#### 1 Abstract

2

The double burden of malnutrition (DBM) in the same individual is a neglected public health 3 concern, especially in low- and middle-income countries (LMICs). The DBM is associated 4 with increased risks of non-communicable diseases, childbirth complications, and healthcare 5 costs related to obesity in adulthood. However, evaluating low prevalence outcomes in 6 relatively small populations is challenging using conventional frequentist statistics. Our 7 study used Bayesian latent models to estimate DBM prevalence at the individual-level in 8 small populations located in remote towns and rural communities in the Brazilian Amazon. 9 We employed a cross-sectional survey of urban and rural children aged 6-59 months, 10 considering DBM as the coexistence of stunting and overweight in the same individual. We 11 evaluated four river-dependent municipalities, sampling children in randomly selected 12 households in each town and a total of 60 riverine forest-proximate communities. Through 13 Bayesian modeling we estimated the latent double burden of malnutrition (LDBM) and 14 credible intervals (CI). The exceedance probability of LDBM was used to quantify this form 15 of malnutrition at the population level. Rural prevalence of LDBM was significantly higher 16 in Jutai (3.3%; CI: 1.5% to 6.7%) compared to Maues and Caapiranga. The likelihood that 17 LDBM rural prevalence exceeded 1% was very high in Jutai (99.7%), and Ipixuna (63.2%), 18 and very low (<2%) in rural communities elsewhere. Exceedance probabilities (at 1%) also 19 varied widely among urban sub-populations, from 6.7% in Maues to 41.2% in Caapiranga. 20 The exceedance probability of LDBM prevalence being above 3.0% was high in rural Jutai 21 (59.7%). Our results have important implications for assessing DBM in vulnerable and 22 marginalized populations, where health and nutritional status are often poorest, and public 23 health efforts remain focused on undernutrition. Our analytical approach could enable more 24 accurate estimation of low prevalence health outcomes, and strengthen DBM monitoring of 25 hard-to-reach populations. 26

27

28

**Keywords:** child malnutrition; health transition; Latin America; Bayesian; epidemiological methods; hard to reach areas

30 Introduction 31

The co-occurrence of undernutrition and overweight is known as the double burden of malnutrition (DBM), an emerging health concern which is characterized by a rapid increase in the prevalence of overweight individuals and slow reduction in rates of undernutrition (1,2), particularly in low- and middle-income countries (LMICs) (3–7). DBM is shaped by changing diets and physical activity patterns, and is associated with increased risks of noncommunicable diseases, childbirth complications, and elevated health costs related to obesity in adulthood (8,9).

39

40 DBM can be assessed at the level of population (e.g. country, sub-national region or rural community), household, and individual. Around nine-in-ten studies have estimated DBM 41 prevalence at the community/population level (1,7,10), largely because this aggregation 42 facilitates straightforward comparison among different populations. Estimating the 43 prevalence of stunting and overweight DBM at the individual level in remote towns and rural 44 communities can be challenging in LMICS, where child health surveys tend to have limited 45 coverage and sampling biased towards larger cities, often excluding vulnerable populations 46 47 such as indigenous people and other traditional rural populations (11). Reliable prevalence estimates are also difficult when studies have relatively small, statistically underpowered 48 sample sizes (12, 13). Nonetheless, reliable estimates of malnutrition are essential for 49 assessing the scale of nutritional problems in specific contexts, and guiding related 50 51 interventions by state and non-state institutions (14).

52

In preschool children, estimates of stunting and overweight DBM prevalence at the individual level are low (typically below 3%), and are mostly based on samples from country-scale or sub-national regional scales (5, 7), in which severe spatial and social inequities in health determinants become homogenized. A lack of stunting and overweight DBM research for specific geographies (including separating rural and urban sub-populations) and vulnerable populations (e.g. traditional forest-dwelling peoples in Amazonia and elsewhere) contributes to poor understanding of this health problem in LMICs (5, 15, 16).

60

61 Nutritional epidemiological studies typically characterize malnutrition based on observed

anthropometric values (e.g. height-for-age z-scores) which fall above or below predefined 62 63 cutoff points (e.g. 2 standard deviations below the reference population's median value). Interpreting prognostic risk is problematic for values near thresholds, near marginal values, 64 and for ethnic minorities (17, 18). Given generally low prevalence of DBM at the individual 65 66 level when using thresholds recommended by the World Health Organization (WHO), some authors adopt alternative definitions (e.g. Sagastume et al. (7) identified 17 DBM typologies) 67 or even alternative thresholds, mainly for the overweight indicator (19, 20), hindering 68 69 comparison across studies. Furthermore, for research into specific populations and/or with 70 relatively small sample sizes, point estimates and interval estimates based on frequentist statistics can be inappropriate due to the likelihood of Type 2 error (false negatives, leading 71 72 to under-estimation of DBM) and unfeasible for low prevalence nutritional outcomes.

73

Overcoming the challenges in estimating low prevalence nutritional outcomes in specific 74 75 populations with restricted sample sizes is necessary for effectively monitoring DBM in 76 LMICs, including robustly evaluating potential interventions for vulnerable populations. In this study, we will use the latent risk of double burden of malnutrition (LDBM) to estimate 77 the magnitude of a low prevalence outcome. In doing so, we attempt to overcome the 78 79 limitations of conventional frequentist approaches for estimating DBM prevalence, particularly for relatively small populations (where the health and nutrition indexes are often 80 poorest (21-24), or situations in which obtaining anthropometric measurements from 81 thousands of individuals is not practical. 82

83

Here, we define LDBM as the probability of stunting and overweight co-occurring. We use 84 'latent' to describe the risk or probability of stunting and overweight occurrence because we 85 do not directly observe and calculate this value, due to unknown population parameters  $\theta$ . 86 87 The population parameters capture important characteristics associated with the outcome, such as mean, variance, and correlation. However, this probability can be estimated through 88 the joint modeling of the two nutritional outcomes of interest, and the associated uncertainty 89 can be quantified by generalizing the uncertainty arising from  $\theta$ , a task well-suited to 90 91 Bayesian inference. The LDBM definition allows estimation even with few observed cases 92 of DBM, since this probability can be extracted from the properties of the joint density rather than a proportion of observed cases. Hence, we consider a bivariate vector  $Y = (Y^{(1)}, Y^{(2)})$ 93

consisting of two variables related to health outcomes,  $Y^{(1)}$  and  $Y^{(2)}$  (e.g., height/length-forage index and body mass index), characterized by a joint density function  $F_{\theta}(y)$  that depends on population parameters  $\theta$ . Given  $\theta$ , LDBM is defined as  $Pr(Y^{(1)} < t_1, Y^{(2)} > t_2 / \theta)$ .

98

Specifically, this paper draws on a unique dataset of rural and urban children in four remote,
 river-dependent municipalities in the Brazilian Amazon to examine whether latent Bayesian
 models may enable researchers to estimate DBM with modest sample sizes. We estimate
 LDBM as the probability of encountering two kinds of malnutrition (stunting and
 overweight) in the same individual child, selected randomly from towns and rural
 communities.

- 105
- 106

# 107

# Study design

Methods

108 We conducted a cross-sectional, population-based study in 2015 and 2016 in four municipalities (Caapiranga, Ipixuna, Jutai, Maues; each composed of an urban centre of the 109 same name, and a surrounding rural area) in Amazonas State, Brazil (Figure 1). The selected 110 municipalities were all highly river-dependent and their urban centres have relatively high 111 112 social vulnerability (e.g. high income poverty and inequality, and deficiencies in terms of household access to tapped water and sanitation, educational continuity, and primary 113 healthcare) relative to urban centres that are road-connected and/or closer to major cities 114 within Amazonia's hierarchical urban network (25). The municipalities were all highly-115 forested with >90% of their original forest cover remaining, at the time. Within the study 116 'universe' of river-dependent municipalities, the four we selected were purposefully far from 117 each other, with varied remoteness from major cities. This remoteness shapes access to 118 119 markets, and public and private institutions (e.g. universities, hospitals). Travel distance by 120 boat from the state capital, Manaus, ranged from 162-km (Caapiranga), 342-km (Maues), 121 947-km (Jutai), to 2,566-km (Ipixuna). Maues was medium-sized (c.35,000 residents and the 122 other towns were small (<15,000 urban residents) (26).

123

124 In order to compare LDBM across rural and urban sub-populations, we sampled children 125 under-five-years-old in randomly selected households in each town (i.e. the urban centre of

126 that municipality) and 60 riverine forest communities, in total (Figure 1a-d) (27). Surveyed 127 households were selected in the context of a broader research project, investigating child 128 health (27) and household food insecurity (28). Consequently, sampling included some households in which there were no children under-five-years-old. In each town, 200 129 130 households were randomly sampled as part of the broader study. Accordingly, 200 urban locations were randomly generated within the boundaries of each town (i.e. 800 urban 131 132 households across the four towns). Urban sampling density was corrected for population 133 density based on census sector-level information from the official 2010 demographic census (25). Urban sampling points were generated using ArcGIS 10.3 along the streets (within 20 134 meters) and were restricted to the potentially habitable area (using satellite imagery and 135 136 openstreetmap.org). For each municipality, we intended to sample 80 rural households from 137 16 surrounding rural communities (five households per community, totaling 320 households from 64 communities) but the final sample was 311 households from 63 communities (27). 138 These communities were not randomly selected but instead chosen because they covered 139 140 diverse geographies, including: a gradient in travel distance from the nearest town (7-249 km); locations inside and outside of Sustainable Use Reserves; locations on the main Amazon 141 142 channel, and second- and third-order tributaries; flooded-forest (várzea) and non-floodplain (terra firme) contexts. 143

144

145 Within each community, we first worked with residents to develop a list of all inhabited households, and then from these we randomly selected five households, whom we invited to 146 participate in the study. In this paper, we only include data from those urban and rural 147 households with children under-five-years-old. All children aged six-to-59 months residing 148 149 in each household were considered eligible (i.e. we did not have an expected number of children in the planned household sample but instead sampled all eligible children within 150 sampled households). The sample for this paper comprises 422 households (all 151 152 georeferenced) and 585 children (Figure 1), predominantly urban (67.1% of households (n=283); 65.0% of sampled children (n=380; Table 1). Reflecting municipality-scale 153 demographic differences and greater household sampling effort in towns, the number of 154 sampled children was smallest in Caapiranga (urban = 65; rural = 35), and largest in Jutai 155 156 (urban = 131; rural = 74) (Table 1).

### 158 Data collection and key variables

159 We used a structured questionnaire which was piloted beforehand in another municipality (Autazes) in Amazonas State, with similar geographic characteristics to the four described 160 161 above. This paper draws on questions in the socio-demographic and child health sections of 162 the survey instrument. When possible, childbirth dates were obtained from official documents held by caregivers. The field research team spent one week training in 163 164 standardized anthropometric data-collection techniques in Manaus, prior to starting 165 fieldwork. In each municipality, half of the urban and rural sample was collected during a low-water dry season field campaign (3-4 weeks per campaign, between August-December 166 2015) and half during a high-water wet season campaign (March-July 2016). Each household 167 168 visit was carried out by a pair of experienced, trained interviewers. Each field campaign 169 included a team of six researchers (i.e. 3 pairs), four of whom were involved in all field campaigns. The other two team members switched halfway through, with further training 170 provided for the two new team members. All researchers were Brazilian, with Masters-level 171 172 education or above. All anthropometric data collection followed (29, 30) under supervision of the first author. Weight and length/height measurements were collected twice for the same 173 174 individual, and the average value was used in the analyses. The z-scores of the height-forage and the Body Mass Index BMI-for-age indicators were estimated from the growth curves 175 of the WHO (29). Height-for-age z-scores below -2 were considered indicative of stunting. 176 177 Z-scores above 2 for BMI-for-age were considered indicators of overweight individuals. 178 Height-for-age z-scores below -6 or above 6, and BMI-for-age z-scores below -5 or above 5 were considered implausible (29). To reiterate, we assessed DBM at the individual level, 179 180 defined by the co-occurrence of stunting and overweight (31), a conventional indicator to 181 estimate the child DBM at the individual level (32,33).

182

### 183 *Ethics*

Data collection was approved by the Brazilian Health Ethics Commission (*Comissão Nacional de Ética em Pesquisa do Conselho Nacional de Saúde*, Protocol 45383215.5.0000.0005) and BLANKED University's Research Ethics Committee (BLANKED). Anonymity, voluntary participation and other ethical considerations were ensured at all stages of the research.

190 *Code availability*191

Our analysis of the latent double burden of malnutrition was performed using the Julia programming language (34). All the code for our analysis, including data cleaning and processing, exploratory data analysis, modeling, and summarizing results, is available at https://erickchacon.gitlab.io/latent-double-burden.

Statistical Analysis

#### 198 Bayesian Model

The latent double burden of malnutrition (LDBM), which refers to the probability of encountering two malnutrition outcomes in the same person (in this case, child) randomly selected from a population, can be expressed by the following equation:

202

196

199

$$p = \Pr(Y^{(1)} < t_1, Y^{(2)} > t_2 / \theta), (1)$$

where the problem of malnutrition occurs if the height-for-age z-scores,  $Y^{(1)}$ , is lower than t<sub>1</sub> and the BMI-for-age,  $Y^{(2)}$ , is greater than  $t_2$ . The comparison direction and thresholds can be easily modified if using other health variables. We modelled LDBM in the four municipalities (i = 1,2,3,4), distinguishing between municipal samples from rural areas (j = 1) and urban centres (j = 2). It is assumed that the *k*-th pair of observations  $y_{ijk} = (y_{ijk}^{(1)}, y_{ijk}^{(2)})$  in region *j* of municipality *i* comes from a bivariate normal distribution:

209

210

$$Y_{ijk} \sim MVN(\mu_{ij}, \Sigma_{ij}).$$
 (2)

Here,  $\mu_{ij} = (\mu_{ij}^{(1)}, \mu_{ij}^{(2)})$  and  $\Sigma_{ij}$  are the mean vector and 2 × 2 covariance matrix for the health 211 outcome variables in region type *j* of municipality *i*. The covariance matrix is parametrized 212 with variances  $(\sigma_{ij}^{(1)})^2$  and  $(\sigma_{ij}^{(2)})^2$  on the diagonal, and the covariance  $\rho_{ij} \times \sigma_{ij}^{(1)} \times \sigma_{ij}^{(2)}$  on the 213 off-diagonal. Notice that  $\sigma_{ii}^{(1)}$  and  $\sigma_{ii}^{(2)}$  are the standard deviations of the nutrition indicator 214 variables in rural and rural areas of a municipality, and  $\rho$  represents the correlation between 215 these variables. It is assumed that the three parameters vary between different municipalities 216 due to differences in their determinants of health and nutrition Depending on the 217 application, other assumptions may be made, including the assumption of constant 218 correlation across municipalities. Therefore, these parameters need to be estimated in order 219 to then calculate the LDBM. 220

- 221

The formulation of our Bayesian model was completed by defining the prior distribution for 222 the parameters. We assumed flat uninformative priors for the mean parameters,  $\pi(\mu_{ij}^{(l)}) \propto 1$ 223 for l = 1,2. Furthermore, a uniform prior was defined for the correlation parameter,  $\rho_{ii} \sim$ 224 U(-1, 1), and log-flat priors were assumed for the standard deviation parameters, 225  $\pi\left(\log\left(\sigma_{ij}^{(l)}\right)\right) \propto 1$  for l = 1,2.

226

Bayesian inference is achieved by calculating the posterior distribution of the parameters, 227  $\pi(\mu_{ij}, \Sigma_{ij}/y_{ij1}, y_{ij2}, \dots, y_{ijn_{ij}})$ , or by obtaining samples from this distribution. We used the 228 Hamiltonian Monte Carlo (HMC) method to obtain samples  $\mu_{ij}^{[m]}$  and  $\Sigma_{ij}^{[m]}$  for  $m = 1, \dots, M$ , 229 where *M* represents the total number of stored samples. The Turing jl package in the Julia 230 programming language was used for this purpose (35).

231

#### 232 **Predicting LDBM**

The exceedance probability, used to quantify the magnitude of malnutrition at the population 233 234 level, was estimated using the posterior LDBM, which is the probability distribution of LDBM given the set of observed values in our sample. It is defined as 235

236

$$\pi\left(p_{ij} / y_{ij1}, \cdots, y_{ijn_{ij}}\right) = \int \pi\left(p_{ij,\mu_{ij},\Sigma_{ij}} / y_{ij1}, \cdots, y_{ijn_{ij}}\right) d\mu_{ij} d\Sigma_{ij}$$

237

 $\pi \left( p_{ij} / y_{ij1}, \cdots, y_{ijn_{ij}} \right) = \int \pi \left( \mu_{ij}, \Sigma_{ij} / y_{ij1}, \cdots, y_{ijn_{ij}} \right) \pi \left( p_{ij} / \mu_{ij}, \Sigma_{ij} \right) d\mu_{ij} \, d\Sigma_{ij}$  where the first 238 term of the integral is the posterior distribution of the parameters, and the second term is the 239 probability of LDBM, based on some observed values for the parameters. Samples from this 240 posterior distribution of LDBM in rural and urban regions *j* of municipality *i* are obtained 241 using samples  $\mu_{ii}^{[m]}$  and  $\sum_{ii}^{[m]}$  for  $m = 1, \dots, M$  from the posterior distribution and calculating:

242

$$p_{ij}^{[m]} = \Pr\left(Y_{ij}^{(1)} > t_1, \ Y_{ij}^{(2)} < t_2 \ / \ \mu_{ij}^{[m]}, \Sigma_{ij}^{[m]}\right). \tag{3}$$

This can be done using the properties of a bivariate normal distribution and can also be calculated when the outcomes are jointly above or below certain cutoff points. The resulting collection  $\left(p_{ij}^{[1]}, p_{ij}^{[2]}, \dots, p_{ij}^{[M]}\right)$  consisted of twenty thousand realizations from the posterior distribution of LDBM that can be used to provide point estimates and their respective credible intervals, as well as exceedance probabilities of the outcome under different circumstances (prevalences being 1%; 3% or correlation 0; see Results section).

250

### 251 Considering association between individuals

In the analysis of the double burden on children, some individuals may belong to the same 252 household, leading to potential associations due to shared exposure factors. To account for 253 254 this, we can extend the previously presented model by incorporating a bivariate householdlevel random effect,  $W_h$ . Let  $Y_{hk}$  represent the health outcomes of the k --th child in household 255 h, then the conditional distribution can be defined as  $Y_{hk} / W_h \sim MVN(\mu + W_h, \Sigma_{ij})$ , such as 256 257 children from the same household share the common random effect  $W_h$ . To ensure identifiability, we assume a zero-mean Gaussian distribution for the bivariate random effect, 258  $W_h \sim MVN(0, \Sigma_w)$ , with diagonal covariance matrix  $\Sigma_w$ . Note that if household dependency 259 exists only for one health outcome,  $W_h$  can be unidimensional. The resulting marginal 260 distribution of the bivariate health outcome is  $Y_{hk} \sim MVN(\mu, \Sigma_w + \Sigma)$ . Using this distribution, 261 the LDBM is computed as explained in the previous section (Equation 3). 262 263

#### 264 **Results**

We analyzed the LDBM in rural and urban areas of four municipalities. Given that some 265 children belonged to the same households (Table 1), we first assessed the need to account for 266 household-level dependency. Using likelihood ratio tests and comparing the Akaike 267 268 Information Criteria (AIC) for z-scores of height-for-age and BMI-for-age, we found no 269 significant improvement from adding random effects in most municipalities and area types 270 at a 10% significance level. However, significant improvements were observed for the urban sub-population in Jutai when including random effects for height-for-age and for the urban 271 272 sub-population in Ipixuna for BMI-for-age (Supplementary Table 1). Consequently, we applied the LDBM model with household-level random effects for height-for-age in urban 273 Jutai, for BMI-for-age in urban Ipixuna, and without random effects for all other sub-274

populations. Models with random effects were re-parametrized after inference to ensurecomparability with models without random effects.

277

The posterior distributions of the means for the stunting indicator were below zero for both 278 279 rural and urban sub-populations in all four municipalities (Figure 2), demonstrating an overall 280 chronic nutritional disadvantage for children in this study. For all municipalities, there was a 281 stronger rural tendency for stunted linear growth relative to urban sub-populations, in the 282 sense that the distributions from rural sub-populations had lower mean height-for-age Z-283 scores compared to urban sub-populations. The apparent 'urban advantage' was less pronounced in Caapiranga, seemingly due to lower rural stunting probability compared to 284 285 other rural sub-populations. For overweight, the posterior distributions of all rural and urban 286 sub-populations were substantially above zero (i.e. there was an overall tendency towards 287 higher BMI-for-age). There was a slightly greater tendency towards overweight among urban 288 sub-populations, apart from Jutai, where rural BMI-for-age z-scores were much higher than 289 for urban children.

290

291 Most of the posterior distributions of the standard deviations for the height-for-age z-scores 292 were above one among children in Ipixuna and Jutai, whereas the distributions of the standard 293 deviations for Caapiranga and Maues children were clustered around one (Figure 3). Hence, 294 variation in height-for-age was greater in the rural and urban sub-populations in Ipixuna and 295 Jutai, and lower in Caapiranga and Maues. Within municipalities, we did not find substantial 296 differences in stunting variability between rural and urban sub-populations. For overweight, 297 the variability was lower in rural areas and was right-skewed distributed (with almost all 298 variability ranging between 0.5 and 1.0 standard deviations), particularly in Caapiranga and 299 Maues. Variability in overweight varied markedly among children in the four urban sub-300 populations and was notably high, above one, in Caapiranga.

301

Urban children tended to have positively correlated height-for-age and BMI-for-age z-scores,
although this was less pronounced in urban Jutai (Figure 3). Rural patterns were more
heterogenous; there was a positive correlation in these indicators for rural Caapiranga and
Maues, whereas the correlations for rural children in Ipixuna and Jutai were mostly negative.
The direction of the correlation between the indicators is important for estimating the

307 prevalence of LDBM, as higher values will be observed when there is congruence between 308 the direction of the bivariate distribution and the quadrant of interest. Accordingly, the 309 exceedance probabilities and the estimated prevalence of LDBM were relatively high among rural children in Ipixuna and Jutai, compared to very low estimated prevalence for rural 310 311 children in Caapiranga and Maues (Supplementary Table 2). There was a clear negative correlation between height-for-age and BMI-for-age z-scores in the rural areas of Ipixuna 312 313 and Jutai, and a positive correlation in Caapiranga and Maues, regardless of whether the 314 children were rural or urban residents (Supplementary Figure 1).

315

316 The estimated prevalence of LDBM was highest in rural areas of Jutai (3.3%; CI: 1.5% to 317 6.7%) and Ipixuna (1.2%; CI: 0.3% to 3.8%), and the urban area of Caapiranga (0.9%; CI:0.3% to 2.4%), and lower in other rural and urban areas (Table 2; Figure 4). The likelihood 318 319 that LDBM prevalence exceeds 1.0% of children under-five-years-old was very high in rural 320 Jutai (exceedance probability of 99.7%), and rural Ipixuna (63.2%), and very low (<2%) for 321 the other two rural sub-populations. Exceedance probabilities also varied widely among 322 urban sub-populations, from 6.7% in Maues to 41.2% in Caapiranga. The exceedance 323 probability of LDBM prevalence being above 3.0% of children was high in rural Jutai 324 (59.7%), and below 6% for all other sub-populations (Table 2). Consequently, in Jutai the 325 prevalence of LDBM was significantly higher among rural children than among their urban 326 counterparts, whereas we did not find evidence of meaningful rural-urban differences (i.e. 327 because credible intervals overlapped) in other municipalities (Figure 4). The prevalence of LDBM was relatively similar across urban sub-populations, whereas rural prevalence varied 328 329 more, being significantly higher in Jutai than in Maues or Caapiranga (Figure 4).

330

#### 331 Discussion

This study is the first, to our knowledge, to estimate the DBM at the individual level among rural and urban children using Bayesian-inference latent modelling. Our approach was designed to improve latent prevalence estimates for low prevalence phenomena, such as DBM. We applied our novel analytical technique to a unique dataset of similar-aged children randomly sampled within remote, river-dependent municipalities in the Brazilian Amazon; an under-studied and historically marginalized population which is vulnerable to the effects of the climate crisis, and other shocks and stressors (36,37). 339

340 In our study, latent DBM (LDBM) at the individual level was at low prevalence (1.2% or 341 below) in the sampled sub-populations, apart from one (rural Jutai), at 3.3% (CI: 1.5% to 6.7%) of children. A meta-analysis using a frequentist approach to report individual-level 342 343 stunting and overweight DBM among children under-five-years-old found a mean prevalence of just 2.3% in low-income countries and 2.7% in middle-income countries (38). Tzioumis 344 345 et al. (38) used data from Demographic and Health Surveys in 36 countries, yet their study 346 populations may be more similar to ours than to that of the National Study of Food and Nutrition (ENANI) of nearly fifteen thousand Brazilian children (39). In Amazonas State 347 (with 62 municipalities) the ENANI sample included only 42 children from metropolitan 348 349 Manaus and a handful from two proximate road-connected municipalities. In Amazonas, the 350 coverage and implementation of universal healthcare (e.g. adequate prenatal care), food and nutrition policies (e.g. adequate school meals, municipal Food Security Councils), and social 351 352 protections (e.g. Maternity Pay) can be relatively weak outside of Manaus (25, 40, 41). Latent 353 modelling is well-suited for studies with restricted sample sizes, such as with hard-to-reach 354 or modest-sized focal populations.

355

356 Our latent models draw on observed variability in stunting and overweight indicators in 357 small-samples and demonstrate that DBM prevalence risks can be above zero for particular 358 sub-populations, even if no DBM cases are recorded based on frequentist classification. For 359 instance, in the rural sub-populations of Caapiranga and Maues (the less remote municipalities in this study), where the randomly sampled households had fewer children 360 under-five-years-old, there was a positive correlation between height-for-age Z-scores and 361 362 BMI-for-age Z-scores. For those sub-populations, there were zero cases of DBM using the frequentist approach yet the estimated prevalences of LDBM were different from zero. 363 Moreover, using our Bayesian approach it was possible to estimate credible intervals, 364 365 parameters such as mean, median, and exceedance probabilities In the two extremely remote 366 municipalities, Ipixuna and Jutai, the z-score correlation was reversed; short height-for-age rural children tended to be overweight, and rural LDBM prevalence was higher than in the 367 less-remote municipalities. This may reflect that healthcare access, sanitation coverage, 368 369 employment opportunities and income, state-led food and nutrition security interventions, 370 and other social determinants of health (42) are worse in more remote parts of Amazonia 371 (25).

372

373 Despite the wide credible intervals, we estimated higher point prevalence of LDBM in Jutai 374 and Ipixuna's rural areas compared to their urban centres, consistent with existing research 375 in LMICs and the well-established notion of 'urban advantage' in health and nutrition. 376 Tzioumis et al. (38) found lower prevalence of stunting and overweight coexistence among urban children (1.1%) compared to their rural counterparts (2.0%). In Brazil, DBM 377 378 prevalence at the individual level is estimated to be 1.0% among the general population of 379 children aged five-to-11-years-old (43). A survey of children under-five-years-old in Kenya 380 observed a higher occurrence of stunting and overweight in the rural zone in comparison to 381 urban zone for both sexes (44). The occurrence of individual-level stunting and overweight 382 DBM in children under-five-years-old in two districts in South Africa had a prevalence of 383 5.7%, with no significant difference between urban and rural areas (45).

384 We found evidence of an emerging malnutrition concern in rural Jutai, where the exceedance 385 probabilities of LDBM being above 1% and 3% of children were very high (99% and 60%, respectively). The geographical locations of the rural communities sampled in Jutai may 386 387 explain this sub-population's higher DBM prevalence. The town of Jutai and some of the surrounding rural communities we sampled are located on the banks of the Solimões River, 388 389 between the regional urban hubs of Tabatinga and Tefé. Towns on this stretch of river have 390 relatively good access to passenger-cargo boats (39), enabling surrounding rural 391 communities to access obesogenic food products (47-49), including ultra-processed foods. 392 Infant formula milk products may be reaching these communities through floating markets, 393 and competing with breastfeeding. This is problematic because breastfeeding is protective 394 against stunting and overweight (50, 51). This may partly explain the greater shift to the right in the overweight curve of children in rural Jutai, compared to other rural sub-populations. 395

Although we did not find evidence of significant differences between the credible intervals of LDBM prevalence across the four sampled urban areas, no null prevalences were generated, and the point estimate of LDBM in Caapiranga was slightly higher than in the other urban sub-populations. Furthermore, interval estimates indicate that this value could approach 2.3%, and the highest probability of this prevalence exceeding 1% in the urban area was in Caapiranga, at about 41%. We cannot fully explain the differences in the LDBM among towns. Nonetheless, potential explanations include the spatial proximity of
Caapiranga to the metropolis of Manaus (159 km travel distance), which could facilitate
access to ultra-processed products, usually high in fat, sugar, or sodium and associated with
overweight/obesity (43, 52–54). Other possibilities include the influence of socioeconomic
variables not evaluated in our study such as maternal education, family size, maternal height
and birth weight, child's diarrhea and household sanitation (55, 56).

408 Our results demonstrate that the precision of LDBM estimates may vary depending on sample 409 size, the variability of posterior distributions, and the congruence of these parameters with the probability that a given child's height-for-age Z-score and BMI-for-age Z-score are 410 simultaneously below -2 and greater than 2 standard deviations, respectively (upper-left 411 412 quadrants in the subplots of Supplementary Figure 2). The credible intervals for LDBM prevalence were relatively wide for two urban sub-populations (Caapiranga and Ipixuna), 413 which also had smaller sample sizes and asymmetric, right-shifted variation in the 414 415 malnutrition indicators compared to the other two urban sub-populations. Interestingly, 416 although more rural children were sampled in Ipixuna and Jutai than in Caapiranga and 417 Maues, credible intervals were much wider for the former two than the latter, possibly related 418 to the negative correlation pattern observed in both urban sub-populations, including a 419 substantial number of marginal values for DBM. Overall, our results show the limitations of 420 traditional frequentist approaches for assessing low-prevalence malnutrition outcomes in 421 relatively small samples. Restricted sample sizes are a common challenge for studies 422 involving specific, and geographically hard-to-reach population groups such as indigenous peoples and other traditional forest-dwelling peoples in Amazonia (23, 57, 58). Our findings 423 demonstrate that these challenges can be partially overcome through the application of 424 425 Bayesian latent models that account for marginal values rather than only considering observed cases for point prevalence estimates, and instead using credible intervals and 426 427 exceedance probabilities. Even using Bayesian latent models, however, further stratifying 428 our modestly-sized sample by age group (for example) would tend to increase the credible 429 intervals, limiting the interpretation of results.

Our study, combined with evidence from other LMICs, suggests that children from
marginalized populations – whether living in rural or urban areas – are susceptible to stunting
and overweight DBM (2, 4, 59). Poor dietary nutrition in terms of both quality and quantity
is one of the possible mechanisms for the co-occurrence of DBM (2). The replacement of

traditional dietary patterns with ultra-processed products, a phenomenon that has intensified
in LMICs like Brazil, may be a crucial factor for the increase in DBM (21, 23, 52, 54, 57). It
is no coincidence that national surveys point to socioeconomically vulnerable population
strata as the most susceptible to the rising trend in the consumption of ultra-processed foods
among Brazilians (60). Therefore, interventions aimed at mitigating DBM should consider
contextual determinants of diet (9, 23, 57, 61, 62).

440 Our study represents an advance by applying Bayesian latent models to compare different 441 contexts of DBM emergence at the individual level among children living in remote areas of Amazonia. Geographically specific studies into under-researched populations are important 442 because the literature on DBM is mainly limited to research assessing DBM in terms of co-443 444 occurrence at the community or household-level (7, 38). Furthermore, although certain 445 credible intervals of our estimates were relatively wide, possibly due to sample size, when compared with results from national surveys, we emphasize the need for analytical 446 447 approaches that allow for the assessment of low-occurrence outcomes in specific groups with 448 restricted population sizes. Aggregating population data at the national, state, or municipal 449 level may obscure health inequities and render invisible the health inequities experienced by 450 marginalized river-dwelling populations in remote parts of Amazonia.

451

452 Using Bayesian latent models may be useful for research or monitoring into other low-453 occurrence health or nutrition conditions at the population level, especially for initiatives 454 lacking the resources of national- or international-scale studies and related sample sizes. Nonetheless, we highlight some limitations with our study. Our Bayesian approach using 455 456 latent models hinders comparability with case-based frequentist analyses of observed 457 prevalence. Our approach also requires greater computational performance and more 458 specialist programming skills relative to conventional statistical analyses. Nevertheless, 459 Hossain et al.'s (63) study into DBM prevalence among reproductive-aged women found that 460 a Bayesian approach like ours obtained more precise parameter estimates and robust conclusions compared with a classical analytical technique (logistic regression) for 461 estimating the prevalence. However, the specificity of our studied population, while making 462 it impossible to select larger and more diversified rural samples, also limits the definition of 463 464 informative priors, which would facilitate more precise (narrower) credible intervals for 465 estimated prevalence (63).

466

## 467 Conclusion

Using latent Bayesian models, we assessed a malnutrition outcome of low prevalence (the 468 coexistence of stunting and overweight in the same individual children) in relatively small 469 470 sample sizes from remote towns and rural communities in Amazonia. Furthermore, we analyzed the latent risk of DBM in vulnerable and marginalized populations, where the health 471 and nutrition status are often poorest and the public health policies tend to focus strictly on 472 473 undernutrition. Our approach can help to obtain more accurate estimates of low prevalence outcomes, and support public health service provision for effectively monitoring DBM in 474 475 476 LMICs, particularly in vulnerable and hidden populations.

478

# References

United Nations Children's Fund (UNICEF), World Health Organization (WHO),
International Bank for Reconstruction and Development/The World Bank. Levels and trends
in child malnutrition: UNICEF/WHO /World Bank Group Joint Child Malnutrition
Estimates: Key findings of the 2023 edition. New York: UNICEF and WHO; 2023. CC BYNC-SA 3.0 IGO.

Popkin BM, Corvalan C, Grummer-Strawn LM. Dynamics of the double burden of
malnutrition and the changing nutrition reality. *The Lancet* 395: 65–74, 2020. doi:
10.1016/S0140-6736(19)32497-3.

487 3. Cut Novianti Rachmi, Mu Li, Louise Alison Baur. The double burden of
488 malnutrition in Association of South East Asian Nations (ASEAN) countries: a
489 comprehensive review of the literature. *Asia Pacific Journal of Clinical Nutrition* 27, 2018.
490 doi: 10.6133/apjcn.062018.02.

491 4. Nugent R, Levin C, Hale J, Hutchinson B. Economic effects of the double burden of
492 malnutrition. *The Lancet* 395: 156–164, 2020. doi: 10.1016/S0140-6736(19)32473-0.

Tzioumis E, Adair LS. Childhood Dual Burden of Under- and Overnutrition in
Low- and Middle-inCome Countries: A Critical Review. *Food Nutr Bull* 35: 230–243,
2014. doi: 10.1177/156482651403500210.

496 6. Lerm BR, Crochemore-Silva I, Costa JC, Victora CG. The double burden of
497 malnutrition in under-five children at national and individual levels: observed and expected
498 prevalence in ninety-three low- and middle-income countries. *Public Health Nutr* 24:
499 2944–2951, 2021. doi: 10.1017/S1368980020001226.

500 7. Sagastume D, Barrenechea-Pulache A, Ruiz-Alejos A, Polman K, Beňová L,
501 Ramírez-Zea M, Peñalvo JL. Quantifying Overlapping Forms of Malnutrition Across Latin
502 America: A Systematic Literature Review and Meta-Analysis of Prevalence Estimates.
503 Advances in Nutrition 15: 100212, 2024. doi: 10.1016/j.advnut.2024.100212.

Min J, Zhao Y, Slivka L, Wang Y. Double burden of diseases worldwide:
 coexistence of undernutrition and overnutrition-related non-communicable chronic
 diseases. *Obesity Reviews* 19: 49–61, 2018. doi: 10.1111/obr.12605.

9. Wells JC, Sawaya AL, Wibaek R, Mwangome M, Poullas MS, Yajnik CS, Demaio
A. The double burden of malnutrition: aetiological pathways and consequences for health. *The Lancet* 395: 75–88, 2020. doi: 10.1016/S0140-6736(19)32472-9.

510 10. Davis JN, Oaks BM, Engle-Stone R. The Double Burden of Malnutrition: A
511 Systematic Review of Operational Definitions. *Current Developments in Nutrition* 4:

512 nzaa127, 2020. doi: 10.1093/cdn/nzaa127.

513 11. Coimbra CE, Santos RV, Welch JR, Cardoso AM, De Souza MC, Garnelo L, Rassi
514 E, Follér M-L, Horta BL. The First National Survey of Indigenous People's Health and
515 Nutrition in Brazil: rationale, methodology, and overview of results. *BMC Public Health*516 13: 52, 2013. doi: 10.1186/1471-2458-13-52.

517 12. Case LD, Ambrosius WT. Power and Sample Size. In: *Topics in Biostatistics*, edited
518 by Ambrosius WT. Humana Press, p. 377–408.

Sondhi A, Segal B, Snider J, Humblet O, McCusker M. Bayesian additional
evidence for decision making under small sample uncertainty. *BMC Med Res Methodol* 21:
221, 2021. doi: 10.1186/s12874-021-01432-5.

522 14. Grellety E, Golden MH. Change in quality of malnutrition surveys between 1986
523 and 2015. *Emerg Themes Epidemiol* 15: 8, 2018. doi: 10.1186/s12982-018-0075-9.

Haddad L, Cameron L, Barnett I. The double burden of malnutrition in SE Asia and
the Pacific: priorities, policies and politics. *Health Policy Plan* 30: 1193–1206, 2015. doi:
10.1093/heapol/czu110.

Pradeilles R, Baye K, Holdsworth M. Addressing malnutrition in low- and middleincome countries with double-duty actions. *Proc Nutr Soc* 78: 388–397, 2019. doi:
10.1017/S0029665118002616.

17. Clemente APG, Santos CDDL, Martins VJB, Benedito-Silva AA, Albuquerque MP,
Sawaya AL. Mild stunting is associated with higher body fat: study of a low-income
population. *J Pediatr (Rio J)* 87: 138–144, 2011. doi: 10.2223/JPED.2071.

18. Caleyachetty R, Thomas GN, Kengne AP, Echouffo-Tcheugui JB, Schilsky S,
Khodabocus J, Uauy R. The double burden of malnutrition among adolescents: analysis of
data from the Global School-Based Student Health and Health Behavior in School-Aged
Children surveys in 57 low- and middle-income countries. *The American Journal of Clinical Nutrition* 108: 414–424, 2018. doi: 10.1093/ajcn/nqy105.

538 19. Engle-Stone R, Guo J, Ismaily S, Addo OY, Ahmed T, Oaks B, Suchdev PS,

Flores-Ayala R, Williams AM. Intraindividual double burden of overweight and
micronutrient deficiencies or anemia among preschool children. *The American Journal of*

541 *Clinical Nutrition* 112: 478S-487S, 2020. doi: 10.1093/ajcn/nqaa101.

542 20. Fongar A, Gödecke T, Qaim M. Various forms of double burden of malnutrition
543 problems exist in rural Kenya. *BMC Public Health* 19: 1543, 2019. doi: 10.1186/s12889544 019-7882-y.

Headey D, Stifel D, You L, Guo Z. Remoteness, urbanization, and child nutrition in
sub-Saharan Africa. *Agricultural Economics* 49: 765–775, 2018. doi: 10.1111/agec.12458.

547 548 549	22. Carignano Torres P, Morsello C, Orellana JDY, Almeida O, De Moraes A, Chacón- Montalván EA, Pinto MAT, Fink MGS, Freire MP, Parry L. Wildmeat consumption and child health in Amazonia. <i>Sci Rep</i> 12: 5213, 2022. doi: 10.1038/s41598-022-09260-3.
550 551 552 553	23. Moraes AODS, Magalhães EIDS, Orellana JDY, Gatica-Domínguez G, Neves PAR, Basta PC, Vaz JDS. Food profile of Yanomami indigenous children aged 6 to 59 months from the Brazilian Amazon, according to the degree of food processing: a cross-sectional study. <i>Public Health Nutr</i> 26: 208–218, 2023. doi: 10.1017/S1368980022001306.
554 555 556 557	24. Veile A, Christopher L, Azcorra H, Dickinson F, Kramer K, Varela-Silva I. Differences in nutritional status between rural and urban Yucatec Maya children: The importance of early life conditions. <i>American Journal of Biological Anthropology</i> 178: 205–222, 2022. doi: 10.1002/ajpa.24510.
558 559 560 561	25. Parry L, Davies G, Almeida O, Frausin G, De Moraés A, Rivero S, Filizola N, Torres P. Social Vulnerability to Climatic Shocks Is Shaped by Urban Accessibility. <i>Annals of the American Association of Geographers</i> 108: 125–143, 2018. doi: 10.1080/24694452.2017.1325726.
562 563	26. IBGE. Sinopse do Censo Demográfico de 2010 [Online]. 2010. https://censo2010.ibge.gov.br/sinopse/index.php?uf=13&dados=8 [10 Jan. 2025].
564 565 566	27. Carignano Torres P, Morsello C, Parry L. Rural–urban mobility influences wildmeat access and consumption in the Brazilian Amazon. <i>Oryx</i> 56: 864–876, 2022. doi: 10.1017/S0030605321001575.
567 568 569 570	28. Rivero SLM, Almeida OTD, Torres PC, De Moraes A, Chacón-Montalván E, Parry L. Urban Amazonians use Fishing as a Strategy for Coping with Food Insecurity. <i>The Journal of Development Studies</i> 58: 2544–2565, 2022. doi: 10.1080/00220388.2022.2113063.
571 572 573	29. De Onis M. WHO Child Growth Standards Length/height-for-age, weight-for-age, weight-for-length, weight-for-height and body mass index-for-age [Online]. https://cir.nii.ac.jp/crid/1573668925513982080 [27 Jan. 2025].
574 575	30. Lohman TG, Roche AF, Martorell R. Anthropometric Standardization Reference Manual. Champaign, IL: Human Kinetics Books; 1958. 1988.
576 577 578	31. WHO. The double burden of malnutrition: policy brief [Online]. World Health Organization. <u>https://apps.who.int/iris/bitstream/handle/10665/255413/WHO-NMH-?sequence=1</u> [27 Jan. 2025].
579 580 581	32. Varela-Silva MI, Dickinson F, Wilson H, Azcorra H, Griffiths PL, Bogin B. The nutritional dual-burden in developing countries–how is it assessed and what are the health implications? <i>Collegium antropologicum</i> 36: 39–45, 2012.

- 582 33. Steyn NP, Nel JH. Prevalence and Determinants of the Double Burden of 583 Malnutrition with a Focus on Concurrent Stunting and Overweight/Obesity in Children and Adolescents. Curr Nutr Rep 11: 437-456, 2022. doi: 10.1007/s13668-022-00417-0. 584 585 34. Bezanson J, Edelman A, Karpinski S, Shah VB. Julia: A Fresh Approach to 586 Numerical Computing. SIAM Rev 59: 65-98, 2017. doi: 10.1137/141000671. 587 35. Ge H, Xu K, Ghahramani Z. Turing: a language for flexible probabilistic inference [Online]. In: International conference on artificial intelligence and statistics. PMLR, p. 588 1682–1690. http://proceedings.mlr.press/v84/ge18b.html?ref=https://githubhelp.com [27 589 Jan. 2025]. 590 Parry L, Radel C, Adamo SB, Clark N, Counterman M, Flores-Yeffal N, Pons D, 591 36. Romero-Lankao P, Vargo J. The (in)visible health risks of climate change. Social Science 592 & Medicine 241: 112448, 2019. doi: 10.1016/j.socscimed.2019.112448. 593 594 37. Chacón-Montalván EA, Taylor BM, Cunha MG, Davies G, Orellana JDY, Parry L. 595 Rainfall variability and adverse birth outcomes in Amazonia. Nat Sustain 4: 583-594, 2021. doi: 10.1038/s41893-021-00684-9. 596 38. Tzioumis E, Kay MC, Bentley ME, Adair LS. Prevalence and trends in the 597 598 childhood dual burden of malnutrition in low- and middle-income countries, 1990–2012. Public Health Nutr 19: 1375–1388, 2016. doi: 10.1017/S1368980016000276. 599 600 39. Universidade Federal do Rio de Janeiro. Estado Nutricional Antropométrico da 601 Criança e da Mãe: Prevalência de indicadores antropométrico de crianças brasileiras 602 menores de 5 anos de idade e suas mães biológicas: ENANI 2019. - Documento eletrônico 603 [Online]. - Rio de Janeiro, RJ: UFRJ, 2022. (96 p.). Coordenador geral, Gilberto Kac. 604 Disponível em: https://enani.nutricao.ufrj.br/index.php/relatorios/ [27 Jan. 2025] 40. 605 Ministério do Desenvolvimento Social e Combate à Fome. Mapeamento de Segurança Alimentar e Nutricional nos Estados e Municípios - Resultados Preliminares 606 (Sumário Executivo) [Online]. . 607 https://www.mds.gov.br/webarquivos/publicacao/seguranca\_alimentar/mapa\_san\_resultado 608 s\_preliminares.pdf [27 Jan. 2025]. 609 610 41. Fausto MCR, Giovanella L, Lima JG, Cabral LMDS, Seidl H. Sustentabilidade da Atenção Primária à Saúde em territórios rurais remotos na Amazônia fluvial: organização, 611 612 estratégias e desafios. Ciênc saúde coletiva 27: 1605-1618, 2022. doi: 10.1590/1413-613 81232022274.01112021. 614 42. Barros FC, Victora CG, Scherpbier R, Gwatkin D. Socioeconomic inequities in the
- 42. Barros FC, Victora CG, Scherpbier R, Gwatkin D. Socioeconomic inequities in the
  health and nutrition of children in low/middle income countries. *Rev Saúde Pública* 44: 1–
  16, 2010. doi: 10.1590/S0034-89102010000100001.

617 43. Conde WL, Monteiro CA. Nutrition transition and double burden of undernutrition
618 and excess of weight in Brazil. *The American Journal of Clinical Nutrition* 100: 1617S619 1622S, 2014. doi: 10.3945/ajcn.114.084764.

44. Minh Do L, Lissner L, Ascher H. Overweight, stunting, and concurrent overweight
and stunting observed over 3 years in Vietnamese children. *Global Health Action* 11:
1517932, 2018. doi: 10.1080/16549716.2018.1517932.

45. Senekal M, Nel JH, Malczyk S, Drummond L, Harbron J, Steyn NP. Provincial
Dietary Intake Study (PDIS): Prevalence and Sociodemographic Determinants of the
Double Burden of Malnutrition in A Representative Sample of 1 to Under 10-Year-Old
Children from Two Urbanized and Economically Active Provinces in South Africa. *IJERPH* 16: 3334, 2019. doi: 10.3390/ijerph16183334.

46. Queiroz KOD. Transporte fluvial no Solimões – uma leitura a partir das lanchas
Ajato no Amazonas. *GEOUSP (Online)* 23: 322–341, 2019. doi: 10.11606/issn.21790892.geousp.2019.133370.

47. Costa EACD, Schor T. Redes urbanas, abastecimento e o café da manhã de idosas
na cidade de Tefé, Amazonas: elementos para a análise da geografia da alimentação no
Brasil. *Hygeia* 9: 52–73, 2013. doi: 10.14393/Hygeia922382.

48. Schor T, Avelino FCDC. Geography of Food and the Urban Network in the TriBorder Brazil-Peru-Colombia: The Case of Production and Commercialization of Poultry in
the Amazon. *Cuad geogr rev colomb geogr* 26: 141–154, 2017. doi:
10.15446/rcdg.v26n1.52301.

49. Schor T, Marinho RR, da Costa DP, de Oliveira JA. Cities, rivers and urban
network in the Brazilian Amazon. *Brazilian Geographical Journal: geosciences and humanities research medium* 5: 19, 2014.

50. Black RE, Victora CG, Walker SP, Bhutta ZA, Christian P, De Onis M, Ezzati M,
Grantham-McGregor S, Katz J, Martorell R, Uauy R. Maternal and child undernutrition and
overweight in low-income and middle-income countries. *The Lancet* 382: 427–451, 2013.
doi: 10.1016/S0140-6736(13)60937-X.

51. Horta BL, Rollins N, Dias MS, Garcez V, Pérez-Escamilla R. Systematic review
and meta-analysis of breastfeeding and later overweight or obesity expands on previous
study for World Health Organization. *Acta Paediatrica* 112: 34–41, 2023. doi:
10.1111/apa.16460.

52. Kraft TS, Stieglitz J, Trumble BC, Martin M, Kaplan H, Gurven M. Nutrition
transition in 2 lowland Bolivian subsistence populations. *The American Journal of Clinical Nutrition* 108: 1183–1195, 2018. doi: 10.1093/ajcn/nqy250.

53. Lopez VK, Dombecki C, Trostle J, Mogrovejo P, Castro Morillo N, Cevallos W,
Goldstick J, Jones AD, Eisenberg JNS. Trends of child undernutrition in rural Ecuadorian

communities with differential access to roads, 2004–2013. *Maternal & Child Nutrition* 14:
e12588, 2018. doi: 10.1111/mcn.12588.

54. Urlacher SS, Snodgrass JJ, Dugas LR, Madimenos FC, Sugiyama LS, Liebert MA,
Joyce CJ, Terán E, Pontzer H. Childhood Daily Energy Expenditure Does Not Decrease
with Market Integration and Is Not Related to Adiposity in Amazonia. *The Journal of Nutrition* 151: 695–704, 2021. doi: 10.1093/jn/nxaa361.

55. Menezes RCED, Lira PICD, Leal VS, Oliveira JS, Santana SCDS, Sequeira LADS,
Rissin A, Batista Filho M. Determinantes do déficit estatural em menores de cinco anos no
Estado de Pernambuco. *Rev Saúde Pública* 45: 1079–1087, 2011. doi: 10.1590/S003489102011000600010.

56. Woodruff BA, Wirth JP, Bailes A, Matji J, Timmer A, Rohner F. Determinants of
stunting reduction in Ethiopia 2000 – 2011. *Maternal & Child Nutrition* 13: e12307, 2017.
doi: 10.1111/mcn.12307.

57. Dufour DL, Piperata BA, Murrieta RSS, Wilson WM, Williams DD. Amazonian
foods and implications for human biology. *Annals of Human Biology* 43: 330–348, 2016.
doi: 10.1080/03014460.2016.1196245.

58. Loihala M, Indar I, Syam A, Syafar M, Abdullah MT, Muis M. Food consumption,
culture, and living environment's impact on stunting cases: A systematic review.

59. Seferidi P, Hone T, Duran AC, Bernabe-Ortiz A, Millett C. Global inequalities in
the double burden of malnutrition and associations with globalisation: a multilevel analysis
of Demographic and Health Surveys from 55 low-income and middle-income countries,
1992–2018. *The Lancet Global Health* 10: e482–e490, 2022. doi: 10.1016/S2214109X(21)00594-5.

677 60. Louzada MLDC, Cruz GLD, Silva KAAN, Grassi AGF, Andrade GC, Rauber F,
678 Levy RB, Monteiro CA. Consumo de alimentos ultraprocessados no Brasil: distribuição e
679 evolução temporal 2008–2018. *Rev saúde pública* 57: 12, 2023. doi: 10.11606/s1518680 8787.2023057004744.

681 61. Alvear-Vega S, Vargas-Garrido H. Social determinants of malnutrition in Chilean
682 children aged up to five. *BMC Public Health* 22: 44, 2022. doi: 10.1186/s12889-021683 12455-4.

684 62. Scrinis G, Castro IRRD. Framing poor diet quality as malnutrition: the Brazilian
685 National Survey on Child Nutrition (ENANI-2019). *Cad Saúde Pública* 39: e00089222,
686 2023. doi: 10.1590/0102-311xen089222.

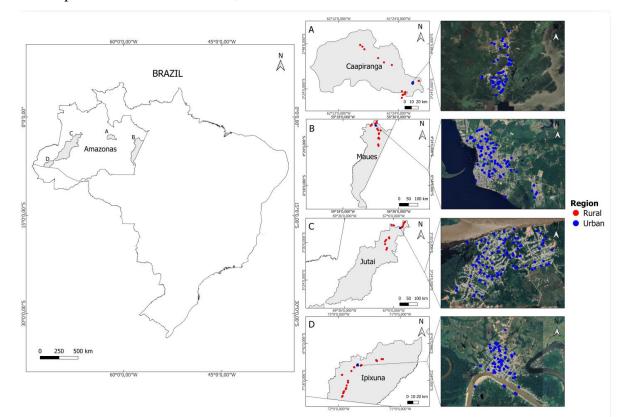
687
688
63. Hossain MdI, Rahman A, Uddin MSG, Zinia FA. Double burden of malnutrition
689 among women of reproductive age in Bangladesh: A comparative study of classical and
690 Bayesian logistic regression approach. *Food Science & Nutrition* 11: 1785–1796, 2023. doi: 10.1002/fsn3.3209.

# 

Table 1. Characteristics of children under 60 months-old and households evaluated,
 according to area and municipality, Amazonas, Brazil, 2015–16.

Area	Municipality	Children	Households	Children per	
		Cililateli	Households	household	DBM
Rural	Caapiranga	35	27	1.3	0%
Rural	Maues	44	33	1.3	0%
Rural	Jutai	74	42	1.8	4.1%
Rural	Ipixuna	52	37	1.4	1.9%
Urban	Caapiranga	65	50	1.3	1.5%
Urban	Maues	108	80	1.4	1.9%
Urban	Jutai	131	91	1.4	0.8%
Urban	Ipixuna	76	62	1.2	0%
Rural Rural Urban Urban Urban	Jutai Ipixuna Caapiranga Maues Jutai	74 52 65 108 131	42 37 50 80 91	1.8 1.4 1.3 1.4 1.4	4.1 1.9 1.5 1.9 0.8

Figure 1. Map of the study area constituting four highly-forested river-dependent municipalities in Amazonas State, Brazil.



In each municipality (A, B, C, D where gray shading indicates the municipality's territory), we sampled children within randomly selected households in the town, and surrounding rural settlements.

Figure 2. Posterior distributions of mean z-scores for stunting (height-for-age) and overweight (BMI-for-age) indicators (x-axes) for children under-five-years-old sampled from rural and urban sub-populations. Dashed vertical lines represent the median values of each indicator from the WHO reference population. 

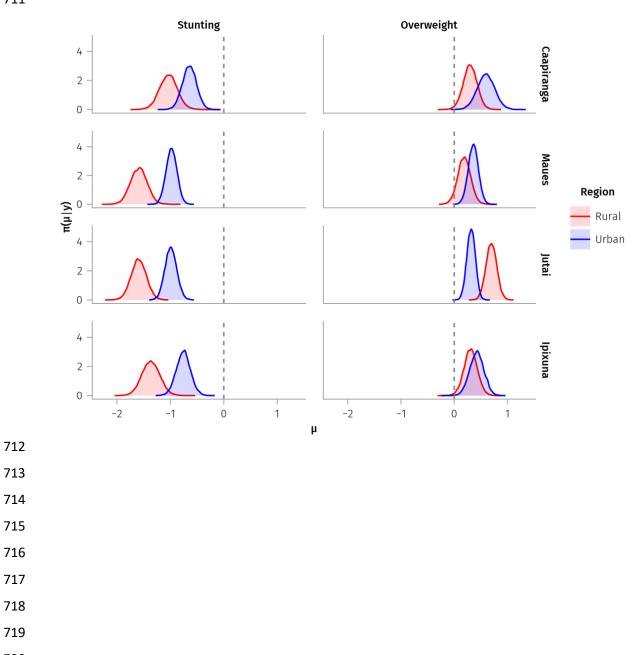
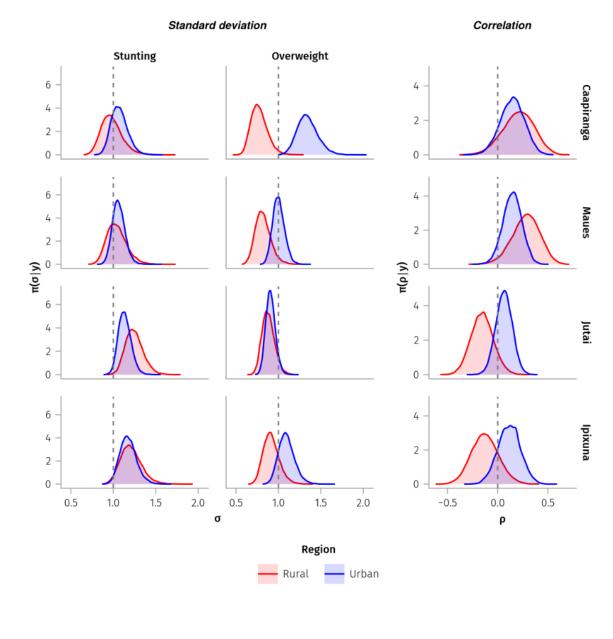


Figure 3. Posterior distributions of the standard deviations ( $\sigma$ ) and correlations ( $\rho$ ) (x-axes) of z-scores of height-for-age (stunting indicator) and BMI-for-age (overweight indicator) from children under-five-years old sampled in rural and urban sub-populations. Vertical dashed lines represent variability of 1 for the standard deviation sub-plots, and zero for the correlation sub-plots.



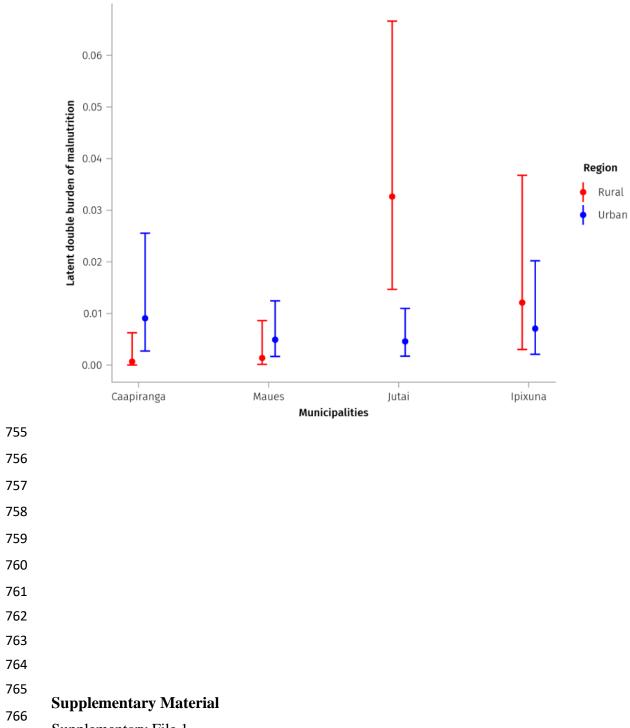
- 728
- 729
- 730

731
 732 Table 2 – Exceedance probabilities\* (pr), prevalence (proportion of children) and quantile based credible intervals (CI) of the prevalence of Latent Double Burden of Malnutrition

(overweight and stunting) among children under-five-years-old sampled in rural and urban areas in Amazonas State, Brazil.

Area	Municipality	Pr(p > 0.01)	Pr(p > 0.03)	Median	LI	LS	LI- HDP	LS- HDP
Rural	Caapiranga	0.007	0.0	0.001	0.0	0.006	0	0.005
Rural	Maues	0.016	0.0	0.001	0.0	0.009	0	0.007
Rural	Jutai	0.997	0.587	0.033	0.015	0.067	0.01	0.062
Rural	Ipixuna	0.618	0.062	0.012	0.003	0.037	0	0.032
Urban	Caapiranga	0.433	0.011	0.009	0.003	0.026	0	0.022
Urban	Maues	0.07	0.0	0.005	0.002	0.012	0	0.011
Urban	Jutai	0.042	0.0	0.005	0.002	0.011	0	0.01
Urban	Ipixuna	0.264	0.002	0.007	0.002	0.02	0	0.017

736 \*Exceedance probabilities (pr) surpassing 1 or 3%. Figure 4. Estimated prevalence and quantile-based credible intervals (CI) of the Latent Double Burden of Malnutrition (overweight and stunting) in sampled rural and urban sub-populations.



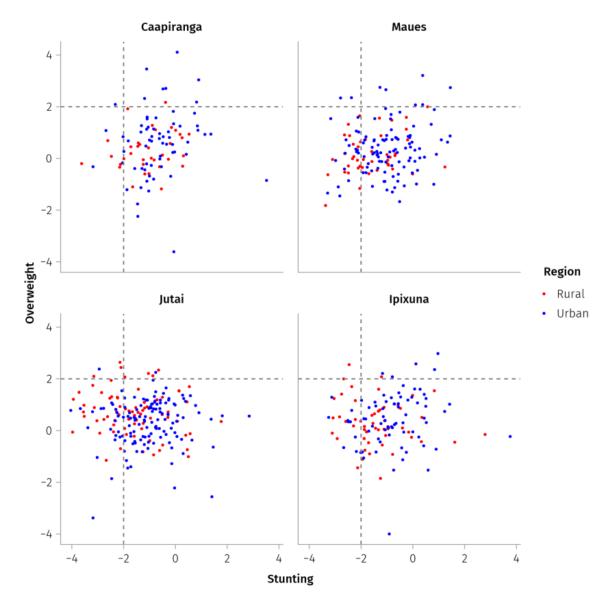
Supplementary File 1

Although the sampling was based on the 2010 public census, we identified that new residential areas had emerged in Jutai by 2015, based on consulting Google Earth imagery and ArcGIS 10.3 basemaps. We used these aerial images to estimate the number of households in these new residential areas. We then assigned a proportional number of target households to each area (e.g., if a new development polygon contained 200 of a town's 5,000 households, it would receive 4% of the sampling effort (i.e., 8 target households).

In rural areas, communities were selected to capture geographical variation in terms of distance to the nearest urban area and the type of natural environment (*varzea* floodplain or *terra firme* upland), given the association between these factors and health determinants, including public service provision, income and agricultural potential. The community selection process was informed by input from local stakeholders. In each municipality, we aimed to sample eight communities each season, without revisiting a community (i.e., 16 communities per municipality). In each season, we tried to select four communities located along the main river (e.g., River Solimoes, for Jutai) and four along one or the smallest sub-tributaries, with varying remoteness from the municipal urban area.

Of the eligible children, 14 were not at home, and the guardians of another ten children refused to allow the collection of a blood sample for hemoglobin measurement. In addition, three children were excluded from the analysis because they had physical or neurological problems. No children were excluded due to implausible anthropometric data.

Supplementary Figure 1. Scatterplots showing the correlations between z-scores of heightfor-age (stunting equal values <-2) and BMI-for-age (overweight equals values >2) for
individual children in rural and urban areas of Amazonas State, Brazil. Each sub-plot presents
data from a municipality consisting of random samples from the urban area (towns), and rural
samples from surrounding settlements. In each subplot, the upper-left quadrant indicates
cases of the double burden of malnutrition at the individual level following a frequentist
approach.



783 Supplementary Table 1. Likelihood ratio tests for the significance of household-level 784 random effects by region type and municipality for z-scores of height-for-age and BMI-for-

age.  $D_1$  and  $D_2$  represent the deviances of the models with and without random effects,

- respectively. Similarly,  $AIC_1$  and  $AIC_2$  are the Akaike Information Criteria for the models
- 787 with and without random effects, respectively.

Region	Municipality	D1	$D_2$	$D_1-D_2$	P-value	AIC <sub>1</sub>	AIC <sub>2</sub>	AIC1-AIC2
Rural	Caapiranga	94.69	93.25	1.44	0.23	98.69	99.25	-0.56
Rural	Maues	124.99	123.69	1.31	0.25	128.99	129.69	-0.69
Rural	Jutai	239.24	239.16	0.08	0.78	243.24	245.16	-1.92
Rural	Ipixuna	163.80	163.80	0.00	1.00	167.80	169.80	-2.00
Urban	Caapiranga	189.96	189.96	0.00	1.00	193.96	195.96	-2.00
Urban	Maues	316.30	314.60	1.70	0.19	320.30	320.60	-0.30
Urban	Jutai	400.50	394.17	6.34	0.01	404.50	400.17	4.34
Urban	Ipixuna	236.78	234.93	1.85	0.17	240.78	240.93	-0.15

Z-score of BMI for age

Region	Municipality	D1	<b>D</b> <sub>2</sub>	$D_1-D_2$	<b>P-value</b>	AIC <sub>1</sub>	AIC <sub>2</sub>	AIC1-AIC2
Rural	Caapiranga	78.05	77.33	0.72	0.40	82.05	83.33	-1.28
Rural	Maues	103.85	103.84	0.01	0.92	107.85	109.84	-1.99
Rural	Jutai	187.77	186.89	0.88	0.35	191.77	192.89	-1.12
Rural	Ipixuna	134.81	134.81	0.00	1.00	138.81	140.81	-2.00
Urban	Caapiranga	219.50	219.50	0.00	1.00	223.50	225.50	-2.00
Urban	Maues	303.81	303.81	0.00	1.00	307.81	309.81	-2.00
Urban	Jutai	342.85	342.80	0.05	0.82	346.85	348.80	-1.95
Urban	Ipixuna	225.20	221.07	4.13	0.04	229.20	227.07	2.13

788