

Measurements and simulation of ionospheric scattering on VHF and UHF radar signals: Coherence times, coherence bandwidths, and S_4

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[1] Irregularities in the electron density of the ionosphere cause phase and amplitude scintillation on transionospheric VHF and UHF radar signals, particularly at lower radio frequencies. The design of radar and other transionospheric systems requires good estimates of the coherence bandwidth (CB) and coherence time (CT) imposed by a turbulent ionosphere. CB and CT measurements of the equatorial ionosphere, made using the Advanced Research Project Agency Long-range Tracking and Identification Radar 158 MHz and 422 MHz phase coherent radar located on Kwajalein (9.4°N, 167.5°E), are presented as a function of the two-way S_4 scintillation index at 422 MHz. The log linear regression equations are $CT = 1.46 \exp(-1.40 S_4)$ s at 158 MHz and $CT = 2.31 \exp(-1.10 S_4)$ s at 422 MHz. CT also varies by a factor of 2–3 depending on the effective scan velocity through the ionosphere, v_{eff} . The CT and CB, as a function of S_4 , have been compared to those from the Trans-Ionospheric Radio Propagation Simulator, a phase screen model. A close agreement is achieved using appropriate values of v_{eff} and midrange values of phase spectral index and outer scale. Validation of CB is, however, limited by insufficient radar chirp bandwidth. Formulating the model in terms of the two-way S_4 index (an easily measurable parameter) rather than more fundamental phase screen parameters (which are difficult to obtain), improves its utility for the systems engineer. The frequency dependencies (spectral indices) of S_4 and of CT are also presented to allow interpolation and some extrapolation of these results to other frequencies.

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1. Introduction

[2] Turbulent processes in the ionosphere create a spectrum of electron density irregularities which forward scatter VHF and UHF radio signals passing through them. The resultant phase and amplitude fluctuations (or scintillation) at the receiver limits the time and bandwidth over which the channel is coherent. The coherence time (CT) and coherence bandwidth (CB) are useful engineering parameters for the design of transionospheric radio and radar systems. For example, the ionospheric CB may limit either the data transmis-

sion rate in a satellite communications link or the range resolution of a transionospheric radar. The ionospheric CT may limit the number of pulses available for coherent pulse integration, which could, for example, limit the along-track resolution in a space-based synthetic aperture radar image [van de Kamp *et al.*, 2009; Belcher and Rogers, 2009].

[3] Studies of scintillation over a two-way (radar) path are relatively uncommon due to the expensive radar facilities required; but see, for example, papers by Knepp [1983a, 1983b] and Coster *et al.* [1993, 2002] who have addressed the impact of the ionosphere on radar phase-coherent pulse integration. This paper extends the earlier work by Cannon *et al.* [2006] and a companion paper [Rogers *et al.*, 2009]. It uses the measurements from the Advanced Research Project Agency (ARPA) Long-range Tracking and Identification Radar (ALTAIR) radar in association with the Trans-Ionospheric Radio Propagation Simulator (TIRPS) [Rogers *et al.*, 2009] to under-

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Table 1. Dates, Times, Maximum Elevations, and Number of CSFs for Passes of Satellite 2826

Date	UT Range	Local Time Range	Maximum Elevation (deg)	Number of CSFs (Above 20° Elevation)
18 Jan 2005	1003–1015	2113–2125	49.5	115
21 Oct 2005	1027–1042	2137–2152	81.1	128
25 Oct 2005	0941–0956	2051–2106	86.5	130
14 Sep 2006	1115–1121	2225–2231	48.4	108
15 Sep 2006	1036–1044	2146–2154	85.9	128
				Total = 609

stand the relationships between CT and CB and parameters such as S_4 . In so doing we have been able to further refine the TIRPS model and we gain insight into a number of important issues.

2. Wideband Ionospheric Distortion Experiment

[4] The measurements in this study were collected as part of the joint UK-U.S. Wideband Ionospheric Distortion Experiment (WIDE) [Cannon *et al.*, 2006]. WIDE uses the ALTAIR monostatic radar located on Kwajalein (9.4°N, 167.5°E) to track orbiting calibration spheres. Linear FM chirps were transmitted coherently at 158 MHz (7 MHz bandwidth) and 422 MHz (18 MHz bandwidth) with a pulse repetition frequency (PRF) in the range 285 ± 50 Hz and with PRF changes occurring no more than once every 20 s. The complex received signal was recorded for analysis as described below. For these studies we used only object 2826, which is at an orbital altitude of 767 ± 6 km altitude and at 70° inclination.

[5] After proof-of-concept trials in January 2005, subsequent measurements took place during the August–October 2005 and 2006 seasonal peak in scintillation occurrence at Kwajalein [Aarons, 1993]. Late evening passes, when the likelihood of strong scintillation was greatest [e.g., Aarons, 1982], and passes with high maximum elevation were selected. Although the measurements were taken near the minimum of the solar activity cycle, strong scintillation was nonetheless observed on several occasions, so providing a wide range of conditions. For each pass the data were processed to generate a series of scattering functions (CSFs) [Cannon *et al.*, 2006; Rogers *et al.*, 2009] from which the CB and CT could be derived.

[6] Each CSF was calculated from sequences of 1024 contiguous radar chirp returns which, at an average pulse repetition frequency (PRF) of 285 Hz, constitute a 3.6 s sample. The component of pulse spreading due to ionospheric dispersion was removed by calculating the total electron content (TEC) from the differential group delay of the 158 and 422 MHz chirp returns. Measurements presented in this paper were derived from channel scattering functions (CSFs) for five passes of object 2826,

giving a total of 609 CSFs (see Table 1). Note that the local time at Kwajalein is 11 h 10 m ahead of UT. Data for elevations below 20° were excluded from the measurements to minimize the impact of ground multipath and any tropospheric perturbations. This also ensures that the radar tracker had established a good lock on the target. Signal-to-noise ratios ranged between 9 and 53 dB.

[7] Under a homogeneous ionosphere (with no irregularities), the CSF profile would be confined to a single Doppler bin at 0 Hz (the Doppler bin width is $1/3.6$ s = 0.28 Hz). The delay profile would exhibit a sinc-squared profile (the linear chirp autocorrelation function) convolved with the Hann filter. This results in a 3 dB width $\approx 1.5/2B$, where B is the chirp bandwidth (=107 ns at 158 MHz and 42 ns at 422 MHz).

3. Trans-Ionospheric Radio Propagation Simulator

[8] The Trans-Ionospheric Radio Propagation Simulator (TIRPS) has been developed to simulate WIDE measurements. The model, based on a thin phase screen, parabolic equation propagation technique [Knepp, 1983a, 1983b], is described in detail by Rogers *et al.* [2009]. The phase screen, which represents the effect of ionospheric irregularities, is defined to be a log-log linear spectrum (equation (1)) which flattens off for irregularities greater than an outer scale size L_o .

$$S_\phi(\kappa) = \left[\frac{1}{4} \pi^{-\frac{3}{2}} r_e^2 \lambda^2 G C_k L \sec(\theta) \left(\frac{2\pi}{1000} \right)^{p+1} \frac{\Gamma(\frac{p}{2})}{\Gamma(\frac{p+1}{2})} \right] \cdot \frac{1}{(\kappa_0^2 + \kappa^2)^{p/2}} \quad (1)$$

where κ = spatial frequency, r_e = classical electron radius, λ = radio wavelength, G is a geometric enhancement factor [see Rino, 1979], $C_k L$ = vertical integrated strength of turbulence at the 1 km scale, θ = propagation zenith angle at the ionospheric pierce point (IPP), p = phase spectral index, Γ = Euler's gamma function and κ_0 = outer scale frequency = $2\pi/L_o$. Equation (1) is derived from equation (16) of Rino [1979] where we have changed the dependent variable from temporal to spatial frequency and

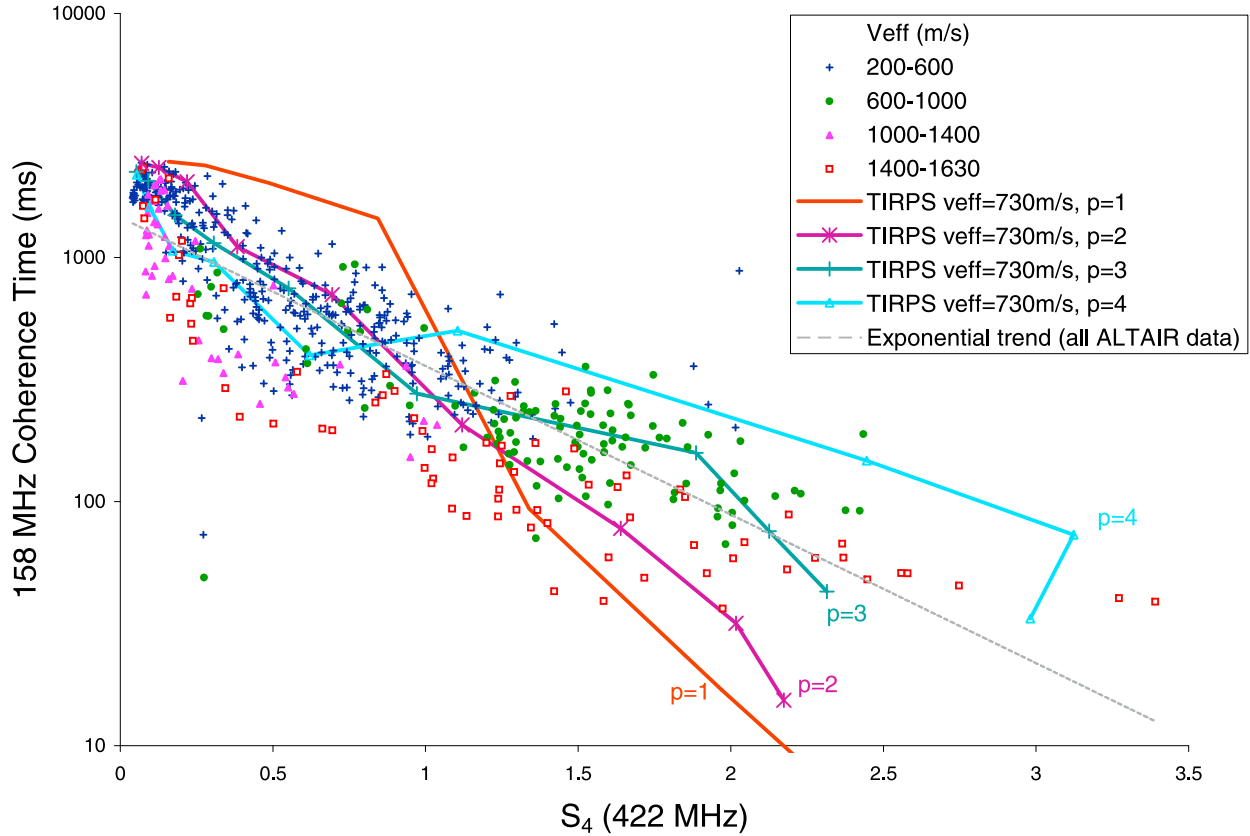


Figure 1. CT measurements for 158 MHz CSFs as a function of the 422 MHz S_4 index. Points represent measured CSF and are categorized by ranges of v_{eff} . Mean simulated values are shown for varying spectral index p (solid lines).

used the definition $C_k L = C_s L (1000/2\pi)^{p+1}$. In the simulations the three important variables are p , L_o and $(G.C_k L.sec(\theta))$, the latter combination having been treated as a single variable parameter.

[9] TIRPS uses Rino's equation to define the phase screen spectrum only. This uses the assumption that a thin phase screen adequately represents the extended scattering region, as demonstrated by Bramley [1977]. Thereafter the Parabolic Equation (PE) approximation [Levy, 2000] is used to describe the wave propagated through free space up to orbit height. This approximation to the full electromagnetic wave equation assumes propagation close to the line-of-sight axis, and assumes that refractive index fluctuations $\Delta n/n \ll 1$ (which implies fractional electron density variations $\Delta N_e/N_e \ll 1$). Errors in the standard PE approximation due to off-axis propagation are of the order 10^{-3} at 10° off-axis [Levy, 2000, p. 11] and so are negligible for the ALTAIR radar geometry which has a 3 dB beam width of approximately 3° at 158 MHz or 1° at 422 MHz. Assuming a typical postsunset F region electron density of 10^{11} m^{-3} , the root-mean-squared

$\Delta N_e/N_e$ is less than 0.2 for $C_k L \leq 10^{33}$ rising to 0.6 at $C_k L = 10^{34}$ (based on Rino's definition of C_s (equation (7) of Rino [1979]) and assuming a scattering path length $L = 200 \text{ km}$, $L_o = 10 \text{ km}$, and $p = 2.5$). The assumption $\Delta N_e/N_e \ll 1$ in the PE method may therefore become unrealistic above around $C_k L = 10^{33}$. In this paper we have not attempted to estimate the scale of the associated errors as this would require the implementation of more complex numerical techniques for solving the full electromagnetic wave equation. Nonetheless the TIRPS model has been shown by Rogers *et al.* [2009] to provide reasonable approximations to the observed channel scattering functions even at high $C_k L$ values.

4. Coherence Time and Coherence Bandwidth and S_4 Measurement and Simulation

[10] Following Cannon *et al.* [2006] and Cannon and Bradley [2003], we have chosen to define the

Table 2. Regression Equations for Various Ranges of v_{eff} for CT at 158 and 422 MHz^a

Frequency (MHz)	v_{eff} Range (m s ⁻¹)	Regression Equation for CT (s)	CT Regression Value at $S_4 = 1.0$ (s)
158	200–600	$1.70 \exp(-1.46 S_4)$	0.39
158	1400–1630	$0.74 \exp(-1.19 S_4)$	0.23
422	200–600	$2.19 \exp(-0.83 S_4)$	0.95
422	1400–1630	$1.55 \exp(-1.17 S_4)$	0.48

^a S_4 is the two-way S_4 at 422 MHz. The regression equations are evaluated for $S_4 = 1$.

coherency time (CT) and coherency bandwidth (CB) as follows:

$$CT = \frac{1}{\Delta B} \quad (2)$$

$$CB = \frac{1}{2\pi\Delta T} \quad (3)$$

where ΔB is the Doppler spread and ΔT is the delay spread, both of which are determined from the CSFs. Doppler spreads are calculated for the central 68.3% of the total power in the CSF (integrated across all delay samples) as this represents the root-mean-squared spread for a Normal power distribution, equivalent to -2.2 dB from the peak. The spread is calculated as the difference between the $50 + (68.3/2)$ percentiles of two cumulative distributions, one summed in the positive delay direction and the other in the negative delay direction. To avoid integrating noise in the measured CSFs, only those points within 6 dB of the peak were used in the power summation. Delay spreads were calculated in a similar manner. The S_4 index (the ratio of the standard deviation of signal intensity to its mean) was calculated over 10s periods (i.e., the central time of the CSF ± 5 s). This period is somewhat shorter than is conventional for GPS satellite measurements and represents a compromise between averaging over many Fresnel zones and minimizing the spatial blurring which is inevitable for a fast moving LEO satellite.

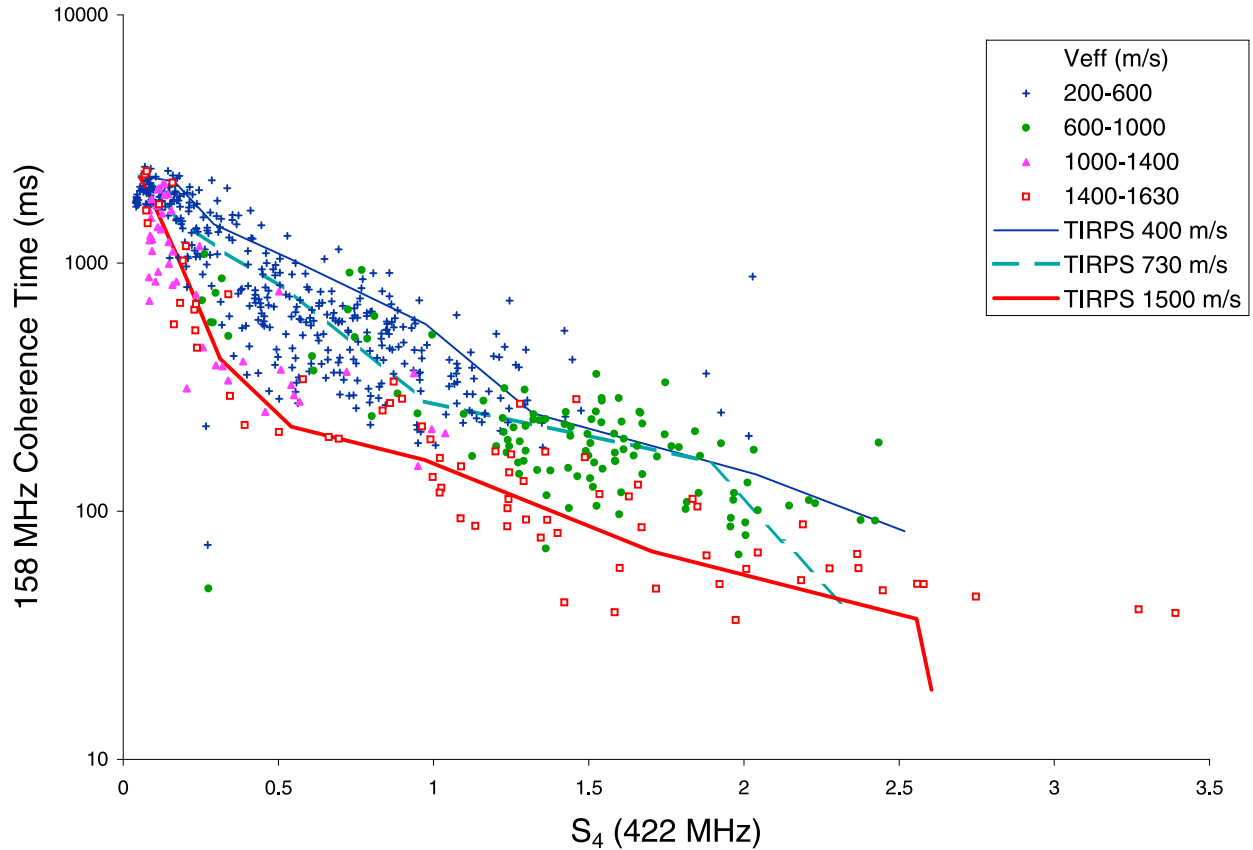


Figure 2. CT measurements for 158 MHz CSFs as a function of the 422 MHz S_4 index. Points represent measured CSF and are categorized by ranges of v_{eff} . Mean simulated values are shown for three values of v_{eff} . The phase screen spectrum (equation (1)) used $p = 3$ and $L_o = 10$ km.

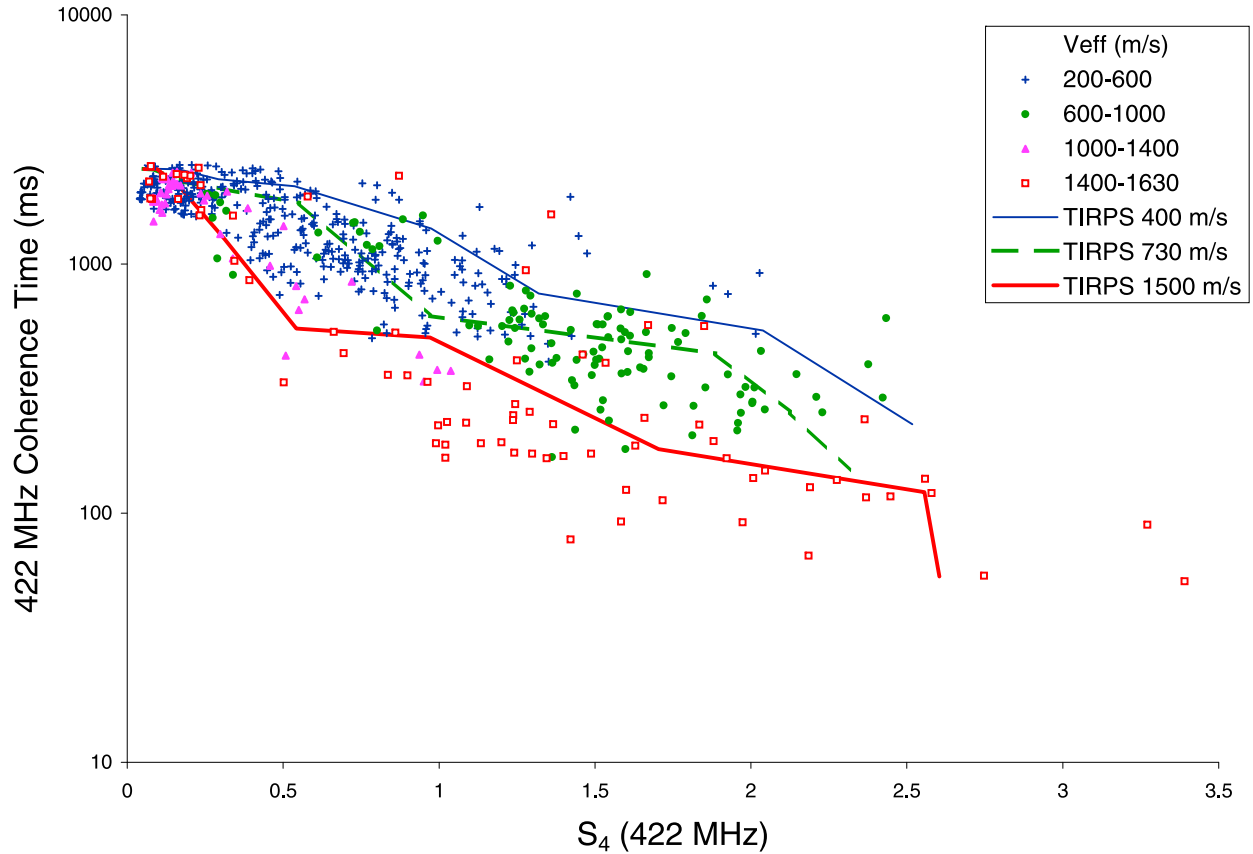


Figure 3. CT measurements for 422 MHz CSFs as a function of the 422 MHz S_4 index. Points represent measured CSF and are categorized by ranges of v_{eff} . Mean simulated values are shown for three values of v_{eff} . The phase screen spectrum (equation (1)) used $p = 3$ and $L_o = 10$ km.

[11] Figure 1 presents a log linear scatterplot of CT for 158 MHz CSFs against the 422 MHz S_4 index. Taking all measurements together, there is a close to exponential decline in CT with S_4 . The log linear regressions (gray dashed line in Figure 1 for 158 MHz) are represented by the equations:

$$CT_{(158 \text{ MHz})} = 1.46 \exp(-1.40 S_4(422 \text{ MHz}))(s) \quad (4)$$

$$CT_{(422 \text{ MHz})} = 2.31 \exp(-1.10 S_4(422 \text{ MHz}))(s) \quad (5)$$

Each point in Figure 1 has also been categorized into one of four ranges of the effective scan velocity, v_{eff} [Rino, 1979]. (Note that v_{eff} was generally much lower than the ionospheric penetration point (IPP) horizontal scan speed since each pass was aligned close to the magnetic meridian (i.e., along the irregularities).) It is clear that the data are well ordered by v_{eff} with a very useful reduction in spread. The corresponding log linear regression equations

are shown in Table 2 for two v_{eff} ranges in the two frequency bands. Table 2 indicates, very broadly, that at both frequencies, a threefold to fourfold increase in v_{eff} results in a twofold increase in CT at $S_4 = 1.0$.

[12] The solid lines in Figure 1 represent mean values obtained from 10 random realizations of the TIRPS model, each line representing a different fixed value of spectral index, p . Each point on the line is connected in order of increasing $\log_{10}(G.C_k L \sec(\theta))$ from 32 to 36 in increments of 0.5, resulting in generally increasing S_4 . A v_{eff} of 730 m s^{-1} (the mean of all v_{eff} values), an outer scale of 10 km and a midrange elevation of 30° are assumed. Choosing $p = 3$ provides a good match to the composite exponential fit, with a similarly good fit observed in the 422 MHz data (dashed line in Figure 3).

[13] Figure 2 reproduces the same ALTAIR measurements of CT but the superposed lines describe TIRPS simulations with fixed $p = 3$ and varying v_{eff} . As previously described, measurements with greater v_{eff} have lower CT values and this trend is reproduced in the

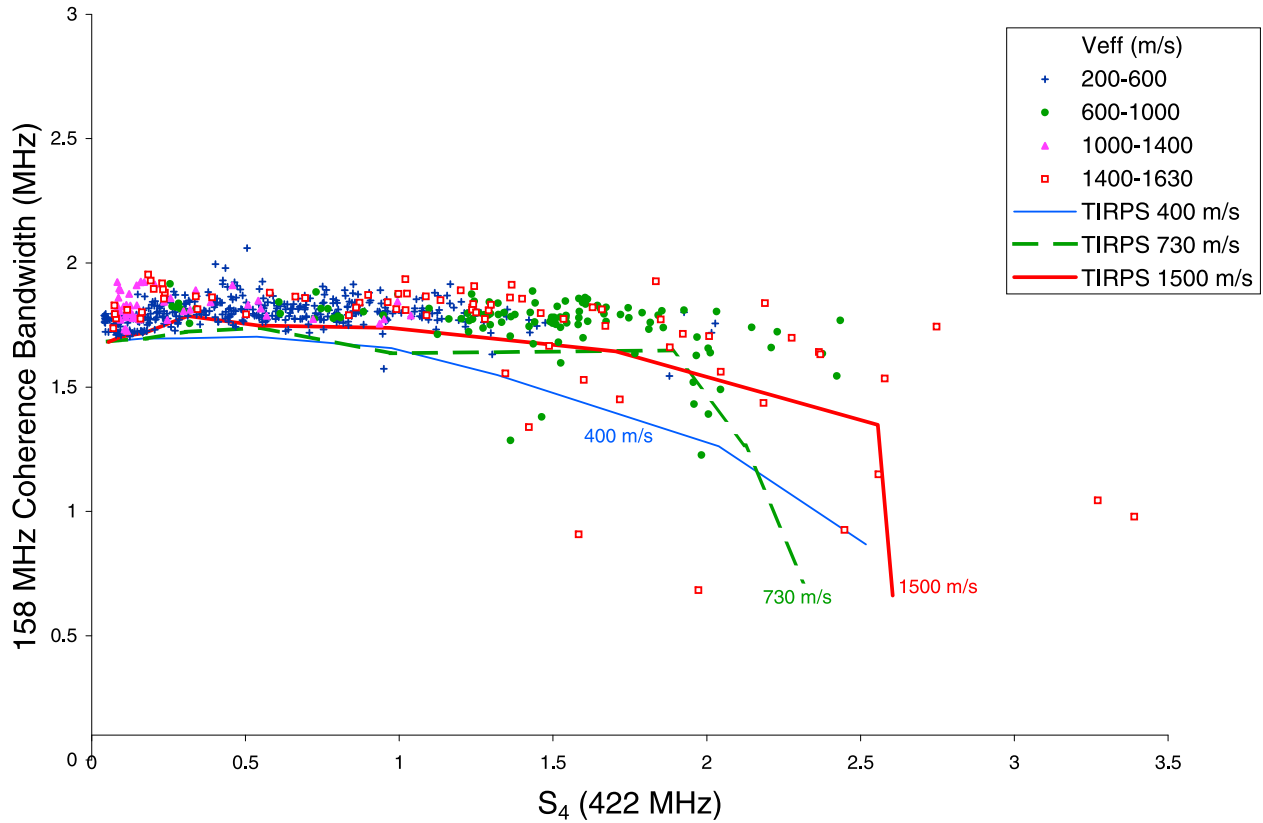


Figure 4. CB measurements for 158 MHz CSFs as a function of the 422 MHz S_4 index. Points represent measured CSF and are categorized by ranges of v_{eff} . Mean simulated values are shown for three values of v_{eff} . The phase screen spectrum (equation (1)) used $p = 3$ and $L_o = 10$ km.

simulations. For example, the lower red line ($v_{eff} = 1500 \text{ m s}^{-1}$) in Figure 2 provides a good fit to measurements in the category $v_{eff} = 1400\text{--}1630 \text{ m s}^{-1}$ (red squares) and similarly the other simulated TIRPS predictions pass through the appropriate range of ALTAIR measurements (though perhaps less well for the lowest v_{eff} range). It is apparent that the inclusion of v_{eff} is a necessary prerequisite of any modeling procedure of the coherency time; without it, CT predictions may be in error by factors of between 2 and 3.

[14] Similar good agreements are observed between the 422 MHz simulations and measurements (Figure 3), although the 422 MHz coherence times were upper limited by the CSF measurement period (~ 3.6 s) for $S_4 < 0.5$. (A similar limitation is evident in the 158 MHz graphs but only for the lowest $S_4 < \sim 0.2$.)

[15] Coherence bandwidths (CB) are presented in Figure 4 for the 158 MHz measurements (points) and for the TIRPS simulations parameterized as in Figure 2. These measurements are upper limited due to the insufficient bandwidth of the radar waveform, and only in the 158 MHz data and above $S_4 = 1.3$ did the CB drop

significantly below this system-imposed limit. The TIRPS model (solid lines in Figure 4) reproduces this behavior reasonably well, at least for higher values of the v_{eff} parameter. The CB for the 422 MHz signals (not shown) fell below the system bandwidth on only three occasions.

[16] It should be noted from observations and simulations of the CSF presented by *Rogers et al.* [2009] that the delay spread of the waveform under strong turbulence conditions is most evident at intensities below the -6 dB noise threshold used in this analysis. While these components would contribute little to the overall coherence bandwidth, in a radar system their presence may raise the clutter background, reducing the probability of detecting smaller secondary targets in the vicinity of the primary target.

5. Radio Frequency Dependencies of S_4 and Coherence Time

5.1. S_4 Index

[17] The results above, relate CT (and to some extent CB) to S_4 at just two spot frequencies. To generalize the

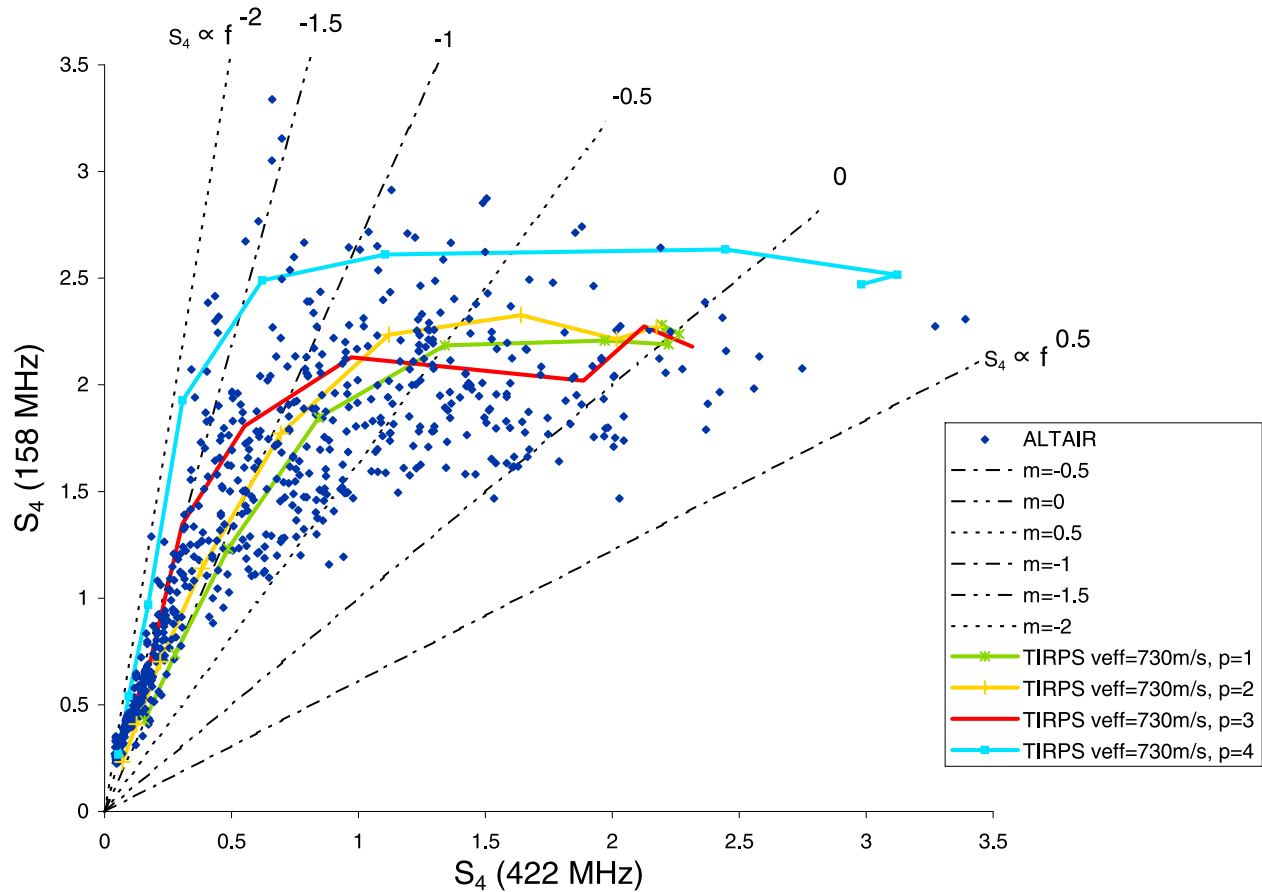


Figure 5. S_4 (158 MHz) versus S_4 (422 MHz) as measured from the ALTAIR radar (points) for 10-s periods coinciding with CSF measurements. Superposed solid lines represent the mean (± 1 standard deviation) of 10 TIRPS simulations at $\log_{10}(G.C_k L.\sec(\theta))$ values ranging from 32 to 36 and for four values of the spectral index p . Dashed diagonal lines indicate spectral indices of S_4 .

results to other frequencies it is necessary to examine the variation of CT and S_4 with frequency. Published observations show that, in the case of low scintillation ($S_4(\text{one-way}) < 0.5$) the S_4 index follows an approximately log-log linear relation to the radio frequency f , i.e., $S_4 \propto f^{-m_{S_4}}$, where m_{S_4} denotes the spectral index for S_4 which varies between 1.6 for low S_4 and 0.8 for high S_4 on one-way paths [Davies, 1990, p. 290, and references therein].

[18] In Figure 5 the S_4 values for 158 MHz signals are plotted against S_4 on the simultaneously recorded 422 MHz signals. Diagonals on this plot indicate the value of $-m_{S_4}$. The same data have been replotted in Figure 6 which presents m_{S_4} as a function of the two-way 422 MHz S_4 index. At low S_4 the points follow the diagonal for $m_{S_4} = 1.5 \pm 0.5$, while at higher S_4 the spectral index reduces. A linear regression to the measurements (dashed gray line) in Figure 6 suggests a two-way

S_4 spectral index of $m_{S_4} = 1.53 - 0.80 S_4(\text{2-way, 422 MHz})$ although the points are widely distributed about this line and the linear fit is poor above $S_4(\text{2-way, 422 MHz}) = 2$ where the 422 MHz waveform exhibits greater S_4 than the 158 MHz waveform (i.e., $m_{S_4} < 0$).

[19] The TIRPS model was also used to determine the spectral index of S_4 as a function of S_4 at the band center frequency. The solid line in Figure 6 represents these TIRPS simulated values (mean \pm one standard deviation of 10 simulations) at each value of $C_k L$ with $p = 3$ and $L_o = 10$ km and $v_{\text{eff}} = 730$ m s $^{-1}$. The simulated m_{S_4} closely follow the linear trend observed in the measurements, reducing from approximately 1.5 at $S_4 = 0$ to zero at $S_4 = 2.0$. The slope of this line is slightly less negative above $S_4 = 2$, as is also observed in the measurements.

[20] The solid lines in Figure 5 describe the TIRPS S_4 values, where each line represents a different value of p . The simulated S_4 index increased with increasing $C_k L$

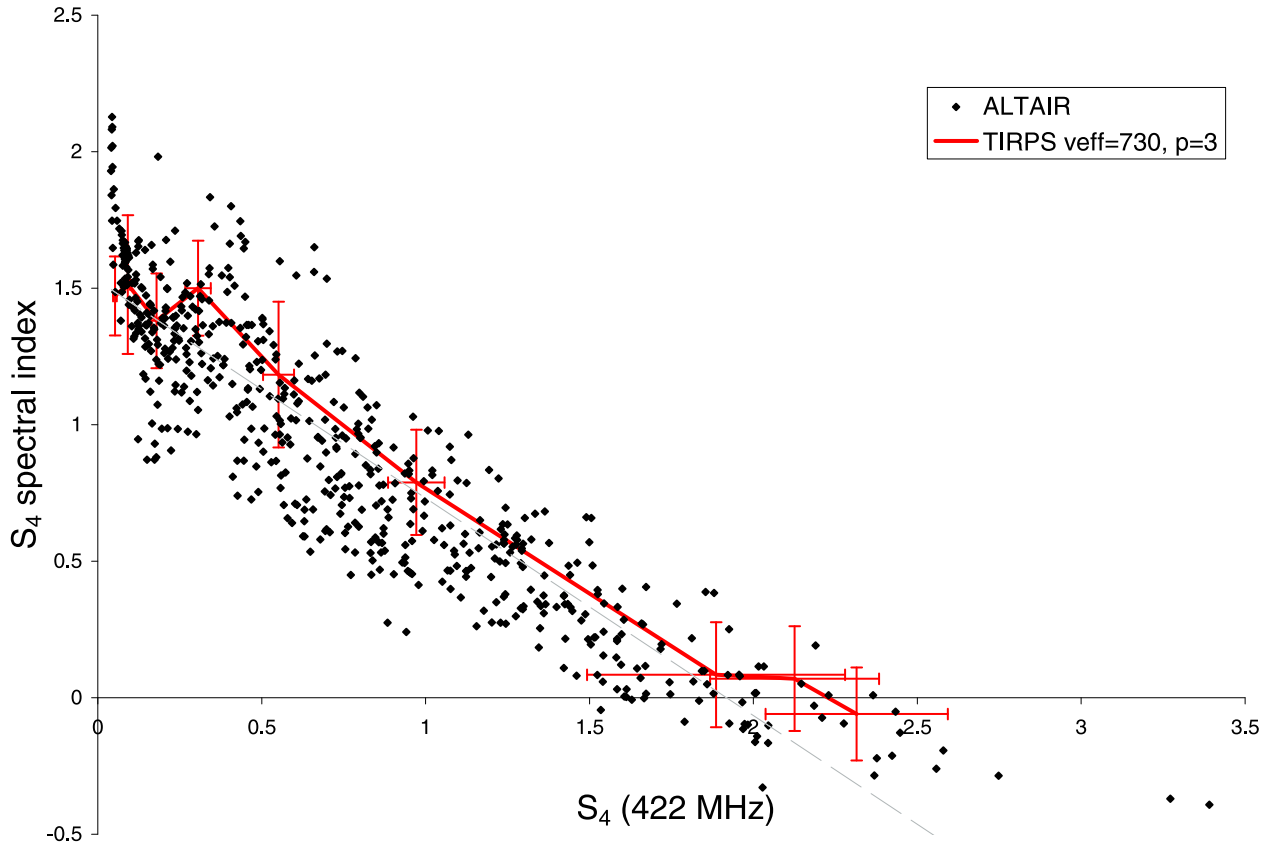


Figure 6. Spectral index of S_4 as a function of the 422 MHz S_4 index. Dots represent calculations from ALTAIR measurements of the 2826 satellite. The solid line represents the mean (± 1 standard deviation) of 10 TIRPS simulations at $\log_{10}(G \cdot C_k L \cdot \sec(\theta))$ values ranging from 32 to 36, with $p = 3$, $v_{eff} = 730 \text{ m s}^{-1}$, and $L_o = 10 \text{ km}$. The gray dashed line shows the linear regression to the ALTAIR measurements.

but saturated close to 2.2 for a spectral index $p \leq 3$, while higher values of S_4 are realizable for $p > 3$. Fremouw and Ishimaru [1992] showed that a limit of $S_4 = 2.2 (= \sqrt{5})$ would be expected for a Rayleigh fading signal on perfectly correlated up and down paths. S_4 greater than 2.2 is possible under conditions of strong focusing which can only be reproduced in highly anisotropic media using spectra with $p > 3$ [Rino, 1980]. The theoretical maximum S_4 is $3.3 (= \sqrt{11})$ for Nakagami- m fading [Nakagami, 1960] on perfectly correlated up and down paths [Fremouw and Ishimaru, 1992] and in the ALTAIR data set only one point exceeded this value (maximum S_4 (422 MHz) = 3.4).

5.2. Coherence Time

[21] Coherence times for the 158 MHz signals are plotted against those recorded simultaneously at 422 MHz in Figure 7. Diagonals in Figure 7 indicate the spectral index assuming a power law relationship with frequency.

The same data are presented in Figure 8 which shows the spectral index of CT as a function of the S_4 index at 422 MHz. Below $S_4 \sim 0.5$ the results are artificially influenced by the finite sample duration (as discussed in section 4) and may be ignored. At higher S_4 there is a wide distribution in the spectral index from 0 to -2 , centered about ~ -0.9 (indicated by the 30-point moving average (gray line in Figure 8)). The spread of the distribution narrows toward higher S_4 (see Figure 8) and lower CT (see Figure 7). These results compare well with a coherence time spectral index of -1 which was predicted from the analytical model of Knepp [1983b], who assumed a Gaussian mutual coherence function and a κ^{-4} spectrum of three-dimensional electron density (equivalent to a phase spectral index, p of 3).

[22] The red solid lines in Figures 7 and 8 represent the ensemble average predictions from the TIRPS model using a spectral index $p = 3$ and a mean effective velocity

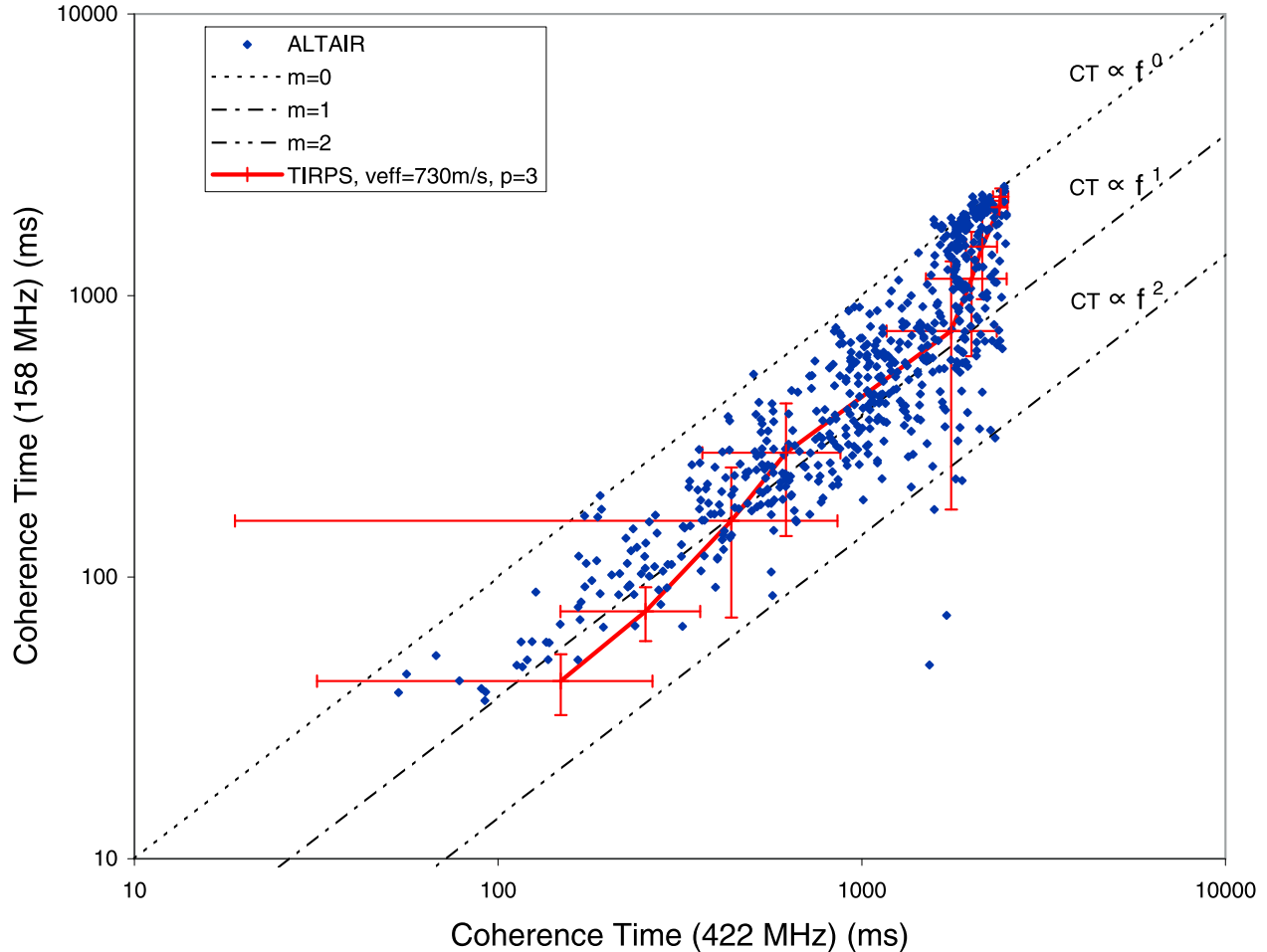


Figure 7. Coherence times of CSFs (points) measured by ALTAIR at 158 MHz plotted against those simultaneously measured at 422 MHz. The solid red line represents TIRPS simulation (mean \pm standard deviation of 10 runs) using $v_{eff} = 730 \text{ m s}^{-1}$, $p = 3$, and $L_o = 10 \text{ km}$.

$v_{eff} = 730 \text{ m s}^{-1}$. Once again the TIRPS model faithfully reproduces the experimental results.

6. Summary and Conclusions

[23] The Wideband Ionospheric Distortion Experiment (WIDE) using the ALTAIR radar sought to measure the equatorial transionospheric propagation channel under a wide variety of ionospheric conditions and to relate those measurements to the design of wideband radio systems, especially space-based wideband synthetic aperture radars. However, from an early stage it was recognized that a dual approach of measurement and modeling was required to best achieve these aims. This led to the implementation of the Trans-Ionospheric Radio Propagation Simulator (TIRPS). By making measurements and

refining this model we have been able to better understand the impact that the ionosphere has on the operation of such sophisticated systems. So far all of our data collects have occurred during the years of sunspot minimum and our experiment lacks the bandwidth to fully elucidate the issue of coherency bandwidth. As we move toward sunspot maximum, the coherency bandwidths and times are likely to reduce and this should mitigate this limitation.

[24] In the work of *Cannon et al.* [2006] we described the WIDE experiment, our first results and provided examples of channel scattering functions and estimates of the coherency bandwidths and times. In the work of *Rogers et al.* [2009], a companion to this paper, we describe the TIRPS model in some detail and undertake some detailed cross comparisons between the measure-

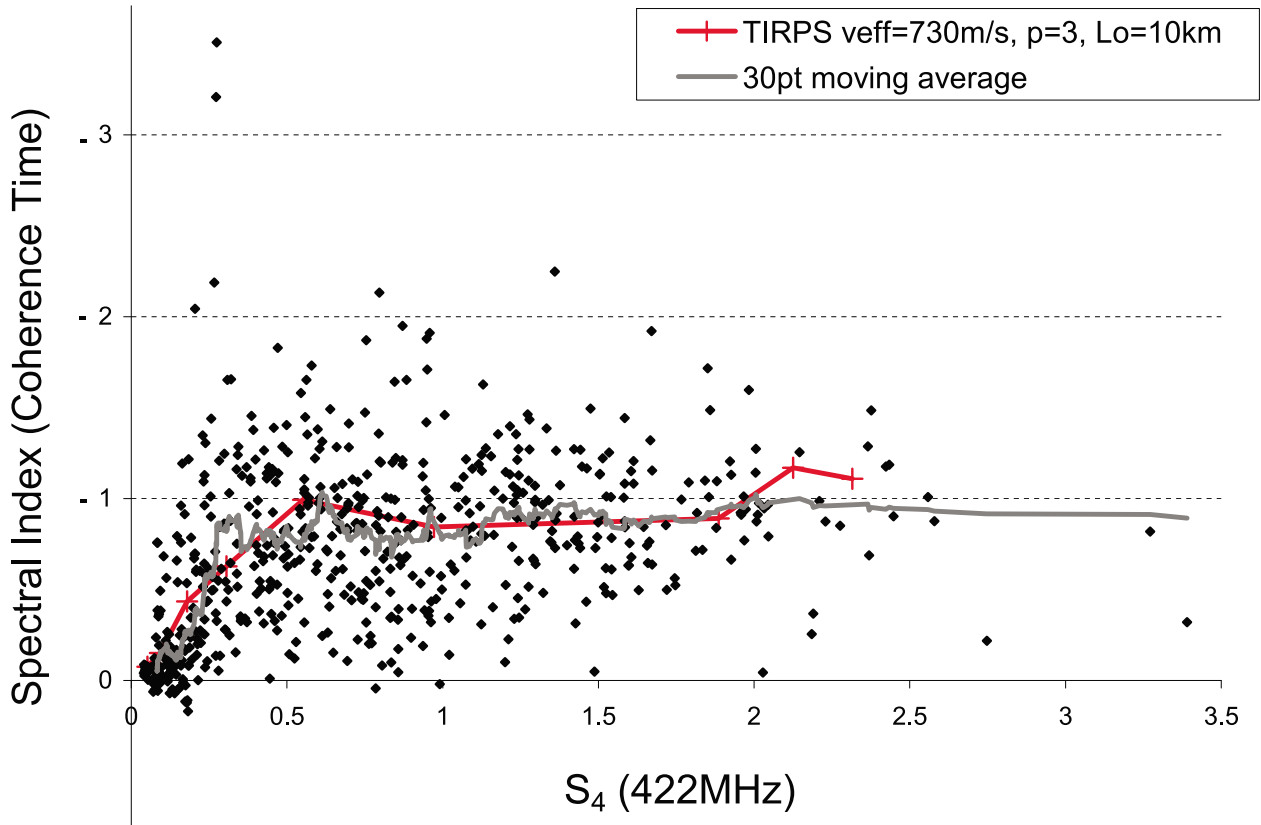


Figure 8. Spectral index of Doppler spread as a function of the 422 MHz S_4 index. The gray line represents a 30-point moving average. The red line indicates TIRPS simulation averages (of 10 runs) using $v_{eff} = 730 \text{ m s}^{-1}$, $p = 3$, and $L_o = 10 \text{ km}$.

ments and the model, thereby providing credence to that model.

[25] In this paper we have extended that cross comparison to look in more detail at the issue of coherency bandwidth and times, for a wide range of conditions from weak scintillation to strong scintillation, under conditions of strong focusing. We have demonstrated a high degree of correlation between the model and the measurements and have demonstrated that the model is able to characterize the CT of the equatorial ionosphere on wideband systems, operating in the frequency range 150 to 450 MHz. While our CB intercomparison is broadly in agreement, the lack of measurement bandwidth means that we are unable to fully validate this aspect of our model.

[26] We have also recognized the need to have a practical strategy for running such a model and we have demonstrated that rather than using the integrated strength of turbulence parameter $C_k L$, we are able to use the common S_4 parameter and produce meaningful results. We note however, that we have demonstrated good correlation between our model and measurements

when using the 422 MHz S_4 derived from our two-way measurements. It remains to be seen if this can be extended to using S_4 from other sensors, particularly from GPS receivers.

[27] Our results may be summarized as follows:

[28] 1. The measured CT decreased exponentially with S_4 (422 MHz) up to the Rayleigh limit of $S_4 = 2.2$. The CT decreased below 100 ms at the highest S_4 (>1.5) and highest v_{eff} .

[29] 2. The TIRPS simulations best matched this trend using a phase screen with $p = 3$. A higher spectral gradient ($p = 4$) was required to simulate the CT for $S_4 > 2.2$, (strong focusing conditions).

[30] 3. There was a decrease in CT for higher values of effective scan velocity (v_{eff}) and the simulations provided a good fit to the CT trend with S_4 when an appropriate value of v_{eff} was used in the simulation.

[31] 4. The coherence bandwidth (CB) was generally limited by the radar chirp bandwidth except for a small number of 158 MHz CSFs above an $S_4(422 \text{ MHz})$ of 1.3, where the CB reduced to as little as 0.7 MHz. This

behavior is again broadly reproduced in the TIRPS simulations (but see comments above).

[32] 5. To extend these results to other radio frequencies we presented the frequency dependences of CT and S_4 and their variation with S_4 at the higher frequency.

[33] 6. The spectral indices of the CT measurements vary widely about a mean of about -0.9 , and this is reproduced by the TIRPS model.

[34] 7. The spectral index of the S_4 measurements decreases linearly with increasing S_4 (422 MHz), ranging between around 1.5 at low S_4 to -0.3 at the highest S_4 . The TIRPS simulations closely follow this trend, for $p = 3$ and with an appropriate v_{eff} and elevation.

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