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The *Herschel* Bright Sources (HerBS): sample definition and SCUBA-2 observations

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ABSTRACT

We present the *Herschel* Bright Sources (HerBS) sample, a sample of bright, high-redshift Herschel sources detected in the 616.4 deg² Herschel Astrophysical Terahertz Large Area Survey. The HerBS sample contains 209 galaxies, selected with a 500 µm flux density greater than 80 mJy and an estimated redshift greater than 2. The sample consists of a combination of hyperluminous infrared galaxies and lensed ultraluminous infrared galaxies during the epoch of peak cosmic star formation. In this paper, we present Submillimetre Common-User Bolometer Array 2 (SCUBA-2) observations at 850 µm of 189 galaxies of the HerBS sample, 152 of these sources were detected. We fit a spectral template to the Herschel-Spectral and Photometric Imaging Receiver (SPIRE) and 850 µm SCUBA-2 flux densities of 22 sources with spectroscopically determined redshifts, using a two-component modified blackbody spectrum as a template. We find a cold- and hot-dust temperature of $21.29_{-1.66}^{+1.35}$ and $45.80_{-3.48}^{+2.88}$ K, a cold-to-hot dust mass ratio of $26.62_{-6.74}^{+5.61}$ and a β of $1.83_{-0.28}^{+0.14}$. The poor quality of the fit suggests that the sample of galaxies is too diverse to be explained by our simple model. Comparison of our sample to a galaxy evolution model indicates that the fraction of lenses are high. Out of the 152 SCUBA-2 detected galaxies, the model predicts 128.4 ± 2.1 of those galaxies to be lensed (84.5 per cent). The SPIRE 500 µm flux suggests that out of all 209 HerBS sources, we expect 158.1 \pm 1.7 lensed sources, giving a total lensing fraction of 76 per cent.

Key words: gravitational lensing: strong – galaxies: high-redshift – submillimetre: galaxies.

1 INTRODUCTION

The Herschel Space Observatory (Pilbratt et al. 2010) has increased the number of known submillimetre galaxies (SMGs) from hundreds to hundreds of thousands. The Herschel Astrophysical Terahertz Large Area Survey (H-ATLAS; Eales et al. 2010; Valiante et al. 2016) is one of the largest legacies of Herschel. This survey observed a total of 616.4 deg² over five fields in five wavebands. The large-area surveys done with Herschel allow us to select sources that are among the brightest in the sky, of which a large percentage are lensed ultraluminous infrared galaxies (ULIRGs; $10^{12} \, \rm L_{\odot} < L_{FIR} < 10^{13} \, \rm L_{\odot}$) and hyperluminous infrared galaxies (HyLIRGs; $L_{\rm FIR} > 10^{13} \, \rm L_{\odot}$) at high redshift.

A similar selection for bright sources was already exploited in the 14.4 deg² Science Demonstration Phase (SDP) of H-ATLAS by Negrello et al. (2010), who used a simple flux cut-off to select lensed sources. They were able to remove all contaminants from their selection, local galaxies and blazars, and identified five lensed galaxies. Wardlow et al. (2013) followed a similar approach on the 94 deg² Herschel Multi-tiered Extragalactic Survey (Her-MES) maps, and selected 13 sources with $S_{500 \, \mu m} > 100 \, \text{mJy}$. Nine of these sources had follow-up data, done with the Submillimeter Array (SMA), the Hubble Space Telescope (HST), Jansky Very Large Array (JVLA), Keck and Spitzer. Wardlow et al. (2013) combined these data for six sources and confirmed their lensing nature, while three other sources had their lensing nature already confirmed by Borys et al. (2006), Conley et al. (2011) and Ikarashi et al. (2011). Recently, Negrello et al. (2017) and Nayyeri et al. (2016) used the same $S_{500 \, \mu m} > 100 \, \text{mJy}$ flux density cut-off on the full

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H-ATLAS (616.4 deg²) and HerMES Large Mode Survey (HeLMS; 372 deg²) maps, and created samples containing 77 and 80 sources, respectively. Spectroscopic and optical follow-up observations were able, so far, to confirm that 20 sources are indeed lensed, one is a protocluster (Ivison et al. 2013), while the remaining sources in Negrello et al. (2017) await more observations to be carried out to confirm their nature.

Large samples of lensed sources are interesting, both because of the lensed source and the intervening lensing galaxy (Treu 2010). The lensed source has an amplified flux density and increased angular size. The amplification in flux density allows us to study sources that would otherwise be too faint to detect. The increase in angular size allows us to study the internal properties of high-redshift sources with high resolution submm/mm and radio observatories, such as Atacama Large Millimeter/submillimeter Array (ALMA) and the Very Large Array (VLA). As most intervening, lensing sources are passively evolving ellipticals, they are submm dim and their contribution to the total measured flux density is minimal. This allowed ALMA Partnership (2015), Dye et al. (2015), Hatsukade et al. (2015), Rybak et al. (2015), Swinbank et al. (2015) and Tamura et al. (2015) to study SDP.81 down to sub-kiloparsec scales, using the increase in angular size in order to resolve the morphological and dynamical properties of a galaxy at a redshift of 3.

Submm detected lensed sources, similar to SDP.81, are forming stars at rates of hundreds to several thousands of solar masses per year, and large samples of them can allow statistically significant studies into these extremely star-forming sources. This is important, because the comoving density of ULIRGs at z=2–4 is about a thousand times greater than in the local Universe, and these dusty star-forming galaxies are estimated to contribute about 10 per cent of the total star formation in this redshift range (Hughes et al. 1998; Blain et al. 1999; Smail et al. 2002; Wardlow et al. 2011; Casey, Narayanan & Cooray 2014). This means that SMGs contribute significantly to the peak in cosmic star formation, which occurred around $z \sim 2.3$ (Chapman et al. 2005).

While the star formation rate of the Universe has been measured up to redshift $z \sim 8$ in rest-frame ultraviolet (UV) surveys, these studies only measure the unobscured star formation rates (Madau & Dickinson 2014). The star formation processes in these dusty star-forming galaxies (DSFGs) tend to be obscured by the dust, and are missed by current optical investigations of the cosmic star formation rate. An added benefit of using submm observations to measure the obscured star formation rate is that submm flux density falls only slowly with redshift, because of the negative K-correction: submm observations observe the Rayleigh-Jeans part of the modified blackbody spectrum, which causes the flux density to increase as the galaxy's redshift increases. This increase is able to compensate for the cosmological dimming due to the increase of luminosity distance, e.g. a redshift 1 or 4 galaxy has a similar flux density in submm wavelengths (Blain & Longair 1993; Blain et al. 2002; Bethermin et al. 2015).

The foreground galaxy's total mass (dark and baryonic) distribution determines the lensed morphology of the submm detected system (Vegetti et al. 2012; Hezaveh et al. 2016a,b). Therefore, high-resolution imaging of the lensed morphology allows the detection of low-mass substructures in lensing galaxies. These substructures can then be used to test the formation of structure in large-scale cosmological simulations, such as the Millennium (Springel et al. 2005) and the recent EAGLE simulation (Schaye et al. 2015).

The statistics of galaxy–galaxy lensing systems furthermore allows for a measurement of global cosmological parameters. For example, the lensing statistics of 28 lensed quasars in the Sloan Digital

Sky Survey (SDSS) Quasar Lens Search (SQLS) gave an estimate of $\Omega_{\Lambda}=0.74\pm0.17$, assuming a spatially flat Universe (Oguri et al. 2012). Selecting lensed sources from bright submm samples is simple and unbiased method because it is based on the source, as the lens is usually faint in the submm. Eales (2015) showed that observations of a sample of 100 lensed *Herschel* sources would be enough to estimate Ω_{Λ} with a precision of 5 per cent and observations of 1000 lenses would be enough to estimate Ω_{Λ} with a precision similar to that obtained from the *Planck* observations of the cosmic microwave background.

A high flux density cut-off ($S_{500 \,\mu\text{m}} > 100 \,\text{mJy}$) eliminates a large amount of possible lenses in order to achieve a low contamination rate from unlensed sources (González-Nuevo et al. 2012). Lowering the cut-off flux density to 80 mJy was already tested in Wardlow et al. (2013). Out of the four galaxies with lensing verification, only one was confirmed to be a lens. In this paper, we will reinvestigate the question of using a lower cut-off flux, by selecting galaxies from the 616.4 deg² H-ATLAS survey. In order to decrease the contamination rate, we impose a photometric cut-off redshift $z_{\text{phot}} > 2$ based on the Herschel-Spectral and Photometric Imaging Receiver (SPIRE) fluxes. The probability of lensing below this redshift falls off sharply, because of the smaller volume available between us and the source (Strandet et al. 2016). We will calculate the expected amount of lensed galaxies in our sample, by comparing the fluxes of our sources to a cosmological evolution model that takes lensing into account

Our sample selection is based on *Herschel* fluxes, and a known problem of sources selected at $500\,\mu m$ with *Herschel* is the large solid angle of the beam (Scudder et al. 2016). This could lead to several sources blending into a single source, and result in a flux that is too large. This is why we observed the majority of our sources at $850\,\mu m$ with the Submillimetre Common-User Bolometer Array 2 (SCUBA-2) instrument on the James Clerk Maxwell Telescope (JCMT), whose beam has a six times smaller solid angle on the sky. The extra data point should also improve the photometric redshift estimates of our sources.

In Section 2, we discuss the selection of the *Herschel* Bright Sources (HerBS) sample, as well as the observations with SCUBA-2. We describe the results of the JCMT observations in Section 3, where we also remove several blazar contaminants from the sample. We rederive a spectral template for our sources with spectroscopically determined redshifts in Section 4. We discuss the effects of source confusion, the properties of the template, the redshift distribution of our sample and estimates of the lensing fraction in Section 5.

Throughout this paper we assume the Λ cold dark model (Λ CDM) model, and the best-fitting parameters found by the Planck Collaboration XIII (2016): $H_0 = 67.7 \, \mathrm{km \, s^{-1} \, Mpc^{-1}}$ and $\Omega_{\mathrm{M}} = 0.307$.

2 SAMPLE AND MEASUREMENTS

2.1 The selection of the HerBS sample

The sample was selected from the brightest, high-redshift sources in the H-ATLAS survey. The H-ATLAS survey used the Photodetector Array Camera and Spectrometer (PACS; Poglitsch et al. 2010) and SPIRE (Griffin et al. 2010) instruments on the *Herschel Space Observatory* to observe the North Galactic Pole (NGP) and South Galactic Pole (SGP) fields and three equatorial fields to a 1σ sensitivity of 5.2 mJy at 250 μ m to 6.8 mJy at 500 μ m, although the noise varies per source (Valiante et al. 2016). The three equatorial

Table 1. The H-ATLAS fields.

Field	Centre		Approxima	te dimensions	Final surface area	Sources	Surface density	
	RA (h:m:s)	Dec. (°:':")	RA (°)	Dec. (°)	(deg^2)		(deg^{-2})	
NGP	13:18:00	29:00:00	15	10	170.1	49	0.288	
GAMA total	_	_	_	_	161.6	72	0.446	
GAMA 9	09:00:00	00:00:00	12	3	53.43	23	0.430	
GAMA 12	12:00:00	00:00:00	12	3	53.56	26	0.485	
GAMA 15	14:30:00	00:00:00	12	3	54.56	23	0.422	
SGP	23:24:46	-33:00:00	42	6	284.8	88	0.309	
Total fields	_	_	_	_	616.4	209	0.339	

Note. Reading from the left, the columns are: column 1 – name of field; columns 2 and 3 – the location of the centre of the field; columns 4 and 5 – the approximate dimensions of the field; column 6 – the surface area from the final maps (Valiante et al. 2016); column 7 – the number of final HerBS sources in each field; column 8 – the surface density of HerBS sources per field.

fields overlap with the Galaxy And Mass Assembly (GAMA) fields 9, 12 and 15 h, and from here on we adopt this naming convention for the equatorial fields (Driver et al. 2011; Liske et al. 2015). The fields are defined in Table 1. In total the H-ATLAS survey detected approximately half a million sources.

We initially selected the HerBS sample from the H-ATLAS point source catalogues of Valiante et al. (2016), who extracted the flux densities at the 250 µm position, and used this position for flux extraction at 350 and 500 µm. The flux densities in the catalogues are not deboosted, however the flux boosting is negligible compared to the flux uncertainty; around 1 per cent at 80 mJy, and diminishing for increasing flux density, as can be seen in table 6 of Valiante et al. (2016). We estimated the redshift of each source by fitting a source template to the 250, 350 and 500 µm flux densities (Pearson et al. 2013). We selected the sources at an estimated redshift, $z_{\rm phot}$, greater than 2 and a 500 μm flux density, $S_{500 \,\mu m}$, greater than 80 mJy. The source template was a two-temperature modified blackbody from Pearson et al. (2013) (see equation 3 and Table 5 in our Section 4). This modified blackbody was derived from the Herschel PACS and SPIRE flux densities of 40 sources with spectroscopically determined redshifts, with 25 sources at low redshifts (z < 1), and only 12 sources at high redshifts (z > 2). Our initial sample consisted of the 223 sources.

Where possible we removed sources that are coincident with a large nearby galaxy or a blazar (Negrello et al. 2010; López-Caniego et al. 2013). However, the pre-selection of blazars was not complete, and it only became clear after we had carried out the SCUBA-2 observations that we had actually observed several blazars (see Section 3). The final HerBS sample consists of 209 submillimetre galaxies after removing all nearby galaxies and blazars, and is listed in Table A1. We plot the positions of the final 209 HerBS sources in the various fields in Fig. 1.

Several of the HerBS sources have been investigated individually. Fu et al. (2012) showed that HATLAS J114637.9–001132 (HerBS-2) is a strongly lensed submm galaxy, with a magnification between 7 and 17. Cox et al. (2011) and Bussmann et al. (2012) found that HATLAS J142413.9+022303 (HerBS-13) is a lensed submm galaxy, with a magnification of 4. At a redshift of 4.24, the source has one of the highest redshifts in our sample. HATLAS J090311.6+003907 (HerBS-19) is also known as SDP.81, and has recently been observed by ALMA Partnership (2015). Negrello et al. (2010) showed SDP.81 is lensed using 880 μ m Submillimeter Array observations. Dye et al. (2015) and Tamura et al. (2015) reconstructed the galaxy from the ALMA observation, by modelling the distorting effect of the lens. They found a magnification of ~11.

This reconstructed image features details on the scale of hundreds of parsecs, and the image shows resolved individual giant molecular clouds in a z = 3.04 galaxy. SDP.81 appears, through reconstructed HST and ALMA imaging, to be two interacting objects, where the dust disc is in a state of collapse.

However, not all our sources are lensed. Ivison et al. (2013) studied HATLAS J084933.4+021442 (HerBS-8), and found it was not a strongly lensed galaxy. Instead, it consists of multiple large galaxies in the process of merging, which has probably triggered starbursts in the individual galaxies, explaining the brightness in submm wavelengths.

Our HerBS sample overlaps partially with the sample from Negrello et al. (2017), as 53 out of the 80 sources in their sample are also found in the HerBS sample. Their sample was designed specifically to find lensed systems, by imposing a flux density cut-off of $100\,\mathrm{mJy}$ at $500\,\mu\mathrm{m}$ and did not have a lower redshift limit.

2.2 Observations with SCUBA-2

We observed 203 sources with the SCUBA-2 array on the JCMT. The instrument consists of 10 000 transition edge sensor (TES) bolometers, distributed over four arrays that observe at 450 μm and four arrays that observe at 850 μm (Holland et al. 2013). Both wavelengths are observed simultaneously, with the use of a dichroic mirror. The voltage across each array is optimized to ensure as many functional bolometers as possible. The optimized voltage places the majority of the bolometers within their sensitive resistance transition, whereupon any temperature fluctuation causes a current change. The resulting magnetic field variations are read out with separate Superconducting Quantum Interference Devices (SQUIDs) located under each bolometer.

The instrument scans the sky in a daisy pattern, circling around the source following a continuous petal-like track, providing a central 3 arcmin region of uniform exposure time, and keeping one part of the array on-source at all times (Chapin et al. 2013).

The observations conditions were in the grade-3 weather band $[0.08 < \tau_{1.3\,\mathrm{mm}} < 0.12]$, which is only suitable for 850 µm observations. The data were flux-calibrated against Uranus, Mars, CRL 618 and CRL 2688 (the Westbrook and Egg nebulae). The calibrators were observed between two and four times per observing run, and the flux calibration factors (FCFs) were estimated linearly for observations in between calibrators, and the closest calibrator was used otherwise (Dempsey et al. 2013).

Our observations consisted of 10 min exposures for each source. The bolometers are sampled at roughly 200 Hz, and the data are

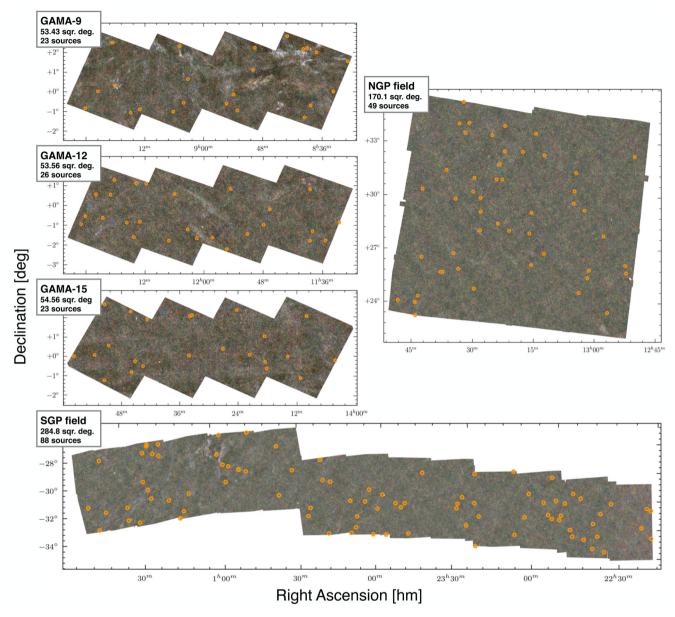


Figure 1. *Herschell*SPIRE colour maps of the H-ATLAS fields. The orange circles mark the positions of the 209 HerBS sources. This figure is similar to fig. 2 in (Negrello et al. 2017), and shows how the sources are distributed over the sky.

stored in 30 s time slices for each of the arrays, where the first and last time slice of each exposure are flat-fields. Flat-fields probe the responsivity of individual bolometers, and are derived from the bolometer's response to the resistance heaters, which are located next to each bolometer.

2.3 Data reduction

The entire data reduction method is shown schematically in Fig. 2, and is described below. The data reduction was done with the ORAC_DR pipeline, which uses the KAPPA and SMURF packages from STARLINK, and the PICARD procedures (Chapin et al. 2010).

The basic data consist of the time-dependent signals from each bolometer and information about the specific scanning pattern of the arrays on the sky. The first step of the data reduction method flat-fields and downsamples the data, to correct for individual bolometer

performance and to reduce the file size by matching the sampling speed to the spatial scale of the maps. The second step removes the noise components in the signal iteratively, starting with the largest noise component (Chapin et al. 2013). Our final reduced map is achieved with additional data reduction steps: jackknife, fake point source injection and matched filtering. The final result is a 4×4 arcmin² image with 1 arcsec resolution.

2.3.1 The iterative data reduction step (make map)

Sky emission is the dominant noise component, and it is shared by all bolometers. This common-mode signal (COM) is calculated by averaging the signals of all bolometers into one signal per subarray. The COM is then subtracted from the signal for each bolometer, taking care to adjust for individual bolometer amplification

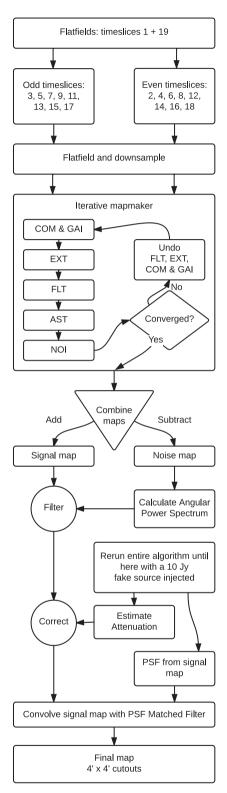


Figure 2. This flowchart shows the data reduction steps schematically, starting from the raw data files at the top, working to the reduced cutouts at the bottom. The intricacies are detailed in the data reduction section. For each observation, two sets of time slices are cleaned and processed through the iterative mapmaker, and these resulting maps are subtracted to provide a jackknife estimate of the noise. A fake source is injected to estimate peak attenuation due to the filtering process, and allows us to create a PSF for the final matched filter step.

differences (GAI). Bolometers that have a signal that is inconsistent with the COM are rejected at this stage.

The signal is then corrected for the atmospheric extinction (EXT), a function of precipitable water vapour and telescope pitch, after which a high-pass Fourier filter (FLT) removes low frequency, 1/f noise. The frequency cut-off is 0.8 Hz, which corresponds to a spatial scale of 200 arcsec.

The next step removes the astronomical signal (AST) from the total signal, in order to estimate convergence of our iterative data reduction step. The signals of all bolometers are projected on to the sky, creating an astronomical map of our observation. Many data points contribute to the estimate of the astronomical signal in each spatial pixel, which greatly reduces the noise compared to the time series data. The map still contains noise, but the assumption made in this step of the iterative data reduction procedure is that everything in this map is real. The astronomical, space-domain map is then used to create a time-domain signal for each bolometer, by simulating an observation of our astronomical map. This is then removed from the signal for each bolometer.

The time-domain signal for each bolometer should now consist only of noise. This noise is calculated and compared to the convergence criterion (NOI), which is a minimum number of loops (four in this case) and a threshold noise level. If convergence is not reached in the NOI step, all the data processing steps (FLT, EXT, GAI and COM) are undone, except for the removal of the astronomical signal. This adds back the common-mode noise and the noise removed in the Fourier-filtering step. All the steps (see upper half of Fig. 2) are then repeated until the convergence criterion is met. After each cycle the new estimate of the astronomical signal is added to the previous estimate. The final image is obtained when the convergence criterion is met.

2.3.2 Extra data reduction steps

Apart from this standard data reduction procedure, shown in the top half of Fig. 2, we added the following additional steps.

For each source, we split the time slices into two sets. Each set consists of the flat-fields (first and last time slice) and either the odd or even half of the time slices. We ran the iterative mapmaker over each set separately, which allows us to execute a jackknife step (ORAC_DR procedure: SCUBA2_JACKKNIFE).

We used the iterative data reduction step to create a separate map for each half of the data. We subtracted one map from the other to create a noise map, from which we calculate the angular power spectrum of the noise. We used this angular power spectrum to construct a map-specific Fourier filter. A combined signal map is calculated by adding the two signal maps, and we then applied this Fourier filter to the signal map.

The high-pass filtering step attenuates the signal, and to account for this, we reran the entire data reduction algorithm with an injected fake source. This fake 10 Jy point source [full width at half-maximum (FWHM) of 13 arcsec – the main beam size of $850\,\mu m$ observations with JCMT; Dempsey et al. 2013] was injected into both the odd and even time slices, offset at 30 arcsec from the centre. This extremely bright, fake source allowed us to calculate an effective point spread function (PSF) and also provided an estimate of the signal attenuation due to the high-pass filtering, which usually was around 15–20 per cent.

Finally, we applied a matched filter to the signal map, in which we convolved our signal map with the PSF found by injecting a fake source. This provided the final, reduced observation map. We

Table 2. SCUBA-2 observations of the HerBS sample.

	Sources	Percentage
HerBS galaxies	209	100
SCUBA-2 observed	189	90.4
Detected $(>3\sigma, \theta < 10 \text{ arcsec})$	152	69.4
Not detected $(<3\sigma)$	27	12.9
Not detected $(>3\sigma, \theta > 10 \text{ arcsec})$	10	8.1
Not observed	20	9.6
Blazar contaminants	14	

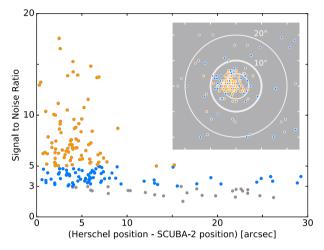


Figure 3. The majority of high signal-to-noise ratio SCUBA-2 fluxes lie in a 10 arcsec circle around the SPIRE position. We choose a cut-off signal-to-noise ratio of 3σ , and a maximum radius of 10 arcsec. The 15 sources with a signal-to-noise ratio between 3 and 5 suggest that the HerBS sources might have two false detections. The overlay graph shows the position of the SCUBA-2 observation, where each point was centred on the SPIRE position.

cropped the observation to a $4 \times 4 \, \rm arcmin^2$ image, and measured the fluxes by measuring the highest flux density pixel in the central $50 \times 50 \, \rm arcsec^2$ region around the SPIRE-estimated position. We determine a SCUBA-2 detection by a combination of proximity to the *Herschel-SPIRE 250* μ m position and the signal-to-noise ratio, as shown in Section 3.

3 RESULTS

We observed 203 of our pre-selected H-ATLAS sources with the SCUBA-2 instrument. In the following analysis, we find that 14 detected sources turn out to be blazars, which leaves our entire HerBS galaxy sample containing 209 sources. 152 of these sources are detected, 27 sources are not detected due to a signal-to-noise ratio cut and 10 sources do have a 3σ detection, but not within the 10 arcsec circle around the SPIRE position. These results are summarized in Table 2.

Fig. 3 shows the distribution of the maximum signal-to-noise ratio in a $50 \times 50 \, \text{arcsec}^2$ box centred on the SPIRE position, as a function of the position offset.

We decide to define a detected source by a signal-to-noise ratio greater than 3 and a positional offset smaller than 10 arcsec. Initially, we find 159 sources that satisfy this criterion, 27 sources that are not detected by the signal-to-noise ratio cut and 17 sources whose positional offset was too large.

Table 3. Re-examined SCUBA-2 observations of HerBS sources with $\theta > 10$ arcsec.

HerBS	θ (arcsec)	S/N	$S_{850 \mu m}$ (mJy)
63	9.45	3.19	33.8
75	7.59	4.24	44.9
96	7.84	2.10	19.5
97	6.57	2.49	28.1
101	1.93	3.42	32.5
118	2.28	2.12	23.3
122	6.97	2.43	21.9
131	5.54	2.95	30.3
140	7.14	3.59	30.3
145	9.59	3.17	33.0
146	7.85	2.92	32.1
148	5.40	3.02	29.0
151	6.33	2.34	23.9
163	6.66	1.85	19.1
172	5.92	1.40	13.7
181	4.06	3.81	32.9
195	3.94	2.61	29.5

For each of the 17 sources that do not have their maximum flux within the 10 arcsec circle around the SPIRE position, which do have a signal-to-noise ratio greater than 3, we decreased the size of the searching box to find the peak in flux. Of these 17 sources, seven sources have fluxes within 10 arcsec from the SPIRE position with a signal-to-noise ratio greater than 3, as shown in boldface in Table 3. These seven sources are added to the detected sources.

Of the sources with signal-to-noise ratios between 3 and 5, 15 are originally situated outside of the 10 arcsec circle. These sources are distributed over 89 per cent of the map (the area outside the 10 arcsec circle). An even distribution of such false detections would result in two (\sim 1.7) false detections inside the HerBS catalogue. The overlay graph inside Fig. 3 shows a strong correlation for most points around the centre, however, all other non-detections appear uniformly scattered, making an even distribution likely.

We know from Negrello et al. (2007) that there is a risk that several of these sources are blazar contaminations. In order to find these contaminants, we plot their flux ratios in Fig. 4.

The top panel shows the flux ratios based on just *Herschel* fluxes. We plot $S_{500\,\mu\text{m}}/S_{250\,\mu\text{m}}$ versus $S_{350\,\mu\text{m}}/S_{250\,\mu\text{m}}$. The sources that lie very close to a known blazar (within 10 arcsec) in the NASA Extragalactic Database (NED) (black circles) lie in the same region as the high-redshift HerBS sources (grey triangles, blue squares and red circles). We also plot the track for the template we derive in Section 4 through the diagram as the redshift changes (black line and circles). Similarly, we show the expected blazar track (assuming synchrotron radiation) for various possible α -values (black dash–dot line and triangles). Note that both these tracks do not differ significantly from each other. The bottom panel shows the flux ratios of the 203 sources with SCUBA-2 observations. We plot $S_{850\,\mu\text{m}}/S_{250\,\mu\text{m}}$ against $S_{350\,\mu\text{m}}/S_{250\,\mu\text{m}}$. Most of the galaxies close to a known blazar occupy a different region of the graph, and can be easily identified and removed from the sample.

One of the sources, HerBS-16, does not have the typical flux ratios of a blazar, and has therefore not been removed. The spectrum also looks dust-like, and has consistent photometric redshift estimates, as can be seen in Fig. 5. The source, in this case, could be close to the blazar by accident. Only one source close to a known blazar

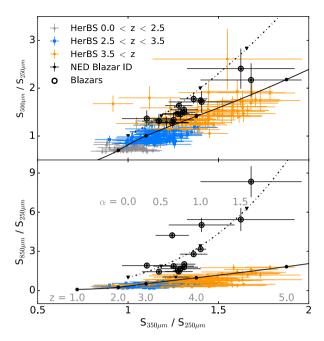


Figure 4. The top panel shows the flux ratios based on just *Herschel* fluxes. We plot $S_{500 \, \mu m}/S_{250 \, \mu m}$ versus $S_{350 \, \mu m}/S_{250 \, \mu m}$. Sources close to a known blazar in NED (black circles) lie in the same region as the high-redshift HerBS sources (grey triangles, blue squares and red circles). The bottom panel shows the flux ratios when we include the SCUBA-2 observations. We plot $S_{850 \, \mu m}/S_{250 \, \mu m}$ against $S_{350 \, \mu m}/S_{250 \, \mu m}$. Most sources close to a known blazar occupy a different region of the graph, and can be easily identified and removed (black circles). The difference between the graphs indicates the necessity of the 850 μm observations for removing blazar contaminants from the sample. We also plot the track for the template we derive in Section 4 through the diagram as the redshift changes (black line and circles). Similarly, we show the expected blazar track for α-values ranging from 0 to 1.5 (black dash–dot line and triangles).

has not been observed, and we have therefore kept it in our HerBS sample (HerBS-112).

The difference between the graphs indicates the need for multiwavelength observations, in order to reliably remove blazar contaminants from the sample. We list the *Herschel* SPIRE and SCUBA-2 positions and fluxes of the removed blazars in Table A2.

After removing 14 blazars from our sample, we are left with 189 HerBS galaxies with SCUBA-2 observations. While some sources close to NED blazars did not have irregular flux ratios, all of the sources with irregular flux ratios are close to known blazars. This suggests our method for finding contaminants in our sample is robust, and thus that the 19 unobserved sources that do not lie close to a NED blazar are not likely to have emission dominated by synchrotron radiation.

For completeness, we plot the blazar spectrum, assuming solely synchrotron radiation, in Fig. 4, following equation:

$$S_{\nu} = A \, \nu^{-\alpha}. \tag{1}$$

Here S_{ν} is the flux density at a specific frequency (ν) , A is a constant factor and α determines the steepness of the slope in the far-infrared wavelength regime. Most of the blazars lie close to this line. We also calculate the value for α for each galaxy, by minimizing χ^2 :

$$\chi^2 = \sum_{i>j} \left[\frac{(S_i/S_j)_{\text{model}} - (S_i/S_j)_{\text{meas}}}{\sigma_{i,j,\text{meas}}} \right]^2.$$
 (2)

The index *i* and *j* iterate over all four wavelengths (250, 350, 500 and 850 μ m), where *i*'s wavelength is always larger than *j*. $\sigma_{i,i,\text{meas}}$

is the combined error of $(S_i/S_j)_{\text{meas}}$. α -values range from 0.24 to 1.66. The individual values can be found in Table A2, and agree well with the positions of the blazar sources in Fig. 4.

We provide postage stamp cutouts of the observations with SPIRE, SCUBA-2 and fits of our templates (Section 4.1) to the 250, 350, 500 and 850 μm flux densities of each source in Appendix B. Typical cutouts of a source detected by SCUBA-2, a source undetected by SCUBA-2 and a blazar are shown in Fig. 5. The bottom row of cutouts shows HerBS-16, which is close to a NED blazar, but has a spectral energy distribution (SED) typical of a submm galaxy.

4 GALAXY TEMPLATES

We derived a galaxy template for our total sample by using the subset of HerBS sources that have spectroscopic redshifts. We fitted a two-temperature, modified blackbody SED to the *Herschel* and the SCUBA-2 flux densities of each source. We list the sources with spectroscopic redshifts in Table 4. These spectroscopic redshifts were found by observing submm spectral lines, in order to ensure we are looking at the same source.

This template is necessary to estimate photometric redshifts and luminosities for our entire sample. Similar to the analysis of Pearson et al. (2013), we fitted the template to the SPIRE (250, 350 and 500 μ m) fluxes, and included our JCMT/SCUBA-2 850 μ m flux densities. We choose to exclude the PACS photometry of our sources in our analysis, as even the brightest sources are poorly detected, due to the high-redshift limit of our sample. Our spectroscopic sample includes eight sources used in Pearson's analysis, and 16 new sources, all of which are at high redshifts ($z_{\rm spec} > 1.5$). We only used HerBS sources for our template to ensure there is 850 μ m photometry of our sources, and only used the galaxies with spectroscopic redshifts estimated from more than one line.

4.1 Template fitting

We fitted the template to the sources' flux densities and rest wavelengths, calculated from their spectroscopic redshifts. We assumed a two-temperature modified blackbody template for the SED,

$$S_{\nu} = A_{\text{off}} \left[B_{\nu} \left(T_{\text{h}} \right) \nu^{\beta} + \alpha B_{\nu} \left(T_{\text{c}} \right) \nu^{\beta} \right], \tag{3}$$

where S_{ν} is the flux at the rest-frame frequency ν , $A_{\rm off}$ is the normalization factor, B_{ν} is the Planck blackbody function, β is the dust emissivity index, $T_{\rm h}$ and $T_{\rm c}$ are the temperatures of the hot and cold dust components and α is the ratio of the mass of the cold to hot dust

We aimed to minimize the following χ^2 for the fluxes that were detected:

$$\chi^{2} = \sum_{i=1}^{n} \chi_{i}^{2} = \sum_{i=1}^{n} \sum_{j=1}^{\lambda} \left[\frac{A_{i} S_{\text{model},i} - S_{\text{meas},i}}{\sigma_{\text{meas},i}} \right]^{2}, \tag{4}$$

where $S_{\text{model},i}$ is the predicted flux of the *i*th source (out of *n*) according to equation (3), with the amplitude A_{off} set to 1. $S_{\text{meas},i}$ and $\sigma_{\text{meas},i}$ are the measured signal and noise values. In the case of all fluxes of the source were detected, we fitted the amplitude of our template, A_i , to the rest-wavelength data points analytically in order to decrease computation time.

$$A_{i} = \left(\sum^{\lambda} \frac{S_{\text{model},j} S_{\text{meas},j}}{\sigma_{\text{meas},j}^{2}}\right) / \left(\sum^{\lambda} \frac{S_{\text{model},j}^{2}}{\sigma_{\text{meas},j}^{2}}\right).$$
(5)

Equation (5) is derived by solving $d\chi_i^2/dA_i = 0$. We left the one source with a spectroscopic redshift did not have a detected

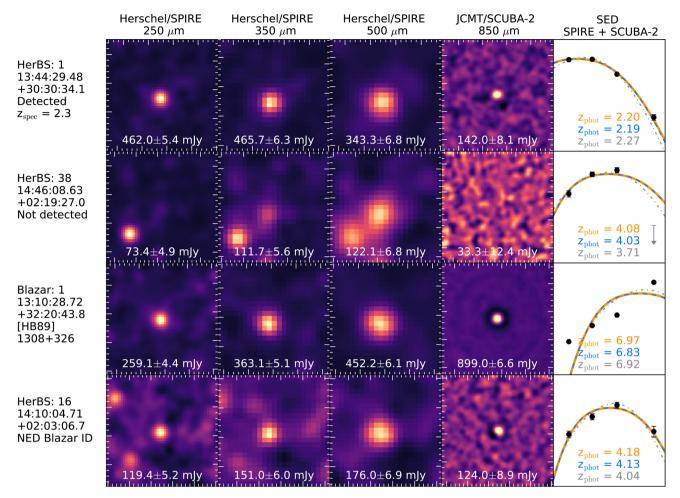


Figure 5. The four different types of sources we found in the SCUBA-2 850 μm observations of our sample: a galaxy detected with SCUBA-2, a galaxy undetected with SCUBA-2, a blazar and HerBS-16, which is close to a known blazar, but has an SED typical of thermal emission from dust. The first three columns of cutouts of each source are the *Herschel* observations shown in 4×4 arcmin² postage stamps. The fourth column shows the 850 μm SCUBA-2 observation in a 4×4 arcmin² postage stamp. All postage stamps are centred at the 250 μm extraction position of the *Herschel* catalogue. The final frame is a fitted SED, with the best-fitting template in orange, fixed β template in blue and Pearson's template in grey (Pearson et al. 2013). Similar figures for the entire HerBS sample can be found in Appendix B.

SCUBA-2 flux, HerBS-71. In this upper limit case, we calculated the χ^2 contribution using the method detailed in Sawicki (2012) and Thomson et al. (2017):

$$\chi^2 = -2\sum_{j} \ln \int_{-\infty}^{3\sigma} \exp \left[-\frac{1}{2} \left(\frac{f - A_j S_{\text{model},j}}{\sigma_{\text{meas},j}} \right)^2 \right] df, \tag{6}$$

where we sum over all non-detections j, which in our case is only the SCUBA-2 flux of HerBS-71, and integrate the Gaussian distribution up to the detection criterion of three times the measured noise (3σ) . The modified χ^2 statistic quantifies the probability of an event where the noise affected the signal to drop below the detection criterion. In the case of the model predicts a flux under the detection limit, there is no discrepancy with the model, and we set the χ^2 -value to zero.

We did this template fitting for two templates: best fit, where we varied all the parameters $(T_c, T_h, \alpha \text{ and } \beta)$; and fixed β , where we varied all parameters except β , which we fixed to 2. We also tried keeping T_c , T_h , α and β fixed to the values found by Pearson et al. (2013). In this case we found the set of A_i that gave the minimum χ^2 fit. The point of this was to determine whether our new templates gave any improvement in the quality of fit over

that found by Pearson et al. (2013). We estimated the uncertainty on each parameter by incrementally changing this parameter until the minimized χ^2 changes by of one (one interesting parameter; Avni 1976). The χ^2 was minimized by allowing the other (two or three) parameters to vary. The best-fitting templates are given in Table 4.

4.2 Template results

We find a cold- and hot-dust temperature of $21.29^{+1.35}_{-1.66}$ and $45.80^{+2.88}_{-3.48}$ K, a cold-to-hot dust mass ratio of $26.62^{+5.61}_{-6.74}$ and a β of $1.83^{+0.14}_{-0.28}$ for the best-fitting template. The results for the other templates, including the fitting of the templates to redshift and luminosity subsets, can be found in Table 5.

We investigated the usefulness of each template for estimating photometric redshifts, by using each template to estimate the photometric redshift of each source, and then calculating $(z_{\rm spec}-z_{\rm phot})/(1+z_{\rm spec})$ for each source. The root mean squared value of $(z_{\rm spec}-z_{\rm phot})/(1+z_{\rm spec})$ for the best-fitting template is 13 per cent, which is similar to the fixed β and Pearson templates. The value of the relative error derived from the best-fitting template

Table 4. The sources from the HerBS sample with measured spectroscopic redshifts.

H-ATLAS name	HerBS	$z_{\rm spec}$	z_{phot}	$\Delta z/(1+z)$	Ref.
	Robust, mi	ulti-line d	etections		
J083518.4+303034	1	2.30	2.20	0.03	H12
J114637.9-001132	2	3.26	2.80	0.11	H12
J082403.8+334407	3	2.95	3.75	-0.20	Н-р
J083051.0+013225	4	3.63	3.09	0.12	R-p
J080520.2+233627	5	3.57	3.72	-0.03	R-p
J082246.8+284449	6	1.68	2.11	-0.16	G13
J082537.0+292326	7	2.78	2.89	-0.03	K-p
J084933.4+021442	8	2.41	2.64	-0.07	L-p
J080214.5+261457	9	3.68	3.87	-0.04	К-р
J113526.2-014606	10	3.13	2.32	0.20	H12
J082620.3+245900	12	3.11	2.29	0.20	R-p
J142413.9+022303	13	4.28	4.53	-0.05	C11
J141351.9-000026	15	2.48	2.62	-0.04	H12
J090311.6+003907	19	3.04	3.76	-0.18	F11
J082310.2+311534	20	1.84	1.88	-0.02	R-p
J083144.0+255054	29	2.34	2.69	-0.11	R-p
J082153.5+341649	30	2.19	3.28	-0.34	R-p
J091840.8+023048	32	2.58	3.03	-0.13	H12
J082949.3+300401	35	2.68	2.73	-0.01	Н-р
J091304.9-005344	59	2.63	2.87	-0.07	N10
J115820.1-013752	66	2.19	2.49	-0.09	Н-р
J113243.0-005108	71	2.58	3.73	-0.32	R-p

Tentative, single-line detections (not used)

J080532.7+275900	31	2.79	3.25	-0.12	_
J083344.9+000109	88	3.10	3.25	-0.04	_
J113803.6-011737	96	3.15	2.88	-0.07	H12
J113833.3+004909	100	2.22	2.66	-0.14	_

Note. Reading from the left, the columns are: column $\overline{1}$ – the official H-ATLAS name; column 2 – HerBS number; column 3 – spectroscopic redshift; column 4 – photometric redshift using the best-fitting model; column 5 – (z_{spec} – z_{phot})/(1 + z_{spec}); column 6 – reference for the spectroscopic redshift: N10 – Negrello et al. (2010); F11 – Frayer et al. (2011); H12 – Harris et al. (2012); G13 – George et al. (2013); L13 – Lupu et al. (2012); B13 – Bussmann et al. (2013); H-p – Harris et al. (in preparation); R-p – Riechers et al. (in preparation); K-p – Krips et al. (in preparation); L-p – Lupu et al. (in preparation).

Table 5. The results of the fitting of the total sample, with a variable and fixed beta, and applying the template from Pearson et al. (2013) to our sources.

	Total	Fixed β	Pearson
$T_{\rm c}$ (K)	$21.29^{+1.35}_{-1.66}$	$20.47^{+0.26}_{-0.26}$	23.9
$T_{\rm h} ({\rm K})$	$45.80^{+2.88}_{-3.48}$	$44.05^{+0.52}_{-0.55}$	46.9
α	$26.69^{+5.61}_{-6.74}$	$30.46^{+1.32}_{-1.42}$	30.1
β	$1.83^{+0.14}_{-0.28}$	2 (fixed)	2 (fixed)
χ^2	812.58	812.96	1101.03
$\Delta z/(z_{\rm spec}+1)$	-0.03 ± 0.14	-0.03 ± 0.14	-0.01 ± 0.12

for each source is given in Table 4, and the mean and standard deviations of this quantity for each template are given in Table 5.

Fig. 6 shows $(z_{\rm spec} - z_{\rm phot})/(1 + z_{\rm spec})$ plotted against spectroscopic redshift for the three templates. The three distributions are very similar. We compare the redshift estimates against the method used in Ivison et al. (2016). They fit three different tem-

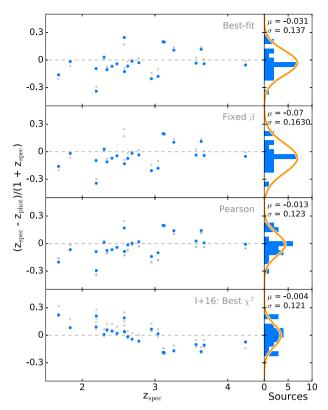


Figure 6. The top three panels show $(z_{\rm spec}-z_{\rm phot})/(1+z_{\rm spec})$ plotted against the spectroscopic redshift for the three templates. The blue dots in each panel show the points for the specified template, while the smaller grey dots show the points for the other two templates. The bottom panel shows $(z_{\rm spec}-z_{\rm phot})/(1+z_{\rm spec})$ for the three templates used for the redshift estimation in Ivison et al. (2016), where the blue dots correspond to the template fit with the lowest χ^2 for each source individually, and the smaller grey dots are the values of the two remaining templates.

plates [ALESS (Swinbank et al. 2014), Cosmic Eyelash (Ivison et al. 2010; Swinbank et al. 2010) and the template from Pope et al. (2008)] to the flux measurements, and use the redshift estimate from the spectrum with lowest χ^2 -value. When we apply this method to our sample of sources with spectroscopic redshifts, we achieve a slightly better redshift accuracy of \sim 12 per cent.

We note that the uncertainty in photometric redshift estimation using our new template, obtained from SCUBA-2 and *Herschel* measurements, is not actually any smaller than that using the template that Pearson et al. (2013) obtained from *Herschel* measurements alone. We discuss the significance of this in the Section 5.

Fig. 7 shows the normalized flux densities of the spectroscopic sources against their rest-frame wavelength, with the three templates overlaid. The flux densities are normalized to give each galaxy the same bolometric luminosity as HerBS-1.

We used the photometric redshifts estimates of our best-fitting template to derive observed bolometric luminosities of the HerBS sources. As the redshift estimates are determined from a different spectrum, some of the photometric redshift estimates, z_{phot} , fall below 2. They are, however, kept in the HerBS sample, as not to increase the complexity of the selection functions.

We calculate the observed bolometric luminosities by deriving the photometric redshift from our best-fitting template, and integrating the template from $\lambda_{rest} = 8$ to $1000 \, \mu m$. The estimated redshifts and bolometric luminosities are listed in Table A1, as well as the

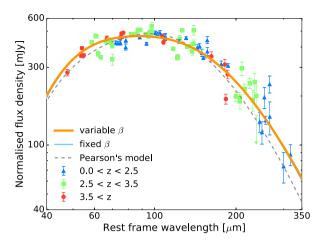


Figure 7. The flux densities of the spectroscopic sources plotted against rest-frame wavelength. The curves show the three templates (best fit is the thick orange line, fixed β is the thin blue line and Pearson's model is the dashed grey line), and all the flux densities of each source are scaled to produce the same bolometric luminosity as the brightest source (HerBS: 1). The sample is split up in three redshift intervals, to associate each galaxy's four data points more easily.

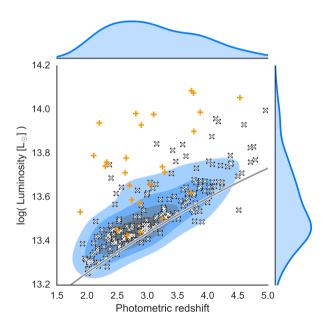


Figure 8. Observed bolometric far-infrared luminosity ($\lambda_{\rm rest} = 8-1000~\mu m$) plotted against photometric redshift, calculated with the best-fitting template. Sources with spectroscopic redshifts are plotted in orange plusses, although the redshifts used in the diagram are their photometric redshifts. The smoothed distributions of redshift and luminosity are shown on the sides of the scatter plots. The grey line shows bolometric luminosity for the best-fitting template, assuming $S_{500~\mu m} = 80~mJy$, as a function of redshift.

photometric redshift estimates using the method from Ivison et al. (2016). Fig. 8 shows the distribution of sources as a function of redshift and luminosity. This figure shows that the majority of our sources with a spectroscopic redshift are in the higher luminosity range, as typically spectroscopic campaigns aim for the brightest sources first.

5 DISCUSSION

5.1 Source confusion

We have selected our HerBS sample using a $500\,\mu m$ flux limit. The large beam width at this wavelength could cause us to confuse multiple line-of-sight sources into a single observed source, and hence yield a $500\,\mu m$ flux density that is too large.

Observationally, high-resolution studies of sub-millimetre galaxies show this to be the case, although the severity of this effect varies from study to study (Hodge et al. 2013; Koprowski et al. 2014). An SMA study by Chen et al. (2013) of sources selected at 450 μm only found 10 per cent of the sources to be significantly amplified by line-of-sight sources. An ALMA survey of 870 μm selected ALESS sources finds that up to 50 per cent of the sources are significantly affected (Hodge et al. 2013; Karim et al. 2013). Longer wavelengths and higher selection flux densities correlate with more source confusion, although all observational multiplicity studies so far focus on SMGs with a low probability of lensing.

A recent study by Scudder et al. (2016) used Bayesian inference methods to estimate the effects of source confusion in *Herschel* observations at $250\,\mu m$. They concluded that individual $250\,\mu m$ sources are often the combination of emission from more than one galaxy.

The solid angle of the beam of the JCMT at 850 µm is six times smaller than the beam of the 500 µm SPIRE observations. We do not see any of our HerBS sources resolve into multiple $>3\sigma$ -detected components. This suggests that our long-wavelength observations are not confused, unless the sources are clustered on a scale smaller than the JCMT's beam size. The small clustering size could be the case, as Karim et al. (2013) find the multiple emissions are separated less than 6 arcsec in the majority of cases of source confusion. Similarly, Chen et al. (2016) measured the clustering of SMGs on scales down to 1.5 arcsec using SCUBA-2 combined with deep nearinfrared and optical data, and they also report a steep increase in angular correlation below 6 arcsec. However, Hayward et al. (2013) simulated light cones to estimate the blending ratio of associated and unassociated SMGs for a 15 arcsec beam, and found that at least 50 per cent of all blended SMGs show an unassociated SMG. The HerBS sources are selected by their 500 µm flux, which has a 36 arcsec beam, and should therefore be more influenced by unassociated SMGs. As these unassociated SMGs are spatially unrelated to the source, they should have shown up in our JCMT analysis. A reason for the lack of source confusion could be due to our selection of lensed sources, as the probability for gravitational lensing is small, and two unrelated sources in the same Herschel beam are unlikely to be both lensed by the same galaxy.

Strong gravitational lensing could also be caused by a cluster of galaxies, which acts on a longer angular scale. These events are less common (Negrello et al. 2017), however Zavala et al. (2015) did report on the redshifts of cluster-lensed sources, one of which turned out to be three sources that was blended and lensed. We did not exclude these possibilities, however considering their infrequency, we can state that this lensing type would not influence the entire sample.

5.2 The diversity of galaxies

In Section 4, we fitted a two-temperature modified blackbody template to 22 HerBS sources with spectroscopic redshifts, the results of which can be seen in Table 5.

Both the fixed- β and best-fitting templates result in similar templates, as the β -value of the best-fitting template is similar within the error bars. The errors on the best-fitting template are slightly larger, as more parameters are being fitted. The temperatures on both fitted templates are slightly cooler than the template from Pearson et al. (2013); however, we do not find an indication of a cool gas component with a temperature $T < 20\,\mathrm{K}$, as found in Planck Collaboration XVI (2011) and Clements, Dunne & Eales (2010). The values we find for the temperatures agree broadly with the initial fitting attempts by Dunne & Eales (2001), and the overall findings of Clements et al. (2010).

The large χ^2 values in Table 5 imply that a single template is not actually a good representation of the data. We fit our template to 22 galaxies, each with four data points, except one source where we only fitted the three SPIRE fluxes, as its SCUBA-2 flux remained undetected. The free parameters in our model are the template parameters (three or four) and the amplitudes for each galaxy (22, equation 5). The expected χ^2 values for the two models, on the assumption that they are a good representation of the data, are therefore

$$\chi^{2}_{\text{best-fit}} \approx N_{\text{data}} - N_{\text{param}} - 1$$

$$\approx 4 \times 22 - 22 - 4 - 1$$

$$\approx 61,$$

$$\chi^{2}_{\text{fixed }\beta} \approx N_{\text{data}} - N_{\text{param}} - 1$$

$$\approx 4 \times 22 - 22 - 3 - 1$$

$$\approx 62.$$

However, we observe χ^2 -values of \sim 812, indicating that our sources are poorly modelled by a single galaxy template.

We tested the photometric redshift estimates of the templates using the same sources we used to derive the best-fitting template. However, we found no improvement in accuracy (Table 5) compared to the older template of Pearson et al. (2013). Similarly, Fig. 6 shows a similar pattern of redshift errors for all three templates. The redshift estimation by Ivison et al. (2016) might provide a slightly better estimation of the redshift, which are therefore added to the catalogue (Table A1). The explanation for this lack of improvement is almost certainly the diversity of the population; the limit on the accuracy of photometric redshift estimates is not set by the accuracy of the average template but by the fact that galaxies have different SEDs.

5.3 Redshift distribution of the HerBS sample

Fig. 9 shows the redshift distribution of the HerBS sample, compared against various other galaxy samples that are summarized in Table 6. The top panel compares the distribution to samples selected with a simple flux cut-off at 500 μm . The sample from Negrello et al. (2017) used a $S_{500\,\mu m}>100\, {\rm mJy}$ flux cut on 600 deg 2 of the H-ATLAS field (they used a conservative mask on the SGP field). The sample from Nayyeri et al. (2016) used the same flux cut on the 372 deg 2 HeLMS and HeRS fields. We plot the total sample from Wardlow et al. (2013). They used the 95 deg 2 HerMES survey, and their 500 μm flux cut-off went down to 80 mJy.

The bottom panel compares the HerBS redshift distribution against samples selected at various wavelengths. The sample from Ivison et al. (2016) is also from the H-ATLAS fields, and contains sources with a colour cut at $S_{500\,\mu\text{m}}/S_{250\,\mu\text{m}} > 1.5$ and $S_{500\,\mu\text{m}}/S_{350\,\mu\text{m}} > 0.85$, in order to select sources at high redshift. The sources were also selected to have relatively low 500 μ m flux

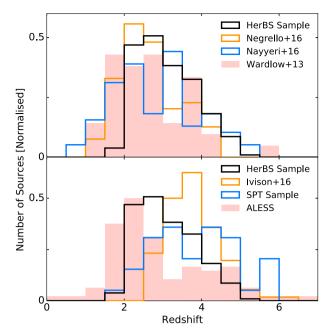


Figure 9. The top panel compares the redshift distribution of the HerBS sample (black) to that of three samples selected with *Herschell*/SPIRE at 500 µm. The bottom panel compares the redshift distribution of the HerBS sample (black) to that of three samples with different selection wavelengths and colour cuts

density of around 50 mJy, in order to select unlensed sources. Their unlensed nature reduces the uncertainty in the intrinsic luminosity of the source. The South Pole Telescope (SPT) lensed sample was selected from 2500 deg² SPT survey by a flux cut at $S_{1.4 \text{mm}} > 20$ mJy, and demanding the source has a dust-like spectrum. Low-redshift sources were removed with radio and far-infrared flux limits (Weiß et al. 2013; Strandet et al. 2016). The ALESS sample is initially selected from the LESS sample at $S_{870\,\mu\text{m}} > 4.4$ mJy from the 0.25 deg² *Extended Chandra Deep Field*-South (ECDFS) field (Weiß et al. 2009). ALMA observations of the LESS sample removed all contaminants, resulting in a final ALMA-LESS (ALESS) sample of 96 SMGs (Simpson et al. 2014).

All samples selected at $500 \, \mu m$ with a simple flux cut have a similar redshift profile, and do not differ significantly from the HerBS sample when we take the photometric redshift cut-off into account. Also, without the photometric redshift cut-off, the standard deviation of the HerBS sample would have been larger.

Typically, higher average redshifts are expected for longer selection wavelengths (Bethermin et al. 2015). We see this for the SPT sample, which has higher average redshifts. The ALESS sample, selected at 870 μm , has a higher average redshift than the 500 μm without redshift constraints, but a lower average redshift than the HerBS sample due to HerBS photometric redshift constraint. The SPT and ALESS samples have a larger standard deviation in their redshifts, because the K-correction is negative for wavelengths between 850 μm and $\sim\!\!3$ mm. Comparison with the Ivison's sample is difficult because of the more complicated selection criteria they employ.

A way of quantifying the similarity between the samples is using the Kolmogorov–Smirnov (KS) test. We compare each sample's sources with a redshift (spectroscopically or photometrically determined) greater than 2 to the photometric redshifts of the HerBS sources with $z_{\rm phot} > 2$. For each sample, we run this method 100 000 times while randomly varying the redshift of each source

Table 6. Redshift distributions of several submm samples.

Sample	$\langle z \rangle \pm \sigma$	Sources	Surface	KS σ-value	Selection criterion
HerBS	3.09 ± 0.71	209	616.4	1.27 ± 0.45	$S_{500 \mu\text{m}} > 80 \text{mJy}; z_{\text{phot}} > 2.0$
HerBS with z_{spec}	3.07 ± 0.72	22	616.4	2.01 ± 0.31	$S_{500 \mu m} > 80 \text{mJy}; z_{\text{phot}} > 2.0$
Negrello	2.64 ± 0.75	80	616.4	1.82 ± 0.77	$S_{500 \mu m} > 100 \text{mJy}$
Nayyeri	2.77 ± 1.02	77	372	0.66 ± 0.50	$S_{500 \mu m} > 100 \text{mJy}$
Wardlow	2.65 ± 0.90	42	95	0.93 ± 0.66	$S_{500 \mu m} > 80 \text{mJy}$
Ivison	3.80 ± 0.67	112	616.4	2.31 ± 0.84	$S_{500 \mu\text{m}} \sim 50 \text{mJy}; S_{500 \mu\text{m}} / S_{250 \mu\text{m}} > 1.5; S_{500 \mu\text{m}} / S_{350 \mu\text{m}} > 0.85$
SPT sample	3.81 ± 1.07	39	2500	0.88 ± 0.55	$S_{1.4\mathrm{mm}} > 20\mathrm{mJy}$
ALESS	2.90 ± 1.22	96	0.25	1.26 ± 0.54	$S_{870 \mu m} > 4.4 \text{mJy}$

according to a Gaussian distribution with a width of $\Delta z = 0.15(1+z)$. For the comparison to Ivison's sample, we only compare it to HerBS sources with a similar colour cut as they employed $(S_{500\,\mu\text{m}}/S_{250\,\mu\text{m}}>1.5$ and $S_{500\,\mu\text{m}}/S_{350\,\mu\text{m}}>0.85)$, which only 26 HerBS sources follow. For the SPT sample, we used our best-fitting template to estimate the flux at 1.4 mm, and only compared the sources that follow the SPT flux cut $(S_{1.4\,\text{mm}}>20\,\text{mJy})$, a property only 60 HerBS sources have. The ALESS flux criterion $(S_{870\,\mu\text{m}}>4.4\,\text{mJy})$ was also estimated using the best-fitting template, and was met by all our 209 sources.

We detail the KS probability values in terms of disagreement between two samples in standard deviations (σ) in Table 6. A comparison between the redistributed redshifts and the original, unvaried redshift estimates of the HerBS sources gives a 1.27 ± 0.45 times the standard deviation, which indicates we should expect rather large uncertainties in the probability measurements. The spectroscopic redshifts of the HerBS sources disagree with 2.01 ± 0.31 times the standard deviation with the redistributed redshifts. When we compare the photometric redshift estimates of these spectroscopic sources to the HerBS sample, this value drops to 0.79 ± 0.56 . Our HerBS sample thus appears probed evenly by the current set of HerBS sources with spectroscopic redshifts.

The sample from Negrello features more galaxies at low selected redshifts (2 < z < 3), causing the disagreement seen by the relatively high KS value. This is contrary to both Nayyeri and Wardlow's samples, who agree strongly with the HerBS sample, suggesting that these sources are drawn from the same population. Only one out of four sources with low 500 µm flux densities (~80 mJy) in Wardlow's sample was found to be lensed. This seems contradictory to the high likeness with the HerBS sample, which has a high lensing fraction of 76 per cent, found in Section 5.4. Only four of Wardlow's sources were checked for their lensing nature, which could indicate that their low lensing fraction is caused by small-number statistics. We can also think of two physical reasons for the low lensing fractions, namely the absence of a redshift selection and the actual decrease in the lensed fraction at lower flux densities. Redshift selection lifts the probability of lensing, by ensuring the sources are drawn from the redshift space most lensed sources are in (Strandet et al. 2016). Similarly, at lower flux densities, the fraction of lensed sources decreases, as can be seen in Fig. 10.

The SPT also seems to probe similar populations to the HerBS sources, further increasing our suspicion of a high lensing fraction in our sample. A slightly less strong agreement with the ALESS sample was found, which probes deeper on a smaller part of the sky. Interestingly, Strandet et al. (2016) report a disagreement of around 2.4 standard deviations between the SPT and ALESS sample. The HerBS sample likeness to the SPT sample is larger, suggesting this sample is more similar than to the deeper ALESS sample, especially as Strandet et al. (2016) found those two samples to be different. This

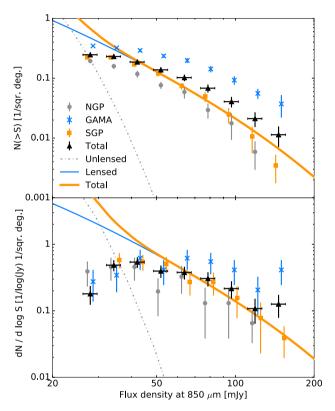


Figure 10. The top panel shows the cumulative number counts and the bottom panel shows the differential number counts of our HerBS sample, compared to the predictions of the model of Cai et al. (2013) for unlensed (dashed grey line) and lensed (solid blue line) galaxies.

is further proven by the small lensing fraction in the ALESS sample, compared to the sizeable lensing fraction in the SPT sample, and the lensing fraction we find in Section 5.4. However, Hodge et al. (2013) and Karim et al. (2013)'s studies of the ALESS sample did suggest a source confusion fraction on the order of 50 per cent of their sample. Even though our samples are not completely similar, this high blending percentage might indicate that our method of estimating the effects of source confusion with the JCMT's beam is incomplete. The low agreement to Ivison's sample suggests that their selection of unlensed SMGs was effective, and it indicates they might select different galaxies than our sample.

5.4 Lensing fraction

The SCUBA-2 observations do not resolve lensing directly, as the beam size (13 arcsec) is much larger than the typical Einstein rings caused by galaxy–galaxy lensing (~1 arcsec; Bussmann et al. 2013;

ALMA Partnership 2015). However, we can estimate the lensing fraction of our sample when we compare the distribution of flux densities of our sources to the predictions of galaxy evolution models that include gravitational lensing.

Here we use the hybrid model by Cai et al. (2013) with a cut-off lensing magnification factor of $\mu=30$. The hybrid model is based on a parametric backward model for redshifts lower than 1.5, whilst it calculates galaxy evolution for redshifts greater than 1.0 using physical models for the evolution of protospheroidal galaxies and their associated AGN. The model matches these two approaches to each other in the region between redshift 1.0 and 1.5. We assume all unlensed sources are high-redshift, protospheroidal galaxies. We did not observe all of the sample at 850 μ m, so we expect that our observed number counts are a lower limit.

Fig. 10 shows a comparison of our number counts at $850 \,\mu m$ with the predictions of the model of Cai et al. (2013). We have plotted the number counts for each of our fields, by summing the number of sources brighter than a given flux, and dividing by the corresponding area of the field, see Table 1. We estimate the error on the counts as the square root of the number of sources in each bin. A comparison of our counts with the predicted counts of the unlensed sources (grey dashed line) immediately suggests most of our sources are lensed. We can quantify this as follows.

At the low fluxes, the data deviate from the model, because of the incompleteness of the HerBS sample at fluxes lower than $\sim\!50\,\text{mJy}$. There are more sources than the model predicts at high fluxes, the significance of which is difficult to pin down due to the small number of sources. It is possible our sources have overestimated 850 μm fluxes, possibly due to source confusion. However, it is important to realize that the model of Cai et al. (2013) is based on fitted luminosity functions. The high flux end of the luminosity function requires large area surveys to be accurately fitted. As our sample is extracted from the largest area Herschel survey, the model is thus comparably uncertain as our data.

We calculate the total number of lensed sources,

$$N_{\text{lens}}(>S_{\nu}) = \sum_{i}^{N_{\text{gal}}(>S_{\nu})} p_{\text{lens}}(S_{\nu,i}).$$
 (7)

We sum the lensing probability, $p_{lens}(S_{\nu,i})$, over all galaxies brighter than the flux cut-off, $N_{gal}(>S_{\nu})$. We calculate the probability, $p_{lens}(S_{\nu,i})$, from the relative proportions of the differential number counts predicted for lensed and unlensed galaxies,

$$p_{\text{lens}}(S_{\nu,i}) = \left[\frac{dN_{\text{lens}}}{dS_{\nu}} \middle/ \left(\frac{dN_{\text{proto}}}{dS_{\nu}} + \frac{dN_{\text{lens}}}{dS_{\nu}} \right) \right]_{S_{\nu,i}}.$$
 (8)

The N_{lens} term refers to the lensed sources, and the N_{proto} term refers to the unlensed protospheroidal galaxies. We evaluate the probability at the flux density of the source, $S_{v,i}$. Using the bottom panel of Fig. 10, p_{lens} can be thought of as the fraction lenses (thin blue line) over the total sources (thick orange line).

We iterate this procedure a 1000 times, varying the 850 μ m flux with a Gaussian distribution with a width of the measurement uncertainty. Table 7 shows the predicted number of lensed sources (equation 7) and the observed number of sources for all SCUBA-2 detected HerBS sources. All of the errors are the standard deviations. Even for sources at $S_{850\,\mu\rm m}>30\,\rm mJy$, the predicted lensing fraction is $\sim\!92\,\rm per\,cent$, increasing to nearly all sources with $S_{850\,\mu\rm m}>40\,\rm mJy$.

We rerun the same procedure on the 500 μ m SPIRE fluxes, which shows that out of all 209 HerBS sources, we expect 158.1 \pm 1.7 lensed sources, giving a total lensing fraction of 75.6 \pm 0.8 per cent.

Table 7. Predicted lenses in the HerBS sample.

$S_{850\mu\mathrm{m}}~(\mathrm{mJy})$	$N(>S_{850\mu\mathrm{m}})$	Lenses	Percentage
All	152.0 ± 0.0	128.4 ± 2.1	84.5 ± 1.4
30	133.8 ± 3.4	123.3 ± 2.9	92.2 ± 0.9
40	107.6 ± 3.9	105.2 ± 3.7	97.8 ± 0.3
50	80.8 ± 3.6	80.5 ± 3.6	99.6 ± 0.1
60	60.0 ± 3.2	59.9 ± 3.2	99.9 ± 0.0
70	44.2 ± 2.9	44.2 ± 2.9	100.0 ± 0.0
80	32.4 ± 2.4	32.4 ± 2.4	100.0 ± 0.0
90	23.7 ± 2.0	23.7 ± 2.0	100.0 ± 0.0
100	17.4 ± 1.7	17.4 ± 1.7	100.0 ± 0.0
120	9.5 ± 1.3	9.5 ± 1.3	100.0 ± 0.0

This suggests that we are missing 29.7 ± 1.6 lensed sources with our SCUBA-2 observations.

Finally, we note that our counts in the GAMA fields are systematically higher than those in the other H-ATLAS fields, a point also noticed by Negrello et al. (2017). Using a similar method for the KS test as described in Section 5.3, we calculate the probability for the GAMA and non-GAMA sources, and find a disagreement of 0.61 \pm 0.47 standard deviations. This suggests the sources themselves do not differ significantly between the GAMA and the NGP+SGP fields.

6 CONCLUSIONS

The HerBS catalogue consists of the brightest, high-redshift sources in the H-ATLAS survey, selected with $S_{500\,\mu\mathrm{m}} > 80\,\mathrm{mJy}$ and $z_{\mathrm{phot}} > 2$. Initially, we selected 223 sources. SCUBA-2 observations of 203 of these sources allowed us to remove 14 blazars from the HerBS sample, leaving 20 HerBS sources unobserved. 152 out of the 189 confirmed high-redshift galaxies were detected at more than 3σ , within 10 arcsec of the SPIRE position. Currently, our HerBS sample consists of 209 galaxies.

While recent studies like Scudder et al. (2016) suggest a significant effect of source confusion in *Herschel* observations, none of our sources feature spatially extended emission with $>3\sigma$. While some sources could be confused on a scale not probed by the SCUBA-2 observations, the lack of any signs at the detectable scales gives us little evidence of source confusion significantly affecting the purity of our sample. A reason for this could be due to our high lensing fraction, especially those caused by galaxy–galaxy lensing systems, whose influence is on a smaller angular scale than the less common galaxy–cluster lensing event.

We fitted a two-temperature blackbody as a template to the subset of 22 HerBS sources with spectroscopically determined redshifts, as well as to subsamples where we divided our sources in redshift or luminosity. We find a cold- and hot-dust temperature of $21.29^{+1.35}_{-1.66}$ and $45.80^{+2.88}_{-3.48}$ K, a cold-to-hot dust mass ratio of $26.62^{+5.61}_{-6.74}$ and a β of $1.83^{+0.14}_{-0.28}$. Overall, the fitted parameters are similar to previous work from Pearson et al. (2013), and they agree broadly with the previous work from Dunne & Eales (2001) and Clements et al. (2010). We do not find evidence of any cold gas with temperatures below 20 K, as was found in Planck Collaboration XVI (2011).

We find a high χ^2 for the template, implying that the SEDs of the high-redshift population are diverse and cannot be represented by a single template. We showed that our improved template, which incorporates the SCUBA-2 flux densities, does not give a more accurate redshift estimates, which can also be explained by the diversity of the population.

Our sample has a similar redshift distribution as other samples selected at $500\,\mu m,$ when we take the photometric redshift cut-off into account. KS tests indicate that we probe a similar sample of galaxies as the SPT sample.

We calculated the number counts of the 850 μ m observations of our sources, and compared them to a galaxy population model by Cai et al. (2013). From this comparison we predict that 128.4 \pm 2.1 out of the 152 SCUBA-2 detected, high-redshift galaxies are strongly lensed. A model based around the 500 μ m flux suggests a total of 158.1 \pm 1.7 of the 209 HerBS sources to be strongly lensed. We report finding more lensed galaxies in the GAMA equatorial fields, when compared to the galaxy population model of Cai et al. (2013), and the other fields (SGP+NGP).

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REFERENCES

ALMA Partnership, 2015, ApJ, 808, L4

Avni Y., 1976, ApJ, 210, 642

Bethermin M., De Breuck C., Sargent M., Daddi E., 2015, A&A, 576, L9

Blain A. W., Longair M. S., 1993, MNRAS, 264, 509

Blain A., Perrotta F., González J. G.-N., Silva L., De Zotti G., Granato G. L., Baccigalupi C., Danese L., 1999, ApJ, 512, L87

Blain A. W., Smail I., Ivison R. J., Kneib J. P., Frayer D. T., 2002, Phys.

Rep., 369, 111

Borys C. et al., 2006, ApJ, 636, 134

Bussmann R. S. et al., 2012, ApJ, 756, 134

Bussmann R. S. et al., 2013, ApJ, 779, 25

Cai Z.-Y. et al., 2013, ApJ, 768, 21

Casey C. M., Narayanan D., Cooray A., 2014, Phys. Rep., 541, 45

Chapin E. L., Berry D. S., Gibb A. G., Jenness T., Scott D., Tilanus R. P. J., Economou F., Holland W. S., 2013, MNRAS, 430, 2545 Chapman S. C., Perrotta F., González J. G.-N., Silva L., De Zotti G., Granato G. L., Baccigalupi C., Danese L., 2005, ApJ, 622, 772

Chen C.-C., Cowie L. L., Barger A. J., Casey C. M., Lee N., Sanders D. B., Wang W.-H., Williams J. P., 2013, ApJ, 776, 131

Chapin E., Dempsey J., Jenness T., Scott D., Thomas H., Tilanus R., 2010, The SCUBA-2 SRO Data Reduction Cookbook, Starlink Cookbook 19

Chen C.-C. et al., 2016, ApJ, 820, 82

Clements D. L., Dunne L., Eales S., 2010, MNRAS, 403, 274

Conley A. et al., 2011, ApJ, 732, L35

Cox P. et al., 2011, ApJ, 740, 63

Dempsey J. T. et al., 2013, MNRAS, 430, 2534

Driver S. P. et al., 2011, MNRAS, 413, 971

Dunne L., Eales S. A., 2001, MNRAS, 327, 697

Dye S. et al., 2015, MNRAS, 452, 2258

Eales S. A., 2015, MNRAS, 446, 3224

Eales S. et al., 2010, PASP, 122, 499

Frayer D. T. et al., 2011, ApJ, 726, L22

Fu H. et al., 2012, ApJ, 753, 134

George R. D. et al., 2013, MNRAS, 436, L99

González-Nuevo J. et al., 2012, ApJ, 749, 65

Griffin M. J. et al., 2010, A&A, 518, L3

Harris A. I. et al., 2012, ApJ, 752, 152

Hatsukade B., Tamura Y., Iono D., Matsuda Y., Hayashi M., Oguri M., 2015, PASJ, 67, 93

Hayward C. C., Behroozi P. S., Somerville R. S., Primack J. R., Moreno J., Wechsler R. H., 2013, MNRAS, 434, 2572

Hezaveh Y. D. et al., 2016a, ApJ, 823, 37

Hezaveh Y. D., Perrotta F., González J. G.-N., Silva L., De Zotti G., Granato G. L., Baccigalupi C., Danese L., 2016b, J. Cosmol. Astropart. Phys., 11, 048

Hodge J. A. et al., 2013, ApJ, 768, 91

Holland W. S. et al., 2013, MNRAS, 430, 2513

Hughes D. H. et al., 1998, Nature, 394, 241

Ikarashi S. et al., 2011, MNRAS, 415, 3081

Ivison R. J. et al., 2010, A&A, 518, L35

Ivison R. J. et al., 2013, ApJ, 772, 137 Ivison R. J. et al., 2016, ApJ, 832, 78

Karim A. et al., 2013, MNRAS, 432, 2

Koprowski M. P., Dunlop J. S., Michałowski M. J., Cirasuolo M., Bowler R. A. A., 2014, MNRAS, 444, 117

Liske J. et al., 2015, MNRAS, 452, 2087

López-Caniego M. et al., 2013, MNRAS, 430, 1566

Lupu R. E. et al., 2012, ApJ, 757, 135

Madau P., Dickinson M., 2014, ARA&A, 52, 415

Nayyeri H., Perrotta F., González J. G.-N., Silva L., De Zotti G., Granato G. L., Baccigalupi C., Danese L., 2016, ApJ, 823, 17

Negrello M., Perrotta F., González J. G.-N., Silva L., De Zotti G., Granato G. L., Baccigalupi C., Danese L., 2007, MNRAS, 377, 1557

Negrello M. et al., 2010, Science, 330, 800

Negrello M. et al., 2017, MNRAS, 465, 3558

Oguri M., Perrotta F., González J. G.-N., Silva L., De Zotti G., Granato G. L., Baccigalupi C., Danese L., 2012, AJ, 143, 120

Pearson E. A. et al., 2013, MNRAS, 435, 2753

Pilbratt G. L. et al., 2010, A&A, 518, L1

Planck Collaboration XVI, 2011, A&A, 536, A16

Planck Collaboration XIII, 2016, A&A, 594, A13

Poglitsch A. et al., 2010, A&A, 518, L2

Pope A. et al., 2008, ApJ, 689, 127

Rybak M., McKean J. P., Vegetti S., Andreani P., White S. D. M., 2015, MNRAS, 451, L40

Sawicki M., 2012, PASP, 124, 1208

Schaye J. et al., 2015, MNRAS, 446, 521

Scudder J. M., Oliver S., Hurley P. D., Griffin M., Sargent M. T., Scott D., Wang L., Wardlow J. L., 2016, MNRAS, 460, 1119

Simpson J. M., Perrotta F., González J. G.-N., Silva L., De Zotti G., Granato G. L., Baccigalupi C., Danese L., 2014, ApJ, 788, 125

Smail I., Perrotta F., González J. G.-N., Silva L., De Zotti G., Granato G. L., Baccigalupi C., Danese L., 2002, MNRAS, 331, 495

Springel V. et al., 2005, Nature, 435, 629

Strandet M. L. et al., 2016, ApJ, 822, 80

Swinbank A. M. et al., 2010, Nature, 464, 733

Swinbank A. M. et al., 2014, MNRAS, 438, 1267

Swinbank A. M. et al., 2015, ApJ, 806, L17

Tamura Y., Oguri M., Iono D., Hatsukade B., Matsuda Y., Hayashi M., 2015, PASJ. 67, 72

Thomson A. P. et al., 2017, ApJ, 838, 119

Treu T., 2010, ARA&A, 48, 87

Valiante E. et al., 2016, MNRAS, 462, 3146

Vegetti S., Lagattuta D. J., McKean J. P., Auger M. W., Fassnacht C. D., Koopmans L. V. E., 2012, Nature, 481, 341

Wardlow J. L. et al., 2011, MNRAS, 415, 1479

Wardlow J. L., Perrotta F., González J. G.-N., Silva L., De Zotti G., Granato G. L., Baccigalupi C., Danese L., 2013, ApJ, 762, 59

Weiß A. et al., 2009, ApJ, 707, 1201

Weiß A. et al., 2013, ApJ, 767, 88 Zavala J. A. et al., 2015, MNRAS, 452, 1140

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APPENDIX A: HerBS CATALOGUE AND BLAZARS

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Table A1. The HerBS sample – SPIRE and SCUBA-2 data. The HerBS number hyperlinks to the NED data base at the position of the source. The RA and Dec. are the SPIRE positions, \triangle RA and \triangle Dec. are the SPIRE positions minus the SCUBA-2 positions. Cursive SCUBA-2 observations are classed as non-detections, as discussed in Section 3. The spectroscopic redshifts are discussed in Section 4, zhon temp refers to the template derived in Section 4 and z_{phot}, 1vi refers to the photometric redshift estimates in Ivison et al. (2016). The bolometric luminosity is calculated using the fitted photometric template.

No.	H-ATLAS ID	RA (h m s)	Dec. (°"')	ΔRA (arcsec)	ΔDec. (arcsec)	S ₂₅₀ (mJy)	S ₃₅₀ (mJy)	S ₅₀₀ (mJy)	S ₈₅₀ (mJy)	Zspec	Zphot,temp	Zphot,Ivi	Lum. $\log (L_{\bigodot})$
1	J134429.5+303034 J114637.9-001132 J132630.1+334408 J083051.0+013225	206.1228 176.6582 201.6255 127.7127	30.5095 -0.1923 33.7355 1.5403	-1.4 -3.61 -2.11 -0.34	2.04 5.15 4.02 4.02	461.9 ± 5.8 316.0 ± 6.6 190.5 ± 5.6 248.5 ± 7.5	465.7 ± 6.5 357.9 ± 7.4 281.3 ± 5.9 305.3 ± 8.1	+++++	+++++	2.30 3.26 2.95 3.63	2.21 2.81 3.77 3.10	2.33 2.54 3.21 2.81	13.94 13.98 14.08 13.98
	J125634.5+233627 J132427.0+284450 J132859.2+292327 J084933.4+021442 J125135.3+261458	194.1352 201.1126 202.2468 132.3893 192.8972	23.6076 28.7472 29.3907 2.2453 26.2494	- 1.71 - 3.17 - 2.95 - 3.39 0.44	2.97 2.97 5.97 -0.95 0.01	209.3 ± 5.6 342.3 ± 5.6 268.4 ± 4.4 216.7 ± 7.5 157.9 ± 5.9	+ + + + +	264.0 ± 7.0 250.9 ± 6.9 248.9 ± 5.9 208.6 ± 8.6 206.8 ± 6.9	160.0 ± 9.7 71.3 ± 10.5 149.1 ± 10.9 61.7 ± 9.7 138.3 ± 10.4	3.56 1.68 2.78 2.41 3.68	2.73 2.11 2.65 3.88	3.11 2.27 2.53 2.57 3.17	14.09 13.79 13.78 13.78
10 112a 123a 14a 15a	J113526.2—014606 J012407.4—281434 J133008.6+245900 J142413.9+022303 J013840.5—281856 J141351.9—0000026	173.8596 21.0308 202.5358 216.0582 24.6687 213.4666	- 1.7685 - 28.2428 24.9833 2.3842 - 28.3154 - 0.0075	- 0.01 - 4.57 - 3.49 - 4.55 - 2.14	-0.05 0.97 0.03 1.97 -2.01	278.8 ± 7.4 257.5 ± 6.4 271.2 ± 5.4 112.2 ± 7.3 116.3 ± 6.1 18.8 6 + 7.4	282.9 ± 8.2 271.1 ± 6.3 278.2 ± 5.9 182.2 ± 8.2 177.0 ± 6.3	204.0 ± 8.6 204.0 ± 7.2 203.5 ± 6.9 193.3 ± 8.5 179.3 ± 7.5	116.3 ± 9.0 94.0 ± 10.3 108.0 ± 10.8 141.3 ± 9.2 103.8 ± 10.8 61.8 ± 8.7	3.13 - 3.11 - 4.24 - 24 - 48	2.33 2.37 2.30 4.54 4.14 2.53	2.35 2.34 3.35 5.55 5.55	13.76 13.75 13.74 14.06 13.96
16^a 17^a 18^a 19^a	J141004.7+020306 J232531.4-302236 J232419.8-323927 J090311.6+003907 J132504.4+311534	212.5196 351.3806 351.0825 135.7987 201.2682	2.0519 -30.3765 -32.6574 0.6521 31.2595	- 2.81 - 5.33 - 4.59 - 0.24	-1.95 1.98 0.05 -0.97 4.04	++++++	++++++	+++++	+++++	3.04	4.18 3.16 2.40 3.77 1.89	3.36 2.77 2.65 3.11	13.95 13.84 13.69 13.90
21 ^a 22 ^a 23 ^a 24 25 ^a 25 ^a 25 ^a 27	J234418.1–303936 J002624.8–341738 J012046.5–282403 J004736.0–272951 J235827.7–323244 J225844.8–295125 J011424.9–333614	356.0755 6.6035 20.1936 11.9 359.6153 344.6867	- 30.6601 - 34.2938 - 28.401 - 27.4974 - 32.5456 - 29.8569 - 29.8569	- 3.05 - 3.21 - 5.14 - 3.42 - 3.82 - 0.03 - 6.66	3.05 1.99 - 0.98 - 0.01 - 0.01 - 1.98	+++++++++++	+++++++++++	155.1 ± 7.4 148.8 ± 7.2 145.7 ± 7.8 145.6 ± 7.4 143.4 ± 6.5 142.6 ± 7.8 138.6 ± 7.0	+++++++++++	1 1 1 1 1 1 1	3.59 3.42 4.07 2.57 3.64 2.48 4.96	3.01 2.84 3.32 2.53 3.07 4.04	13.84 13.82 13.88 13.65 13.62 14.00
28° 29° 30	J230815.6–343801 J133846.5+255055 J132301.7+341649 T125652 5+275900	347.065 204.6939 200.757	- 34.6337 25.8485 34.2804 27.9834	1.09 - 1.72 - 3.89	3.98 2.97 2.98	79.4 ± 5.8 159.0 ± 5.8 124.1 ± 5.6 133.9 ± 5.8	+++++	140.0 ± 7.4 137.6 ± 7.5 137.0 ± 7.2 131.8 ± 7.4		2.34 2.19	4.60 2.70 3.29 3.25	2.54 2.87 2.87	13.93 13.65 13.72
31° 32° 33° 34° 35°	J12562.:.+275900 J091840.8+023048 J224805.4-335820 J133413.8+260458 J133543.0+300402	194.2186 139.6702 342.0223 203.5577 203.929	27.9834 2.5135 -33.9723 26.0828 30.0671	1.61 - 0.45 - 1.84 - 7.14 - 2.74	1.0 2.04 1.05 1.05 3.04	+++++	164.1 ± 6.0 150.7 ± 8.2 135.6 ± 6.6 161.0 ± 5.5 145.7 ± 5.8	131.8 ± 7.4 128.4 ± 8.7 126.9 ± 7.5 126.5 ± 6.8 125.0 ± 6.9	88.6 ± 8.8 61.5 ± 9.2 68.4 ± 9.2 61.4 ± 12.6 58.7 ± 8.7	2.58	3.25 3.04 3.14 2.84 2.74	2.73 2.74 2.60 2.53	13.74 13.66 13.66 13.63 13.59
36 37 ^a 38 ^a 39 ^a 40 ^a	J235623.1–354119 J232623.0–342642 J144608.6+021927 J232900.6–321744 J013240.0–330907	359.0961 351.596 221.5359 352.2526 23.1666	- 35.6886 - 34.4451 2.3242 - 32.2956 - 33.1518	- 1.68 - 0.49 19.42 - 0.7 4.41	4.02 - 1.96 - 12.99 6.99 2.08	++++++	161.0 ± 6.7 178.4 ± 5.2 111.7 ± 8.1 141.2 ± 5.5 148.8 ± 6.5	125.5 ± 7.7 123.5 ± 6.6 122.1 ± 8.7 119.7 ± 6.8 117.7 ± 7.3		1 1 1 1 1	3.47 2.46 4.08 3.00 2.99	2.83 2.67 3.35 2.99	13.76 13.57 13.75 13.62 13.61
41 42 ^a	J000124.9–354212 J000007.5–334060	0.3537	-35.7033 -33.6833	2.42 - 2.62	-2.05 -0.03	63.3 ± 6.2 130.3 ± 5.8	91.1 ± 6.1 160.0 ± 6.1	121.7 ± 7.4 116.2 ± 6.8	56.7 ± 9.3 84.6 ± 9.0	1 1	4.39	3.91 2.66	13.75

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Table A

Lum. $\log(L_{\odot})$	13.77 13.49 13.39	13.49 13.50 13.47 13.68	13.45 13.83 13.39 13.73	13.65 13.64 13.59 13.57	13.79 13.46 13.43 13.83	13.45 13.65 13.42 13.42 13.42	13.62 13.67 13.56 13.50 13.45	13.44 13.54 13.60 13.51 13.36 13.36 13.59 13.45 13.47
Zphot,Ivi	3.19 2.54 2.11	2.52 2.51 2.39 3.18 2.82	2.35 3.89 2.33 3.10 2.53	3.09 2.65 2.72 2.57 3.21	3.36 2.50 2.41 3.88 2.53	2.48 3.20 2.33 2.53 2.48	3.25 3.10 2.53 3.03 2.42	2.53 2.72 2.90 2.62 2.34 2.93 2.53 4.03 2.57
Zphot,temp	4.02 2.14 1.93	2.53 2.54 2.39 3.78 3.40	2.25 4.76 2.11 3.81 2.80	3.64 3.09 3.22 2.88 3.88	4.38 2.44 2.44 4.71 2.75	2.50 3.88 2.20 2.16 2.32	3.72 3.81 2.90 2.99 2.41	2.53 2.94 3.45 2.87 2.18 3.36 2.57 2.57 2.66
Zspec	1 1 1	1 1 1 1 1	1 1 1 1 1	_ _ _ _ _ _	1 1 1 1 1	2.19	2.58	1 1 1 1 1 1 1 1 1 1
S ₈₅₀ (mJy)	81.2 ± 11.4 51.1 ± 10.2 27.3 ± 10.4	39.8 ± 10.2 35.5 ± 11.2 40.7 ± 9.5 40.9 ± 11.6 88.8 ± 8.4	42.5 ± 9.0 80.1 ± 12.0 27.2 ± 8.9 96.5 ± 11.1 38.2 ± 10.3	47.0 ± 10.3 85.9 ± 10.4 59.5 ± 13.0 67.1 ± 9.0 56.7 ± 9.8	79.6 ± 9.4 36.1 ± 9.6 33.8 ± 10.6^{b} 96.5 ± 10.6 46.3 ± 7.3	40.2 ± 9.2 61.3 ± 9.8 48.5 ± 9.1 41.8 ± 11.2 20.2 ± 9.7	25.4 ± 10.0 68.5 ± 10.0 73.3 ± 10.1 29.8 ± 9.9 44.9 ± 10.7^b	31.5 ± 8.9 28.6 ± 10.4 60.8 ± 8.9 48.8 ± 9.1 22.0 ± 9.5 42.7 ± 9.6 35.3 ± 9.4 71.2 ± 10.0 36.8 ± 9.6 27.2 ± 10.4
S ₅₀₀ (mJy)	115.4 ± 6.3 114.9 ± 7.2 113.1 ± 7.6	111.8 \pm 8.7 111.4 \pm 6.3 110.9 \pm 7.7 110.4 \pm 7.3 110.2 \pm 8.6	110.3 ± 8.7 109.4 ± 7.2 108.4 ± 8.8 108.6 ± 7.1 107.1 ± 6.6	105.8 ± 6.7 105.4 ± 6.4 104.5 ± 7.1 104.3 ± 7.7 103.6 ± 7.5	103.9 ± 7.7 103.4 ± 8.6 102.0 ± 7.0 101.5 ± 6.4 101.6 ± 7.7	101.5 ± 7.9 100.8 ± 8.0 100.5 ± 6.6 100.3 ± 7.3 100.0 ± 7.1	99.8 ± 8.8 99.6 ± 7.7 99.6 ± 7.4 98.8 ± 8.7 98.7 ± 7.8	98.5 ± 7.0 98.3 ± 7.7 98.2 ± 8.8 97.9 ± 7.3 97.7 ± 7.6 97.5 ± 7.2 96.8 ± 8.0 94.1 ± 8.8 97.0 ± 7.6
S ₃₅₀ (mJy)	116.0 ± 5.2 186.8 ± 5.8 160.2 ± 6.1	132.6 ± 8.4 138.7 ± 5.1 142.6 ± 7.4 110.9 ± 6.2 142.8 ± 8.2	149.2 ± 8.1 96.8 ± 5.9 137.7 ± 8.2 116.1 ± 6.1 116.5 ± 5.5	106.1 ± 5.5 147.3 ± 5.2 111.5 ± 5.9 136.8 ± 7.4 101.2 ± 6.1	112.1 ± 7.4 135.5 ± 8.2 121.0 ± 6.0 101.1 ± 5.3 98.3 ± 7.2	123.7 ± 7.7 88.1 ± 6.5 144.8 ± 5.4 154.5 ± 6.0 136.8 ± 5.8	105.8 ± 8.2 100.7 ± 7.4 129.0 ± 6.2 104.1 ± 8.1 134.7 ± 5.9	124.3 ± 6.0 135.2 ± 8.9 102.4 ± 8.1 115.3 ± 6.0 122.1 ± 6.3 114.8 ± 5.9 123.2 ± 7.6 79.7 ± 8.1 123.0 ± 6.4 104.2 ± 7.4
S ₂₅₀ (mJy)	84.4 ± 4.9 164.3 ± 5.8 164.6 ± 5.8	126.7 ± 7.3 127.4 ± 4.6 136.6 ± 6.6 76.8 ± 6.0 114.3 ± 7.3	143.2 ± 7.4 57.4 ± 5.8 141.2 ± 7.4 94.0 ± 5.7 109.0 ± 5.3	80.3 ± 5.4 118.1 ± 4.9 99.0 ± 5.5 118.2 ± 6.4 73.3 ± 5.8	67.4 ± 6.5 119.7 ± 7.4 119.3 ± 5.4 60.2 ± 4.8 109.6 ± 6.4	119.8 ± 6.8 73.0 ± 5.9 139.1 ± 5.3 140.4 ± 5.8 119.6 ± 5.8	67.8 ± 7.3 78.8 ± 6.5 117.1 ± 6.0 88.7 ± 7.4 124.4 ± 5.8	108.5 ± 5.9 93.2 ± 5.8 87.7 ± 7.3 103.4 ± 5.6 122.7 ± 5.7 82.8 ± 5.6 114.5 ± 6.7 49.5 ± 7.2 105.1 ± 5.9
ΔDec. (arcsec)	2.0 1.99 -5.96	4.99 4.01 - 0.37 4.95 3.0	-0.04 3.0 0.16 1.01 5.02	2.0 - 2.06 2.0 3.02 0.03	- 5.96 - 0.53 - 4.97 - 2.05	$ \begin{array}{c} -1.88 \\ 1.01 \\ 4.02 \\ 2.04 \\ 20.02 \end{array} $	3.19 0.97 6.0 16.21 2.98	-0.0 -14.01 1.03 -5.03 6.97 -1.02 -5.04 4.87 4.01
ΔRA (arcsec)	- 3.38 - 1.36 0.12	3.08 - 0.7 - 3.14 - 1.87 - 1.83	-6.67 -2.67 -3.76 -8.92 2.99	- 5.82 - 1.75 - 2.63 - 2.25 - 7.39	- 1.65 - 1.16 - 8.09 - 1.62 - 0.49	- 1.67 - 2.19 - 4.33 - 5.03 - 14.49	-21.18 -1.38 0.04 -0.91 -6.97	5.77 17.72 - 4.33 4.69 3.68 - 7.33 - 5.57 - 2.73 - 9.42
Dec. (° "' ')	32.1311 34.3689 - 30.3134	- 0.8148 - 31.6161 - 0.8229 - 33.1774 - 1.215	- 1.7841 25.8249 - 1.4437 26.3895 - 32.2462	-30.6234 -30.5193 24.7786 -0.8956 -27.5229	- 1.6789 - 0.8723 - 30.3366 25.619 23.3311	- 1.6313 - 32.6999 - 30.9745 - 31.0834 29.4882	- 0.8525 - 0.253 - 33.4554 0.5832 - 27.7344	34.3097 -31.2017 2.0715 33.8719 -31.4646 1.1106 1.3116 -34.0086 -0.9754
RA (h m s)	201.0792 203.2325 12.8867	221.4838 343.2114 183.2566 346,4427 180.8296	181.7886 192.8577 177.801 198.9192 24.9664	8.0321 12.2219 195.8881 138.2708 14.351	180.3652 183.9281 12.8833 195.3252 206.0943	179.584 340.5301 339.4743 21.0666 195.4176	173.1795 221.3006 22.2208 181.5029 19.5991	203.892 14.1234 218.4685 198.642 345.0109 5.2274 182.9369 184.5534 341.0035
H-ATLAS ID	J132419.0+320752 J133255.8+342208 J005132.8-301848	J144556.1—004853 J225250.7—313658 J121301.5—004922 J230546.3—331039 J120319.1—011253	J120709.2—014702 J125125.8+254930 J115112.2—012637 J131540.6+262322 J013951.9—321446	J003207.7-303724 J004853.3-303110 J130333.1+244643 J091304.9-005344 J005724.2-273122	J120127.6-014043 J121542.7-005220 J005132.0-302012 J130118.0+253708 J134422.6+231952	J115820.1—013752 J224207.2—324159 J223753.8—305828 J012416.0—310500 J130140.2+292918	J113243.0—005108 J144512.1—001510 J012853.0—332719 J120600.7+003459 J011823.8—274404	J133534.1+341835 J005629.6-311206 J143352.4+020417 J131434.1+335219 J230002.6-315005 J02054.6-312752 J121144.8+010638 J121812.8+011841 J224400.8-340031
No.	43 <i>a</i> 44 <i>a</i> 45 <i>a</i>	46 ^a 47 ^a 48 49 ^a 50	51 52 ^a 53 54 ^a 55 ^a	56 ^a 57 ^a 58 ^a 59 ^a 60	61 ^a 62 63 ^a 64 ^a 65 ^a	66 68 ^a 69 ^a 70	71 72 73 74 75	77 77 77 77 80 80 82 83 83 83 84 85

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Lum. $\log (L_{\odot})$	13.58 13.40 13.50 13.75 13.75	13.32 13.82 13.48 13.45	13.44 13.42 13.49 13.46 13.38 13.38	13.43 13.32 13.51 13.35	13.38 13.56 13.43 13.67	13.39 13.61 13.55 13.46 13.42	13.74 13.63 13.57 13.52 13.57	13.55 13.46 13.36 13.31 13.52	13.53 13.41 13.40 13.65 13.29
Zphot,Ivi	3.00 2.46 3.10 3.37 3.36	2.07 4.02 2.87 2.57 3.48	2.72 2.78 4.40 2.67 2.53 3.09	2.35 2.21 2.96 2.33	2.53 2.87 2.34 3.22	2.70 3.05 2.89 2.73 2.63	3.38 2.94 3.28 2.96 3.05	2.93 3.16 2.39 2.06 2.96	2.95 2.43 2.49 3.35 2.29
Zphot,temp	3.56 2.36 3.25 4.21 4.08	1.97 5.23 3.15 2.70 4.39	2.89 2.70 3.79 2.75 2.67 2.28 3.67	2.36 1.98 3.31 2.13	2.54 3.27 2.35 3.96	2.42 3.77 3.28 2.99 2.38	4.33 3.59 3.80 3.46 3.63	3.28 3.09 2.38 2.03 3.22	3.29 2.44 2.47 4.12 2.03
zsbec	3.10	1 1 1 1 1	3.15	1 1 1 1	1 1 1 1	1 1 1 1 1	1 1 1 1 1	1 1 1 1 1	1 1 1 1 1
S ₈₅₀ (mJy)	53.0 ± 8.1 30.3 ± 8.0 19.4 ± 8.9 81.8 ± 7.3 48.4 ± 9.2	34.0 ± 9.5 - 30.2 ± 8.3 33.3 ± 9.4	+++++++++++++++++++++++++++++++++++++++	59.1 ± 10.9 28.2 ± 8.7 37.6 ± 7.5 33.1 ± 9.9	1 + 1 + 1 + 1	24.7 ± 10.6 - 44.6 ± 8.7 30.2 ± 10.4	80.8 ± 9.3 62.7 ± 10.7 23.3 ± 11.1^{b} 17.4 ± 11.3 29.5 ± 9.3	54.1 ± 11.4 21.9 ± 9.1^{b} 29.1 ± 11.4 42.5 ± 9.3 38.9 ± 7.2	48.2 ± 10.2 - 37.6 ± 8.0 56.4 ± 8.9 24.8 ± 8.4
S ₅₀₀ (mJy)	96.0 ± 7.4 96.0 ± 7.3 95.9 ± 8.8 95.7 ± 7.0 95.6 ± 7.4	95.1 ± 8.6 94.9 ± 7.2 94.8 ± 7.0 94.7 ± 6.9 94.7 ± 7.6	+++++++++++++++++++++++++++++++++++++++		1 + + + + +	92.7 ± 7.4 92.2 ± 7.0 92.0 ± 7.0 91.8 ± 7.7 91.8 ± 6.9	93.6 ± 8.5 91.6 ± 6.9 90.9 ± 7.7 91.2 ± 8.6 90.7 ± 7.6	90.6 ± 7.2 90.3 ± 7.6 90.0 ± 7.5 89.8 ± 8.6 89.8 ± 7.1	89.8 ± 8.8 89.5 ± 6.9 89.2 ± 7.1 89.0 ± 7.0 88.8 ± 8.6
S ₃₅₀ (mJy)	90.7 ± 5.8 127.8 ± 6.1 96.0 ± 8.1 103.4 ± 5.7 96.9 ± 6.2	128.8 ± 8.1 75.3 ± 6.0 87.3 ± 5.7 114.4 ± 6.0 101.3 ± 5.7	+++++++++	131.2 ± 5.7 128.5 ± 6.1 88.5 ± 8.1 125.6 ± 5.9	1 +1 ++ ++	115.6 ± 6.2 87.0 ± 5.8 103.4 ± 6.0 93.8 ± 6.0	96.6 ± 8.2 112.7 ± 5.9 84.3 ± 6.6 85.6 ± 8.1 101.3 ± 6.4	99.1 ± 6.3 95.8 ± 6.0 107.9 ± 6.0 116.1 ± 8.2 103.4 ± 5.7	95.9 ± 8.2 122.7 ± 6.1 111.2 ± 5.9 85.4 ± 5.9 118.7 ± 8.1
S ₂₅₀ (mJy)	77.4 ± 5.6 114.7 ± 5.2 71.0 ± 7.6 71.8 ± 5.7 59.5 ± 5.9	139.2 ± 7.3 42.2 ± 5.7 77.3 ± 5.4 100.0 ± 5.4 61.9 ± 5.7	+++++++++++++++++++++++++++++++++++++++		1 + + + + +	105.9 ± 6.5 71.8 ± 5.8 80.7 ± 5.9 81.7 ± 5.9 116.2 ± 5.6	65.1 ± 7.4 81.0 ± 5.6 60.0 ± 6.3 68.5 ± 7.2 61.8 ± 5.9	85.4 ± 6.0 73.7 ± 5.7 106.2 ± 5.9 135.7 ± 7.3 75.7 ± 5.8	81.9 ± 7.2 110.0 ± 5.5 106.4 ± 5.7 59.4 ± 5.9 119.4 ± 7.3
ΔDec. (arcsec)	-0.96 3.02 -12.98 -1.03	1.01 - 0.03 - 2.02	- 4.28 6.0 - 3.01 - 4.04 - 13.92 0.03	4.01 5.96 - 5.0 0.94	3.94	1.04 - - 1.95 - 3.99	$0.49 \\ 3.04 \\ -1.97 \\ -12.84 \\ 3.04$	0.01 5.0 - 0.01 - 3.85 - 2.0	2.05 - 0.02 - 0.02 - 4.95
ΔRA (arcsec)	-5.37 -7.5 -1.37 -2.16	- 0.08 0.62 + 0.08	- 6.99 - 2.68 - 11.67 8.41 - 0.54 - 1.94 - 2.92	6.64 0.07 - 4.69 - 1.75	4.22 - 5.77 7.04	23.34 - 3.39 -1.74	$ \begin{array}{r} -2.55 \\ -2.4 \\ 0.98 \\ -10.21 \\ -1.89 \end{array} $	$ \begin{array}{r} -2.9 \\ 1.16 \\ -22.8 \\ -3.13 \\ -0.15 \end{array} $	1.49 - 0.74 - 0.91 - 6.15
Dec. (° "')	-33.1864 -33.6406 0.0193 28.2053 -29.8441	0.0255 25.8647 - 35.492 - 35.6414 26.6552	-1.2937 -34.5263 -33.106 0.3248 0.8194 -33.103 -32.8422	-32.5845 -35.6925 -1.2995 -31.5847	-31.643 -0.6929 28.3206 1.0368	-33.5512 30.5095 32.6436 -27.6401 26.9617	1.1368 -35.2014 -35.9395 -1.7822 -27.749	-34.5503 -32.5519 -33.2049 0.5573 29.894	- 1.2383 28.3389 30.5938 26.0509 0.3829
RA (h m s)	358.3528 6.3899 128.4374 199.0479 14.2473	140.3987 204.5371 356.9606 2.4605 205.9272	174.5151 340.1158 2.6255 139.5397 174.639 18.1935 352.6006	343.351 4.6613 129.8843 4.509	26.3335 129.5726 202.2519 214.6375	339.9268 202.7852 198.0479 20.5394 203.9095	183.4504 2.0283 350.5003 174.6412 20.593	339.0635 9.3208 352.6554 185.494 196.1341	222.8969 200.369 196.0607 195.2242 216.777
H-ATLAS ID	J235324.7–331111 J00253.6–333826 J083344.9+000109 J131611.5+281219 J005659.4–295039	J092135.6+000131 J133808.9+255153 J234750.5-352931 J000950.5-353829 J134342.5+263919	J113803.6-011737 J224027.8-343135 J001030.1-330622 J091809.5+001929 J113833.3+004909 J011246.5-330611 J233024.1-325032	J225324.2—323504 J001838.7—354133 J083932.2—011758 J001802.2—313505	J014520.0–313835 J083817.4–004134 J132900.4+281914 J141832.9+010212	J223942.4–333304 J133108.4+303034 J131211.5+323837 J012209.5–273824 J133538.3+265742	J121348.0+010812 J000806.8-351205 J232200.1-355622 J113833.8-014655 J012222.3-274456	J223615.2—343301 J003717.0—323307 J233037.3—331218 J122158.5+003326 J130432.2+295338	J145135.2—011418 J132128.6+282020 J130414.6+303538 J130053.8+260303 J142706.4+002258
No.	88 88 89 90	91 92 93 94	96 97 98 99 100 101	103 104 105	107 108 109 110	111 112 113 114	116 117 118 119 120	121 122 123 124 125	126 127 128 129 130

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A1	
Table	

Lum. $\log (L_{\bigodot})$	13.44	13.46	13.51	13.64	13.50	13.62	13.48	13.30	13.52	13.37	13.30	13.44	13.46	13.39	13.54	13.34	13.40	13.31	13.32	13.71	13.53	13.49	13.37	13.53	13.63	13.34	13.53	13.50	13.43	13.70	13.55	13.52	13.34	13.46	13.41	13.54	13.53	13.65	13.43	13.07	13.60	13.39	13.46	!
Zphot,Ivi	2.66	2.71	5.66	3.16	2.65	3.10	2.72	2.24	2.77	2.53	2.24	2.96	2.78	2.55	3.35	2.25	2.42	2.24	2.40	3.54	3.08	4.05	2.51	3.04	3.22	2.34	2.83	3.11	2.53	3.53	3.24	2.81	2.43	2.64	2.73	4.91	3.34	3.19	2.53	5.33	2.88	27.7	2.83	1
Zphot,temp	2.88	2.94	3.16	3.86	3.14	3.78	2.97	2.09	3.38	2.53	2.03	3.22	3.03	2.48	3.87	2.09	2.55	2.08	2.31	4.57	3.49	3.91	2.18	3.35	3.95	2.40	3.25	3.52	2.77	4.50	3.82	3.34	2.50	2.98	3.01	4.52	3.77	4.02	2.71	4.24	3.66	2.90	3.14 2.33	ì
2spec	I	I	I	ı	I	I	ı	I	ı	I	I	ı	ı	ı	I	I	ı	ı	I	I	I	1	ı	I	I	I	ı	I	I	I	I	I	I	I	I	I	I	I	I	I	I	I	l l	
S_{850} (mJy)	30.3 ± 10.5^{b}	31.0 ± 10.2	ı	61.9 ± 10.6	I	50.7 ± 12.2	38.3 ± 8.9	Н		30.3 ± 8.5^{b}	28.4 + 10.5	H				32.1 ± 11.1^b	42.5 ± 9.1	$29.0 + 9.6^{b}$			23.9 ± 10.2^{b}	23.3 ± 9.0	44.5 ± 10.3	52.1 ± 8.4	+	35.0 ± 10.4	49.3 ± 8.2	І Н	+	57.6 ± 10.1	+	\mathbb{H}	+	+ -	26.7 ± 9.7	+	+	+	42.3 ± 7.9	/0.4 ⊞ 9.7		Н -	31.7 ± 9.0 196 + 93	1
S ₅₀₀ (mJy)		90.6 ± 7.8	88.1 ± 7.3	87.9 ± 7.3	87.8 ± 7.5	87.7 ± 8.6	87.7 ± 8.6	87.4 ± 7.8	87.4 ± 6.8	+	87.3 + 7.5	+	+	+		8.9 ± 9.98		+	1 +	+	85.8 ± 6.9	85.8 ± 6.9	+	85.6 ± 7.2	85.6 ± 7.2	85.4 ± 6.9	+	85.1 ± 7.2	85.0 ± 7.1	84.8 ± 7.1	82.4 ± 8.8	\mathbb{H}	84.5 ± 7.6	+ -	84.3 ± 8.7	$^{\rm H}$	84.3 ± 7.2	84.0 ± 7.5	84.0 ± 8.7	02.0 H 7.0	83.4 ± 8.6	83.3 ± 8.9	83.3 ± 7.2 83.2 + 7.4	:
S ₃₅₀ (mJy)	+	\mathbb{H}	\mathbb{H}	+	96.7 ± 6.2	97.5 ± 8.2	103.6 ± 8.0	111.2 ± 6.4	82.9 ± 5.9	98.5 ± 8.2	124.4 + 6.5	+	+	116.5 ± 8.2	+	134.6 ± 5.4		121.2 ± 5.5	103.3 ± 6.0	+	92.9 ± 5.8	53.4 ± 6.0	Н	87.9 ± 5.9	+	91.3 ± 6.1	+	Н	+	84.2 ± 6.0	75.7 ± 8.1	92.5 ± 7.3	\mathbb{H}	H -	80.2 ± 8.0	50.1 ± 8.5	\mathbb{H}	88.1 ± 6.1	105.2 ± 8.2	0.0 H 0.0/	97.4 ± 8.1	85.1 ± 8.1	92.7 ± 6.0 84 8 + 5 9	
$S_{250} $ (mJy)		86.7 ± 5.8	85.4 ± 5.5	\mathbb{H}	85.4 ± 5.5	68.3 ± 7.5	86.0 ± 7.2	120.4 ± 5.8	+	Н	122.1 + 6.1	+	77.7 ± 6.5	+	+	122.4 ± 5.2	+			+	64.2 ± 5.8	47.7 ± 5.6		79.1 ± 5.6	59.9 ± 5.8	103.7 ± 5.7	+	64.7 ± 5.4	+		+	+	+	+ -	73.4 ± 7.4	32.4 ± 7.2	\mathbb{H}	+	95.2 ± 7.5	Н	71.3 ± 7.3		73.3 ± 5.6	:
ΔDec. (arcsec)	-0.01	3.08	I	-1.0	ı	0.97	-0.96	1.03	1	4.96	-19.03	5.05	-0.96	0.9	8.95	-2.99	4.04	-0.97	1.0	-6.19	-1.0	86.6	0.04	0.0	-2.97	3.97	-1.03	-2.03	5.99	-5.01	-1.12	0.9	-5.96	0.7	9.98	5.97	16.01	3.04	4.97	- 1.0	(-3.0	- 4.99 8 96	;
ΔRA (arcsec)	-5.52	-2.59	ı	2.85	Ι	-5.61	-8.27	-5.53	1	-5.15	-11.19	-2.55	-1.26	3.76	-3.3	-7.27	-2.33	-5.29	- 3.83	- 2.84	6.26	-2.85	1.22	-0.68	3.1	0.35	- 4.84	-0.17	-0.12	-0.06	1.1	-1.81	2.99	- 4.33	- 14.64	-1.5	4.51	1.13	3.33	0.01	1 1	5.1	- 5.11 - 15.94	
Dec. (° "' ')	- 32.9305	-29.8407	24.0626	35.5281	-32.948	-0.9578	0.0689	-32.122	24.1292	0.08	-31.0264	-1.0663	-0.6298	-32.1866	-31.7718	-33.6304	0.0429	-31.8652	31.6654	-0.9465	-30.4192	31.2928	1.9179	32.8473	-32.1934	-29.8716	1.1204	31.2579	-33.4839	-31.8038	-0.5465	-0.5095	-34.3373	-1.6179	-1.0118	-30.8133	31.6315	-30.7887	2.2239	- 55.1500	2.1728	0.5594	32.83/9 - 28 6903	
RA (h m s)	343.413	348.0216	206.1728	203.6684	344.0486	133.2857	223.4052	19.3764	207.2317	215.4183	341,9986	138.7253	214.542	336.6226	20.8963	350.5454	218.5149	340.1106	204.6149	186.2466	21.3772	202.7394	220.6809	200.7423	0.8778	5.4368	132.4905	200.8745	357.8416	17.5604	186.031	220.893	1.941	183.5682	136.5576	336.2657	195.9229	342.6896	129.7472	1.6207	129.9378	222.6688	93.696	
H-ATLAS ID	J225339.1-325550	J231205.2 - 295027	J134441.5+240345	J133440.4 + 353141	J225611.7—325653	J085308.5-005728	J145337.2 + 000407	J011730.3-320719	J134855.6+240745	J142140.3 + 000447	1224759.7—310135	J091454.0-010358	J141810.0 - 003747	J222629.4 - 321112	J012335.1 - 314619	J232210.9—333749	J143403.5+000234	J224026.5-315155	J133827.6+313956	J122459.1 - 005647	J012530.5-302509	J133057.5+311734	J144243.4+015504	J132258.2 + 325050	J000330.7-321136	J002144.8-295218	3084957.7 + 010713	J132329.9+311528	J235122.0—332902	J011014.5-314814	J122407.4-003247	1144334.3 - 003034	J000745.8-342014	J121416.3—013704	1090613.8-010042	J222503.8 - 304848	J130341.5+313754	J225045.5—304719	J083859.3+021325	1000433.4—330012	J083945.0+021021	1145040.5+003333	1131804./+325016	
o	131	132	133	134	135	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	1/0	171	172	173	

Table A1 - continued

No.	H-ATLAS ID	RA (h m s)	(° "')	ΔKA (arcsec)	ΔDec. (arcsec)	.3250 (mJy)	, 2350 (mJy)	0500 (mJy)	2850 (mJy)	2spec	Zphot,temp	Zphot,Ivi	$\log{(\mathrm{L}_{\odot})}$
175	J121900.8+003326	184.7537	0.5575	- 0.63	- 0.93	56.7 ± 7.4	81.5 ± 8.0	81.9 ± 8.8	54.8 ± 10.5	ı	4.24	3.36	13.65
9/1	J131222.2+270219	198.0926	27.0386	I	ı		90.1 ± 5.8	+		I	3.30	2.72	13.51
177	J115433.6 + 005042	178.6402	0.8451	1.79	2.0	+	+	+	+	I	4.71	3.89	13.76
178	J011850.1 - 283642	19.7087	-28.6118	-3.51	1.06	$^{\rm H}$	113.2 ± 6.1	$^{\rm H}$	34.9 ± 8.6	ı	2.61	2.58	13.41
179	J115521.0 - 021329	178.8376	-2.2249	-1.16	1.33	62.9 ± 7.3		82.2 ± 8.5		I	4.07	3.19	13.63
180	J131539.2+292219	198.9134	29.372	-2.16	5.97	\mathbb{H}	+	+	+	I	2.65	2.58	13.39
181	J005850.0 - 290122	14.7082	-29.0229	-0.61	-4.02	+	+	+	32.9 ± 8.8^{b}	I	2.61	2.81	13.41
182	J230538.5-312204	346.4106	-31.3678	I	I	89.0 ± 5.7	+	82.3 ± 7.9		I	2.93	2.59	13.48
183	J090453.2+022017	136.222	2.3383	-1.34	-3.03	+	+	+	44.5 ± 8.8	I	2.94	2.64	13.46
184	J234955.7—330833	357.4821	-33.1425	ı	I	91.9 ± 5.9	107.6 ± 6.0	+	I	I	2.73	2.54	13.43
185	1092408.8 - 005017	141.0368	-0.8382	-2.64	1.03	+	+	82.2 ± 8.5	61.6 ± 9.4	I	3.68	3.08	13.58
981	J013217.0-320953	23.0708	-32.1647	-8.36	3.0	+	+		51.3 ± 10.4	I	4.03	3.25	13.60
187	1083705.2 + 020033	129.2719	2.0092	2.4	0.02	108.0 ± 7.2	97.0 ± 8.1	82.0 ± 8.6	31.3 ± 7.4	I	2.19	2.24	13.29
188	1084259.9 + 024959	130.7498	2.8331	I	ı	+	+	+	I	ı	3.02	2.63	13.48
189	J225600.7 - 313232	344.0029	-31.5421	-1.36	0.99	+	+		74.2 ± 10.2	I	2.50	2.58	13.45
190	1090405.3 - 003332	136.0222	-0.5591	-0.5	0.99				42.3 ± 8.2	I	3.00	2.69	13.45
191	J124753.3+322448	191.9722	32.4134	-3.12	0.97	+	+	+	37.8 ± 9.2	I	3.74	3.19	13.54
192	J222628.8 - 304421	336.6202	-30.739	I	I	101.3 ± 7.7			I	I	2.34	2.33	13.32
193	1085352.0 - 000804	133.4669	-0.1346	-3.58	-0.99		+	+	52.9 ± 9.5	ı	2.77	2.53	13.43
194	1085521.1 - 003603	133.8382	-0.6011	4.66	-0.99	95.6 ± 7.5	98.8 ± 8.1	+	45.8 ± 8.1	ı	2.71	2.53	13.41
195	J145754.2+000018	224.476	0.0051	3.61	4.02	\mathbb{H}	\mathbb{H}	81.0 ± 8.8	29.5 ± 10.0^{b}	I	3.14	2.85	13.45
961	J134403.1 + 242628	206.0131	24.4411	I	I	+	+	+	I	ı	2.79	2.53	13.41
197	J122034.2 - 003805	185.1429	-0.635	11.49	13.92	81.9 ± 7.5	93.8 ± 8.2	84.8 ± 8.7	37.7 ± 11.6	ı	2.96	2.65	13.44
198	J222235.8 - 324528	335.6493	-32.7577	I	I	\mathbb{H}	\mathbb{H}	+	I	I	3.39	2.73	13.50
199	J133352.2+334913	203.4674	33.8203	19.0	-18.05	112.4 ± 5.4	\mathbb{H}	80.6 ± 7.0	18.4 ± 9.7	I	2.01	2.22	13.25
200	J014313.2—332633	25.8052	-33.4425	- 9.04	20.05	\mathbb{H}	+	+	21.5 ± 11.0	I	2.19	2.33	13.30
201	J141117.8-010655	212.8246	-1.1155	1.97	3.02	+	78.6 ± 8.2		39.4 ± 9.4	ı	4.00	3.31	13.58
202	J143328.4 + 020811	218.3684	2.1365	-5.9	4.03	117.5 ± 7.3	$^{+}$	80.4 ± 8.5	35.7 ± 8.4	I	2.02	2.05	13.26
203	J141827.4—001703	214.6145	-0.2843	5.53	-19.01		116.4 ± 7.4	\mathbb{H}	22.0 ± 10.6	I	2.01	2.13	13.27
204	J132909.5+300957	202.2896	30.1658	I	I	57.9 ± 5.5	\mathbb{H}	$^{\rm H}$	I	I	4.18	3.01	13.67
205	J145132.7+024101	222.8866	2.6837	-6.1	1.98	+	+	80.2 ± 8.9	45.5 ± 10.5	I	3.01	2.67	13.48
506	J140421.7—001217	211.0907	-0.2048	0.43	1.96				32.2 ± 10.1	I	2.94	2.72	13.44
207	J005506.5-300027	13.777	-30.0076	-6.0	-0.01	96.9 ± 5.9	121.7 ± 6.1	$^{\rm H}$	41.8 ± 9.7	I	2.60	2.77	13.42
208	J225744.6 - 324231	344.4358	-32.7086	I	I	69.4 ± 5.1	$^{\rm H}$		I	I	3.60	2.85	13.56
500	J224920.6 - 332940	342.3358	-33.4944	I	I			80.1 ± 7.5	I	I	2.90	2.59	13.45

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Table A2. Blazars - SPIRE and SCUBA-2 data. The blazar index hyperlinks to the NED data base at the position of the source. These sources have been removed from the HerBS sample in Section 2. The RA and Dec. are the SPIRE positions, ΔRA and $\Delta Dec.$ are the SPIRE positions minus the SCUBA-2 positions. The spectroscopic redshifts are discussed in Section 4. The α value defines the steepness of the slope of the synchrotron radiation, and is calculated in Section 2.

No.	H-ATLAS ID	RA (h m s)	Dec. (°"')	ΔRA (arcsec)	ΔDec. (arcsec)	S ₂₅₀ (mJy)	S ₃₅₀ (mJy)	S ₅₀₀ (mJy)	S ₈₅₀ (mJy)	Zspec	α
_	J131028.7+322044	197.6197	32.3455	- 2.06	2.05	259.1 ± 4.4	363.1 ± 5.1	452.2 ± 6.1	820.0 ± 6.0	1.0	0.93 ± 0.01
2	J114637.9 - 001132	137.2924	1.3597	-0.52	-0.03	256.5 ± 3.8	327.0 ± 4.5	375.3 ± 6.0	390.7 ± 7.7	1.02	0.32 ± 0.01
3	1014503.4 - 273333	26.264	-27.5591	-0.67	0.98	131.5 ± 5.7	179.1 ± 6.3	233.5 ± 7.2	365.8 ± 6.7	1.16	0.83 ± 0.02
4	3083051.0 + 013225	194.4888	32.4918	-2.12	3.03	143.7 ± 5.1	188.4 ± 5.7	214.9 ± 6.7	290.0 ± 7.6	0.81	0.54 ± 0.02
2	J224838.6 - 323551	342.1608	-32.5974	-1.18	2.99	119.2 ± 5.5	152.8 ± 5.8	194.8 ± 6.7	173.5 ± 7.2	2.27	0.24 ± 0.03
9	J121758.7—002946	184.4947	-0.4961	-2.62	1.01	115.7 ± 5.3	151.5 ± 5.7	179.2 ± 6.6	206.7 ± 7.2	0.42	0.44 ± 0.03
7	3014310.0 - 320056	25.7917	-32.0157	-2.38	4.0	96.0 ± 5.3	119.5 ± 5.9	122.4 ± 7.2	405.6 ± 8.5	0.38	1.02 ± 0.04
8	1084933.4 + 021442	203.2808	27.4217	-5.76	1.01	89.3 ± 5.3	104.6 ± 5.5	117.1 ± 6.4	128.5 ± 10.4	2.13	0.3 ± 0.05
6	J131736.4 + 342518	199.4017	34.4217	0.21	90.9	77.1 ± 5.1	99.5 ± 5.5	112.0 ± 6.8	129.0 ± 7.8	1.06	0.39 ± 0.05
10	J113526.2 - 014606	358.4476	-30.6294	-2.06	3.99	77.1 ± 5.1	96.6 ± 5.8	103.1 ± 7.0	143.9 ± 8.1	1.06	0.48 ± 0.05
11	J132952.9+315410	202.4703	31.9027	-2.92	-1.0	50.5 ± 5.2	71.0 ± 5.5	86.4 ± 7.3	253.4 ± 7.8	0.34	1.27 ± 0.06
12	1235935.3 - 313343	359.8972	-31.5621	-4.16	5.04	61.4 ± 5.5	67.7 ± 5.8	83.7 ± 7.4	117.3 ± 8.6	0.99	0.54 ± 0.06
13	1142413.9 + 022303	177.6818	-0.3985	-1.4	5.98	34.5 ± 5.3	56.1 ± 5.5	83.2 ± 6.7	187.9 ± 9.3	1.98	1.37 ± 0.07
14	J131059.2 + 323331	197.7467	32.5587	7.4	2.03	37.6 ± 5.3	63.2 ± 5.7	81.7 ± 6.5	313.7 ± 7.8	1.64	1.67 ± 0.07

APPENDIX B: CUTOUTS OF THE ENTIRE HERBS SAMPLE

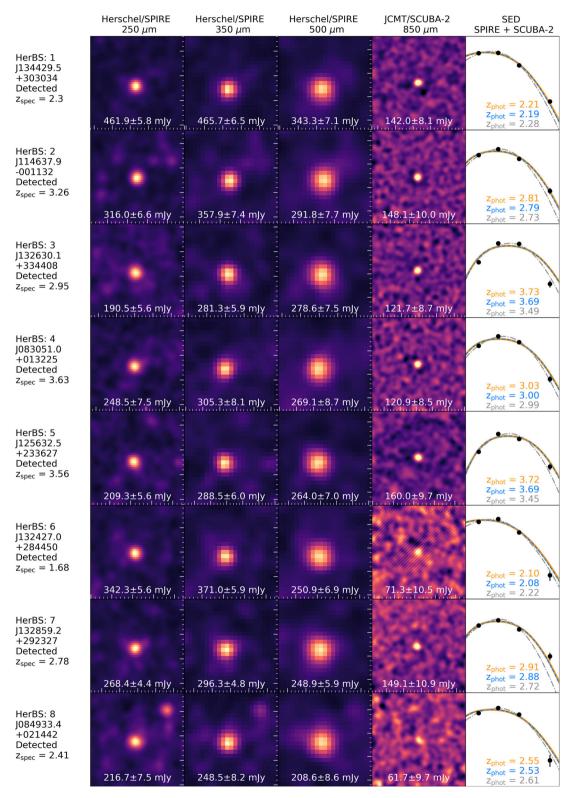


Figure B1. The cutouts of the first 8 HerBS sources. The cutouts of all HerBS sources can be found in the online version of this paper. The first three columns of cutouts of each source are the *Herschel* observations shown in 4×4 arcmin² postage stamps. The fourth column shows the 850 μm SCUBA-2 observation, where available, in a 4×4 arcmin² postage stamp. All postage stamps are centred at the 250 μm extraction position of the *Herschel* catalogue. The final frame is a fitted SED, with the best-fitting template in orange, fixed β template in blue and Pearson's template in grey (Pearson et al. 2013).

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