

Data fidelity-oriented spatial-spectral fusion of CRISM and CTX images

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Abstract: The Compact Reconnaissance Imaging Spectrometer for Mars (CRISM) is a Mars-dedicated compact reconnaissance imaging spectrometer that captures remote sensing data with very fine spectral resolution. However, the spatial resolution of CRISM data is relatively coarse (18 m), limiting its application to regional scales. The Context Camera (CTX) is a digital camera equipped with a wide-angle lens, providing a finer spatial resolution (6 m) and larger field-of-view, but CTX provides only a single panchromatic band. To produce CRISM hyperspectral data with finer spatial resolution (e.g., 6 m of CTX images), this research investigated spatial-spectral fusion of 18 m CRISM images with 6 m CTX panchromatic images. In spatial-spectral fusion, to address the long-standing issue of incomplete data fidelity to the original hyperspectral data in existing methods, a new paradigm called Data Fidelity-oriented Spatial-Spectral Fusion (DF-SSF) was proposed. The effectiveness of DF-SSF was validated through experiments on data from six areas on Mars. The results indicate that the fusion of CRISM and CTX can increase the spatial resolution of CRISM hyperspectral data effectively. Moreover, DF-SSF can increase the fusion accuracy noticeably while maintaining perfect data fidelity to the original hyperspectral data. In addition, DF-SSF is theoretically applicable to any existing spatial-spectral fusion methods. The 6 m CRISM hyperspectral data inherit the advantages of the original 18 m data in spectral resolution, and provide richer spatial texture information on the Martian surface, with broad application potential.

Keywords: Compact Reconnaissance Imaging Spectrometer for Mars (CRISM), Context Camera (CTX), downscaling, spatial-spectral fusion, data fidelity, area-to-point kriging (ATPK).

1. Introduction

As a neighboring planet in the solar system, Mars has always been a focus of human fascination and, more

33 recently, an emerging target for human exploration. Its known, abundant resources, based on our gradually
34 deepening understanding of its geology, landform and atmosphere, may be important for the future
35 development of human society. With advances in space technology, Mars exploration is increasingly seen as
36 an important pathway for space resources development and scientific technological innovation.

37 As an advanced imaging technology, hyperspectral remote sensing provides data with a very fine spectral
38 resolution for observing the surface of Mars, offering unique opportunities for a deeper understanding of the
39 geology and environment of Mars. The main advantage of hyperspectral images over multispectral images
40 lies in the richer spectral information, which is crucial for studying the mineral composition and formation
41 mechanisms on the surface of Mars. The Mars Reconnaissance Orbiter (MRO) was launched on August 12,
42 2005 (Zurek and Smrekar, 2007) to investigate the geology and climate of Mars. Its scientific objectives
43 include observing the current climate of Mars, searching for water activity, mapping surface features on Mars,
44 and studying potential future landing sites. The MRO carries several instruments, including the Compact
45 Reconnaissance Imaging Spectrometer for Mars (CRISM) (Murchie et al., 2007) and the Context Camera
46 (CTX) (Malin et al., 2007). These two sensors capture information about the same area with different spectral
47 and spatial resolutions simultaneously. Specifically, CRISM is operated in hyperspectral mode, acquiring
48 hyperspectral images covering more than four hundred spectral bands from the visible to near-infrared
49 wavelengths. However, its spatial resolution is 18 m, which is relatively coarse for observing detailed spatial
50 texture information in local areas. The primary function of CTX is to provide background information for
51 other MRO instruments through simultaneous observations. The coverage of the images captured by CTX is
52 larger than that of CRISM and the spatial resolution is about 6 m, which is three times finer than for CRISM
53 (Malin et al., 2007). However, these images are single-band and do not provide spectral information. This
54 study proposed to downscale the 18 m CRISM hyperspectral images to 6 m, with the aid of the 6 m fine
55 spatial resolution CTX images. The 6 m hyperspectral images can potentially provide more spatial details
56 about the surface of Mars while preserving the fine spectral resolution of CRISM.

57 Spatial-spectral fusion (also known as pan-sharpening) aims to fuse images with fine spectral resolution,
58 but coarse spatial resolution with images with fine spatial resolution, but coarse spectral resolution (e.g.,
59 panchromatic image) in the same region to create images with both fine spatial and spectral resolutions
60 (Zhang and Shen, 2016). It can resolve the trade-off that occurs between spatial and spectral resolution when
61 designing a single sensor. The existing spatial-spectral fusion methods include component substitution
62 (CS)-based, multi-resolution analysis (MRA)-based, variational optimization (VO)-based, matrix
63 factorization, learning-based, and geostatistical approaches (Ghamisi et al., 2019; Loncan et al., 2015;
64 Thomas et al., 2008; Vivone et al., 2014; Yang et al., 2022). The main idea of the CS methods is to transform

65 the multi/hyperspectral images into another space, and utilize the panchromatic image to substitute the
66 transformed coarse spatial resolution component (Aiazzi et al., 2007; Thomas et al., 2008). Representative
67 methods include principal component analysis (PCA) (Shah et al., 2008; Shettigara, 1992), Gram-Schmidt
68 transformation (GS) (Laben and Brower, 2000), Gram-Schmidt adaptive (GSA) (Aiazzi et al., 2007). The
69 core idea of MRA is to extract fine spatial resolution details from the panchromatic image and inject them
70 into the coarse spatial resolution multi/hyperspectral images (Chavez et al., 1991). Representative methods
71 include smoothing filter-based intensity modulation (SFIM) (Liu, 2000), generalized Laplacian pyramid
72 (GLP) with modulation transfer function (MTF)-matched filter (MTF-GLP) (Aiazzi et al., 2006), and GLP
73 with MTF-matched filter and multiplicative injection model (MTF-GLP-HPM) (Lee and Lee, 2009). The
74 VO-based methods construct a variational optimization model to take full advantage of the spatial
75 information of panchromatic image and spectral information of coarse spatial resolution multispectral image.
76 For example, the variational approach developed by Fang et al. (2013) consists of three terms, which aim to
77 minimize the difference in spatial gradients between the panchromatic image and fused image, the difference
78 between original coarse multispectral image and (degraded) fused image, and the difference in spectral
79 gradients between original coarse multispectral image and fused image. The matrix factorization methods
80 were proposed from the perspective of spectral unmixing. A representative method in this category is coupled
81 nonnegative matrix factorization (CNMF) (Berne et al., 2010; Yokoya et al., 2012), which extracts
82 endmembers from coarse spatial, but fine spectral resolution image and proportions from fine spatial, but
83 coarse spectral resolution image. The CNMF prediction is the linear combination of the proportions and
84 endmembers. The learning-based methods focus on establishing a nonlinear mapping relationship between
85 the fine spatial resolution panchromatic images and coarse spatial resolution multi/hyperspectral images or
86 learning the intrinsic structure of the data observed. Deep learning has become a common choice for
87 spatial-spectral fusion due to its strong fitting ability. Early attempts are mainly supervised methods, which
88 require multi/hyperspectral images at the target fine spatial resolution. Examples for this type of methods
89 include the pan-sharpening neural network (PNN) (Masi et al., 2016) and a deep network architecture for
90 pansharpening (PanNet) (Song et al., 2018; Yang et al., 2017, 2018). Recently, more advanced versions were
91 developed, such as domain transform model driven by deep learning (Sun et al., 2024) and progressive
92 multi-iteration registration-fusion co-optimization network (Qu et al., 2024). For supervised methods,
93 however, the applicability in reality can be compromised, as it can be difficult to collect required fine spatial
94 resolution multi/hyperspectral images for training. Alternatively, unsupervised deep learning strategies have
95 been developed for spatial-spectral fusion in recent years (Ma et al., 2020; Qu et al., 2023; Sun et al., 2023),
96 which do not need multi/hyperspectral images at the target fine spatial resolution for training, but learn the

97 intrinsic structure from the input data. Specifically, the input panchromatic image and coarse multispectral
98 image are used in the construction of loss functions to constrain the predictions of the networks. Spatially, it is
99 assumed that the spatial information presented by the (spectrally degraded) fused image should be similar to
100 that of the panchromatic image. Spectrally, it is assumed that the (spatially degraded) fused image should be
101 the same as the input multispectral image. The geostatistical approaches can take into account the changes in
102 the spatial support of the data and the point spread function (PSF) effect of sensors (Atkinson et al., 2008;
103 Wang et al., 2014). The most significant advantage of geostatistical methods is that the downscaling results
104 are consistent with the original coarse spatial resolution data. Representative methods include area-to-point
105 regression kriging (ATPRK) (Wang et al., 2016), downscaling cokriging (DSCK) (Pardo-Igúzquiza et al.,
106 2006), and kriging with an external drift (KED) (Sales et al., 2012).

107 Significant progress has been made in research on spatial-spectral fusion based on various Earth
108 observation datasets. However, research on fusion of datasets on other planets is relatively limited. To the
109 best of our knowledge, there has been no study on the fusion of CTX and CRISM images for Mars. The
110 surface of Mars is generally covered by rocks and minerals with various terrain and landform features, which
111 is substantially different from that for the Earth surface. The main advantage of hyperspectral image over
112 multispectral image is that the former can provide more detailed spectral information, which significantly
113 enhances the ability to distinguish between different types of rocks and minerals. In this case, the
114 effectiveness of existing spatial-spectral fusion methods needs to be validated. Most current spatial-spectral
115 fusion methods suffer from a long-standing issue: they cannot achieve data fidelity of the original coarse
116 spatial resolution images. That is, when the spatial-spectral fusion results are degraded to the original coarse
117 spatial resolution, they are not consistent with the original coarse image. To realize data fidelity is crucial for
118 hyperspectral sharpening, as the reliability of spectra plays key role in downstream applications such as rock
119 and mineral identification.

120 Geostatistics provides a new solution for realization of spatial-spectral fusion with perfect data fidelity to
121 the original coarse spatial resolution images. Specifically, various models based on area-to-point kriging
122 (ATPK) (Atkinson, 2013; Kyriakidis, 2004; Kyriakidis and Yoo, 2005; Wang et al., 2015) including DSCK,
123 KED, and ATPRK, have significant advantages in preserving the original coarse image. That is, when the
124 spatial-spectral fusion result is degraded to the original spatial resolution, it is completely consistent with the
125 original image. This characteristic of complete data fidelity is also referred to complete data coherence in
126 geostatistics.

127 This paper proposed a completely new paradigm of spatial-spectral fusion called DF-SSF (Data
128 Fidelity-oriented Spatial-Spectral Fusion) for fusion of CTX and CRISM images, where the CTX image is

129 treated as the panchromatic image. It aims to preserve perfectly the original CRISM data. DF-SSF achieves
130 this by utilizing ATPK to downscale the difference (i.e., coarse residual image) between the existing fusion
131 result (i.e., produced by any of the existing spatial-spectral fusion methods) and the original coarse spatial
132 resolution image. The produced fine spatial resolution residual image is then added to the existing fusion
133 result to obtain the final fusion result with complete data fidelity. The contributions of this paper mainly lie in
134 two aspects.

- 135 1) It is the first study on the fusion of CTX and CRISM images on Mars to enhance the spatial resolution
136 of CRISM hyperspectral images. Although spatial-spectral fusion has been developed over decades, to
137 the best of our knowledge, there is no research on Mars remote sensing data dominated by rocks and
138 minerals, especially for fusion of CTX and CRISM data, where the preservation of original spectra is
139 crucial for downstream applications.
- 140 2) A completely new paradigm DF-SSF, is proposed for spatial-spectral fusion with complete data fidelity
141 to the original coarse spatial resolution data. DF-SSF is theoretically applicable to any existing
142 spatial-spectral fusion method.

143 The remainder of this paper is divided into five sections. Section 2 provides a brief introduction to the
144 study area, research data, and the corresponding processing. Section 3 explains the principles of the proposed
145 DF-SSF method. The experimental results for validation of the method are presented in Section 4. Section 5
146 discusses issues related to the proposed method and outlines future directions. Finally, Section 6 concludes
147 the paper.

150 **2. Study area and data**

152 **2.1. Study area**

154 The study area of this paper consists of six regions, as shown in Table 1 (Bennett et al., 2014). Among
155 them, Eberswalde Crater, Mawrth Vallis, and Holden Crater (Poulet et al., 2014) were once considered as
156 candidate landing sites for Mars missions. The Melas Chasma area is a canyon on the Martian surface, while
157 the Gale Crater (Peulvast and Masson, 1993; Poulet et al., 2014) was the location where the Curiosity Rover
158 landed successfully in 2012 and is currently considered for scientific exploration. The Jezero Crater (Goudge
159 et al., 2015) was the landing site of the Perseverance Rover, which landed successfully in 2021. These six
160 regions have become the focus of scientific research due to their unique geological and geomorphological

161 characteristics. Utilizing the hyperspectral remote sensing data covering these areas, it is possible to study
162 Martian rocks, minerals and many other topics. The abundance, distribution, and properties of these rocks
163 and minerals can provide insights into the composition and evolutionary processes of the Martian surface.
164 In-depth study of these regions can help us understand the geological history and hydrological processes of
165 Mars more comprehensively.

167 2.2. CRISM images

169 All CRISM images used in this paper are Map-Projected Targeted Reduced Data Record (MTRDR)
170 (Murchie et al., 2007) products obtained at the latest, publicly available calibration level. The MTRDR
171 includes map-projected Targeted Empirical Record corrected (TER) calibrated I/F (the ratio of the sensor's
172 spectral irradiance to the solar spectral irradiance) spectral information and excludes spectral channels with
173 questionable radiance measurements ("bad bands"). The hyperspectral image cubes in the MTRDR product
174 suite are stored as 32-bit real number units. As a hyperspectral sensor, CRISM covers the spectral range from
175 362 nm to 3920 nm with a fine spectral resolution of 6.55 nm per channel. This range includes the visible,
176 near-infrared and shortwave infrared wavelengths. Through these channels, CRISM obtains spectral
177 information from the Martian surface, which can be used for studying Martian mineralogy, geology and
178 geomorphology. The CRISM data used in this study are MTRDR products with a spatial resolution of about
179 18 m in this hyperspectral mode.

181 2.3. CTX images

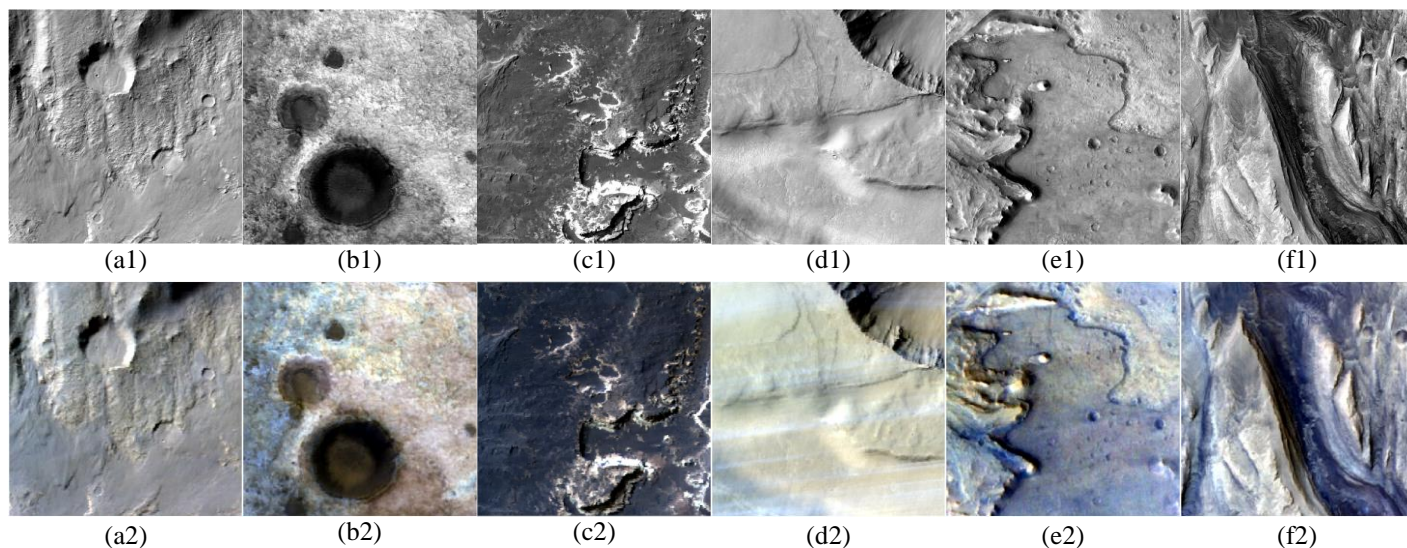
183 The CTX images used in this paper are Experiment Data Record (EDR) (Malin et al., 2007) products
184 containing raw CTX images along with their associated metadata information (e.g., observation time,
185 exposure time, camera parameters, etc.). The raw EDR data are convenient for further processing, analysis
186 and utilization. Unlike multispectral images, CTX images contain only a single-band, with a spectral range
187 from 500 nm to 700 nm. On the MRO's near-circular, near-polar mapping orbit, the spatial resolution of CTX
188 is about 6 m. This relatively fine spatial resolution enables CTX to capture more detailed surface features on
189 Mars, including impact craters, canyons, dunes, and some other intricate information.

191 2.4. Data processing

193 The CRISM MTRDR images were used as originally provided, while CTX images were processed using
 194 the ISIS3 (Sucharski et al., 2020) pipeline. The raw CTX image files were first converted to ISIS3 image
 195 format and then subjected to image map projection (Equidistant cylindrical). Since precise alignment
 196 between the input hyperspectral and panchromatic images is essential for spatial-spectral fusion, image
 197 registration was also performed. Geometric registration between the CRISM and CTX images was achieved
 198 by using rasterio's virtual warping to reproject the CRISM images into the coordinate reference system of the
 199 corresponding CTX images. However, even within the same coordinate system, the CRISM and CTX images
 200 may not be perfectly aligned. Therefore, subsequent registration is necessary. In this paper, the software
 201 ENVI was employed for local registration through the Harris corner detection algorithm. The final 6 m CTX
 202 and 18 m CRISM images of the study area are shown in Fig. 1. The spatial sizes of CTX and CRISM images
 203 used in each region are 900×900 and 300×300 pixels, respectively.

Table 1. Locations of the six study regions.

Regions	Latitude (°)		Longitude (°)	
	Min	Max	Min	Max
Eberswalde crater	-24.5	-23.4	-34.0	-32.7
Mawrth Vallis	23.3	24.6	-19.6	-18.4
Holden crater	-27.6	-25.9	-36.0	-34.0
Melas Chasma	-10.5	-8.7	-78.0	-75.0
Jezero crater	18.0	18.8	77.2	78.4
Gale crater	-0.9	-3.8	135.9	139.9



207 Fig. 1. The CTX (6 m) and CRISM (18 m) images of the six regions (bands 37, 25 and 12 as RGB). The spatial sizes of the CTX
 208 and CRISM images are 900×900 and 300×300, respectively. (a) Eberswalde Crater. (b) Mawrth Vallis. (c) Holden Crater. (d) Melas
 209 Chasma. (e) Jezero Crater. (f) Gale Crater.

211

212 **3. Methods**

213

214 3.1. Overview of DF-SSF

215

216 The main requirement of the Wald protocol I (Wald et al., 1997) in spatial-spectral fusion is that there
 217 should be no deviation between the spatial-spectral fusion result and the original coarse image. That is, when
 218 the fused image is degraded to the original coarse spatial resolution, it should be exactly the same as the
 219 observed coarse image. However, the reality is that existing spatial-spectral fusion models struggle to achieve
 220 data fidelity in the true mathematical sense, meaning that the residuals (i.e., the difference between the fusion
 221 result and the original coarse data) are commonly non-zero. Achieving data fidelity to the original coarse
 222 image plays a crucial role in enhancing the reliability of the fused data. Therefore, this paper proposes a
 223 completely new spatial-spectral fusion paradigm (DF-SSF) that can realize complete data fidelity to the
 224 original coarse image:

$$\widehat{\mathbf{HS}}_k = \widehat{\mathbf{HS}}_k' + \Delta \mathbf{R}_k, \quad k = 1, 2, \dots, N \quad (1)$$

225 where k denotes the result of the k -th band ($k=1,2,\dots,N$, where N is the total number of bands), $\widehat{\mathbf{HS}}_k$ is the
 226 spatial-spectral fusion result that enables complete data fidelity, $\widehat{\mathbf{HS}}_k'$ is the prediction of any existing
 227 spatial-spectral fusion model, and $\Delta \mathbf{R}_k$ represents the fine spatial resolution residuals present in the existing
 228 spatial-spectral fusion model. Details for calculation of $\widehat{\mathbf{HS}}_k'$ and $\Delta \mathbf{R}_k$ are introduced in the following
 229 Sections 3.2 and 3.3, respectively. The whole flowchart of the proposed DF-SSF method is sketched in Fig.
 230 2.

231

232 3.2. Estimation based on existing SSF methods

233

234 The widely used spatial-spectral fusion algorithms generally follow the basic principles of CS or MRA.
 235 Therefore these two categories of methods are the focus of this paper. Their main principles are briefly
 236 described as follows.

237 For the CS-based methods, the spatial-spectral fusion result is defined as:

$$\widehat{\mathbf{HS}}_k' = \widetilde{\mathbf{HS}}_k + g_k^C (\mathbf{P} - \mathbf{I}_L), \quad k = 1, 2, \dots, N \quad (2)$$

238 in which $\widehat{\mathbf{HS}}_k'$ denotes the fusion result for the k -th band, $\widetilde{\mathbf{HS}}_k$ denotes the multi/hyperspectral image

239 interpolated to the spatial size of the panchromatic image, g_k^C is the weight of the fine spatial resolution gain
 240 injected into the k -th band (where C represents the CS-based methods), and \mathbf{P} denotes the panchromatic
 241 image. \mathbf{I}_L is defined as:

$$\mathbf{I}_L = \sum_{i=1}^N \omega_i \widetilde{\mathbf{H}}\mathbf{S}_i \quad (3)$$

242 in which ω_i represents the fitting weight for the i -th ($i=1,2,\dots,N$) band of the multi/hyperspectral image.

243 For the MRA-based method, the spatial-spectral fusion result is defined as:

$$\widehat{\mathbf{H}}\mathbf{S}'_k = \widetilde{\mathbf{H}}\mathbf{S}_k + g_k^M(\mathbf{P} - \mathbf{P}_L), \quad k = 1, 2, \dots, N \quad (4)$$

244 where \mathbf{P}_L represents the coarse spatial resolution version of the image \mathbf{P} , and g_k^M is the weight of the fine
 245 spatial resolution gain for the k -th band (where M represents the MRA-based methods).

246

247 3.3. Estimation of the residuals at fine spatial resolution

248

249 For existing spatial-spectral fusion models, it is inevitable that there are coarse spatial resolution residuals
 250 (denoted as $\Delta\mathbf{R}_k^C$) in their predictions, as defined as follow:

$$\Delta\mathbf{R}_k^C = \mathbf{H}\mathbf{S}_k - \widehat{\mathbf{H}}\mathbf{S}'_k \uparrow \quad (5)$$

251 where $\mathbf{H}\mathbf{S}_k$ represents the observed coarse spatial resolution image of the k -th band, \uparrow denotes the
 252 degradation operation, and $\widehat{\mathbf{H}}\mathbf{S}'_k \uparrow$ indicates the result of degrading the spatial-spectral fusion result of the
 253 k -th band to the original coarse spatial resolution.

254 In this paper, we utilized ATPK to estimate the spatial resolution fine residuals $\Delta\mathbf{R}_k$ in Eq. (1).
 255 Specifically, for the residual of the fine spatial resolution pixel at spatial position \mathbf{x} in the k -th band (denoted
 256 as $\Delta\mathbf{R}_k(\mathbf{x})$), its value can be predicted through a linear combination of L spatially adjacent coarse residuals in
 257 image $\Delta\mathbf{R}_k^C$:

$$\Delta\mathbf{R}_k(\mathbf{x}) = \sum_{i=1}^L \beta_i \Delta\mathbf{R}_k^C(\mathbf{x}_i), \quad s.t. \quad \sum_{i=1}^L \beta_i = 1 \quad (6)$$

258 where \mathbf{x}_i denotes the spatial location of the i -th neighborhood, β_i denotes the weight of its corresponding
 259 coarse residual, and L is the number of neighboring coarse pixels used in the prediction. The L weights (i.e.,
 260 $\beta_1, \beta_2, \dots, \beta_L$) in Eq. (6) are calculated by the kriging equation as follows:

$$\begin{bmatrix} \gamma_{CC}^k(\mathbf{x}_1, \mathbf{x}_1) & \cdots & \gamma_{CC}^k(\mathbf{x}_1, \mathbf{x}_L) & 1 \\ \vdots & \ddots & \vdots & \vdots \\ \gamma_{CC}^k(\mathbf{x}_L, \mathbf{x}_1) & \cdots & \gamma_{CC}^k(\mathbf{x}_L, \mathbf{x}_L) & 1 \\ 1 & \cdots & 1 & 0 \end{bmatrix} \begin{bmatrix} \beta_1 \\ \vdots \\ \beta_L \\ \theta \end{bmatrix} = \begin{bmatrix} \gamma_{FC}^k(\mathbf{x}, \mathbf{x}_1) \\ \vdots \\ \gamma_{FC}^k(\mathbf{x}, \mathbf{x}_L) \\ 1 \end{bmatrix} \quad (7)$$

261 where the term $\gamma_{CC}^k(\mathbf{x}_m, \mathbf{x}_n)$ ($m, n=1,2,\dots,L$) is the coarse-to-coarse residual semivariogram between coarse
 262 pixels centered at \mathbf{x}_m and \mathbf{x}_n in the k -th band, $\gamma_{FC}^k(\mathbf{x}, \mathbf{x}_m)$ is the fine-to-coarse residual semivariogram between
 263 fine and coarse pixels centered at \mathbf{x} and \mathbf{x}_m in the k -th band, and θ is the Lagrange multiplier. Further details
 264 on calculation of the semivariograms can be found in Wang et al. (2015, 2016).

265

266 3.4. Perfect data fidelity of DF-SSF

267

268 An important advantage of ATPK is the perfect coherence of the prediction with the input coarse image.
 269 That is, once the ATPK prediction is degraded to the original coarse spatial resolution, it is exactly identical
 270 to the original coarse data. Based on the perfect coherence of ATPK, the coarse residuals $\Delta \mathbf{R}_k^C$ can be
 271 accurately reproduced when the ATPK predictions $\Delta \mathbf{R}_k$ are degraded to the coarse spatial resolution as
 272 follows:

$$\Delta \mathbf{R}_k \uparrow = \Delta \mathbf{R}_k^C \quad (8)$$

273 As described in Eq. (1), the prediction of DF-SSF is composed of $\widehat{\mathbf{H}}\mathbf{S}_k'$ predicted by any of the existing
 274 spatial-spectral fusion methods and $\Delta \mathbf{R}_k$ predicted by ATPK. Combining Eqs. (1), (5) and (8), we can derive
 275 the following:

$$\begin{aligned} \widehat{\mathbf{H}}\mathbf{S}_k \uparrow &= (\widehat{\mathbf{H}}\mathbf{S}_k' + \Delta \mathbf{R}_k) \uparrow \\ &= \widehat{\mathbf{H}}\mathbf{S}_k' \uparrow + \Delta \mathbf{R}_k \uparrow \\ &= \widehat{\mathbf{H}}\mathbf{S}_k' \uparrow + \Delta \mathbf{R}_k^C \\ &= \widehat{\mathbf{H}}\mathbf{S}_k' \uparrow + \mathbf{H}\mathbf{S}_k - \widehat{\mathbf{H}}\mathbf{S}_k' \uparrow \\ &= \mathbf{H}\mathbf{S}_k \end{aligned} \quad (9)$$

276 Eq. (9) means that once the prediction of DF-SSF (i.e., $\widehat{\mathbf{H}}\mathbf{S}_k'$) is degraded to the original coarse spatial
 277 resolution, it is exactly identical to the original coarse image (i.e., $\mathbf{H}\mathbf{S}_k$), thereby, achieving complete data
 278 fidelity to the original data.

279

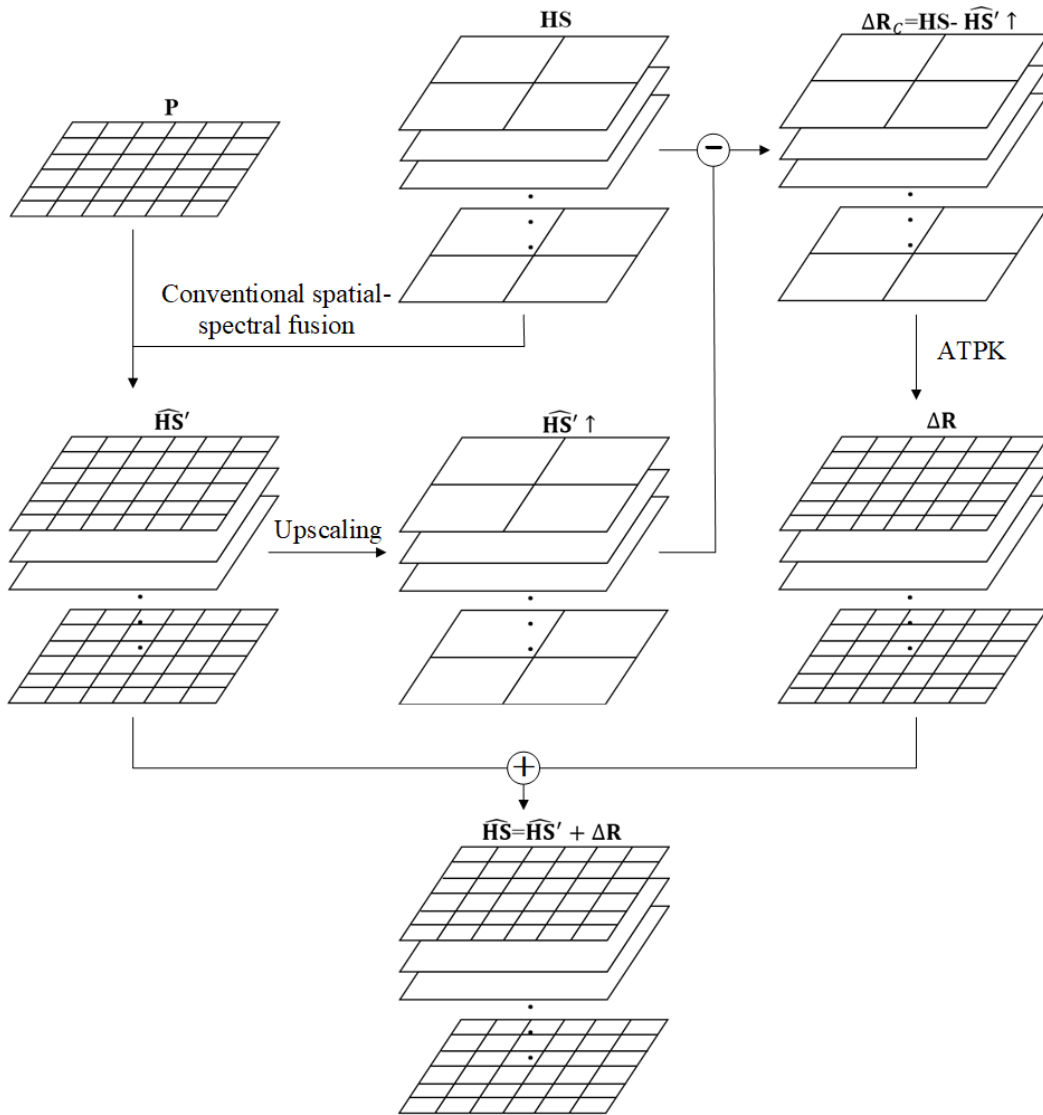


Fig. 2. Flowchart of the proposed DF-SSF.

4. Experiments

4.1. Experimental setup

In this paper, two sets of experiments were designed to validate the feasibility of the spatial-spectral fusion of CRISM and CTX data, as well as the effectiveness of our proposed DF-SSF model (e.g., its data fidelity ability). The six regions introduced in Section 2 were selected. For the CRISM hyperspectral data, after removing the noisy bands, the first 70 bands covering the spectral range similar to that of the CTX

292 panchromatic image were selected in the experiments.

293 In the first set of experiments, the effectiveness of DF-SSF was validated utilizing simulated data.
294 Specifically, due to the absence of 6 m CRISM images, there are no reference data for objective evaluation of
295 the 6 m results produced by fusion of the 18 m CRISM data and the 6 m CTX data. Therefore, to ensure the
296 existence of reliable hyperspectral reference images at the target fine spatial resolution, a commonly used
297 strategy was adopted: the 18 m CRISM hyperspectral image and the 6 m CTX panchromatic image were
298 degraded to 54 m and 18 m, respectively. Then the two degraded images were fused to obtain the 18 m
299 hyperspectral image by spatial-spectral fusion. The original 18 m CRISM hyperspectral image was used as
300 the reference image to evaluate the accuracy of the 18 m fusion result. During the degradation process, the
301 Gaussian PSF (with a convolution kernel parameter of 0.5) was used in the experiments. This paper employs
302 five evaluation metrics for quantitative assessment, including correlation coefficient (CC), spectral angle
303 mapper (SAM), root mean square error (RMSE), relative global-dimensional synthesis error (ERGAS)
304 (Ranchin and Wald, 2000) and universal image quality index (UIQI) (Wang and Bovik, 2002). For CC,
305 RMSE, and UIQI, the values were computed band-by-band, and then averaged across all bands. For SAM, it
306 was first calculated pixel-by-pixel and finally averaged across all pixels. To evaluate the data fidelity
307 capability, we also evaluated the metric of coherence, which involves degrading the spatial-spectral fusion
308 image to the original coarse spatial resolution and to calculate the CC with the original input coarse
309 resolution image.

310 In the second set of experiments, the actual 18 m CRISM hyperspectral data were fused with 6 m CTX
311 panchromatic data to obtain CRISM hyperspectral data at 6 m spatial resolution. The spatial-spectral fusion
312 performance was evaluated mainly based on visual inspection and the metric of coherence.

313 CS and MRA are two types of the most widely used spatial-spectral fusion methods. Therefore, we applied
314 DF-SSF to seven methods within the two categories: GS, GSA, PCA, SFIM, MTF-GLP, MTF-GLP-HPM,
315 and guided filter PCA (GFPCA) (Liao et al., 2015). In addition, we also examined the applicability of
316 DF-SSF to the unsupervised deep learning-based method, and a typical method of this type, that is,
317 pansharpening based on a generative adversarial network (Pan-GAN) (Ma et al., 2020), was considered.

318 319 4.2. 18 m fusion results

320
321 1) *Visual evaluation*: Fig. 3 shows the spatial-spectral fusion results of different CS and MRA methods in
322 the six regions. Note that the sub-areas marked in red are zoomed in Fig. 4 for clearer comparison. Visually,
323 it is evident that all methods produce results closer to the reference images after considering data fidelity by

324 DS-SSF. Specifically, using the DF-SSF method, the spectral distortion present in the GS and PCA methods
325 (such as in the alluvial fan and channel areas of the Eberswalde Crater region in Fig. 3) is significantly
326 reduced. The fusion results of the GFPCA and SFIM methods based on DS-SSF reproduce more spatial
327 structures (as seen in the Mawrth Vallis region where surface features are depicted as relatively small and
328 dense layers of sediment). For the MTF-GLP and MTF-GLP-HPM methods, the spectral and spatial
329 distortions in the results are relatively minor, but when considering data fidelity, the results are closer to the
330 reference images in the hue.

331 2) *Accuracy evaluation*: Firstly, for a clearer comparison of the results from different methods, we selected
332 two bands from the fusion results in Fig. 3 for analysis, and produced the error maps in Fig. 5. It can be
333 observed clearly that, for all seven methods, the errors are significantly reduced when using the DF-SSF
334 method, particularly in areas such as smooth river channels, weathered regions, and impact craters. Hence,
335 the fusion results obtained by DF-SSF exhibit smaller errors compared to those of the original methods.
336 Secondly, scatterplots representing the results of the original and DF-SSF methods are given in Fig. 6. From
337 the scatterplots, it is apparent that the results of the original spatial-spectral fusion methods are relatively
338 scattered along the axes, while the fusion results of DF-SSF are more concentrated around the $y=x$ line,
339 indicating that its results are closer to the reference.

340 Table 2 provides quantitative evaluation results for the various methods in the six regions. It can be seen
341 that the accuracy of the DF-SSF results is obviously greater than that of the original methods. For example,
342 the CC and UIQI values of all six regions are increased by over 0.0120, the ERGAS values are all decreased
343 by more than 0.0500, and the SAM values are all decreased by more than 0.0003. It is worth noting that even
344 in some regions where several methods present lower accuracies (e.g., GS, GSA, and PCA in the Jezero
345 Crater area), the accuracy is increased noticeably by using the DF-SSF method.

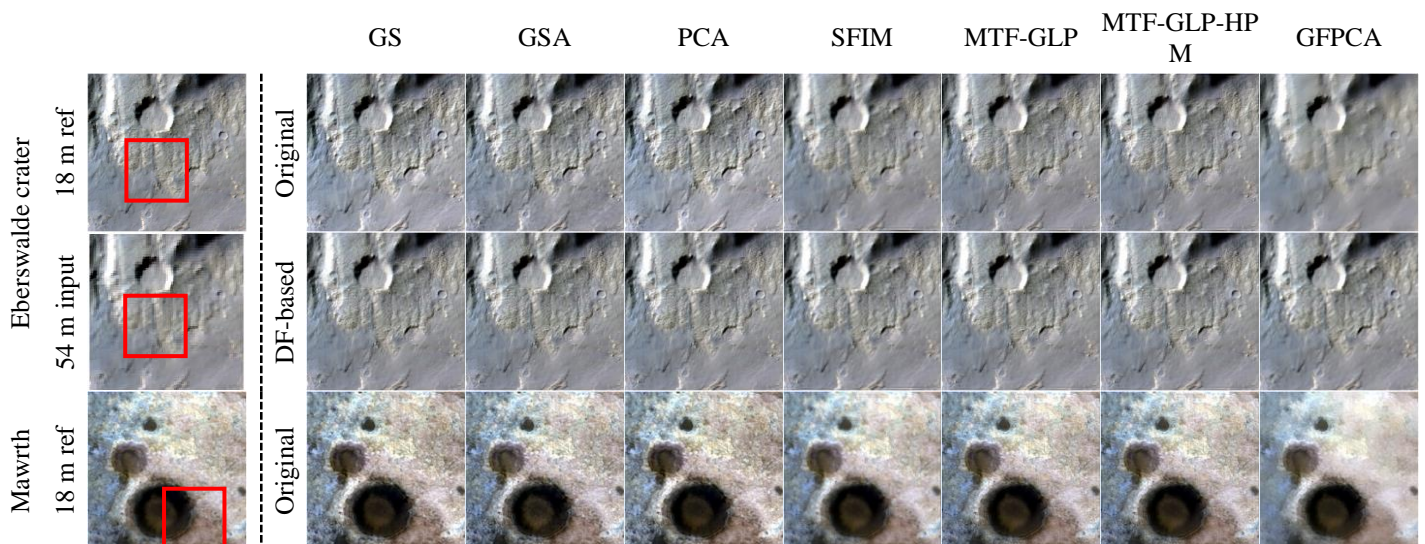
346 3) *The effect of band correlation*: Generally, spatial-spectral fusion methods perform better on bands that
347 have larger correlation with the panchromatic image. Fig. 7 presents the fusion accuracy (using CC as an
348 example) of various methods for all bands in the six regions (left) and also the relationship (in terms of CC)
349 between the original CTX data and CRISM hyperspectral bands (right). As shown in Fig. 7, the trend of all
350 curves in the left column is similar to that of the corresponding curves in the right column. Taking the
351 Eberswalde crater region as an example, in the right plot of Fig. 7(a), the first 20 bands present a smaller
352 correlation with the panchromatic image compared to other bands. Correspondingly, the fusion accuracy of
353 all methods for the first 20 bands in the left plot of Fig. 7(a) is relatively lower. The physical reason for this
354 phenomenon is that the first 20 bands are not completely covered by the panchromatic image. For the
355 remaining 50 bands in the visible range, the panchromatic image provides more correlated information for

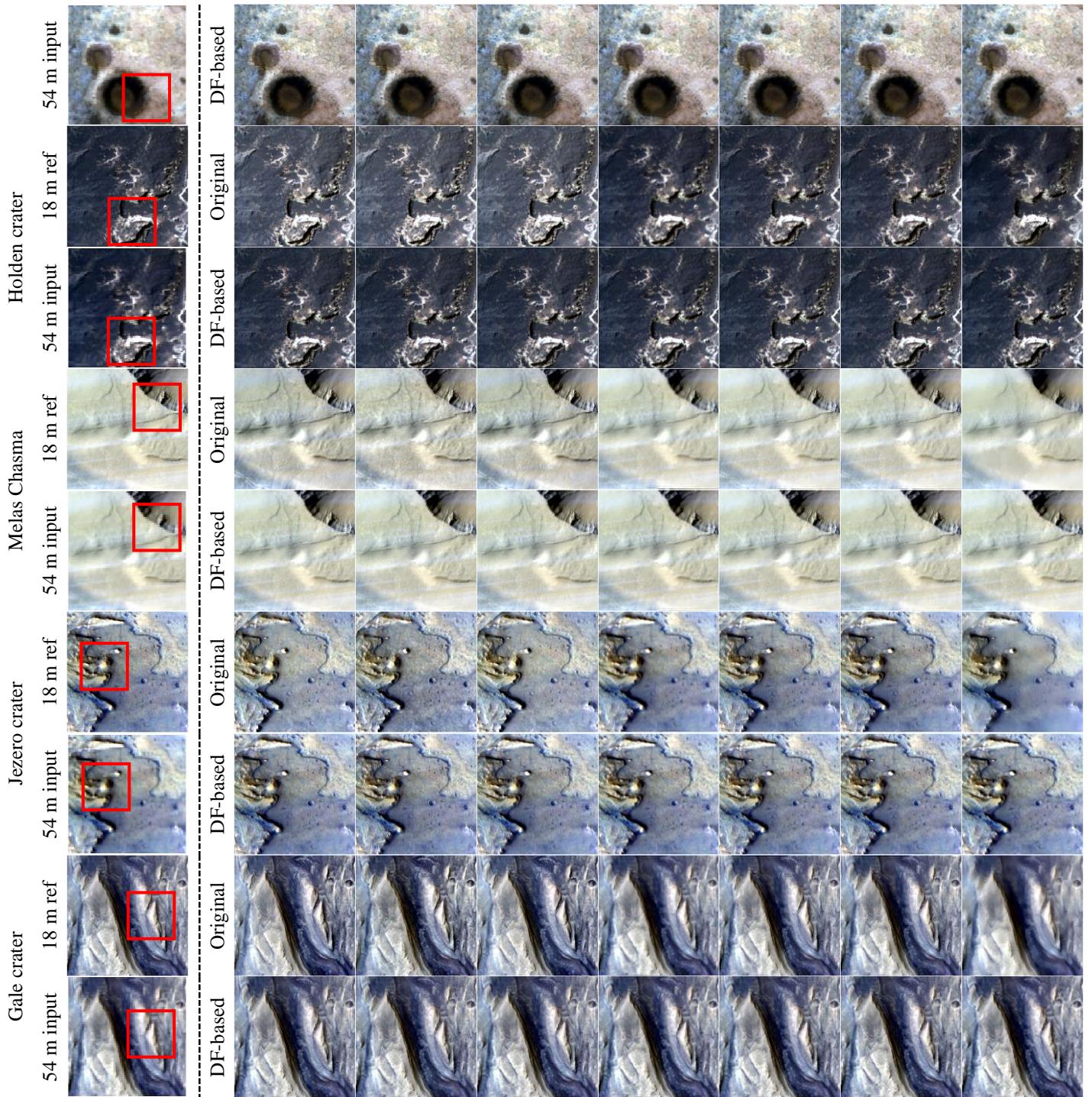
356 the fusion process, leading to more accurate fusion results.

357 4) *Coherence*: Coherence is an important indicator for evaluating the quality of the spatial-spectral fusion
358 results in terms of data fidelity. We degraded the 18 m spatial-spectral fusion results of various methods to 54
359 m, and compared them with the input 54 m CRISM hyperspectral data. Table 3 shows the overall coherence
360 (in terms of CC) assessment for all six regions. It can be seen clearly that the proposed DF-SSF model
361 achieves perfect coherence for all original methods, indicating its ability to preserve the original coarse data
362 completely. This advantage of DS-SSF lies in the perfect coherence property of ATPK, as demonstrated
363 mathematically in Section 3.4.

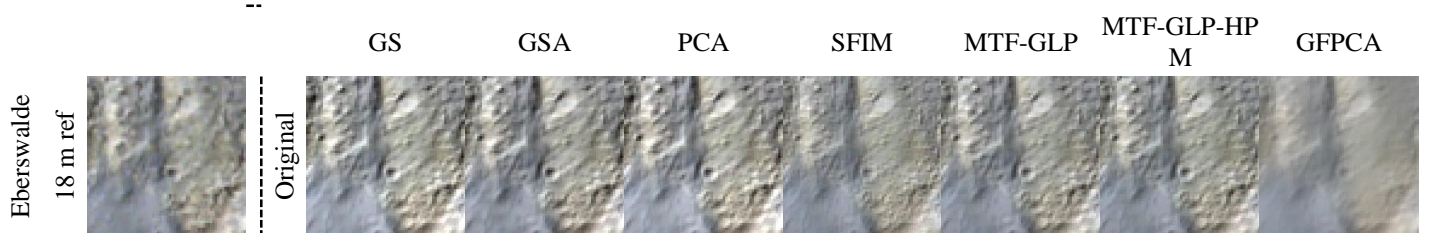
364 5) *Unsupervised deep learning-based fusion results*: We apply DF-SSF to Pan-GAN to validate its
365 applicability to the unsupervised deep learning method. Since the performance of deep learning-based
366 methods relies on the number of training data, different numbers of pairs (including 53, 28 and 14 pairs) of
367 CRISM and CTX images were considered for training, and DF-SSF was examined in all these cases. The
368 accuracy evaluation results are shown in Table 4. It can be seen that the spatial-spectral fusion accuracy of
369 the proposed DF-SSF method is consistently greater than that of the original methods in all cases. For
370 example, in the case of 53 pairs of training data, both CC and UIQI are increased by more than 0.0200, and
371 ERGAS is decreased by more than 0.1500. Moreover, when the number of training data decreases, the
372 accuracy of original Pan-GAN decreases correspondingly, but the advantage of DF-Pan-GAN is more
373 obvious. For example, for the Eberswalde Crater data, the CC gain of DF-Pan-GAN over Pan-GAN is around
374 0.07 in the case of 53 pairs, and the gain further increases to 0.10 in the case of 14 pairs. Therefore, the
375 proposed DF-SSF method is also effective for the unsupervised deep learning approach, even under various
376 numbers of training data.

377





378 Fig. 3. 18 m spatial-spectral fusion results (300×300 pixels) of the six regions (bands 37, 25 and 12 as RGB). The first and second
 379 rows of each region are the results of the original SSF and DF-SSF, respectively. The sub-areas marked in red are zoomed in Fig. 4.
 380



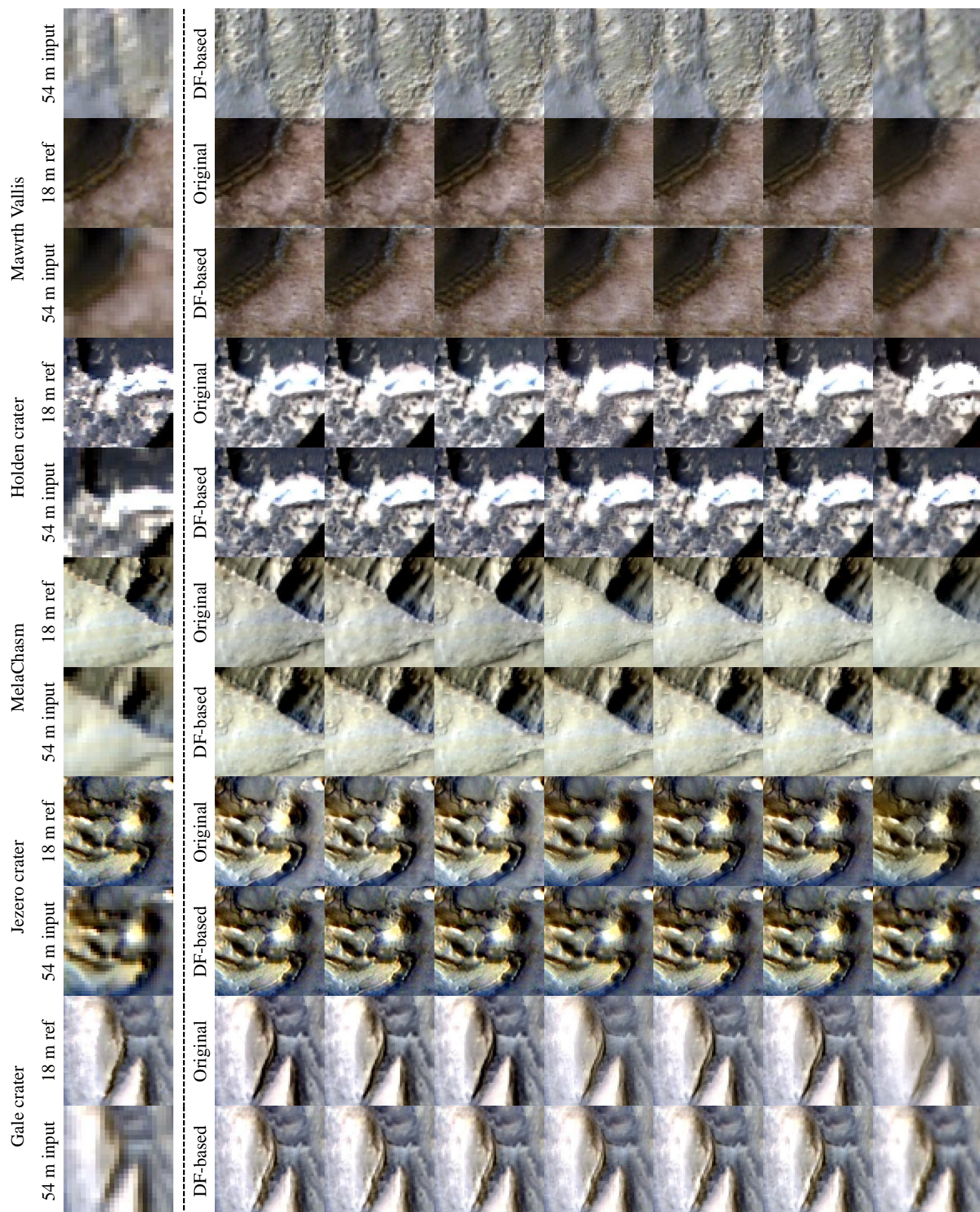


Fig. 4. The sub-areas of 18 m spatial-spectral fusion results in Fig. 3.

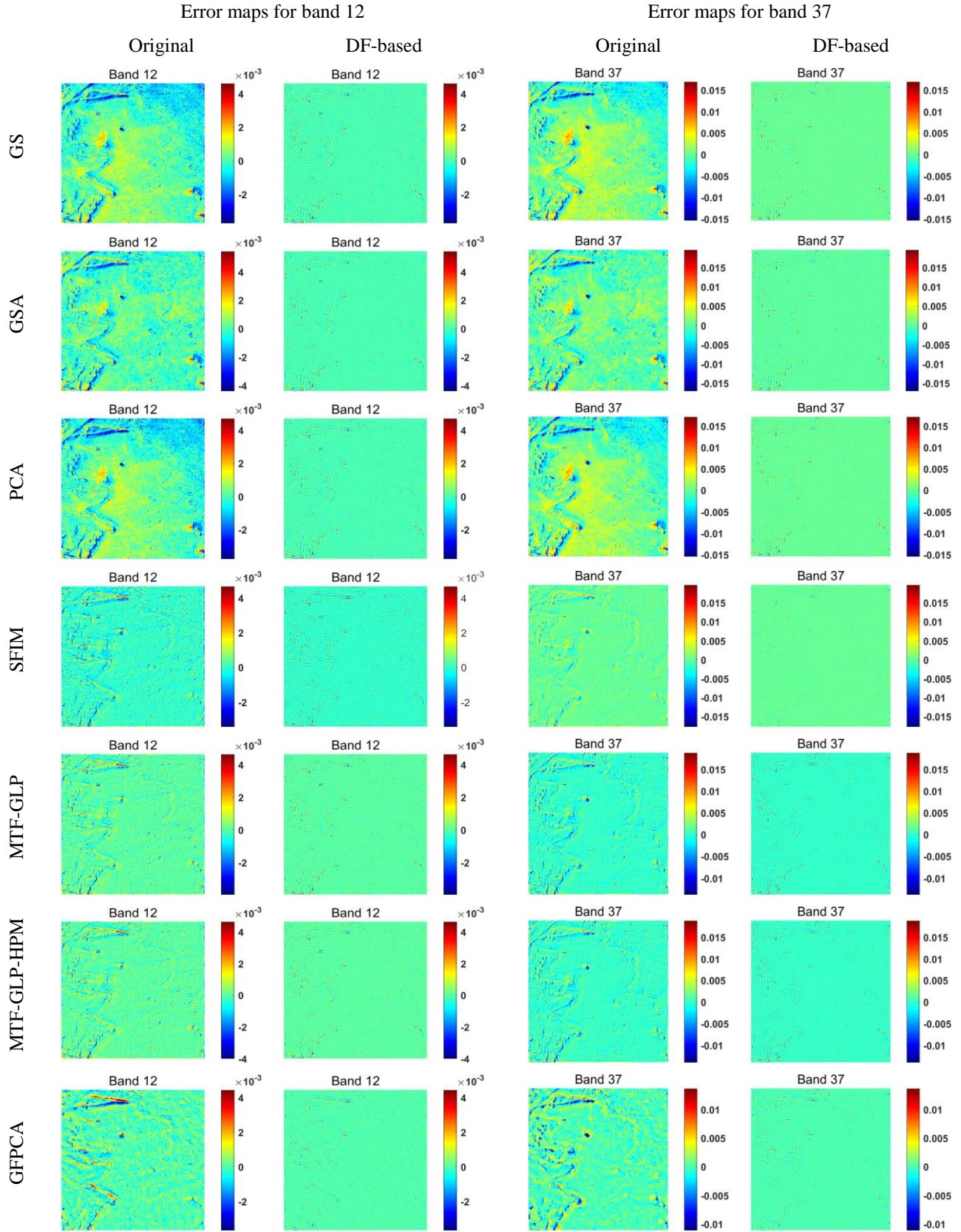
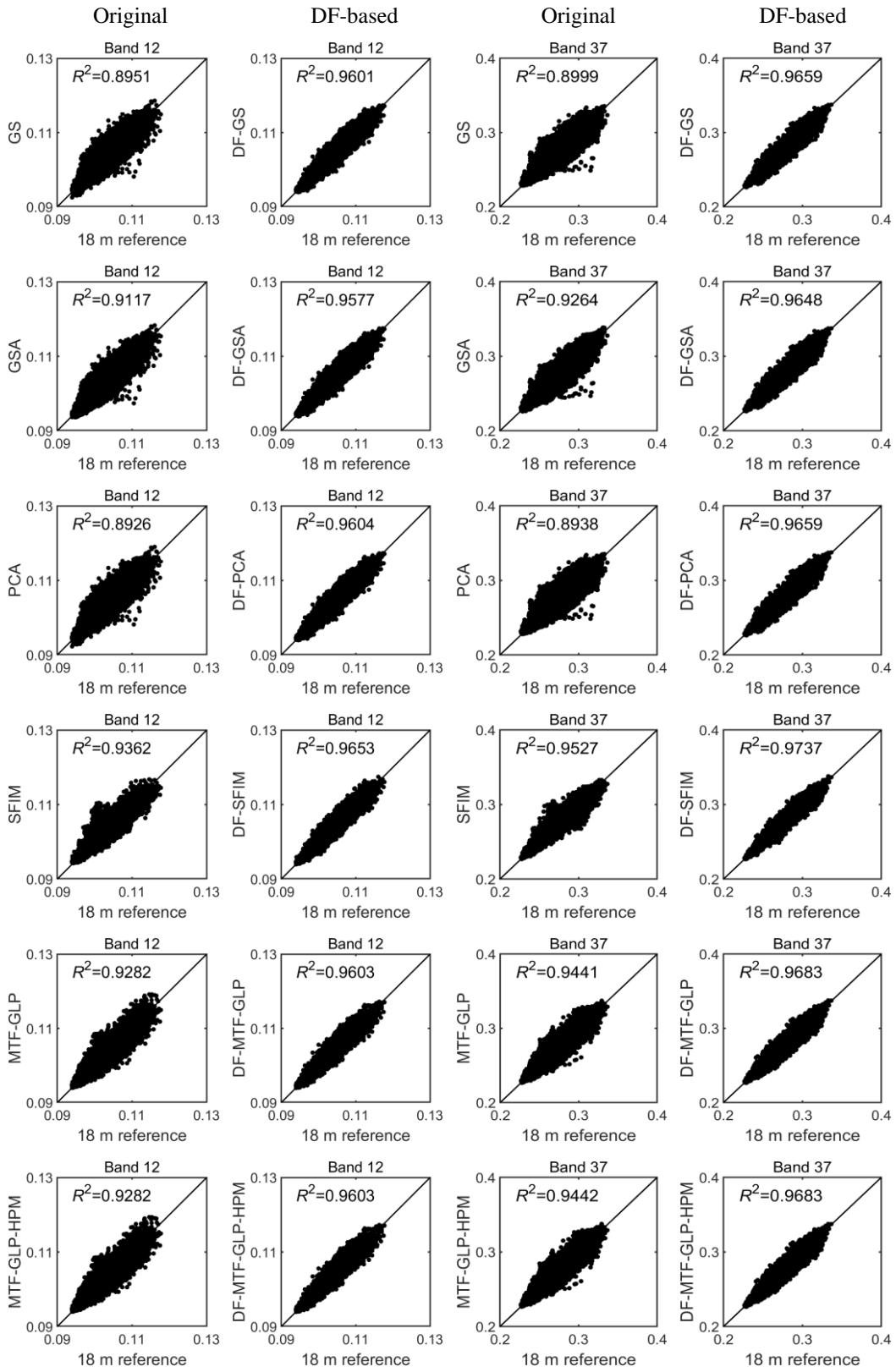


Fig. 5. Error maps for selected bands 12 and 37 in the Jezero crater region.

Table 2. Quantitative assessment of different spatial-spectral fusion methods for the six regions.

	Methods	CC		SAM		RMSE		ERGAS		UIQI	
		Original	DF-based	Original	DF-based	Original	DF-based	Original	DF-based	Original	DF-based
Eberswalde Crater	GS	0.8937	0.9654	0.0065	0.0051	0.0044	0.0025	1.3041	0.7638	0.8912	0.9654
	GSA	0.9264	0.9620	0.0062	0.0051	0.0038	0.0027	1.1300	0.8041	0.9260	0.9619
	PCA	0.8937	0.9655	0.0065	0.0051	0.0044	0.0025	1.3054	0.7638	0.8912	0.9654
	SFIM	0.9318	0.9682	0.0059	0.0050	0.0035	0.0024	1.0521	0.7252	0.9310	0.9682
	MTF-GLP	0.9317	0.9660	0.0060	0.0050	0.0036	0.0025	1.0685	0.7548	0.9317	0.9659
	MTF-GLP-HPM	0.9312	0.9656	0.0060	0.0051	0.0036	0.0025	1.0723	0.7603	0.9312	0.9655
	GFPCA	0.9561	0.9796	0.0063	0.0049	0.0029	0.0019	0.8602	0.5755	0.9505	0.9705
Mawrth Vallis	GS	0.9477	0.9817	0.0039	0.0027	0.0049	0.0029	0.7137	0.4203	0.9474	0.9816
	GSA	0.9598	0.9809	0.0035	0.0027	0.0043	0.0030	0.6266	0.4280	0.9597	0.9809
	PCA	0.9451	0.9817	0.0040	0.0027	0.0051	0.0029	0.7355	0.4204	0.9449	0.9817
	SFIM	0.9725	0.9851	0.0032	0.0025	0.0034	0.0026	0.4996	0.3721	0.9727	0.9851
	MTF-GLP	0.9686	0.9824	0.0033	0.0026	0.0038	0.0028	0.5543	0.4075	0.9686	0.9824
	MTF-GLP-HPM	0.9687	0.9825	0.0033	0.0026	0.0038	0.0028	0.5439	0.4072	0.9686	0.9824
	GFPCA	0.9734	0.9900	0.0037	0.0024	0.0033	0.0020	0.4861	0.2962	0.9722	0.9900
Holden Crater	GS	0.8701	0.9576	0.0127	0.0095	0.0105	0.0061	2.9637	1.7348	0.8632	0.9576
	GSA	0.8971	0.9540	0.0121	0.0097	0.0096	0.0064	2.7250	1.8149	0.8971	0.9540
	PCA	0.8702	0.9577	0.0129	0.0095	0.0105	0.0061	2.9659	1.7339	0.8635	0.9577
	SFIM	0.9104	0.9583	0.0113	0.0095	0.0088	0.0061	2.4776	1.7155	0.9067	0.9579
	MTF-GLP	0.9134	0.9576	0.0113	0.0095	0.0086	0.0061	2.4446	1.7303	0.9127	0.9575
	MTF-GLP-HPM	0.9131	0.9574	0.0113	0.0095	0.0087	0.0061	2.4520	1.7378	0.9123	0.9573
	GFPCA	0.9121	0.9656	0.0121	0.0092	0.0088	0.0055	2.4991	1.5544	0.8934	0.9650
Melas Chasma	GS	0.8938	0.9814	0.0036	0.0026	0.0059	0.0025	1.0204	0.4311	0.8930	0.9814
	GSA	0.9244	0.9803	0.0035	0.0027	0.0052	0.0026	0.9023	0.4455	0.9234	0.9803
	PCA	0.8974	0.9815	0.0036	0.0026	0.0058	0.0025	1.0036	0.4305	0.8967	0.9815
	SFIM	0.9636	0.9836	0.0031	0.0026	0.0034	0.0023	0.5984	0.4030	0.9635	0.9836
	MTF-GLP	0.9613	0.9820	0.0032	0.0026	0.0036	0.0024	0.6212	0.4227	0.9613	0.9820
	MTF-GLP-HPM	0.9615	0.9821	0.0032	0.0026	0.0035	0.0024	0.6191	0.4212	0.9618	0.9821
	GFPCA	0.9623	0.9897	0.0036	0.0026	0.0034	0.0018	0.6045	0.3176	0.9599	0.9897
Jezero Crater	GS	0.8077	0.9607	0.0029	0.0021	0.0023	0.0010	0.3687	0.1640	0.8052	0.9606
	GSA	0.8509	0.9543	0.0027	0.0021	0.0021	0.0011	0.3477	0.1783	0.8483	0.9541
	PCA	0.8068	0.9609	0.0029	0.0021	0.0023	0.0010	0.3719	0.1639	0.8048	0.9608
	SFIM	0.9377	0.9670	0.0023	0.0020	0.0012	0.0009	0.2030	0.1461	0.9362	0.9669
	MTF-GLP	0.9282	0.9618	0.0024	0.0020	0.0013	0.0010	0.2213	0.1593	0.9280	0.9617
	MTF-GLP-HPM	0.9281	0.9617	0.0024	0.0020	0.0013	0.0010	0.2216	0.1596	0.9278	0.9616
	GFPCA	0.9144	0.9744	0.0027	0.0020	0.0014	0.0007	0.2381	0.1253	0.9011	0.9742
Gale Crater	GS	0.9306	0.9793	0.0052	0.0033	0.0062	0.0034	1.0395	0.5700	0.9297	0.9793
	GSA	0.9471	0.9782	0.0045	0.0033	0.0054	0.0035	0.9186	0.5846	0.9470	0.9781
	PCA	0.9280	0.9794	0.0053	0.0033	0.0063	0.0034	1.0619	0.5702	0.9273	0.9793
	SFIM	0.9617	0.9819	0.0040	0.0031	0.0045	0.0031	0.7651	0.5258	0.9612	0.9819
	MTF-GLP	0.9590	0.9801	0.0042	0.0032	0.0047	0.0033	0.7987	0.5535	0.9590	0.9801
	MTF-GLP-HPM	0.9588	0.9800	0.0042	0.0032	0.0047	0.0033	0.8013	0.5560	0.9588	0.9800
	GFPCA	0.9697	0.9873	0.0042	0.0029	0.0041	0.0026	0.6934	0.4349	0.9665	0.9872



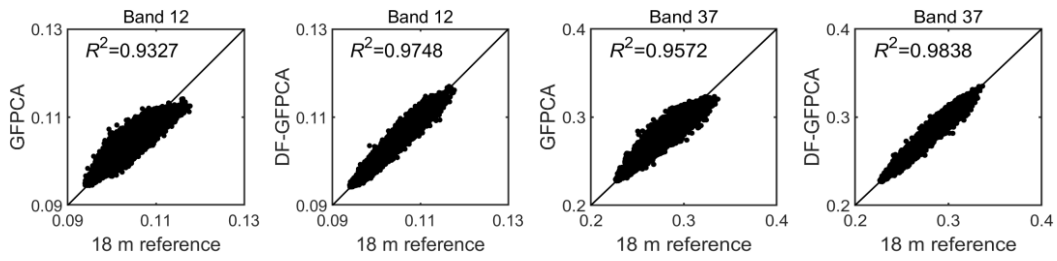
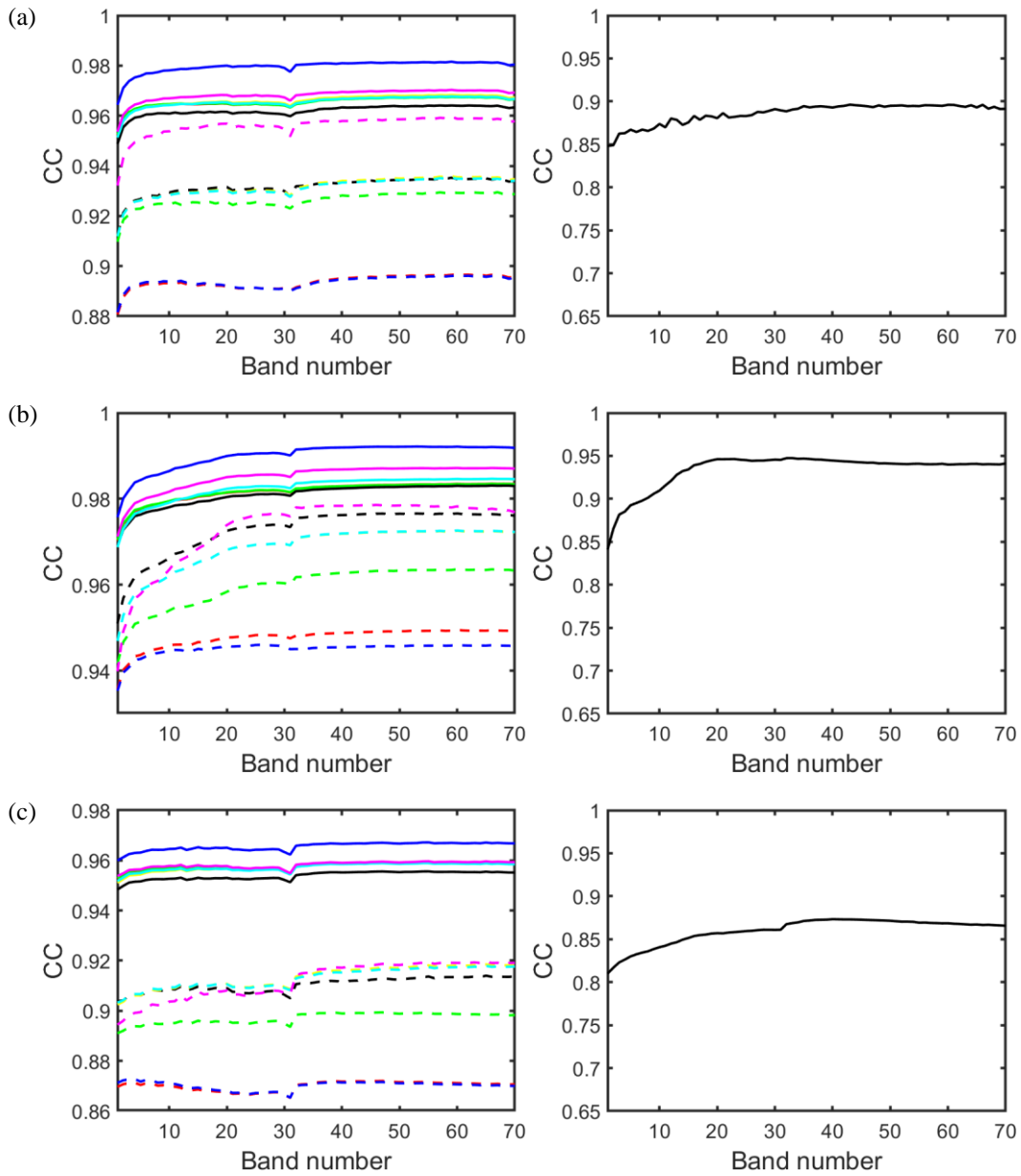


Fig. 6. Scatterplots of predicted against actual coarse pixel values (18 m) in the Mawrth Vallis region.



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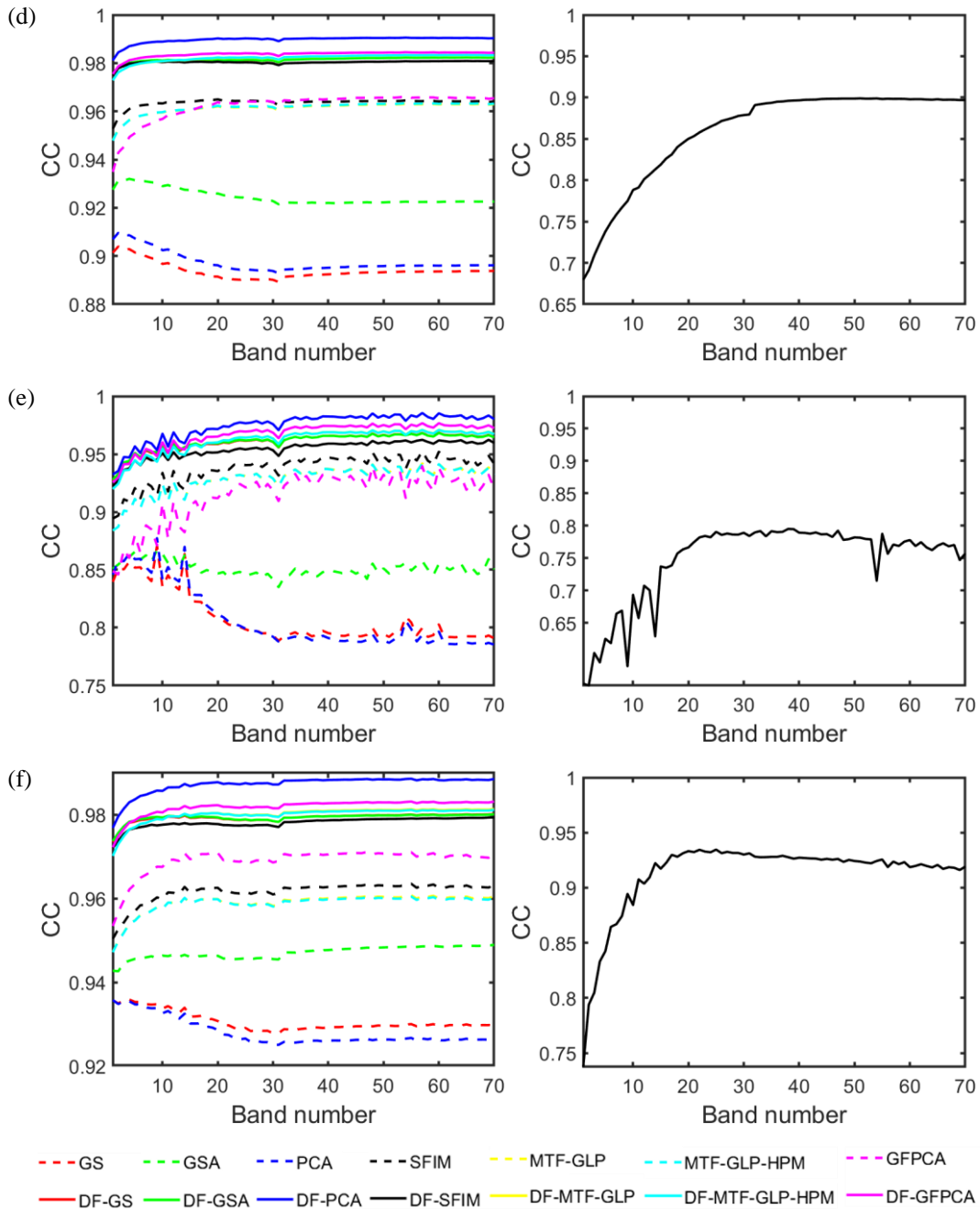


Fig. 7. The spatial-spectral fusion accuracy (in terms of CC) of each band (left) and relation (in terms of CC) between the panchromatic (degraded) and hyperspectral bands (right) for the six regions. (a) Eberswalde crater. (b) Mawrth Vallis. (c) Holden crater. (d) Melas Chasma. (e) Jezero crater. (f) Gale crater.

Table 3. Evaluation (in terms of CC) of the data fidelity ability of the 18 m spatial-spectral fusion results for the six regions.

		Eberswalde crater	Mawrth Vallis	Holden crater	Melas Chasma	Jezero crater	Gale crater
GS	Original	0.9397	0.9760	0.9319	0.9285	0.8611	0.9634
	DF-based	0.9998	0.9999	0.9997	0.9998	0.9997	0.9999
GSA	Original	0.9763	0.9885	0.9616	0.9584	0.9144	0.9808
	DF-based	0.9998	0.9999	0.9997	0.9998	0.9996	0.9999
PCA	Original	0.9395	0.9732	0.9311	0.9320	0.8591	0.9591
	DF-based	0.9998	0.9999	0.9997	0.9998	0.9997	0.9999
SFIM	Original	0.9771	0.9934	0.9714	0.9878	0.9833	0.9884

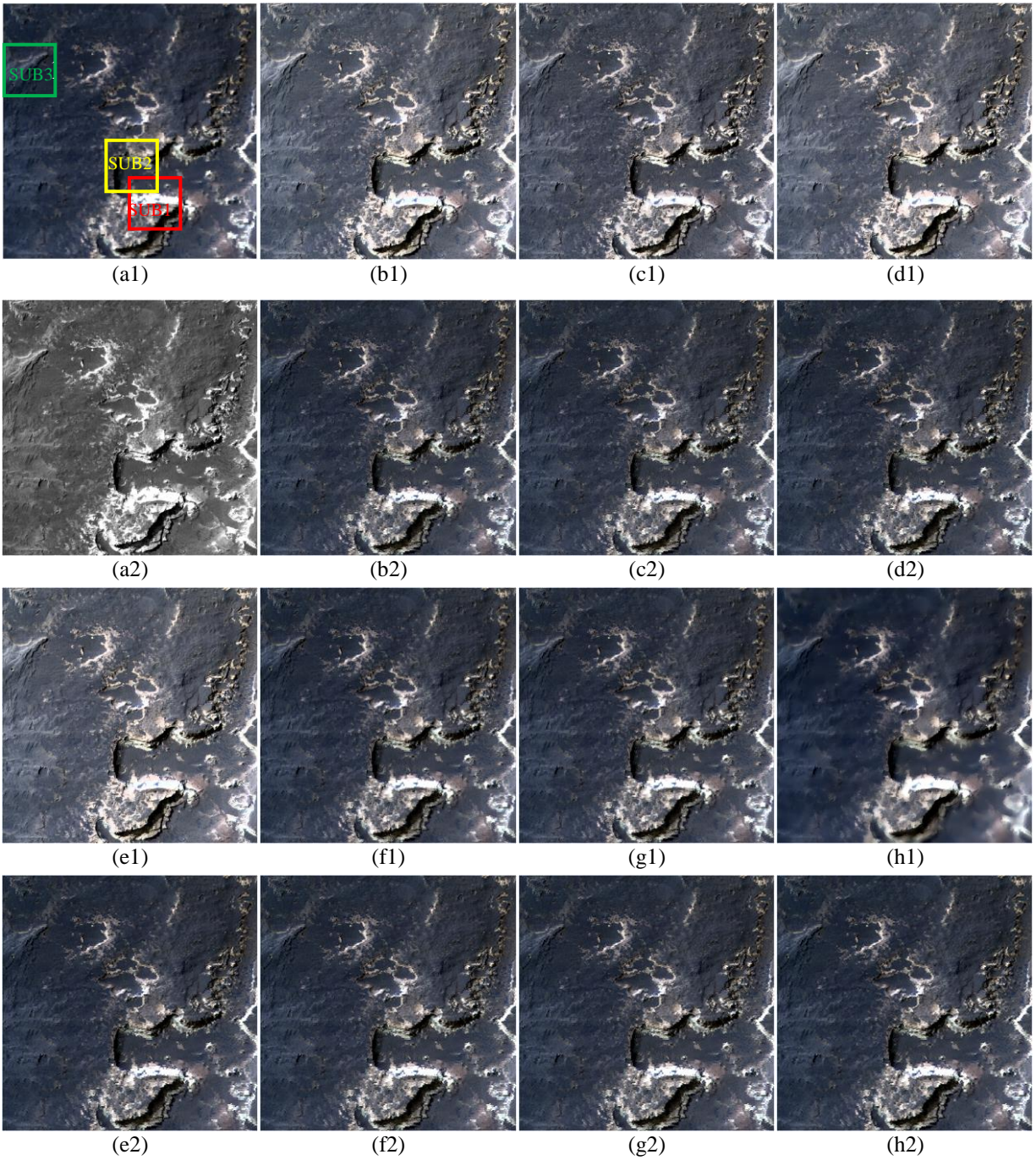
MTF-GLP	DF-based	0.9998	0.9999	0.9997	0.9999	0.9999	0.9999
	Original	0.9794	0.9934	0.9738	0.9886	0.9818	0.9887
MTF-GLP-HPM	DF-based	0.9998	0.9999	0.9998	0.9999	0.9998	0.9999
	Original	0.9795	0.9934	0.9738	0.9886	0.9818	0.9887
GFPCA	DF-based	0.9998	0.9999	0.9997	0.9999	0.9998	0.9999
	Original	0.9884	0.9909	0.9663	0.9833	0.9597	0.9914
	DF-based	0.9999	0.9999	0.9997	0.9999	0.9998	0.9999

Table 4. Quantitative assessment of the unsupervised deep learning method (Pan-GAN) for the six regions.

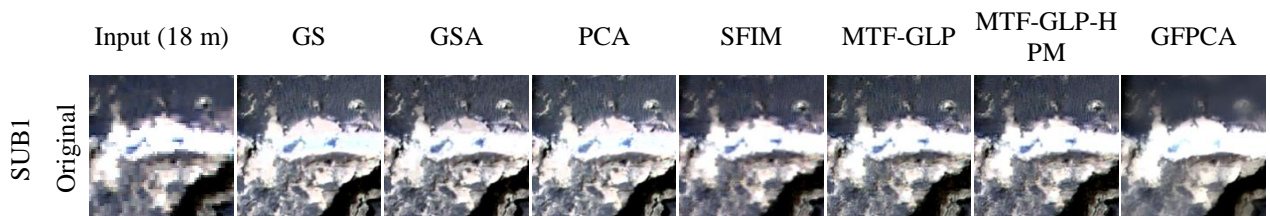
Regions	CC		SAM		RMSE		ER GAS		UIQI		
	Original	DF-based	Original	DF-based	Original	DF-based	Original	DF-based	Original	DF-based	
53 pairs of training data	Eberswalde Crater	0.9057	0.9756	0.0093	0.0044	0.0049	0.0022	1.4642	0.6674	0.8981	0.9753
	Mawrth Vallis	0.9716	0.9934	0.0029	0.0012	0.0037	0.0016	0.5531	0.2396	0.9689	0.9933
	Holden Crater	0.9424	0.9843	0.0150	0.0087	0.0082	0.0038	2.3353	1.0794	0.9361	0.9840
	Melas Chasma	0.9596	0.9919	0.0034	0.0013	0.0040	0.0016	0.6958	0.2867	0.9570	0.9919
	Jezero Crater	0.9463	0.9874	0.0227	0.0007	0.0016	0.0006	0.2773	0.0979	0.9318	0.9871
	Gale Crater	0.9468	0.9880	0.0042	0.0019	0.0056	0.0023	0.9637	0.3952	0.9389	0.9878
28 pairs of training data	Eberswalde Crater	0.8986	0.9736	0.0094	0.0048	0.0054	0.0024	1.6128	0.7143	0.8845	0.9729
	Mawrth Vallis	0.9609	0.9899	0.0036	0.0015	0.0045	0.0020	0.6515	0.2955	0.9578	0.9897
	Holden Crater	0.9363	0.9806	0.0156	0.0088	0.0090	0.0044	2.3837	1.7723	0.9315	0.9802
	Melas Chasma	0.9524	0.9881	0.0036	0.0015	0.0046	0.0018	0.7861	0.3039	0.9517	0.9880
	Jezero Crater	0.9393	0.9800	0.0236	0.0009	0.0018	0.0008	0.3008	0.1203	0.9177	0.9795
	Gale Crater	0.9449	0.9864	0.0047	0.0022	0.0057	0.0025	0.9720	0.4233	0.9360	0.9861
14 pairs of training data	Eberswalde Crater	0.8609	0.9632	0.0117	0.0061	0.0063	0.0028	1.8772	0.8310	0.8450	0.9625
	Mawrth Vallis	0.9491	0.9852	0.0044	0.0022	0.0049	0.0023	0.7235	0.3486	0.9449	0.9848
	Holden Crater	0.9349	0.9763	0.0169	0.0100	0.0091	0.0046	2.4019	2.0302	0.9279	0.9740
	Melas Chasma	0.9510	0.9874	0.0044	0.0021	0.0054	0.0021	0.7879	0.3616	0.9509	0.9872
	Jezero Crater	0.9297	0.9795	0.0216	0.0013	0.0023	0.0015	0.3196	0.1439	0.9269	0.9732
	Gale Crater	0.9439	0.9847	0.0047	0.0028	0.0058	0.0025	1.0006	0.4401	0.9354	0.9841

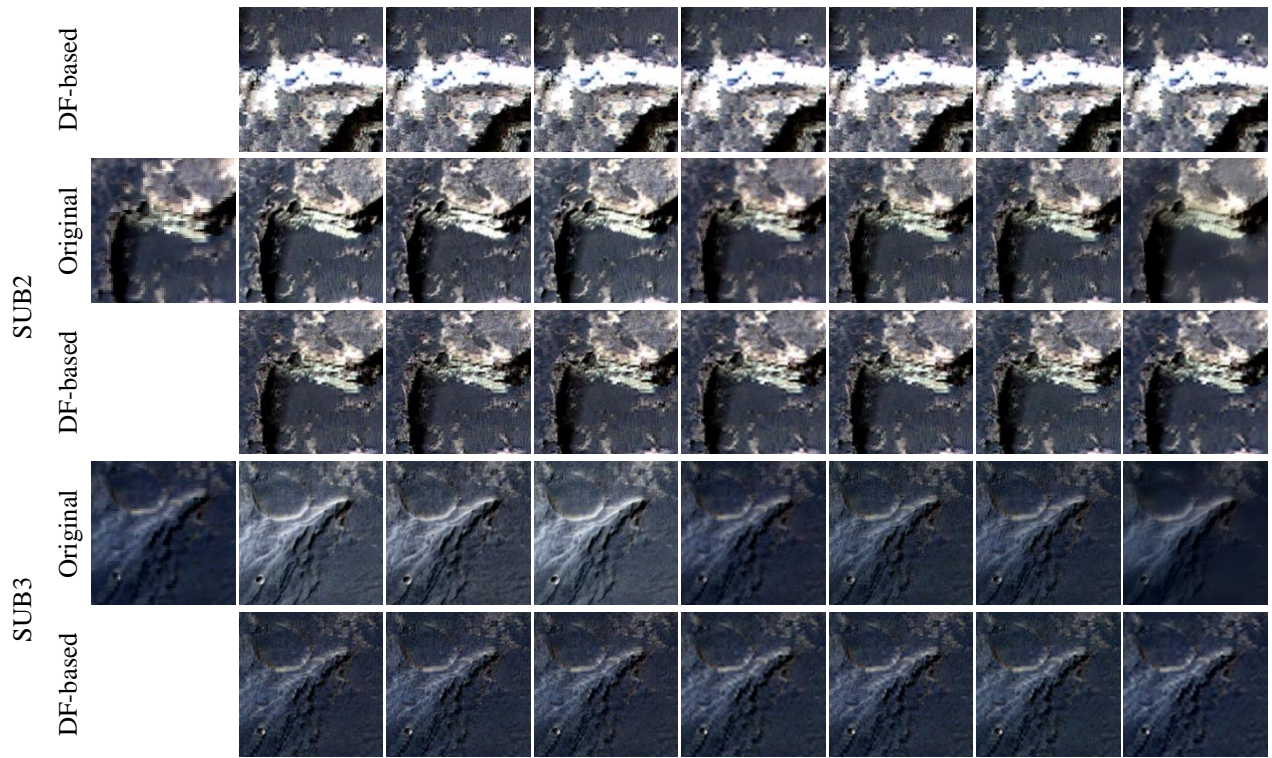
4.3. 6 m fusion results

In this set of experiments, the original fusion and DF-SSF methods were used for spatial-spectral fusion of the original 18 m CRISM hyperspectral data and 6 m CTX panchromatic data, to create 6 m CRISM hyperspectral images. The Gaussian PSF with a convolution kernel parameter of 0.5 was used. The 6 m fusion results for the Holden crater are shown in Figs. 8 and 9, while the results for the Gale crater regions are shown in Figs. 10 and 11. Note that Figs. 9 and 11 show the zoom images of three sub-regions in Figs. 8 and 10, respectively. It is evident that the 6 m CRISM images are visually more pleasant, which present more spatial details. Furthermore, the 6 m DF-SSF results are more similar in color to the original 18 m images, indicating greater data fidelity. Table 5 provides the coherence evaluation results for the Holden Crater and Gale Crater regions. It is apparent that the data fidelity of the seven methods is increased using the proposed model (e.g., the coherence is increased by at least 0.0080).

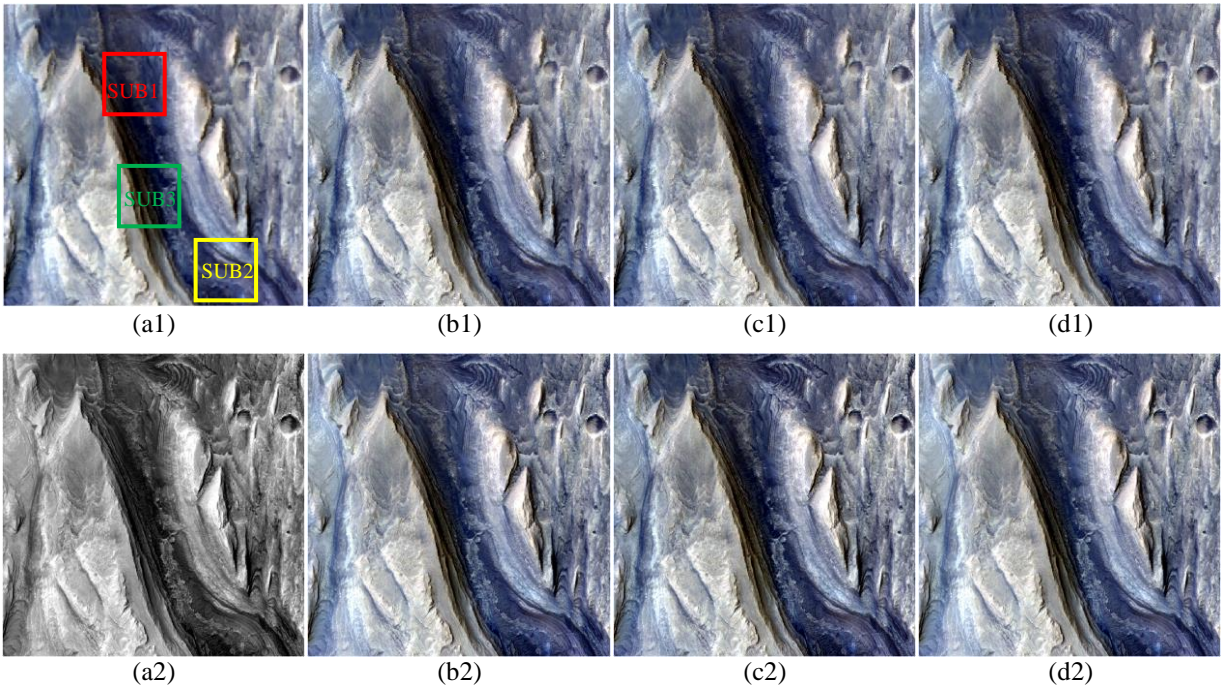


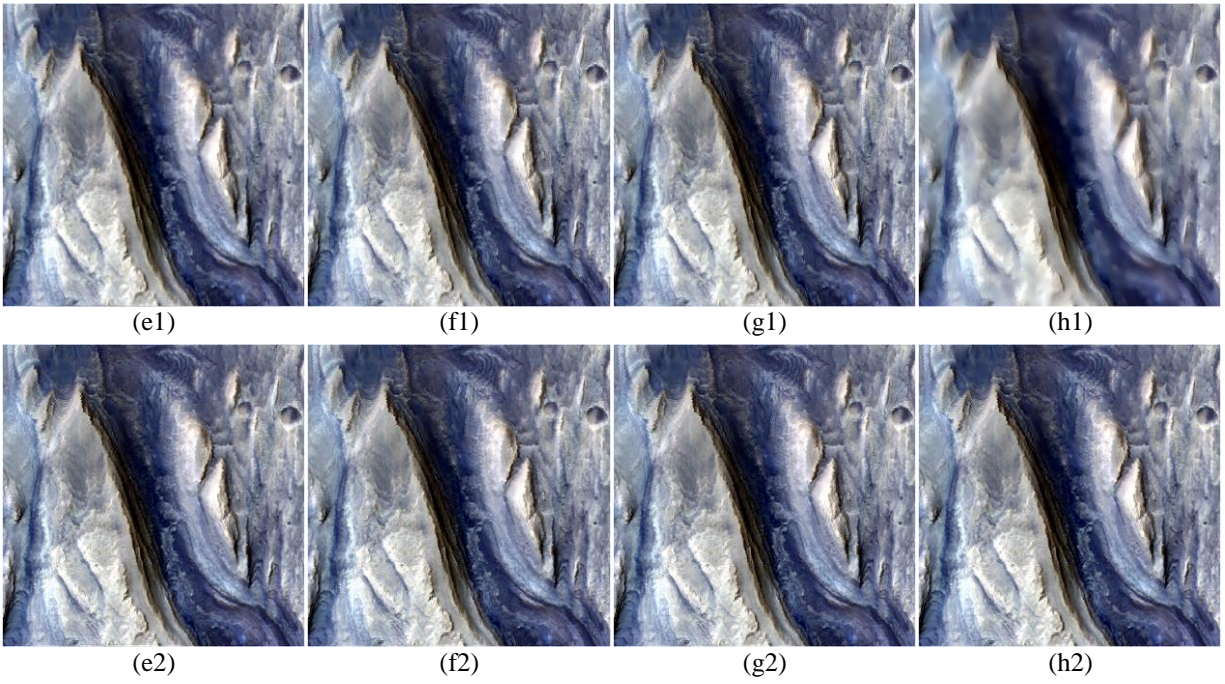
415 Fig. 8. 6 m spatial-spectral fusion results for the Holden crater region (bands 37, 25 and 12 as RGB). The sizes of the panchromatic
 416 and hyperspectral images are 900×900 and 300×300, respectively. (a1) 18 m CRISM. (a2) 6 m CTX. (b1)-(h1) show the results of
 417 the original SSF, while (b2)-(h2) show the corresponding results of DF-SSF. (b) GS. (c) GSA. (d) PCA. (e) SFIM. (f) MTF-GLP. (g)
 418 MTF-GLP-HPM. (h) GFPCA.
 419





420 Fig. 9. 6 m spatial-spectral fusion results of the three sub-areas in Fig. 8. The first row of each sub-area shows the results of
 421 original SSF and the second row shows the results of DF-SSF.
 422





423 Fig. 10. 6 m spatial-spectral fusion results for the Gale crater region (bands 37, 25 and 12 as RGB). The sizes of the panchromatic
 424 and hyperspectral images are 900×900 and 300×300, respectively. (a1) 18 m CRISM. (a2) 6 m CTX. (b1)-(h1) show the results of
 425 the original SSF, while (b2)-(h2) show the corresponding results of DF-SSF. (b) GS. (c) GSA. (d) PCA. (e) SFIM. (f) MTF-GLP. (g)
 426 MTF-GLP-HPM. (h) GFPCA.
 427

	Input (18 m)	GS	GSA	PCA	SFIM	MTF-GLP	MTF-GLP-HPM	GFPCA
SUB1	Original							
	DF-based							
SUB2	Original							
	DF-based							
SUB3	Original							

DF-based

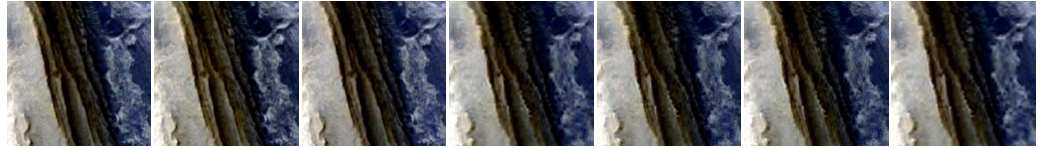


Fig. 11. 6 m spatial-spectral fusion results of the three sub-areas in Fig. 10. The first row of each sub-area shows the results of original SSF and the second row shows the results of DF-SSF.

Table 5. Evaluation (in terms of CC) of the data fidelity ability of the 6 m spatial-spectral fusion results for the Holden crater region and the Gale crater region.

	Holden crater		Gale crater	
	Original	DF-based	Original	DF-based
GS	0.8739	0.9993	0.9325	0.9997
GSA	0.8960	0.9992	0.9475	0.9997
PCA	0.8745	0.9993	0.9300	0.9997
SFIM	0.9796	0.9997	0.9929	0.9999
MTF-GLP	0.9789	0.9996	0.9917	0.9999
MTF-GLP-HPM	0.9786	0.9996	0.9917	0.9999
GFPCA	0.9521	0.9995	0.9808	0.9998

5. Discussion

5.1. Uncertainty in spatial-spectral fusion of CRISM and CTX images

While the experiments validated the effectiveness of fusing CTX and CRISM hyperspectral data, there still exists uncertainty in the fusion process.

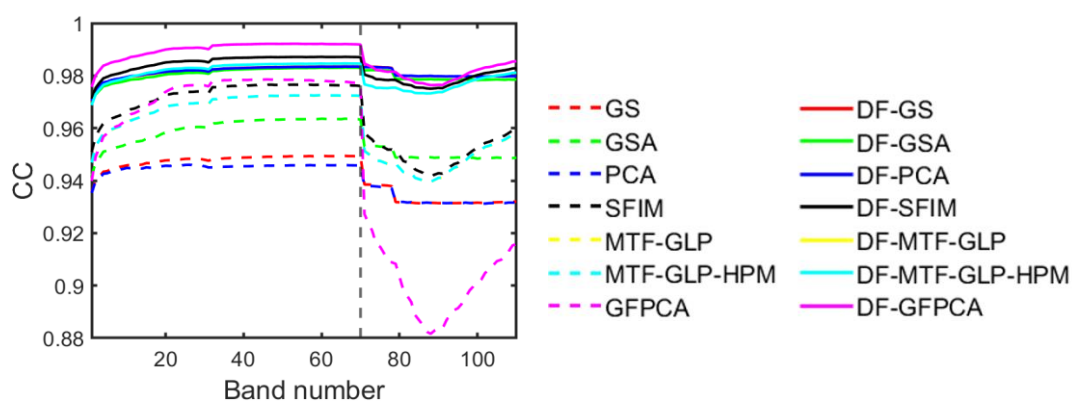
Spectrally, uncertainty may be introduced if the spectral ranges of CTX image and CRISM hyperspectral images do not match, especially for hyperspectral bands that are not covered by the spectral range of the CTX panchromatic image (as shown in the fusion accuracy of the first 20 bands in Fig. 7). Therefore, the spectral overlap between the CTX image and the CRISM hyperspectral image should be considered before spatial-spectral fusion. Since the CTX image contains only one visible band, while the CRISM image contains both visible and infrared bands, to mitigate the uncertainty in the experiments, only the first 70 bands of CRISM that roughly match with the CTX spectral coverage were considered. For further analysis of the uncertainty, we evaluated the fusion accuracy for the 71st to the 110th bands of the CRISM hyperspectral data in the Mawrth Vallis region. The results are shown in Fig. 12. It is seen clearly that when there is no spectral overlap between CTX and CRISM hyperspectral images (e.g., for the 71st to the 110th bands), the fusion accuracy decreases obviously, especially for the original version without the consideration of DF.

Temporally, it is important to ensure that the CTX and CRISM data were observed at the same time. In

453 practice, due to many factors (e.g., shooting time, camera operating mode, etc.), it can sometimes be
 454 challenging to obtain CTX and CRISM data for the same area at the same time. When there is a significant
 455 time gap, there may be certain changes in Martian surface between the two datasets (e.g., the formation of
 456 new impact craters on the Martian surface due to recent impact events), which may lead to uncertainties in
 457 the fusion process.

458 Spatially, accurate geometric registration is a crucial prerequisite for spatial-spectral fusion. When fusing
 459 CTX images with CRISM hyperspectral images, it is essential to consider fully the geometric registration
 460 accuracy between the two datasets. Although reliable registration was performed between the CTX and
 461 CRISM data in this study, it is worth noting that the registration accuracy may not be perfect, which can also
 462 introduce some uncertainties.

463



464 Fig.12. Quantitative assessment (in terms of CC) of the spatial-spectral fusion methods for bands 1 to 110 (the Mawrth Vallis
 465 region as an example).
 466

467 5.2. Advantages of using ATPK in DF-SSF

468

469 The use of ATPK in DF-SSF lies in the appealing advantage of maintaining completely the original coarse
 470 data. To analyze the advantages of ATPK in residual downscaling in DF-SSF, we selected the bicubic
 471 interpolation (BI) method to downscale the residuals in existing spatial-spectral fusion methods and
 472 compared it with the proposed method. BI offers a good balance between accuracy and computational
 473 complexity and has been used widely in various studies, but it cannot preserve the original data perfectly. The
 474 experimental results are shown in Table 6. It is evident that the proposed method produces more accurate
 475 fusion results in all cases. This illustrates directly the benefit of achieving complete data fidelity in
 476 spatial-spectral fusion. Note that in existing studies, some methods were also designed with the objective to
 477 achieve data fidelity, such as the VO-based methods. Mathematically, however, they can only approach the
 478 original coarse images gradually to achieve approximate fidelity. This is different from ATPK, which can

479 achieve data fidelity in the true mathematical sense.

480

481 Table 6. Comparison between the use of bicubic interpolation (BI) and ATPK (i.e., the proposed method) for residual downscaling
 482 in spatial-spectral fusion (the Eberswalde crater region as an example).

	CC		SAM		RMSE		ERGAS		Coherence	
	BI-based	DF-based	BI-based	DF-based	BI-based	DF-based	BI-based	DF-based	BI-based	DF-based
GS	0.9592	0.9654	0.0053	0.0051	0.0028	0.0025	0.8304	0.7638	0.9983	0.9998
GSA	0.9554	0.9620	0.0054	0.0051	0.0029	0.0027	0.8767	0.8041	0.9980	0.9998
PCA	0.9592	0.9655	0.0053	0.0051	0.0028	0.0025	0.8304	0.7638	0.9983	0.9998
SFIM	0.9625	0.9682	0.0053	0.0050	0.0026	0.0024	0.7832	0.7252	0.9981	0.9998
MTF-GLP	0.9590	0.9660	0.0053	0.0050	0.0028	0.0025	0.8258	0.7548	0.9981	0.9998
MTF-GLP-HPM	0.9585	0.9656	0.0053	0.0051	0.0028	0.0025	0.9312	0.7603	0.9981	0.9998
GFPCA	0.9745	0.9796	0.0052	0.0049	0.0021	0.0019	0.6452	0.5755	0.9984	0.9999

483

484 5.3. DF-SSF vs ATPRK

485

486 In ATPRK, the fusion process is achieved by two steps: regression modeling and ATPK-based residual
 487 downscaling. The regression part links the coarse multi/hyperspectral image and fine panchromatic image
 488 through a linear fitting process, and the ATPK part downscales the coarse residuals in the regression process
 489 to the target fine spatial resolution. However, the relation between multi/hyperspectral and panchromatic
 490 images is sometimes complicated, which may not be characterized accurately by a simple linear model. As a
 491 result, the residuals of the regression model may be large, and the uncertainty introduced into the predictions
 492 of post-ATPK may be correspondingly large. As an alternative, the DF-SSF method proposed in this paper
 493 uses any of the existing spatial-spectral fusion method as the first step (i.e., instead of the regression step in
 494 ATPRK). To analyze the influence of magnitude of the residuals in the methods, Table 7 presents the
 495 quantification of coarse residuals for various spatial-spectral fusion methods and the regression part of
 496 ATPRK (in terms of the RMSE), while Table 8 compares the accuracy between DF-SSF and ATPRK. It can
 497 be observed that the RMSE of the regression part of ATPRK is larger than that of the existing spatial-spectral
 498 fusion methods and the accuracy is generally smaller than the DF-SSF-based methods. This suggests that the
 499 DF-SSF method can take full advantage of existing spatial-spectral fusion methods by using them as the
 500 primary step to reduce the coarse residuals, which is more competitive than the regression step in ATPRK.

501

502 Table 7. RMSE of the seven spatial-spectral fusion methods and regression modeling of ATPRK (R-ATPRK) for the Gale crater
 503 region.

	GS	GSA	PCA	SFIM	MTF-GLP	MTF-GLP -HPM	GFPCA	R-ATPRK
RMSE	0.0062	0.0054	0.0063	0.0045	0.0047	0.0047	0.0041	0.1864

504

505

506

Table 8. Accuracy evaluation of DF-SSF and ATPRK for the Gale crater region.

Methods	CC	SAM	RMSE	ERGAS	UIQI
DF-GS	0.9793	0.0033	0.0034	0.5700	0.9793
DF-GSA	0.9782	0.0033	0.0035	0.5846	0.9781
DF-PCA	0.9794	0.0033	0.0034	0.5702	0.9793
DF-SFIM	0.9819	0.0031	0.0031	0.5258	0.9819
DF-MTF-GLP	0.9801	0.0032	0.0033	0.5535	0.9801
DF-MTF-GLP-HPM	0.9800	0.0032	0.0033	0.5560	0.9800
DF-GFPCA	0.9873	0.0029	0.0026	0.4349	0.9872
ATPRK	0.9785	0.0033	0.0034	0.5792	0.9785

507

508 5.4. Generalization ability of DF-SSF

509

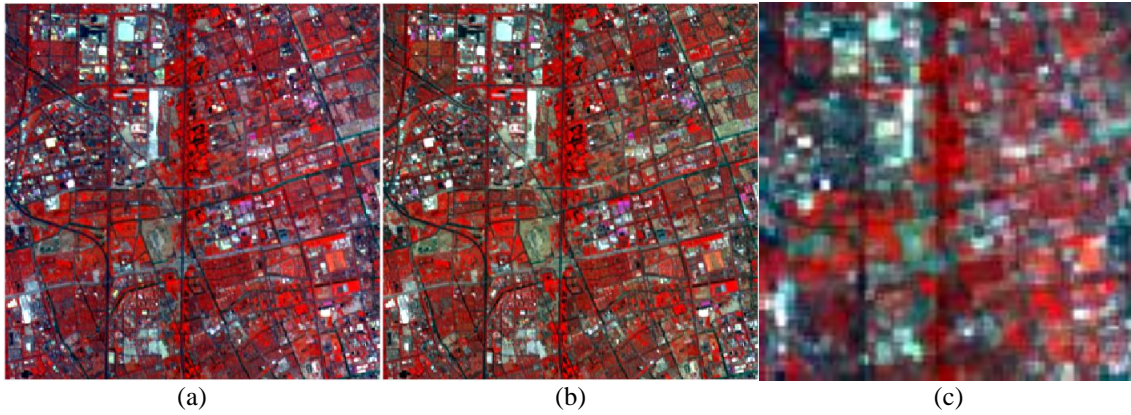
510 In this paper, DF-SSF was proposed for Mars remote sensing data with complex surface configurations
511 and examined on seven classical spatial-spectral fusion methods of CS and MRA and also an unsupervised
512 deep learning-based method. By applying the DF-SSF model to these methods, the fusion accuracy is
513 increased noticeably, demonstrating the generalization ability of DF-SSF for existing methods. In this section,
514 we also further examined the generalization ability of DF-SSF from three aspects: 1) extension to
515 spatial-spectral fusion of Earth observation data, 2) extension to the more challenging fusion of hyperspectral
516 and multispectral images and 3) application to more fusion methods. Accordingly, a GF-5 hyperspectral
517 dataset covering an urban area in Shanghai, China was used. The spatial resolution is 30 m. The spatial size is
518 300×300 pixels, and the number of VNIR bands used is 150. A four-band 30 m multispectral image was
519 synthesized by averaging 37 (or 38) consecutive bands of the 150 bands. Moreover, a 120 m coarse
520 hyperspectral image was simulated by spatially degrading the 30 m hyperspectral image with a zoom factor
521 of four. The three images of the study area are shown in Fig. 13. The task is to fuse the 120 m hyperspectral
522 image with the four-band, 30 m multispectral image to reconstruct the 30 m hyperspectral image. For CS and
523 MRA-based methods, two types of schemes (i.e., the selected band and synthesized band schemes) were
524 considered for using multiple bands of the 30 m multispectral image (Butera et al., 2015). In addition, the
525 matrix factorization (i.e., CNMF) method was also examined. The accuracy evaluation results are exhibited
526 in Table 9. It is clear that the accuracy is increased by using the DF-SSF method. This indicates that the
527 method proposed in this paper is also applicable to the three cases listed above.

528

529 In future, DF-SSF can be applied to more up-to-date spatial-spectral fusion methods. For example,
530 supervised learning-based spatial-spectral fusion methods have received increasing attention in recent years
531 (Sun et al., 2021; Ren et al., 2022). Such methods require a large amount of training data (particularly for
532 deep learning-based versions), which is harder to obtain for the Mars remote sensing data studied in this
paper, thus, preventing validation of these methods. In future research, the generalization ability of DF-SSF

533 for supervised learning-based spatial-spectral fusion methods can be investigated based on Earth observation
 534 data.

535



536 Fig. 13. The GF-5 hyperspectral image used for test. (a) 30 m GF-5 hyperspectral image (300×300 pixels; bands 150, 39 and 3 as
 537 RGB). (b) 30 m multispectral image (300×300 pixels; bands 4, 2 and 1 as RGB) simulated by degrading (a) spectrally. (c) 120 m
 538 hyperspectral images (75×75 pixels; bands 150, 39 and 3 as RGB) simulated by degrading (a) spatially.

539

540

Table 9. Quantitative assessment of the spatial-spectral fusion methods for the GF-5 data set.

Methods	CC		SAM		RMSE		ERGAS		UIQI		
	Original	DF-based	Original	DF-based	Original	DF-based	Original	DF-based	Original	DF-based	
Selected band	GS	0.8992	0.9447	0.0468	0.0352	0.0115	0.0072	2.5827	1.7943	0.8578	0.9300
	GSA	0.9957	0.9965	0.0176	0.0160	0.0020	0.0018	0.4954	0.4451	0.9955	0.9964
	PCA	0.9000	0.9251	0.0476	0.0387	0.0111	0.0075	2.5747	1.9875	0.8470	0.9091
	SFIM	0.9612	0.9675	0.0377	0.0314	0.0086	0.0068	1.8736	1.5024	0.9314	0.9590
	MTF-GLP	0.9749	0.9782	0.0310	0.0266	0.0067	0.0055	1.4832	1.2454	0.9571	0.9708
	MTF-GLP-HPM	0.9756	0.9790	0.0315	0.0269	0.0065	0.0053	1.4553	1.2188	0.9584	0.9717
	GFPCA	0.9071	0.9226	0.0612	0.0421	0.0147	0.0101	3.1901	2.2263	0.7558	0.9067
Synthesized band	GS	0.9010	0.9459	0.0447	0.0337	0.0114	0.0071	2.5675	1.7746	0.8602	0.9313
	GSA	0.9981	0.9984	0.0087	0.0081	0.0013	0.0012	0.3115	0.2854	0.9981	0.9984
	PCA	0.9004	0.9262	0.0460	0.0373	0.0110	0.0073	3.4169	1.9711	0.8486	0.9103
	SFIM	0.9628	0.9687	0.0357	0.0294	0.0085	0.0067	1.8513	1.4786	0.9331	0.9602
	MTF-GLP	0.9768	0.9796	0.0282	0.0241	0.0065	0.0054	1.4499	1.2135	0.9591	0.9722
	MTF-GLP-HPM	0.9774	0.9803	0.0288	0.0245	0.0063	0.0052	1.4216	1.1863	0.9603	0.9731
	GFPCA	0.9047	0.9217	0.0596	0.0411	0.0146	0.0101	3.1860	2.2267	0.7536	0.9057
	CNMF	0.9864	0.9915	0.0214	0.0142	0.0043	0.0026	0.9973	0.6317	0.9787	0.9905

541

542 5.5. Applicability of the 6 m CRISM data

543

544 Compared to 18 m CRISM data, 6 m CRISM data present significant advantages. First, from the spatial
 545 aspect, 6 m CRISM data can provide more detailed texture information. Second, from the spectral aspect, 6
 546 m CRISM data fully inherit the fine spectral resolution (i.e., 6.55 nm) of the original 18 m CRISM data,
 547 which is much finer than that of multispectral sensors. The hyperspectral data can capture more detailed

548 spectral characteristics of the Martian surface, offering broader application prospects. For example, when
549 spacecraft select suitable landing sites on the Martian surface in the future, if some small impact craters,
550 canyons and ditches are smaller than 18 m, they are often represented as mixed pixels in 18 m CRISM data,
551 making it difficult to determine the fine topography and geomorphology. However, in 6 m spatial resolution
552 CRISM data, these small-sized features can be more effectively identified. Additionally, the Martian surface
553 is covered by complex geological and topographical characteristics. At 18 m spatial resolution, the texture
554 details of mineral-rich areas cannot be observed clearly. For example, the boundaries of impact craters (e.g.,
555 in the Eberswalde crater area) and canyons (e.g., the Gale crater area) appear blurred, and weathering layers
556 and river sediments are difficult to identify. In the 6 m CRISM data, the textures of these features can be
557 recognized more effectively, with great potential to enhance the accuracy of mineral identification.

560 **6. Conclusion**

561
562 The CRISM can capture hyperspectral images spanning multiple spectral channels from the visible to the
563 near infrared, offering unique advantages for studying minerals, geology, and surface features on Mars.
564 However, the spatial resolution of CRISM data is 18 m, which may be relatively coarse for observing surface
565 texture details in local areas. Here, by spatial-spectral fusion, 18 m CRISM hyperspectral data were
566 downscaled to 6 m, using 6 m CTX images as the panchromatic image. To address the challenge of data
567 fidelity to the original coarse hyperspectral data in spatial-spectral fusion, a novel paradigm called DF-SSF
568 was proposed. It utilizes ATPK to downscale the difference (i.e., coarse residual image) between the
569 spatial-spectral fusion result of any existing method and the original hyperspectral images. The produced fine
570 spatial resolution residual image is then added to the spatial-spectral fusion result of the existing method to
571 yield a spatial-spectral fusion result with complete data fidelity to the original hyperspectral image. The
572 experimental results in six regions show that the fusion of CRISM and CTX can result in finer spatial
573 resolution CRISM hyperspectral images with satisfactory accuracy (based on DS-SSF, the CC is above
574 0.9600 in all cases). Furthermore, by applying the DF-SSF model to existing spatial-spectral fusion methods,
575 complete data fidelity to the original CRISM hyperspectral original data can be achieved, increasing the
576 fusion accuracy of the existing methods. DF-SSF is theoretically applicable to any existing spatial-spectral
577 fusion methods. Compared with the 18 m CRISM data, the 6 m CRISM data not only provide more detailed
578 texture information, but also inherit the fine spectral resolution, offering broader application potential.

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