A Housekeeping Prognostic Health Management Framework for Microfluidic Systems

H. Khan, Q. Al-Gayem and A.M. Richardson, Member IEEE

Abstract—Micro-electro-mechanical Systems and microfluidics are becoming popular solutions for sensing, diagnostics and control applications. Reliability and validation of function is of increasing importance in the majority of these applications. Online testing strategies for these devices have the potential to provide real-time condition monitoring information. It is shown that this information can be used to diagnose and prognose the health of the device. This information can also be used to provide an early failure warning system by predicting the remaining useful life. Diagnostic and prognostic outcomes can also be leveraged to improve the reliability, dependability and availability of these devices. This work has delivered a methodology for a “lightweight” prognostics solution for a microfluidic device based on real-time diagnostics. An oscillation based test methodology is used to extract diagnostic information that is processed using a Linear Discriminant Analysis based classifier. This enables the identification of current health based on pre-defined health levels. As the deteriorating device is periodically classified, the rate at which the device degrades is used to predict the devices remaining useful life.

Index Terms: Microfluidics, Prognostics and health Management, Microelectrodes, Design-for-testability, Machine learning algorithms.

I. INTRODUCTION

A novel implementation of a prognostics function for a microfluidic device based on MEMS technology is presented. The term “prognostics” has been defined in various different ways depending on context [1], this research considers the definition given by ISO13381-1 as the most comprehensive. It states that prognostics is not only the prediction of the time to failure but also the risk of one or more existing or future failure modes [2].

Studies have revealed some excellent Prognostic and Health Management (PHM) solutions that provide deep and detailed prognostic capabilities for micro-devices with a high level of accuracy. The use of machine learning [3] and physics based prognostics [4] is being actively explored. PHM solutions similar to these are designed from the ground up in a device specific framework with the prognostics modules being tightly coupled with the physics of failure of the device. While these PHM systems perform very well in conjunction with their target devices, flexibility and wide scale adoption in other MEMS devices is quite challenging.

The onus of most PHM frameworks is to provide prognosis at the highest possible confidence level thus providing the most reliable Remaining Useful Life (RUL) predictions [5] [6] [7]. However, this comes at a cost, be it a heavy processing requirement or the aforementioned rigidity or complexity, to name two. This work proposes a “Housekeeping” Prognostics and Health Management (HPHM) framework that has a conservative prognostic mandate. Such a framework caters strictly for wear during normal use and evolving faults. This affords the usage of simpler models that are easy to adapt, implement and use.

The scope of this HPHM is to predict patterns of low intensity failures and drift due to gradual aging and non-catastrophic faults during normal operation. The advantages this capability offers is simplicity and speed of adaption with none of the overheads associated with more traditional prognostic methodologies. Furthermore, ease of implementation and cross-device compatibility makes pure hardware realization credible.

II. OVERVIEW

The design and performance of a HPHM solution for a microfluidics based MEMS sensor chip with embedded micro-electrodes is presented in this paper. Such devices are increasingly being engineered for new areas of application. Research is being carried out into embedding microelectrodes directly into human bodies [8] [9] [10] and even into the human brain [11] [12] [13] [14]. Microelectrode based devices are quickly evolving from being temporary and disposable to being devices designed for long term use [15]. The development of a prognostics framework for such devices is relevant given these trends.

For the purpose of this research, experiments have been conducted using a device that is able to mix a reagent and analyze and detect conductivity of the product using embedded electrodes that line the channel.

The proposed prognostics model presented in this work is not a system level solution. It is classified at component level as its focus is limited to the health of the sensing electrodes. The electrodes have been shown to be the most critical components of the microfluidics chip. They have also been shown to be the most vulnerable to failure due to usage and environmental
factors. Repeated experiments using similar chips (microfluidic chips with electrodes used for sensing) showed electrode failure to be the largest root cause of system failure in these types of devices followed by blockage and leakage. This is consistent with various other studies available in literature [16] [17] [18] [19].

A diagnostic-prognostics pairing has been proposed for the HPHM:
- Diagnosis: A modified Oscillation Based Testing (OBT) technique has been used to provide real time diagnostics. This forms the input to the prognostics module.
- Pre-prognosis: A machine learning algorithm based on a Linear Discriminant Analysis (LDA) classifier has been used to identify the level of health the sensor is trending towards.
- Prognosis: Periodic health classification is used to process the normal wear and aging trend of the chip. This is used to calculate the RUL.

III. BACKGROUND

Microfluidic devices have distinctive properties when compared to other types of MEMS in the context of reliability, the main difference being the operational load and environmental conditions they are exposed to. There are therefore unique challenges associated with a HPHM framework for these devices.

Applications are wide ranging and include “Lab-on-Chip” devices were there is an increasing interest in MEMS integration due to the improved sensitivity and faster response which have been well documented [20] [21]. Of special interest are technologies capable of integrating microfluidics with electronic sensing, actuation, control and processing. A number of technologies that exist show the capabilities and potential of these integrated chips [22]. With their rapid commercialization, the need for fault tolerant design with integrated health monitoring and health prediction capabilities are gaining traction. The examples quoted here have sensing components and failure modes similar to the MEMS chips used in this study.

This research specifically targets the development of microfluidic MEMS devices with embedded electrodes because there are a number of interesting applications, in addition to those cited above that require the interfacing of microfluidic structures to electronic circuitry [23]. This provides the opportunity for electronic sensing, actuation and processing. The integration with electronics provides a platform for a prognostics processing unit which would not otherwise be possible.

A. Reliability and Failures

The reliability of Bio-MEMS devices is yet to be established as is microfluidics in general that is currently limited in industrial uptake. A number of public bodies are, however, committed to accelerating uptake of these technologies [24].

Failures in Microfluidic devices have been identified to be unique [25] due to direct contact of their components with fluids, i.e. liquid bio-chemical assays. In addition to degradation due to direct contact, failure mechanisms including blockages and fouling are significant and sensitive to the density and/or viscosity of the liquids. The chip used in this research demonstrated two levels of failure:
- Blockage of and sedimentation on the electrode surface.
- Deterioration and aging due to normal use.

IV. FAULT MODEL

Electrode degradation causes significant loss in monitoring ability, especially in MEMS device based sensing of cellular level specimens. The development of embedded test methods based on OBT [26] [27] forms an important contribution to the prognostic methodology proposed. The experiments conducted in this research validated the premise that the electrodes are the key target for a first-generation prognostics solution for electrode based microfluidics.

A. Embedded Electrodes – Failure Mechanisms and Failure Modes

Electrode failure involves either:
- Catastrophic Failure (leading to complete loss of operational functionality).
- Gradual Degradation causing a deviation in normal parameter drift associated with operational wear and tear.

Three main fault mechanisms have been observed in the electrodes of the MEMS chips that were used in this work. They are:
- Degradation due to surface material loss. This is due to ion loss in the mixture that surrounds the electrodes.
- Settling and sometimes scaling of bio-chemical matter on the electrode surface that is not always removed by cleaning.
- Minor damage due to the cleaning process. Ideally, the electrode structures should be cleaned immediately after every test cycle because residual bio-chemical specimens may be impossible to remove after a delay due to electrolyte evaporation.

The failure modes associated with the electrodes after degradation:
- Marked increase in the impedance / decrease in admittance of the electrode.
- A fluctuation in the bio-fluidic interface capacitance of the electrode.
- A reduction in the Signal to Noise Ratio (SNR) in the signal extracted from the electrodes.

The OBT is leveraged in this work to non-intrusively extract the admittance and capacitance of the electrode over a specified bandwidth, at a given concentration of the specimen being tested and a specific flow rate of the reagents. These health sensitive features form the input to the classifier that, in turn, is able to compute the health level of the electrodes under test.
V. Oscillation Based Test (OBT) Diagnostics

The proposed HPDM framework consists of two subcomponents as described in section 2, i.e. the OBT self-test based diagnostics and the LDA based prognostics. The output of the diagnostic forms the input to the prognostics module. This section will discuss the diagnostics in some detail.

In OBT, the system being tested is designed to operate at specific oscillation frequencies. This oscillation frequency is a function of the material properties and physical structure of the system. Faults can be identified because they cause a deviation in the oscillation frequency from its nominal value. One of the earlier adaptions of this method to test analogue integrated circuits was presented by B Kaminska et al. [28]. The validity of this technique has been verified as a test method for operational amplifiers and analogue to digital converters.

The authors of this paper previously demonstrated a scheme for effective degradation monitoring of electrodes within microfluidics systems using OBT [26] [27]. The solution was based on fault modelling and impedance analysis of the interface between the electrode and the electrolyte. The method has also been evaluated within a MEMS based system through work on a monolithic magnetometer [29]. The potential for using OBT in a DNA sensor array has also been researched [30] where both the sensing and test modes can be realised in an oscillation based structure. Some DNA sensors that employ micro-electrodes are similar to the chip used in these experiments. The potential of OBT in such DNA sensors has been explored [31]. It has been observed that normal sensing operation results in the hybridized DNA strands deposited on the electrodes causing the displacement of ions from the surface which results in a considerable change in the interface capacitance of the electrical double layer. OBT converts this varying capacitance to a frequency as a means of testing the integrity and state of operational health of the electrode.

A. Experimental Setup

The experiments to extract health data from physical devices were based on microfluidic mixing chips using electrode based sensing. A picture and a schematic of one such chip is shown in Fig 5.1. Two liquid specimens are pumped into the chip which are mixed in the mixing chamber. The resultant electrolyte is analysed via electrolysis when the solution is exposed to a pair of electrodes lined within the outgoing microchannel.

The experiments utilised a microfluidic platform which can be used to demonstrate a number of sensing, mixing and separating experiments, a schematic of which is shown in Fig 5.2 and pictures of which are shown in Fig 5.3 and Fig 5.4. The setup consists of a base board that can host the chip via connectors and fluidic interfaces. Standard lithographic and machining processes have been used to etch the micro channels in both the chip and the base-board that are constructed of Poly-methyl methacrylate (PMMA), acrylic glass and SU-8 photoresist.

The platform consists of a pair of microfluidic precision pumps, an impedance analyser, base-board mounted microscope as well as the control software. The pumps can control the bi-directional flow rate of the liquids accurately and quantifiably down to the µ-meter per minute flow rate.

The mixing chip shown in Fig 5.1 is made of SU-8. It has two inlets A and B, a mixing chamber and an outlet C. The chip is connected to the base board with the inlets and outlet connected to pipes at special joints with fluidic seals. It features two functional sections, the “Delay Channel” (DC) and the “Sensing Chamber” (SC). The DC is used to allow two input chemicals enough time and mutual exposure for the desired reaction to complete between them. The contours in the DC are used to introduce turbulence in the fluid flow. The serpentine channel ensures even mixing of the two species [32] [33]. Prior to
injection into the sensing chamber. The Channel is 150 μm wide and 75 μm deep. The total length of the DC is 9 cm. A channel length above 1 cm in a mixing chamber with the dimensions used here to induce turbulence is considered to be sufficient to ensure a mixing index of above 0.95 [34], even for low Reynolds number (≥1). During experiments, mixing efficiency was observed to be above 90% at 1 μL/min flow rates which dropped to below 50% at 6 μL/min. The total volume of the DC is approximately 1.0124 μL.

The sensing chamber has been fabricated with two Nickel electrodes with two arms each, one on top of the other. The electrode arms are 0.25 mm thick and 2.15 mm long. They overlap each other with a distance approximating the height of the chamber. The SC is as deep as the DC but is 2.35 mm wide and 5 mm long.

A software controller written in LABVIEW is used to control the flow of the reagents. The precision pumps connected to the PC serially via RS232 interface are controlled using this software controller. The software controller can control the pumps individually. Based on the flow orientation required and diameter of the reagent filled syringes that are used to feed the pumps, different flow rates can be maintained on each individual pump.

The experiment involves pumping in 0.1 M NaOH at an infusion rate of 1 μL/min throughout the test at room temperature. The second pump introduces 0.1 M HCl at initially 0.1 μL/min, gradually increasing at discrete intervals until matching the flow rate of NaOH. This is done to ensure that the HCl solution does not contaminate the sensing chamber. These flow rates were chosen to ensure optimal mixing of the reagents in the DC. This was validated by introducing solutions into the chip with coloured agents and observing their diffusion visually under the microscope.

Experiments were designed to conclude after a maximum of 5 hours. Healthy chips are exposed to multiple cycles, with a cleaning session preceding each test cycle. It has been observed that the electrical characteristics of the Nickel electrodes start deviating from expected behaviour after the 3 hour mark of the first cycle, indicating a deterioration of the electrode surface.

The objective of the experiment is to test the conductivity of the resulting fluid at different flow rates and sensing its composition based on its electrical properties. The measurements are observed directly from a Wayne Kerr Precision Impedance Analyser 6500 that is connected to the electrodes. As mentioned before, the flow rates are controlled using the LABVIEW controller, though they can also be manipulated directly on the pumps, albeit, with a lesser degree of sensitivity.

B. Results & Observations

The primary objective of the experiments was to generate data to train and test the prognostics module. For this purpose, the experiments were designed keeping the needs of the prognostics module in mind. This is reflected in the discussion about the experimental stages as follows:

1) Experimental Stages

The prognostics solution uses machine learning engines. A machine learning classifier needs to be trained using experimental data and needs to be experimentally tested after it is trained. Consequently, the experiments were divided into two similar but distinct phases, namely:

- **Training Data Collection:** Diagnostic data was generated by OBT. This was a set of parameters representing the known health of electrodes at various stages of degradation and aging. This data was then used to train a number of supervised machine learning classifiers. Based on this training, the prognostics system is able to compute the health of the electrodes and over a period of time (typically 5-10 cycles of observation) to predict the RUL of the system based on its current and historical health status. The frequency of these observations depends on the volatility of the system under observation. The prognostics module presented in this research has been discussed in detail in section 6.2. The training depends on but is not limited to:
  - The design of the fault model and identification of the most significant parameters.
  - The quality and reliability of data.
  - The volume of the data.

- **Testing:** Here, healthy chips were again used to take measurements on the solution while known patterns of operational wear and aging were simultaneously applied to the electrodes. In this round of experiments, the wear predictions of the “trained” system were observed and compared with the “actual” wear of the electrodes.

The experiment utilised a 50 mV electrode stimulus at the 1 KHz and 50 MHz frequency ranges. Hundreds of readings were observed and recorded for the mixing for a range of flow rates that were increased in discrete steps. The flow rate is important as the speed of the fluid flow has a bearing on the quality and consistency of product. The rate of flow should be sufficiently slow for proper mixing to take place before the mixture passes the electrode. This is due to the low Reynolds numbers involved and the dominance of diffusion in the mixing process given laminar flow.

After recording sufficient readings over different flow rates and consequently different chemical constistutions, the electrodes were artificially degraded using 5V pulses and the experiments repeated. The deterioration achieved tracked the normal degradation process albeit at a highly accelerated rate. The impedance analyser was connected to both electrodes for impedance measurements. The measurements were taken periodically within the stress program. The period of the stress pulse was 20 s with a stress program duration of 140 s.
This experiment was repeated over a batch of chips. Data in excess of 32 thousand samples was gathered. That volume of data was calculated to be reasonably sufficient for the effective training of the offline system.

2) Data Analysis

OBT was used to extract the following three electrical parameters (1 input and 2 output parameters)

- Frequency (Hz) – (input)
- Admittance (S) – (output)
- Capacitance (F) – (output)

The mechanical deterioration of the electrodes manifested in changes in these electrical properties. This is evident from two sets of observations seen in Fig. 5.5 and two overlapped observations seen in Fig. 5.6. These are actual screenshots captured from the Wayne Kerr Precision Impedance Analyser 6500.

A closer look at the shorter ranges for admittance and capacitance can be seen in Fig. 5.7 and Fig. 5.8 respectively. Each of these figures shows observations at 4 different levels of health. These 4 levels of health formed the basis of the 4-class health classifier that the prognostics module uses to identify levels of health and their rates of deterioration.

Fig. 5.5: [Impedance Analyser screen-grab] (a) Shows an output for a healthy electrode, where the blue curve is the admittance and the yellow curve is the capacitance of the electrode. (b) Shows the same electrode after induced aging. The change in both the admittance and capacitance is evident.

This experiment was repeated over a batch of chips. Data in excess of 32 thousand samples was gathered. That volume of data was calculated to be reasonably sufficient for the effective training of the offline system.

2) Data Analysis

OBT was used to extract the following three electrical parameters (1 input and 2 output parameters)

- Frequency (Hz) – (input)
- Admittance (S) – (output)
- Capacitance (F) – (output)

The mechanical deterioration of the electrodes manifested in changes in these electrical properties. This is evident from two sets of observations seen in Fig. 5.5 and two overlapped observations seen in Fig. 5.6. These are actual screenshots captured from the Wayne Kerr Precision Impedance Analyser 6500.

A closer look at the shorter ranges for admittance and capacitance can be seen in Fig. 5.7 and Fig. 5.8 respectively. Each of these figures shows observations at 4 different levels of health. These 4 levels of health formed the basis of the 4-class health classifier that the prognostics module uses to identify levels of health and their rates of deterioration.

VI. PROGNOSTICS

The prognostics module comprises of two algorithms:

- The first algorithm is the classifier that identifies the current health of the system in quantifiable terms.
- The second algorithm uses the series of classifier outputs (i.e. the state of health) and predicts the future health of the electrodes based on their changing health. It only predicts the deterioration in health (as there is
no conceivable scenario where the health of the electrode would ever improve).

A summary of the life cycle of a generic prognostics system is given in Fig 6.1.

A. The LDA based classifier

In the previous section, we have seen that the OBT is able to convey reliable data about the capacitance and conductance across electrodes at given frequencies. This information cannot be used in isolation as the capacitance or conductance at any given frequency also depends on the constituency and the flow rate of the fluid. In this work, this quantification has been achieved using a classification technique.

Classification techniques have been extensively used in the areas of machine learning and statistics. These techniques have found wide range of usage in the field of information technology, specifically in the areas of pattern classification and image recognition [35]. Many such techniques have matured over time and are currently industry standards and are known as classifiers.

Linear Discriminant Analysis (LDA) is one well established classification technique. LDA has found application in the areas of banking, financial market predictions, face recognition and studies of epidemiological trends [36] [37] [38]. The basic idea of an LDA classification is to find a transformation for a sample of features that allows for a linear discrimination between classes. Generally speaking, any classifier is an algorithm that is able to distinguish and classify an entity based on certain features. In the context of the sensor under study, electrodes can be classified in terms of their health “class”, from within a set of predefined discrete health classes. Health determining features need to reflect the device health. As indicated in the previous section, the features in this study are frequency, capacitance and conductance.

Even though LDA are traditionally binary classifiers (i.e. they can be used to differentiate between two classes only), they have evolved to accommodate multi-class identification. Literature, especially that pertaining to pattern recognition has firmly established that the LDAs can easily be extend to a multi-class cases [39] and have been successfully used in many recognition tasks [39].

Fisher’s LDA (FLD) [40], which produces discriminative feature transforms as a set of eigenvectors, is an established standard in the domain of pattern recognition. FLD can be easily extended to multi-class cases via multiple discriminant analysis [41]. In fact, discriminant analysis has been widely used in this way in pattern recognition problems, and its use in reducing facial recognition problems is well documented [42]. This has been the motivation to use discriminant analysis for multiple distinct binary classifications.

LDA is a “supervised learning” classification technique. This implies that the system has to be trained under “supervision” to “learn” how to distinguish between classes. This process is known as training and is a critical part of LDA. The quality and comprehensiveness of training data can affect the quality of performance (class identification).

A collection of feature samples representing known values of health are used as training data. Ideally, all classes of health are represented comprehensively. For the initial tests, 4 levels of electrode health were defined. The 4 classes being:

1. Healthy - health level 1
2. Somewhat healthy - health level 2
3. Somewhat sick - health level 3
4. Sick - health level 4

Although these 4 levels of health have been chosen for this demonstrator, the system can be scaled to accommodate more degrees of health.

A batch of chips were tested at different (four) levels of electrode health. The corresponding values for frequency, capacitance and conductance for each observation were logged. A total of 32000 samples of known health were collected. Subsets of this data were used for both training and validation of the system. A subset of the actual “training data” can be seen in Table I. A summary of the “training data” set is shown in Table II. The training data consists of data collected for known health at different flow rates and fluid concentrations. The behaviour input allows the classifier to correctly identify levels of health at the flow rates and concentration levels at which the data was generated.

### Table I Training Data Sample Subset

<table>
<thead>
<tr>
<th>Frequency (Hz)</th>
<th>Conductance (S)</th>
<th>Capacitance (F)</th>
<th>Health</th>
</tr>
</thead>
<tbody>
<tr>
<td>…</td>
<td>…</td>
<td>…</td>
<td>…</td>
</tr>
<tr>
<td>109892</td>
<td>0.0071345</td>
<td>2.95E-09</td>
<td>1</td>
</tr>
<tr>
<td>122583</td>
<td>0.0072786</td>
<td>2.42E-09</td>
<td>1</td>
</tr>
<tr>
<td>136740</td>
<td>0.0074053</td>
<td>1.97E-09</td>
<td>1</td>
</tr>
<tr>
<td>152532</td>
<td>0.0075154</td>
<td>1.59E-09</td>
<td>1</td>
</tr>
<tr>
<td>12213.7</td>
<td>0.0046113</td>
<td>2.27E-09</td>
<td>2</td>
</tr>
<tr>
<td>…</td>
<td>…</td>
<td>…</td>
<td>…</td>
</tr>
<tr>
<td>122583</td>
<td>0.0050376</td>
<td>2.02E-09</td>
<td>3</td>
</tr>
<tr>
<td>152532</td>
<td>0.005246</td>
<td>1.37E-09</td>
<td>3</td>
</tr>
<tr>
<td>170147</td>
<td>0.005308</td>
<td>1.11E-09</td>
<td>3</td>
</tr>
<tr>
<td>189797</td>
<td>0.0054034</td>
<td>9.02E-10</td>
<td>3</td>
</tr>
</tbody>
</table>
Table II  Summary of the training data

<table>
<thead>
<tr>
<th>Total</th>
<th>Frequency (Hz)</th>
<th>Conductance (S)</th>
<th>Capacitance (F)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean</td>
<td>25497.9</td>
<td>0.001930322</td>
<td>1.54261E-08</td>
</tr>
<tr>
<td>Max</td>
<td>51134.8</td>
<td>0.005555673</td>
<td>3.702E-08</td>
</tr>
<tr>
<td>Min</td>
<td>9925.47</td>
<td>0.00042518</td>
<td>5.99685E-09</td>
</tr>
</tbody>
</table>

Class 1

| Mean  | 25488.38      | 0.003049       | 2.22E-08       |
| Max   | 51134.8       | 0.005555673    | 3.7E-08        |
| Min   | 9925.47       | 0.0001106      | 8.8E-09        |

Class 2

| Mean  | 25488.38      | 0.001535       | 1.33E-08       |
| Max   | 51134.8       | 0.003609023    | 2.36E-08       |
| Min   | 9925.47       | 0.0001106      | 6.66E-09       |

Class 3

| Mean  | 25488.38      | 0.001247       | 1.13E-08       |
| Max   | 51134.8       | 0.002537       | 1.66E-08       |
| Min   | 9925.47       | 0.000425       | 6.00E-09       |

A scatter plot of the training data can be seen in Fig. 6.2. Even though we can see a fine separation in the data at different levels of health, we can see in Fig. 6.3 there is an overlap between health levels. The LDA seeks to:

- Further increase the separation between the classes.
- Reduce the dimension of the feature set for ease in prognostics computations.

A number of LDA classifiers were trained using subsets of the master training data. Other subsets from within were used to validate classification performance.

The following section details the training process. An evenly distributed subset of 1000 samples was used for one training session \( (n = 1000) \). The samples were divided evenly to represent each class (i.e. 250 samples for each health level, ordered by the health, as seen in Table I).

The matrix for the samples is represented as \( X \) and the corresponding health values by the matrix \( H \) in the following expression:

\[
X = \begin{bmatrix}
  x_{1\text{freq}} & \ldots & x_{1\text{cap}} \\
  \vdots & & \vdots \\
  x_{1000\text{freq}} & \ldots & x_{1000\text{cap}} 
\end{bmatrix},
\]

\[
H = \begin{bmatrix}
1 \\
1 \\
\vdots \\
4 
\end{bmatrix}
\]

Where \( H \) is a \([1 \times 1000]\) matrix corresponding to the 1000 known samples used in one training session. The typical data in matrix \( X \) is derived from the master sample space which has been summarized in Table II.

The first step was the calculation of means of all the features w.r.t classes i.e. means of all values of \( x \) for frequency at health 1 … health 4 individually, and so on for the rest of the features.

\[
m_i = \begin{bmatrix}
  \mu_{\omega_1(\text{freq})} \\
  \mu_{\omega_1(\text{con})} \\
  \mu_{\omega_1(\text{cap})}
\end{bmatrix} \quad \text{where } i = 1, 2, 3, 4 \text{ (the classes of health)}
\]

In the above expression, \( m_i \) is the mean vector. The contents of this matrix are referenced in Table II.

1) LDA Training

At this point we are ready to train the data. As we are using FLD, we are expecting a transformation with the following outcome:

- A scatter matrix where with minimal spread within a class and maximum spread between classes.
A scatter matrix which allows linear discrimination between classes.

Information about possible dimensionality reduction i.e. identification of features that do not have significant say in classification. These features can be disregarded in the actual classification.

FLD requires us to compute two kinds of matrices, namely; the within-class (SW) and inter-class (SB) scatter matrices.

The within-class (SW) scatter matrix is computed as follows:

\[ S_W = \sum_{i=0}^{4} S_i \quad \text{where} \]
\[ S_i = \sum_{x \in S_i} (x - m_i)(x - m_i)^T \]

Which is calculated for all features within each class individually using the relevant value of \( m_i \) computed earlier. In our case, the \( S_w \) was a [3x3] matrix.

The [3x3] inter-class (SB) scatter matrix is calculated as follows:

\[ S_B = \sum_{i=0}^{4} 250 (m_i - M)(m_i - M)^T \]

\[ M \text{ is the total mean for all classes} \]

The matrix A is calculated using the \( S_W \& S_B \) matrices as follows:

\[ A = S_W^{-1} S_B \]

The eigenvectors and their eigenvalues are used to project the data into a new feature subspace. The resulting new feature subspace separated the health classes very cleanly.

It is important to note that eigenvectors with the lowest eigenvalues bear the least amount of information about data distribution. Any eigenvector with an eigenvalue significantly smaller than other eigenvalues can be ignored with minimal effect on the classification. In our experiments, one eigenvector had a significantly lower eigenvalue (close to 1% compared to the first and the second). This allowed us to drop this feature and use a simpler feature set for our classification. After dropping the third eigenvector, we were able to make our reduced [3x2] transformation matrix \( W \). The resulting reduced \( W \) matrix can be seen in Table III.

\[ Y = X.W \]

Y is the [1000x2] weighted matrix that will be used to classify any incoming data. The scatter plot of the Y matrix can be seen in Fig 6.4. The stated objectives for the classifier were a reduction in feature dimension and an increase in data separation. It is evident from the figure that these objectives have been achieved.

Table IV Summary of reduced Y-Matrix reduced to two feature dimensions. Total number of determination sets 16000, with 4000 representing each class (1-4)

<table>
<thead>
<tr>
<th>Feature 1</th>
<th>Feature 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Total</td>
<td></td>
</tr>
<tr>
<td>Mean</td>
<td>2.65E-08</td>
</tr>
<tr>
<td>Max</td>
<td>4.51E-08</td>
</tr>
<tr>
<td>Min</td>
<td>1.55E-08</td>
</tr>
<tr>
<td>Class 1</td>
<td></td>
</tr>
<tr>
<td>Mean</td>
<td>4.22E-08</td>
</tr>
<tr>
<td>Class 2</td>
<td></td>
</tr>
<tr>
<td>Mean</td>
<td>2.56E-08</td>
</tr>
<tr>
<td>Class 3</td>
<td></td>
</tr>
<tr>
<td>Mean</td>
<td>2.11E-08</td>
</tr>
<tr>
<td>Class 4</td>
<td></td>
</tr>
<tr>
<td>Mean</td>
<td>1.69E-08</td>
</tr>
</tbody>
</table>

In this particular instance, a level of separation has been achieved where feature 2 can be discarded without compromising the performance of the classifier. The decision to discard a feature as such can only be made after the extra features have been reduced by the feature reduction algorithm. In this case, the resultant classes can be identified using feature 1 alone. However, this is often not the case.

3) Classifier Usage

Input to the prognostics engine is a vector with three values corresponding to the chosen feature set, i.e. frequency, capacitance and conductance (X'). The sample is transformed into the reduced feature space by computing a dot product with the W matrix (Table III) after subtracting the (total) mean matrix M from it. We obtain the transformed \( Y'' \) as follows:

\[ X'' = X'.W \]

\( Y'' \) is a [1x2] matrix representing a point in a two dimensional plane representing the sample to be classified.

The Euclidian distance between \( Y'' \) and the mean of each class is measured to determine which class X' belongs to.

A number of samples with known levels of health are fed to the classifier. The classification output is compared to their actual health to validate the performance of the classifier. This is discussed in some detail in the next section.

4) Classifier Validation

The measure of confidence in a classifier is the ratio between the "true positives" with the "false positives".

The program to validate the classifier used a subset of 1000 strong "testing samples" at each instance of the test. The classifier was subjected to multiple validation tests. The test samples were similar to the one shown in Table I but exclusive to the subset used to train the classifier. The health of each
testing sample was also part of the input, i.e. the class (health) of the testing samples is known. This is the reference for comparison to the classifier output. The performance of the classifier has been represented in the form of a confusion matrix shown in Table V. This is a map comparing input health (Actual <class>) to classifier output (Predicted <class>).

The job of the classifier is to assign every test sample to the correct class. If a sample that belongs to class C, the event is known as a “true positive” (TP) with respect to C. False positives (FP) with respect to C are the samples that are assigned to C but in fact, belong to another class. The corresponding True Positives (TP), True Negatives (TN), False Positives (FP) and False Negative (FN) scores are given in Table VI.

The accuracy of the classifier is the percentage of correctly predicted labels divided by all predictions. Two further measures to evaluate classifier performance are precision and recall.

Precision for a class C can be represented as:

\[ \text{precision}_C = \frac{TP_C}{TP_C + FP_C} \]

While the recall for a class C can be represented as:

\[ \text{recall}_C = \frac{TP_C}{TP_C + FN_C} \]

The average accuracy of the LDA classifier across all classes for this validation test was found to be 98.1%. Similarly the average precision and recall were also 98.1%. A number of validation runs provided similar classification performance. Even as the number of test samples was increased to 16000 (with uneven class distribution), none of the performance variables went below 95%.

5) Conclusion

So far, a 4 (health) class system has been discussed. In later experiments the number of classes was increased to 16 levels of health. It was observed that the system input had to be restricted to a shorter spectrum and at a higher resolution to achieve an acceptable level of separation between features identifying the classes. Consequently, the average accuracy of the classification deteriorated to 82.61%.

A variety of robust and mature methodologies for classifications and feature reduction are being used in various fields today. These experiments serve to present the potential to identify the health of a device using one such technique. This research presents the idea that classification methods can be used to facilitate the automatic diagnosis and prognosis of components under test using a programmable chip.

B. End of Life Predictor

The classification data was used to identify the health of the electrodes as they changed. This change in the health was logged over time and a quadratic linear algorithm was applied to predict the prognostic data. This data was compared with a predefined “total failure” threshold. Based on the rate and amount of change, the system was able to make predictions about the remaining useful life of the system within a reasonable horizon.

In normal operation, a periodic OBT self-test is initiated. Each iteration of this test generates a data set consisting of values for input: frequency, capacitance and conductance. This is reduced to a [1x2] matrix using the W matrix in Table III. The resulting Y” value is analyzed against the means of the 4 individual health classes of the classifier data. This classifier data is the reduced 2 feature data set summarized in Table IV. The Euclidean distance(s) between the observed sample and mean of each class is measured. The sample is labelled to the class whose mean the sample is at the minimum distance to. All the analytical data of interest is logged at every point of observation. This includes, but is not limited to:

- The reduced 2 feature set of observed data
- The assigned class of the observed sample
- The Euclidean distance(s) between the sample and mean of each class
- The percentage distance between the two nearest classes, relative to the nearest class (\(d_n\) being the distance from the nearest class and \(d_s\) that from the second nearest). governed by the following expression:

\[ P = \left( \frac{d_n}{d_n + d_s} \right) \times 100 \]
The prognostic module has been designed for a two feature system. This program has access to the observations that are logged. This log of observed and processed data forms the basis of the quadratic predictor at the heart of the prognostic engine. In its current version, the prognostics engine observes samples every 10 clock cycles and does not start to operate before the first 50 clock cycles (5 cycles of observation). As the system deteriorates, the sample moves from better health, to worse. This is reflected in subsequent observations and their distances from class means available in the log.

The module subjects the observed values to quantized normalization to bring them in alignment. Each adjusted observation $P_n$ can be represented as follows:

$$P_n = C - t + \sqrt{\left(\frac{P}{100} - t\right)^2}$$

Where

- $C = \text{assigned class}$
- $P = \text{percentage distance}$
- $t = \text{trend}$
  - 0 if observation leans to a healthier class
  - 1 if observation leans to unhealthy class

$$0 \leq P_n \leq (\max(C \text{ value}) + 1)$$

In the 4-class paradigm, the prognostic program filters out any value above 4 by default. Any $P_n$ value above 4 represents an event past system failure, and is hence, useless.

The $P_n$ values always move from their first observation towards 4 as the device ages and performance degrades. As successive changes in health are stored, this historical data is used to derive a health trend over time (observation cycle numbers), which in turn is extrapolated to predict the time when the system will reach total failure. The point of observation where $P_n$ crosses 4 is considered to be the time of actual failure.

Several tests were performed to test this algorithm and the health predictions at various points were observed. These were then compared to eventual points of failure. An example of some failure predictions over a sequence of tests for a system which was artificially and drastically aged are shown in Table VII.

Data generated from the program has been imported to MATLAB to produce the graphical representations shown in Fig 6.5.

<table>
<thead>
<tr>
<th>Cycle of prediction</th>
<th>Predicted EoL</th>
</tr>
</thead>
<tbody>
<tr>
<td>150</td>
<td>218.18</td>
</tr>
<tr>
<td>200</td>
<td>258.60</td>
</tr>
<tr>
<td>240</td>
<td>278.78</td>
</tr>
<tr>
<td>270</td>
<td>278.78</td>
</tr>
</tbody>
</table>

In the example that has been presented, the electrodes were aggressively aged. Normal prognostics tests were performed over a significantly larger volume of data.

These experiments present a blueprint laying out the foundations for the development of a prognostics system for a MEMS device. The algorithm is scalable enough to be refined to provide prognostics over larger horizons with minimal overhead.

The use of a lightweight and simple predictor allowed the prognostics module to be implemented with low processing overhead and reasonable memory requirements. This translates
VII. CONCLUSION

The principle outcome of this research is a proof of concept design for a housekeeping prognostics health management solution for MEMS sensors. This is significant as there is very little published work that provides health prediction for MEMS devices.

This work has introduced the concept of “housekeeping” prognostics. The “housekeeping” paradigm has conservative accuracy to enable its realization in a resource constraint framework common to MEMS. At the same time it delivered the potential for an unprecedented reduction in maintenance overheads. This research validated the viability of integrating prognostics in MEMS by demonstrating the use of simplified statistical prognostics techniques in MEMS sensors in the case study presented. While the techniques applied are well established in the fields of finance, computing and image processing, they had not been used to predict the future health trends in MEMS artefacts before.

In the case study, systems were tested using experiments that gradually aged embedded electrodes (being the single most critical components of the MEMS sensor under test). The usage degradation and aging processes were electrically self-induced and controlled. The decay process represented a gradual drift in health as the prognostic system was designed to detect and predict a deterioration of this nature. This is satisfactory as far as the requirements of a “housekeeping” prognostics module are concerned. The consequent light weight processing allowed for the integration of such housekeeping PHMs at a relatively low overhead. However, the PHM is not designed to predict sudden and catastrophic failures.

It was observed that the PHM was consistent with its requirements and design, i.e. while it was able to predict the RUL with gradual aging and drift due to failure; it was unable to respond or detect abrupt or rapid failures. The prognostics module predicted the projected levels of gradual aging of the electrode sensors after 5 cycles of observation (50 clock cycles) with good accuracy.

The challenge of meaningful identification of electrode health was successfully achieved using LDA classifiers with minimal overlaps. The log of this health data formed input to the Linear Predictor that was able to predict the future health of the system.

The scope of this PHM is aging and does not cater for systems that are susceptible to sudden failures leading to critical faults. This research proposes the use of these “intermediate-level” prognostic capabilities that may not be fully featured as more complex PHM systems but still provide a significant advantage in the reliability and maintenance of MEMS devices.

These experiments open up the possibilities to study patterns of abnormal behaviour to predict reliability based on anomalous health patterns. This is critical for systems that may functionally be in a state of degradation without triggering the flags or markers that identify a system to be progressing towards a fatal state.

VIII. REFERENCES


**H. Khan** received his M.Sc. degree in System Engineering from Esslingen University, Germany, in 2006, and a Ph.D. degree in Engineering from Lancaster University, U.K., in 2016. He is an Assistant Professor with the Engineering Department, COMSATS Institute of Information Technology, Pakistan. His primary research interests include reliability and fault tolerance of micro/nano scale systems and the development of self-test techniques for health diagnostics and prognostics for micro sensors.

**Qais Al-Gayem** received the BS degree in Electrical and Electronic Engineering from the University of Babylon, and the MS degree in Electronic Engineering from University of Technology, Iraq, in 1999 and 2001, respectively. Between 2002 and 2008, he worked as a lecturer in Electrical Department, University of Babylon, Iraq. Following this, he studies for his PhD in the Engineering Department, Lancaster University, UK, and graduated in 2012. He is currently associated professor in the Electronic and Electrical Department, Faculty of Engineering, University of Babylon, Iraq. His research interests include built-in-self-test (BIST) of MEMS and NEMS, health monitoring, and dependability in Bio-fluidic microsystems.

**A.M. Richardson** became a member of IEEE in 2006. He received a BSc in Electrical & Electronic Engineering from Manchester University, UK in 1984 and a PhD in the field of reliability & test engineering from Lancaster University, UK in 1992. He is currently a Professor in Microsystems Engineering at Lancaster University with research interests in self-healing systems, prognostics and design-for-test engineering. He also runs a consultancy enablingMNT, UK specializing in design-for-test engineering and training. He has previously held engineering positions at Rockwell Graphic Systems and Videcom Ltd. and spent several years as a Scientific Director of DOLPHIN Integration SA.