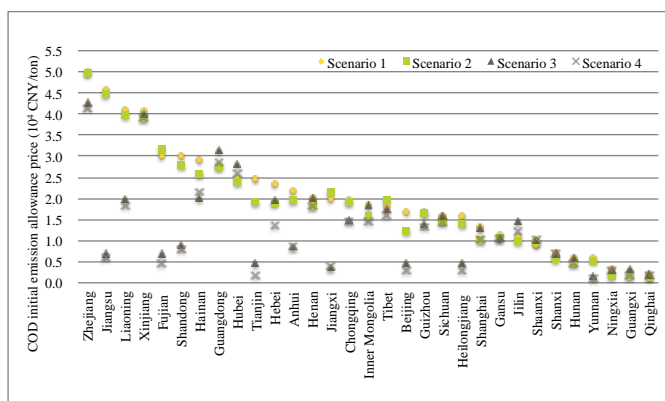


Fig 7 COD initial emission allowance price of each region in S1–S4

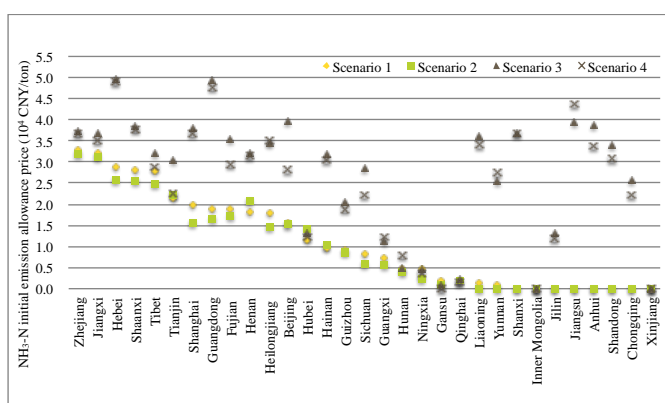


Fig 8 NH₃-N initial emission allowance price for each region in S1–S4

Interestingly, the initial allowance price of NH₃-N in some regions was found to be zero, as shown in Fig 8. In the modeling process, we set the price of the COD and NH₃-N initial allowance as two independent variables, to avoid duplicating charges to different pollutants discharged by the same enterprise under the existing synergistic control effect. When the enterprises adjust the output of product, the amount of pollutants will also be changed. Depending on the enterprise and the production process, some products discharge both COD and NH₃-N contaminants, but the production process of others discharges a single contaminant, such as only COD or NH₃-N. For products that discharge two contaminants simultaneously, if the enterprise adjusts the product output, the amount of both pollutants will change in a collinear trend. In this way, if adjust the emission of one pollutant, then the other associated pollutant emission will also be changed. For enterprises discharging two pollutants simultaneously, if charge is for one pollutant for emission control, the other associated pollutant emission will be under control also. Therefore, the model provides the simulation results: if most of the enterprises discharge COD and NH₃-N simultaneously in one region,

1 then only charging for the COD emission allowance, or charging for NH₃-N according to the
2 ratio of NH₃-N discharged by the only NH₃-N emission enterprises to total NH₃-N emission
3 in the region, can achieve the region's optimal social benefit. This explains why the NH₃-N
4 price in some regions is lower than the COD price, or even zero.

5 Next, the TEC policy effect on price is discussed. As shown in Fig 7 and Fig 8, the price
6 trend of S3 and S4 considering the TEC policy are obviously different from S1 and S2. The
7 COD price in S1 is higher than S3. Moreover, the COD price in S2 is higher than in S4. The
8 NH₃-N price shows an opposite trend, that S1 is lower than S3, and the NH₃-N prices in some
9 regions are zero. According to the principle of optimal social benefits, a model should charge
10 treatment facilities producing major pollutants. When considering the TEC policy that is
11 restricted by a target emission, the model calculation should determine the best emission
12 quantities in close proximity to the emission target as principle. According to the best
13 emission quantities in Fig 6, when pollutants emissions are beyond the restricted target, the
14 beyond part will be “punished”. Thus, the NH₃-N price considering the TEC policy is higher
15 than that without the TEC policy. When the region’s total NH₃-N emission is beyond the
16 restricted target, the enterprises in the region must pay for NH₃-N at a high price. Remember
17 that the treatment facilities have a synergistic effect on COD and NH₃-N, which means if the
18 NH₃-N emission is controlled, then COD will be controlled. So, if the enterprises pay for the
19 NH₃-N emission at a high price, then they could pay for COD at a low price.

21 *6.4 Difference of price for pollutants compared to the pollution charge*

22 If the difference of price for S1 and S2 is equal to the pollution charge fee, then we
23 demonstrate the previous hypothesis: to achieve the best emission under the optimal social
24 benefit, the cost paid by the enterprise should include the compensation for environmental
25 damages and scarcity rents gained by the enterprises that are using the environmental
26 capacity. However, in reality, only compensation for the environmental damage was charged,
27 the scarcity rents were missed. The model setting in this research calculates the scarcity rents
28 deducting the pollution charge, the PIEA policy compensates for the missing scarcity rents.

29 To demonstrate that the differences between S1 and S2, S3 and S4 are caused by the
30 pollution charge, we did paired t-tests for the difference of S1 minus S2 to the pollution
31 charge, and S3 minus S4 to the pollution charge, as shown in Table 3. According to the paired
32 t-test results, S1 minus S2 and S3 minus S4 exhibit no significant difference with the

1 pollution charge. This condition suggests that the PIEA price for scenarios regardless of the
 2 PC policy always achieves the optimal social benefits. The empirical results support the
 3 PIEA theory that the price difference of S1–S2 and S3–S4 should be the PC price.

4 Table 3 Difference in two scenarios' emissions PIEA prices compared to the pollution charge
 5 price paired t-test

Item	Variable	Obs	MeanDiff	t
Difference of two scenarios' COD PUER price with EC price	S1–S2 with EC price	31	-0.0593548	t = -1.9816
	S3–S4 with EC price	31	-0.0487097	t = -1.2884
Difference of two scenarios' NH ₃ -N PUER price with EC price	S1–S2 with EC price	31	-0.1774194	t = -2.9543
	S3–S4 with EC price	31	-0.06	t = -1.5030

6 From the result, we know that whether PIEA is implemented or PIEA in combination with
 7 PC, the two types of scenarios can achieve equal social benefits. We can infer that no matter
 8 what kind of policy, they achieve equivalent optimal social benefits. Therefore, in the PIEA
 9 and PC mixed policy, the combination policy can achieve the optimal social benefit in the
 10 current condition. Therefore, in this policy design, PIEA is complimenting a missing part of
 11 the optimal pollution charge rather than duplicating it with PC.

12 In the model assumption, the investment will be placed in existing facilities if the enterprise
 13 decides to invest more to improve the treatment efficiency, which means improving the
 14 existing facilities, rather than adding new facilities. A disparity exists between the
 15 assumption and reality. Adding new facilities or processes is not easy. Many factors need to
 16 be considered when adding new facilities, such as the enterprise pollution generation quantity.
 17 The treatment process is constrained by the concentration if a new process is implemented in
 18 an existing structure or new structure. All of the problems should be discussed according to a
 19 concrete case, rather than a general summary. Thus, in the model assumption, the effects
 20 caused by investment improved the existing treatment facility efficiency. By employing this
 21 process, an enterprise for which the primary pollutant is COD (NH₃-N is synergistic pollutant)
 22 chooses to improve the production output. Next, NH₃-N generation will increase. However,
 23 the facilities aimed at NH₃-N have not been improved. This factor will result in an NH₃-N

1 emission increase. Thus, the result is a warning because of insufficient treatment capabilities.
2 NH₃-N emissions will increase after PIEA is implemented if new treatment facilities are not
3 added.
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7 **7 Conclusions and Policy Implications**

8 *7.1. Conclusions*

9 We establish an optimal control-based model with COD and NH₃-N, two independent
10 pollutants variables, to calculate the initial emission allowance price in PIEA policy and
11 simulate the results after the policy is applied. At the same time, we illustrate the impact of
12 pre-existing policies on the performance of the PIEA policy. Using data containing 3
13 categories, 39 industries, and 30,865 enterprises samples, we obtain the optimal social benefit,
14 the best pollutant emissions, and the initial emission allowance price.
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25 First, because PIEA policy increases the enterprises' discharging cost, most regions' COD
26 emissions are less than the baseline. However, there are exceptions, Beijing, Shanghai,
27 Jiangsu, Zhejiang, Fujian, Shandong, and Guangdong, in which emission quantities are
28 greater than the baseline. We inferred that in the case when the marginal profit caused by
29 pollutant emissions per ton are higher than the PIEA expenditure, the enterprises choose to
30 increase pollutant emissions. For the other case of water pollutants, the NH₃-N emission
31 shows an opposite trend. The simulation result is that excluding Inner Mongolia, Hubei,
32 Hunan, Tibet, Gansu, Qinghai, Ningxia, and Xinjiang, the NH₃-N emissions in the rest of
33 regions are increased. We inferred the reason is that the pollution treatment facility is mainly
34 for COD and the NH₃-N reduction is a synergistic effect.
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45 Second, whether only the PIEA policy or PIEA combined with the PC policy, both types of
46 policy can achieve equal optimal social benefits and best pollutant emissions. However, the
47 initial emission allowance price in S1 that only implements the PIEA policy is higher than the
48 price in S2, where PIEA is combined with the PC policy. By paired t-test, we inferred that
49 there is no significant difference between the price difference between S1 and S2 and the
50 pollution charge price. At the same time, the price of the NH₃-N initial allowance in some
51 regions was zero. We set the COD and NH₃-N initial allowance prices as two independent
52 variables to avoid the duplicated charges to different pollutants discharged by the same
53 enterprise under the existing synergistic control effect.
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1 Third, the COD emission quantity with TEC is lower than that without the TEC policy,
2 Therefore, the TEC policy will be effective for pollutant emission control. At the same time,
3 the TEC policy will also affect price. The TEC policy means that regions have their own
4 target emissions, and when the emission is beyond the restricted target, the beyond part will
5 be “punished”. Then, the pollutant beyond the restricted target will be charged a payment for
6 IEA at a higher price than without the TEC policy.

7 *7.2 Policy implications*

8 In this study, the pricing method for initial allowance in the PIEA policy considers the
9 existing pollution charge policy. When the PIEA policy has not been implemented, only a
10 pollution charge is not sufficient to achieve the best pollutant emissions. In the pricing
11 method designed, the initial allowance fee and the pollution charges are combined to achieve
12 the best pollutant emissions. This study proves that under the pricing method designed, the
13 PIEA policy is not a duplicate policy of the pollution charge, but rather a supplement to the
14 existing pollution charge for achieving the best emission discharge.

15 According the result that the social benefit after being charged the PIEA fee with TEC is
16 lower than without it, we can infer that the social benefit will lose economic efficiency with
17 the TEC policy. Although economic efficiency is lost under the TEC policy, it necessary for
18 the areas whose pollutant emission increase after being charged the PIEA fee because the
19 increment of pollutants will be higher than without the TEC policy.

20 In reality, certain enterprises’ pollution treatment facilities are primarily for COD, and the
21 NH₃-N reduction is a synergistic effect. The simulation results indicate that under the
22 assumption that enterprises invest in the existing facilities instead of adding new facilities,
23 the NH₃-N emission will increase because of insufficient treatment capability. Thus, the
24 NH₃-N emission will increase after PIEA is implemented if new treatment facilities are not
25 added. The government should increase treatment facilities for NH₃-N.

26 The effect of economic policy is inclined to screen higher marginal benefit income
27 enterprises which use emission allowances rather than reducing pollutant emissions. Some
28 regions’ pollutant emissions will increase even if charged PIEA fees, meanwhile other
29 regions’ pollutant emissions will decrease after being charged. Therefore, the policy maker

1 should take into consideration the appropriate time for launching a new policy in the whole
2 nation because a new policy may induce an economic recession.

3 4 5 6 7 8 4 *7.3. Research limitation*

9
10 5 There are some inadequacies in this research. In the social benefit model, only the recovery
11 6 cost method is used to calculate the damage caused by the pollutants discharged into the
12 7 environment, and the damage to the ecological environment and human health is not
13 8 considered. The heterogeneous pollutants effects on human health and ecological service is
14 9 related to the place where the point source is located. The point source location belonging to
15 10 which environmental function zone should be determined following the discharge standards
16 11 and considering the effects of the pollution source on the humans living in the area and the
17 12 surrounding ecological environment. Not enough information on the human living nearby
18 13 and the ecological environment surrounding the pollution source were available to support
19 14 calculations in this research. Therefore, we use the cost for removing pollutants discharged to
20 15 the environment the pollutant damage effect instead of the costs to the ecological
21 16 environment and to human health. Similarly, the income caused by the environmental quality
22 17 improvement is not included.

23 18 In the model assumptions, there are some simplified situations, such as when the firm
24 19 determines its product output, they do not consider the market equilibrium of the product
25 20 supply and demand, and keep the price stable. In the simulation of enterprises
26 21 decision-making behavior, some details cannot be shown. There are three ways to reduce
27 22 pollutant emissions for enterprises: promoting the production process technology, updating
28 23 the end of pipe technology, and improving the efficiency of the existing facilities; but in the
29 24 model, the emission reduction method is only the improvement of efficiency of the existing
30 25 facilities, technological progress has not yet been considered.

31 26 Due to lacking fixed investment data for pollutant treatment facilities, all the parameters
32 27 involved in the pollution reduction cost in this study are based on the operating costs of the
33 28 enterprises' pollution abatement facilities. The state variables in the model are the only
34 29 present emissions reduction facility operating costs in this part.

35 30 The empirical simulation result has finite precision because of model simplification and lack
36 31 of data. The model has been simplified for curving the complicated realistic situation under
37 32 certain hypotheses. Thus, in the future, we will take the pollutant emission effect on human

1 health and the ecological service function into consideration as components of the social
2 benefit.

3 4 5 6 7 **4 Supporting Information**

8
9
10 5 Additional information includes details on data, modeling process, parameters and
11 6 implementation algorithms. This material is available free of charge via the Internet at
12 7 XXXX.
13
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15

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17
18
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Figure 1

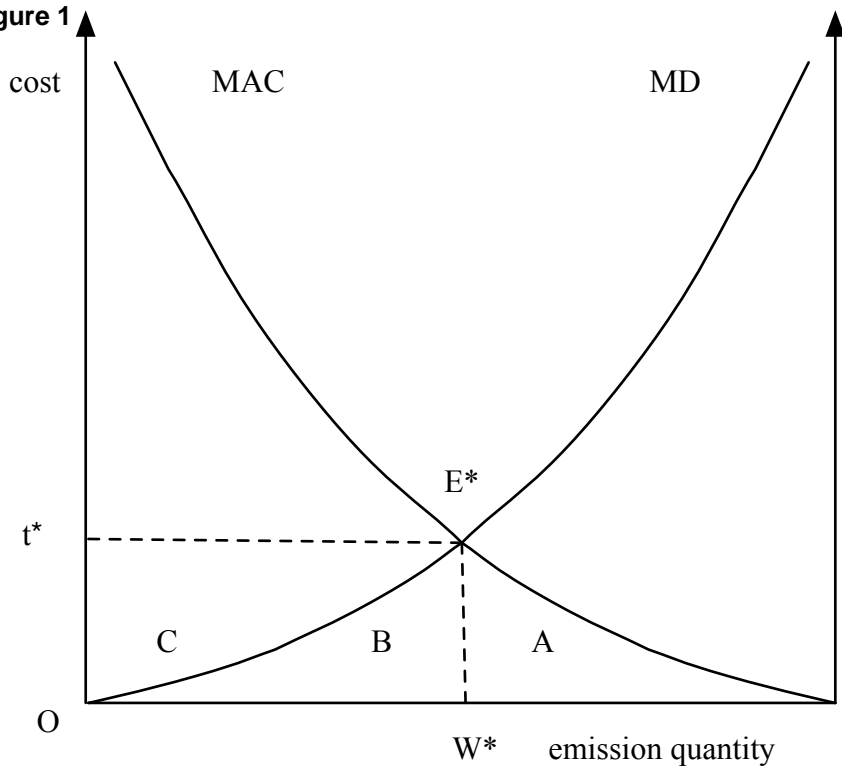
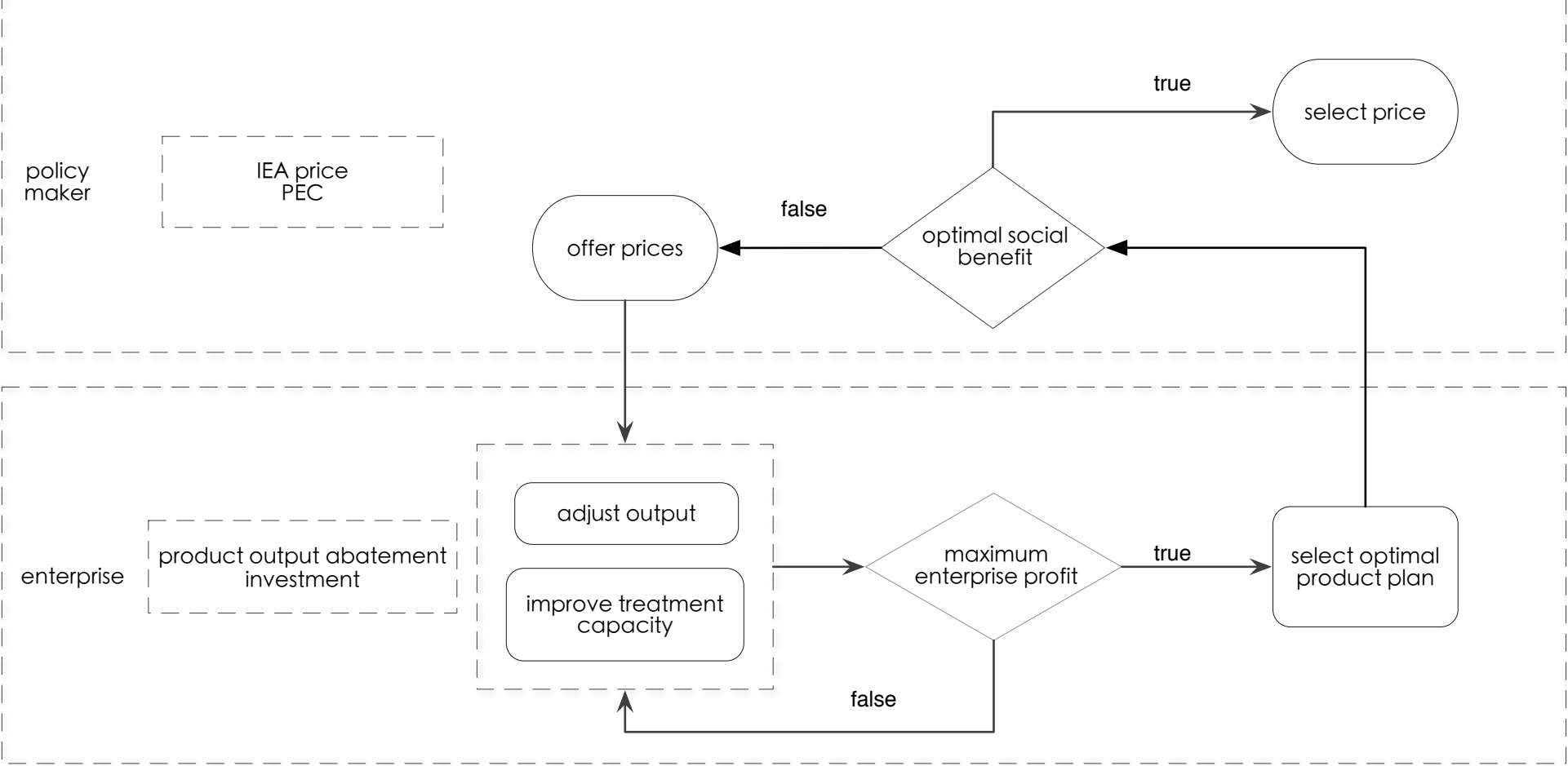


Figure 2



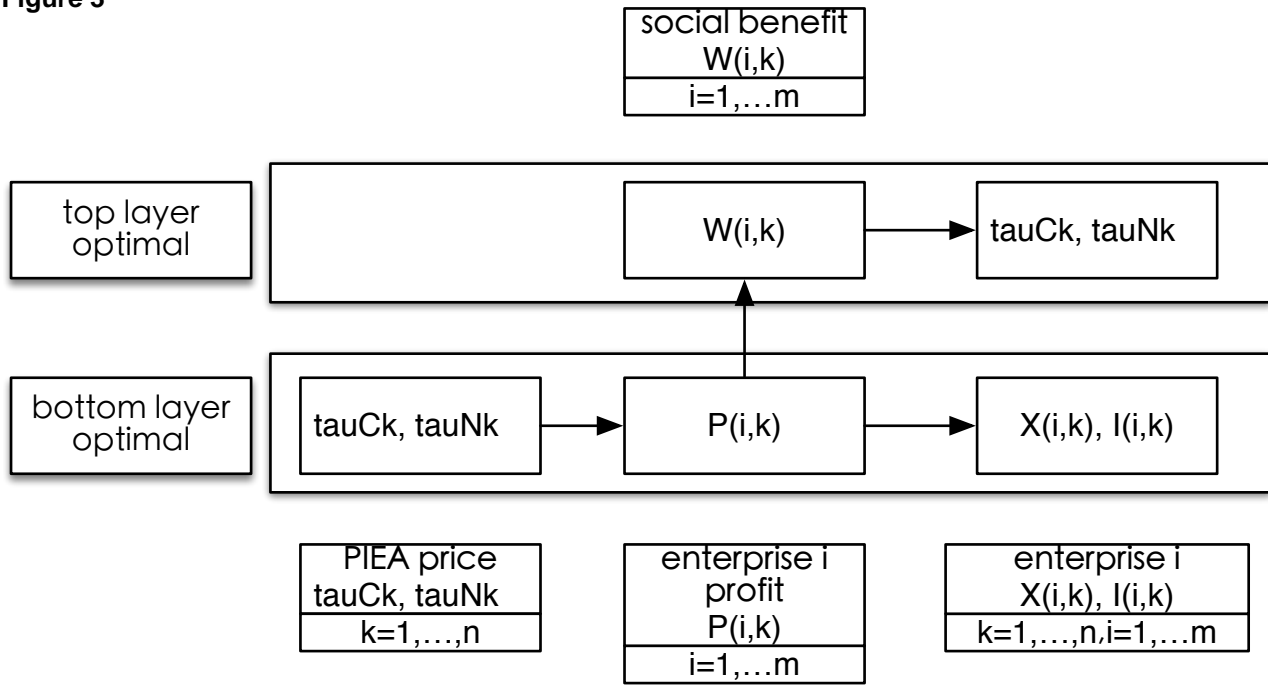
control variable

strategy sets

judgement basis

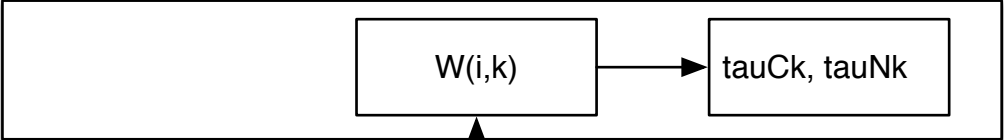
decision

Figure 3

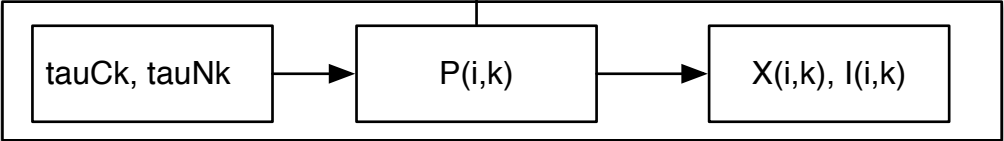


social benefit
 $W(i,k)$
 $i=1, \dots, m$

top layer
optimal



bottom layer
optimal



PIEA price
tauCk, tauNk
 $k=1, \dots, n$

enterprise i
profit
P(i,k)
 $i=1, \dots, m$

enterprise i
X(i,k), I(i,k)
 $k=1, \dots, n, i=1, \dots, m$

Figure 4

Social benefits comparison between mean and baseline

(million CNY)

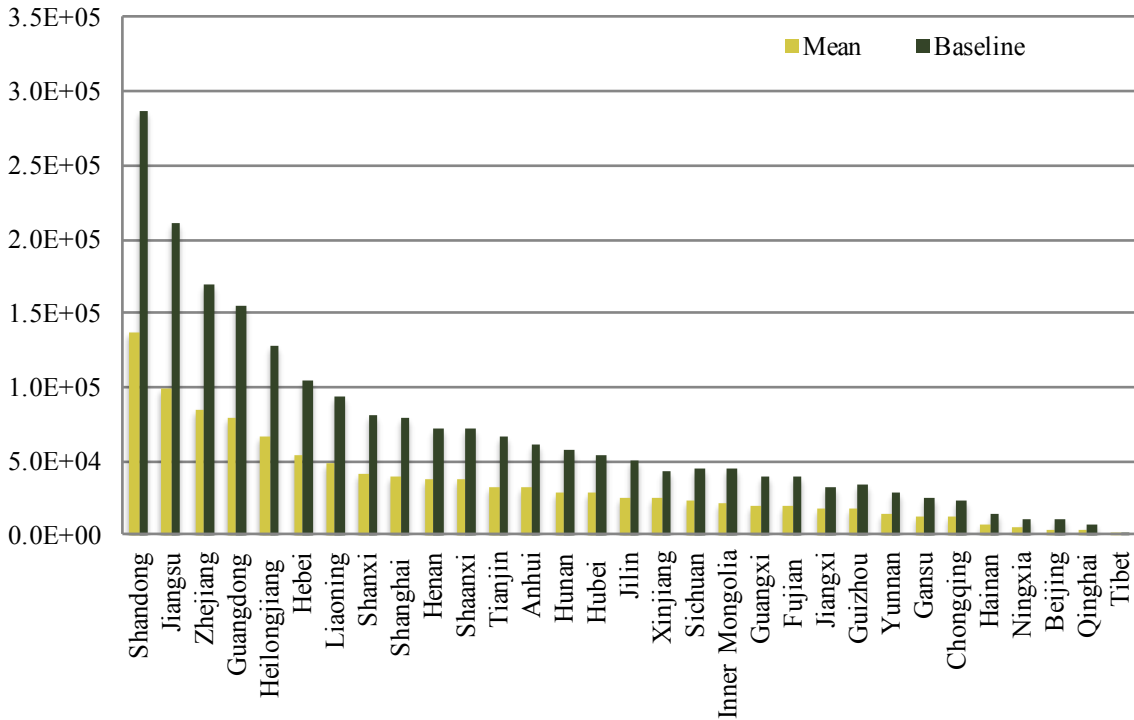


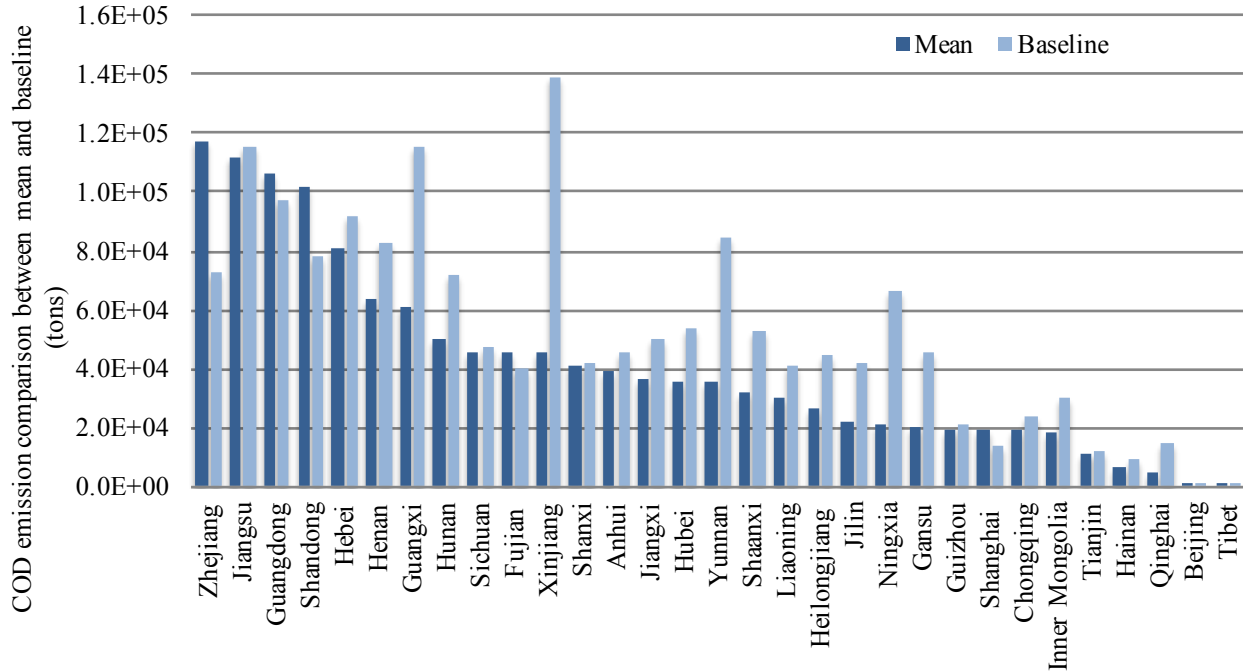
Figure 5

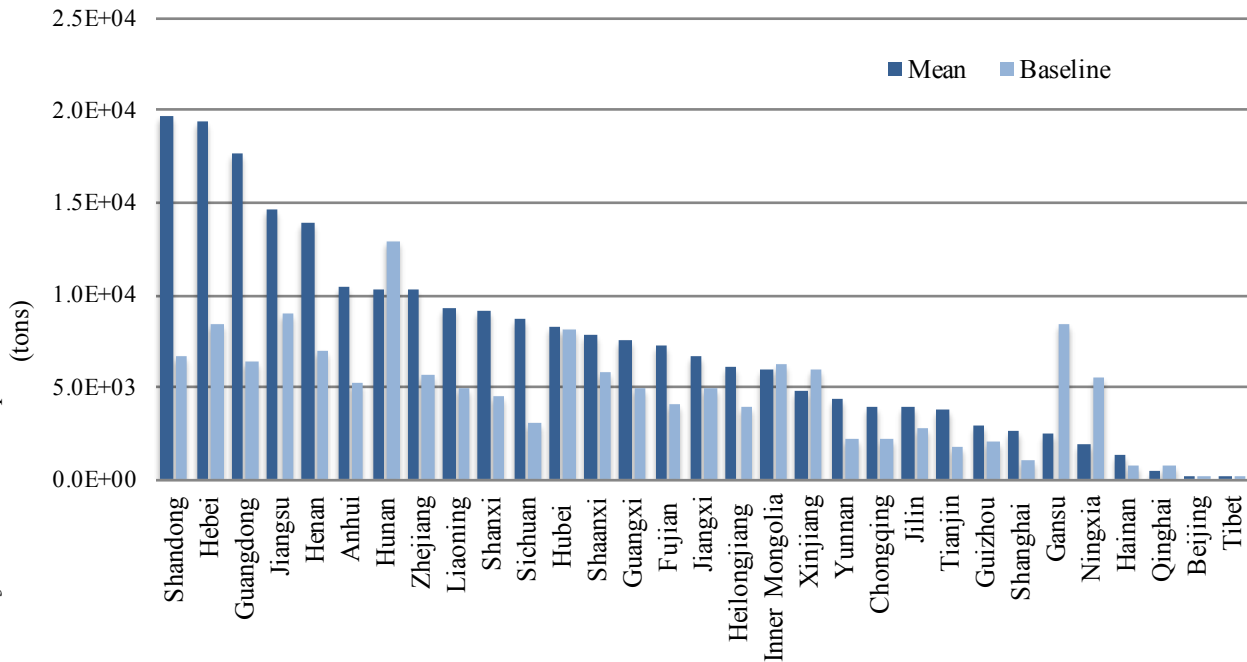
Figure 6NH₃-N emission comparison between mean and baseline

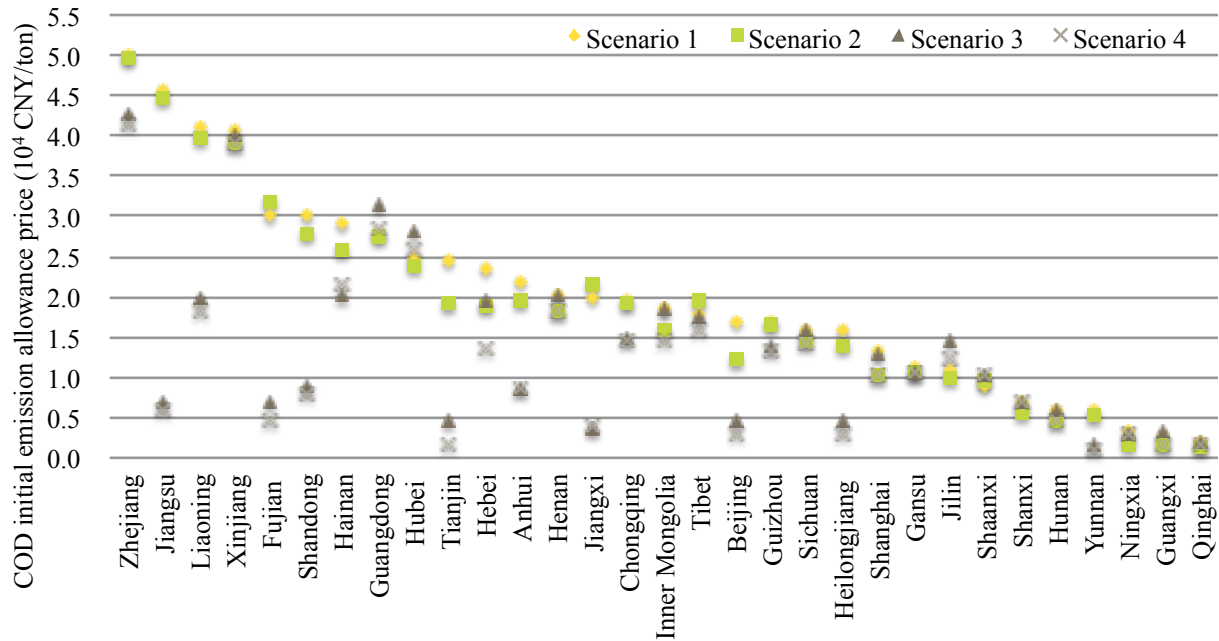
Figure 7

Figure 8